

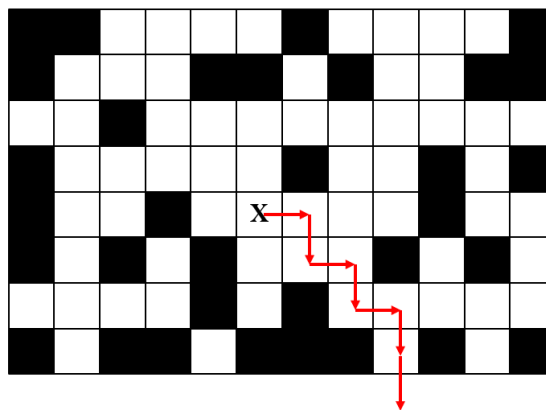
## MINI PROJECT DESCRIPTION

### 1. MAZE

A Maze is represented by a 0-1 matrix  $a_{N \times M}$  in which  $a_{i,j} = 1$  means cell (i,j) is an obstacle,  $a_{i,j} = 0$  means cell (i,j) is free.

From a free cell, we can go up, down, left, or right to an adjacent free cell.

Compute the minimal number of steps to escape from a Maze from a given start cell  $(i_0, j_0)$  within the Maze.



Escape the Maze after 7 steps

- **Input**
  - Line 1 contains  $N, M, i_0, j_0$  ( $2 \leq N, M \leq 900$ )
  - Line  $i+1$  ( $i = 1, \dots, N$ ) contains the  $i$ th line of the matrix  $a_{N \times M}$
- **Output**
  - Unique line contains the number minimal of steps to escape the Maze or -1 if no way to escape the Maze.
- **Example**

Input	Output
8 12 5 6 1 1 0 0 0 0 1 0 0 0 0 1 1 0 0 0 1 1 0 1 0 0 1 1 0 0 1 0 0 0 0 0 0 0 0 0 1 0 0 0 0 0 1 0 0 1 0 1 1 0 0 1 0 0 0 0 0 1 0 0 1 0 1 0 1 0 0 0 1 0 1 0 0 0 0 0 1 0 1 0 0 0 0 0	7

1 0 1 1 0 1 1 1 0 1 0 1	
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## 2. Bus scheduling

There are  $n$  passengers  $1, 2, \dots, n$ . The passenger  $i$  want to travel from point  $i$  to point  $i + n$  ( $i = 1, 2, \dots, n$ ). There is a bus located at point 0 and has  $k$  places for transporting the passengers (it means at any time, there are at most  $k$  passengers on the bus). You are given the distance matrix  $c$  in which  $c(i, j)$  is the traveling distance from point  $i$  to point  $j$  ( $i, j = 0, 1, \dots, 2n$ ). Compute the shortest route for the bus, serving  $n$  passengers and coming back to point 0 (the route visits each point  $1, 2, \dots, 2n$  exactly once).

- **Input**
  - Line 1 contains  $n$  and  $k$  ( $1 \leq n \leq 11, 1 \leq k \leq 10$ )
  - Line  $i+1$  ( $i = 1, 2, \dots, 2n+1$ ) contains the  $(i-1)^{\text{th}}$  line of the matrix  $c$  (rows and columns are indexed from  $0, 1, 2, \dots, 2n$ )
- **Output:**
  - Unique line contains the length of the shortest route
- **Example**

Input	Output
3 2 0 8 5 1 10 5 9 9 0 5 6 6 2 8 2 2 0 3 8 7 2 5 3 4 0 3 2 7 9 6 8 7 0 9 10 3 8 10 6 5 0 2 3 4 4 5 2 2 0	25

**Explanation**

There are 3 passengers need to be transported. The bus has 2 places for passengers (at any moment, there are at most 2 passengers on the bus)

The optimal route of the bus is:  $0 \rightarrow 3 \rightarrow 1 \rightarrow 4 \rightarrow 2 \rightarrow 6 \rightarrow 5 \rightarrow 0$ , and the length of the optimal route is  $c(0,3) + c(3,1) + c(1,4) + c(4,2) + c(2,6) + c(6,5) = 1 + 3 + 6 + 8 + 2 + 2 + 3 = 25$

That means: the bus goes to pickup passenger 3 and then pickup passenger 1, then goes to delivery passenger 1, then goes to pickup passenger 2, then goes to delivery passenger 3, then goes to delivery passenger 2, and finally comes back to the depot 0.

