

1, 2, 3, 4

1 Eigenvalues and Eigenvectors

Find the eigenvalues and eigenvectors of the following matrix:

$$\begin{bmatrix} 2 & i \\ -i & 2 \end{bmatrix}.$$

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2 Digital Logic Circuits

Design and draw a simple logic circuit that takes two classical bits as input and is described by the following truth table:

A	B	Out
0	0	1
0	1	1
1	0	0
1	1	1

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3 Qubit States and Measurements

A qubit is prepared in the quantum state $|\psi\rangle = \frac{1}{\sqrt{3}}|0\rangle + i\sqrt{\frac{2}{3}}|1\rangle$.

1. What is the probability that an ideal projective measurement in the $\{|a\rangle, |a_\perp\rangle\}$ basis will find the qubit in the state $|a\rangle$ if $|a\rangle = |0\rangle$?
2. What if $|a\rangle = \frac{1}{\sqrt{2}}(|0\rangle + |1\rangle)$?

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4 Matrix Operations

Write down a matrix U_χ such that $U_\chi \begin{bmatrix} a \\ be^{i\varphi} \end{bmatrix} = \begin{bmatrix} a \\ be^{i(\varphi+\chi)} \end{bmatrix}$ for any real numbers a , b , and φ . Is U_χ a unitary matrix?

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