### 3. Balanced Academic Curriculum Problem

The BACP is to design a balanced academic curriculum by assigning periods to courses in a way that the academic load of each period is balanced .

There are  $N$  courses  $1, 2, \dots, N$  that must be assigned to  $M$  periods  $1, 2, \dots, M$ . Each course  $i$  has credit  $c_i$  and has some courses as prerequisites. The load of a period is defined to be the sum of credits of courses assigned to that period.

The prerequisites information is represented by a matrix  $A_{N \times N}$  in which  $A_{i,j} = 1$  indicates that course  $i$  must be assigned to a period before the period to which the course  $j$  is assigned. Given constants  $a, b$ . Compute the solution satisfying constraints

- Total number of courses assigned to each period is greater or equal to  $a$  and smaller or equal to  $b$
- The maximum load for all periods is minimal

#### • Input

- Line 1 contains  $N$  and  $M$  ( $2 \leq N \leq 16, 2 \leq M \leq 5$ )
- Line 2 contains  $c_1, c_2, \dots, c_N$
- Line  $i+2$  ( $i = 1, \dots, N$ ) contains the  $i^{\text{th}}$  line of the matrix  $A$

#### • Output

- Unique line contains that maximum load for all periods of the solution found

#### • Example

Input	Output
6 2	12

4 4 4 4 2 4	
0 0 0 0 0 0	
0 0 0 0 0 0	
0 0 0 0 0 0	
0 0 1 0 0 0	
0 0 1 0 0 0	
1 0 0 0 0 0	

#### 4. Paper Reviewers Assignment Problem

The chair of a conference must assign scientific papers to reviewers in a balance way. There are  $N$  papers 1, 2, ...,  $N$  and  $M$  reviewers 1, 2, ...,  $M$ . Each paper  $i$  has a list  $L(i)$  of reviewers who are willing to review that paper. A review plan is an assignment reviewers to papers. The load of a reviewer is the number of papers he/she have to review.

Given a constant  $b$ , compute the assignment such that

- Each paper is reviewed by exactly  $b$  reviewers
- The maximum load of all reviewers is minimal

##### • Input

- Line 1 contains  $N$ ,  $M$  and  $b$
- Line  $i+1$  ( $i = 1, \dots, N$ ) contains a positive integer  $k$  followed by  $k$  positive integers representing the list  $L(i)$

##### • Output

- Unique line contains the maximum load for all reviewers of the solution found or contains -1 if no solution found.

##### • Example

Input	Output
10 6 2 3 6 5 4 5 4 6 3 1 2	4

5 6 3 2 4 1	
4 1 6 2 3	
5 4 5 2 6 3	
2 4 6	
4 1 5 4 2	
2 5 3	
3 2 3 1	
5 5 6 3 2 1	

## 5. Balanced Course Assignment

### a. Problem description

At the beginning of the semester, the head of a computer science department  $D$  have to assign courses to teachers in a balanced way. The department  $D$  has  $m$  teachers  $T=\{1, 2, \dots, m\}$  and  $n$  courses  $C=\{1, 2, \dots, n\}$ . Each teacher  $t \in T$  has a preference list which is a list of courses he/she can teach depending on his/her specialization. We know a list of pairs of conflicting two courses that cannot be assigned to the same teacher as these courses have been already scheduled in the same slot of the timetable. The load of a teacher is the number of courses assigned to her/him. How to assign  $n$  courses to  $m$  teacher such that each course assigned to a teacher is in his/her preference list, no two conflicting courses are assigned to the same teacher, and the difference between maximal load and minimal load is minimal.

*InputFile* The input consists of following lines

- Line 1: contains two integers  $m$  and  $n$  ( $1 \leq m \leq 10, 1 \leq n \leq 30$ )
- Line  $i+1$ : contains an positive integer  $k$  and  $k$  positive integers indicating the courses that teacher  $i$  can teach ( $\forall i = 1, \dots, m$ )
- Line  $m+2$ : contains an integer  $k$
- Line  $i+m+2$ : contains two integer  $i$  and  $j$  indicating two conflicting courses ( $\forall i=1, \dots, k$ )

*OutputFile*

The output contains a unique number which is the maximal load of the teachers in the solution found and the value -1 if not solution found.

**Example:**

Input	Ouput
4 9	3
4 1 2 3 5	
5 1 2 5 6 8	
6 1 2 4 5 7 9	
4 3 4 5 9	
13	
1 3	
1 2	
2 5	
1 8	
1 4	
4 9	
5 7	
2 3	
1 7	
6 9	
4 8	
3 5	
2 7	

Courses assigned to teacher 1: 1, 5

Courses assigned to teacher 2: 2, 6, 8

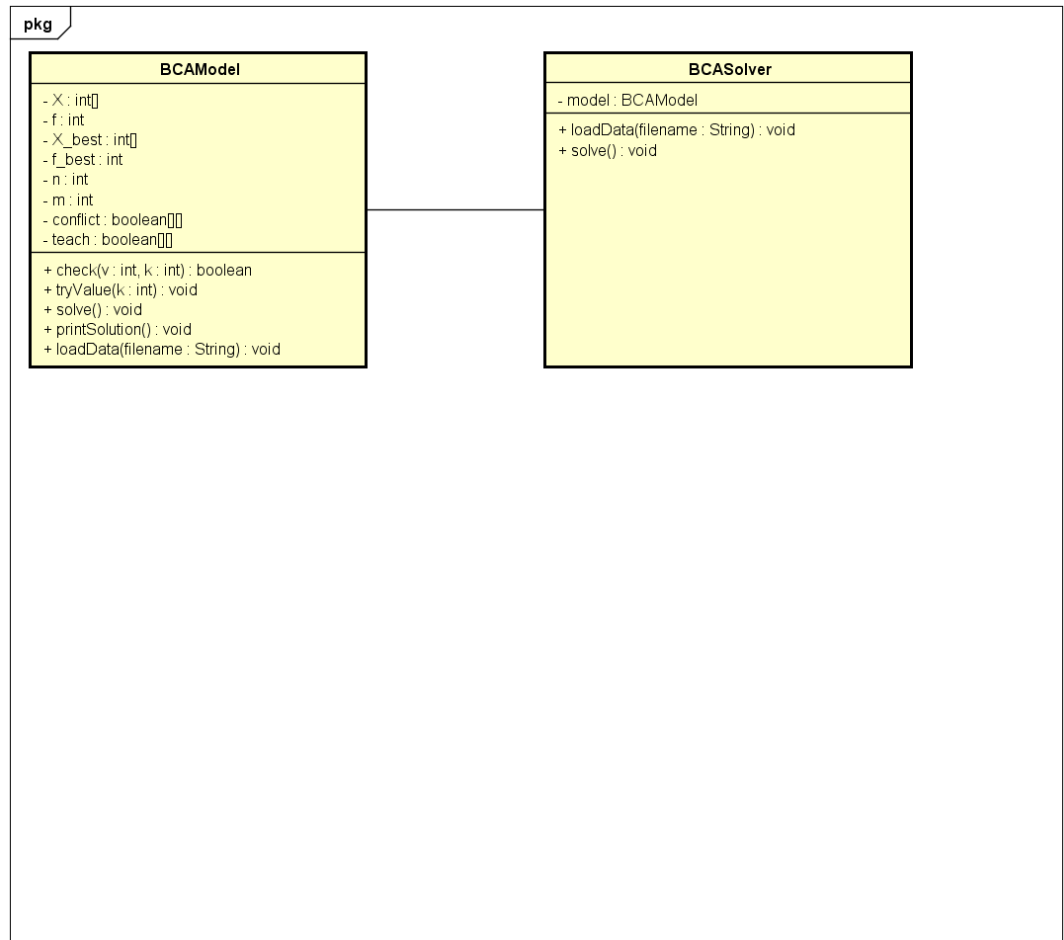
Courses assigned to teacher 3: 4, 7

Courses assigned to teacher 1: 3, 9

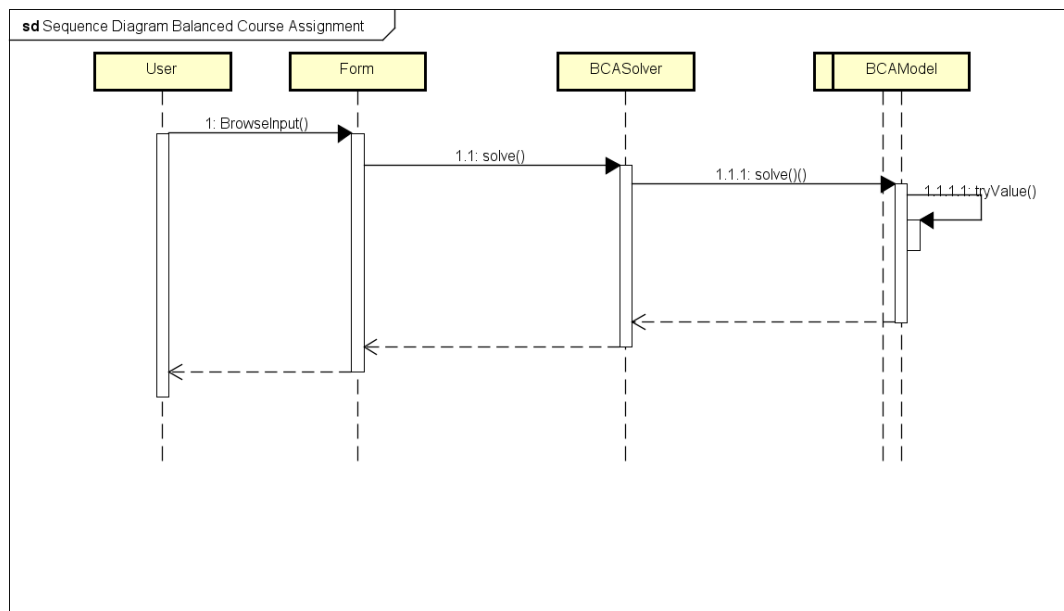
Maximal load = 3, minimal load = 2

## **b. Design**

- Use backtracking search to explore all possibilities in the search space.
- Decision variables  $X[]$  in which  $X[i]$  represents the index of teacher assigned to the course  $i$ .
- Method `tryValue(int k)` tries all values for  $X[k]$
- Method `check(int v, int k)` returns true if value  $v$  can be assigned to  $X[k]$  without violating constraints of the problem
- Data structures
  - `conflict[i][j]` = true if courses  $i$  and  $j$  conflict to each other
  - `teach[t][i]` = true if teacher  $t$  can teach course  $i$



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## 6. Sudoku

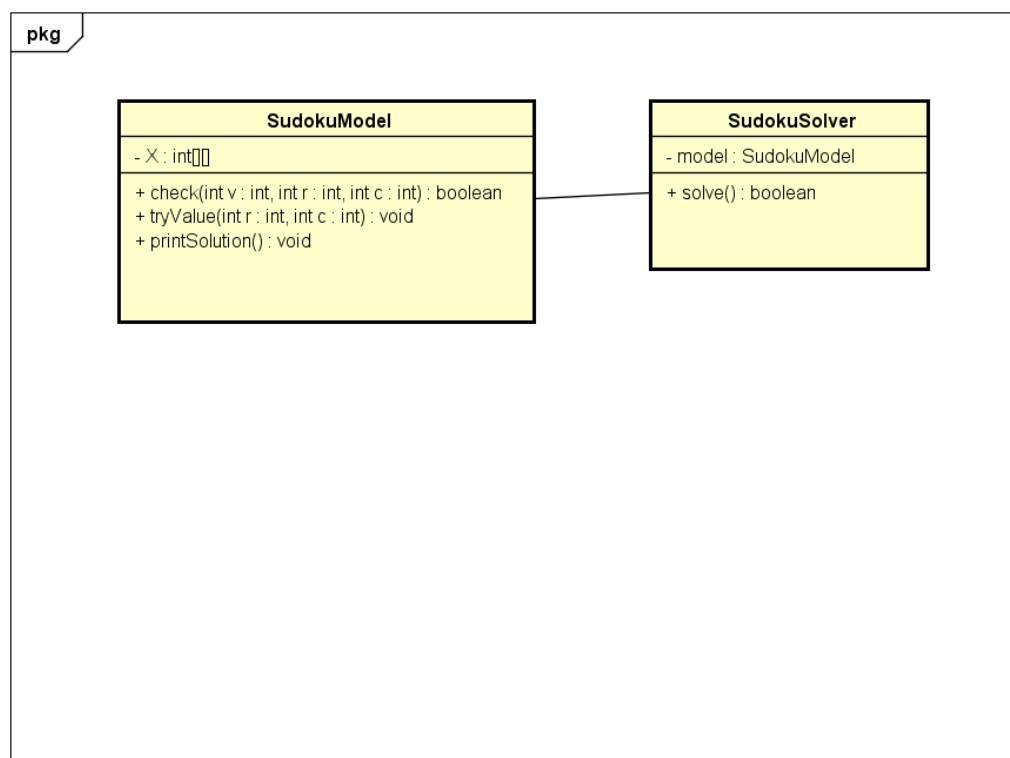
### a. Problem description

There is an incomplete 9x9 table of numbers. Fill each empty cell a number from 1 to 9 satisfying following constraints

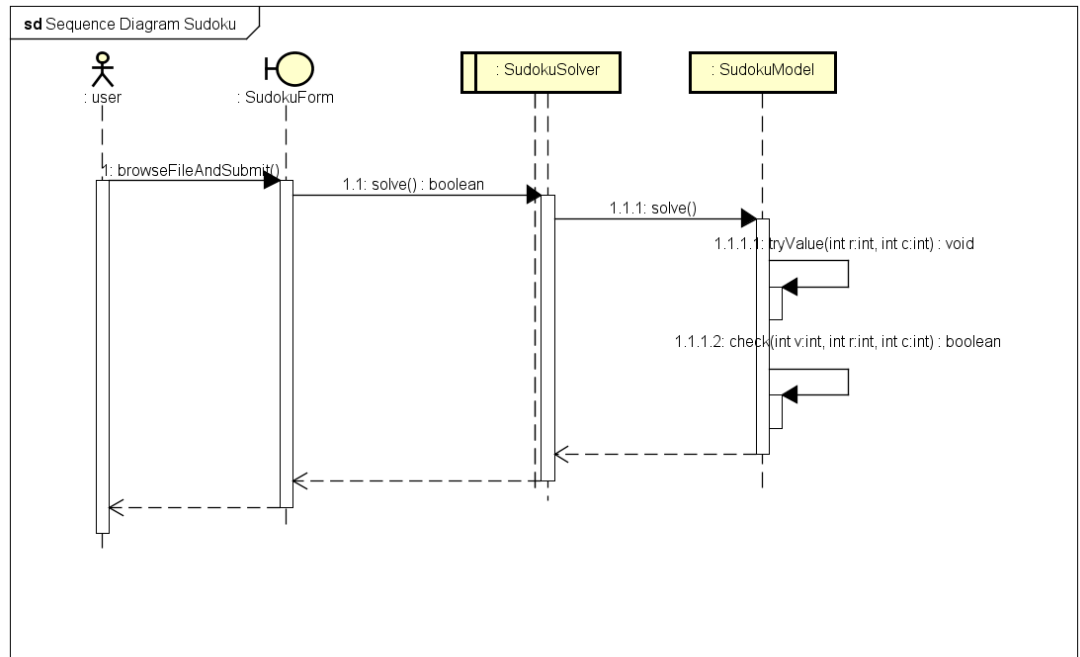
- Numbers within any of the 9 individual 3x3 boxes are different
- Numbers within any row of the given 9x9 table are different
- Numbers within any column of the given 9x9 table are different

**b. Design**

- Use backtracking search to explore all possibilities in the search space.
- Decision variables  $X[i][j]$  in which  $X[i][j]$  represents the value assigned to the cell row  $i$  and column  $j$  of the table.
- method `tryValue(int i, int j)` tries all values for cell  $(i, j)$  of the table
- method `check(int v, int i, int j)` returns **true** if  $v$  can be assigned to cell  $(i, j)$  without violating constraints of the problem.







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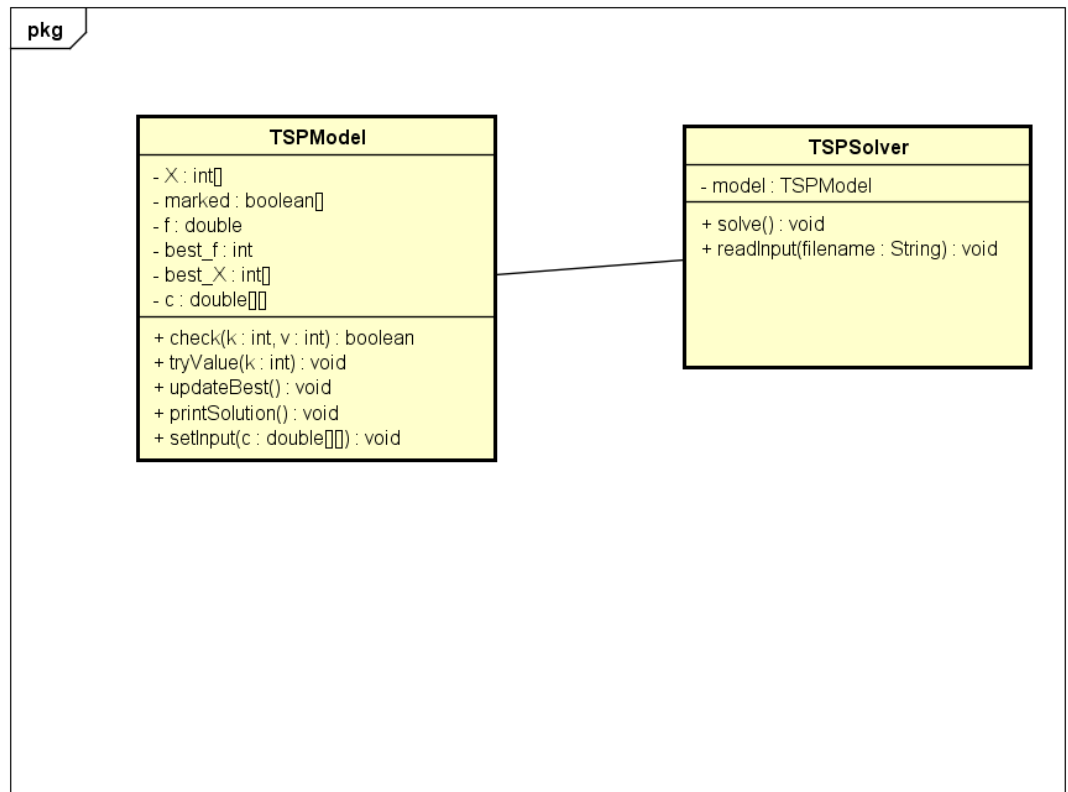
## 7. Shipping route

### a. Problem description

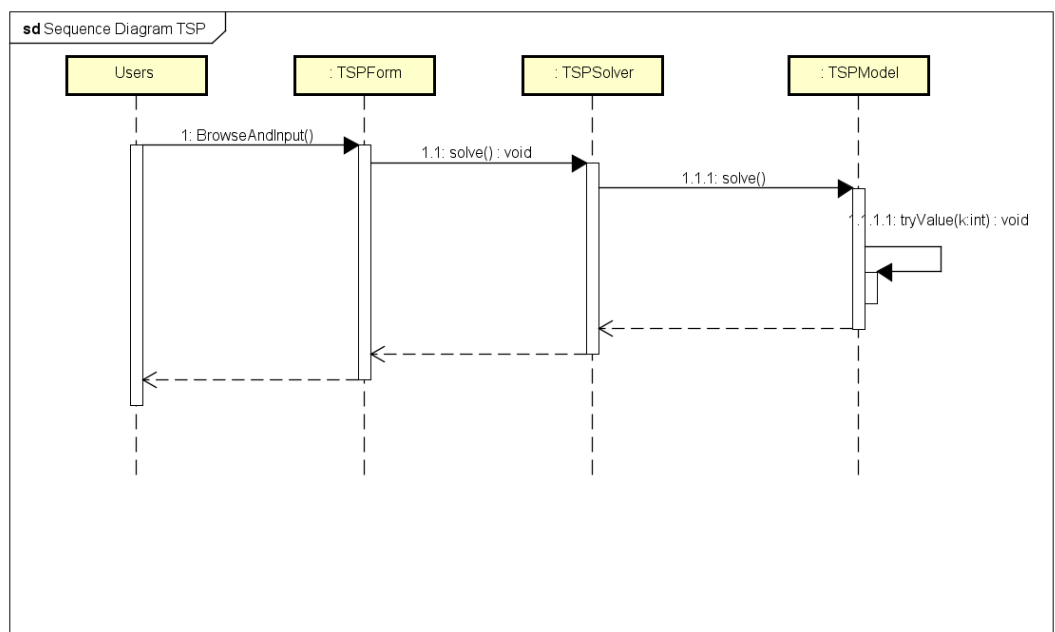
A shipper must delivery goods to  $N$  customers represented by points 1, 2, ...,  $N$  from the store represented by the point 0. The travel distance from point  $i$  to point  $j$  is  $c_{i,j}$  ( $i, j = 0, 1, \dots, N$ ). Find the shipping route from the store, visiting  $N$  customers and returning to the store such that to total travel distance is minimal.

### b. Design

- Use backtracking search to investigate all candidate solutions in the solution space.
- Decision variables  $X[]$  in which  $X[i]$  is the  $i^{\text{th}}$  point of the route, for all  $i = 0, 1, 2, \dots, N$ : the route of the shipper is  $X[0] \rightarrow X[1] \rightarrow X[2] \rightarrow \dots \rightarrow X[N] \rightarrow X[0]$  ( $X[0] = 0$  is the starting point).
- method `tryValue(int k)` tries values for  $X[k]$
- method `check(int v, int k)` returns true if value  $v$  can be assigned to  $X[k]$  without violating constraints of the problem (each customer point is visited exactly once).



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*InputFile* The input consists of following lines

- Line 1: contains an integer  $N$  ( $1 \leq N \leq 20$ )
- Line  $i+1$  ( $i=1,2,\dots,N+1$ ): contains the  $(i-1)^{\text{th}}$  row of matrix  $c$

### *OutputFile*

The output contains a unique number which is the maximal load of the teachers in the solution found and the value -1 if not solution found.

### **Example:**

Input	Ouput
3 0 4 1 8 1 0 7 5 7 6 0 1 8 2 6 0	5

Shortest route is:  $0 - 2 - 3 - 1 - 0$  and the distance is  $c_{0,2} + c_{2,3} + c_{3,1} + c_{1,0} = 1 + 1 + 2 + 1 = 5$

## **8. Water Jug**

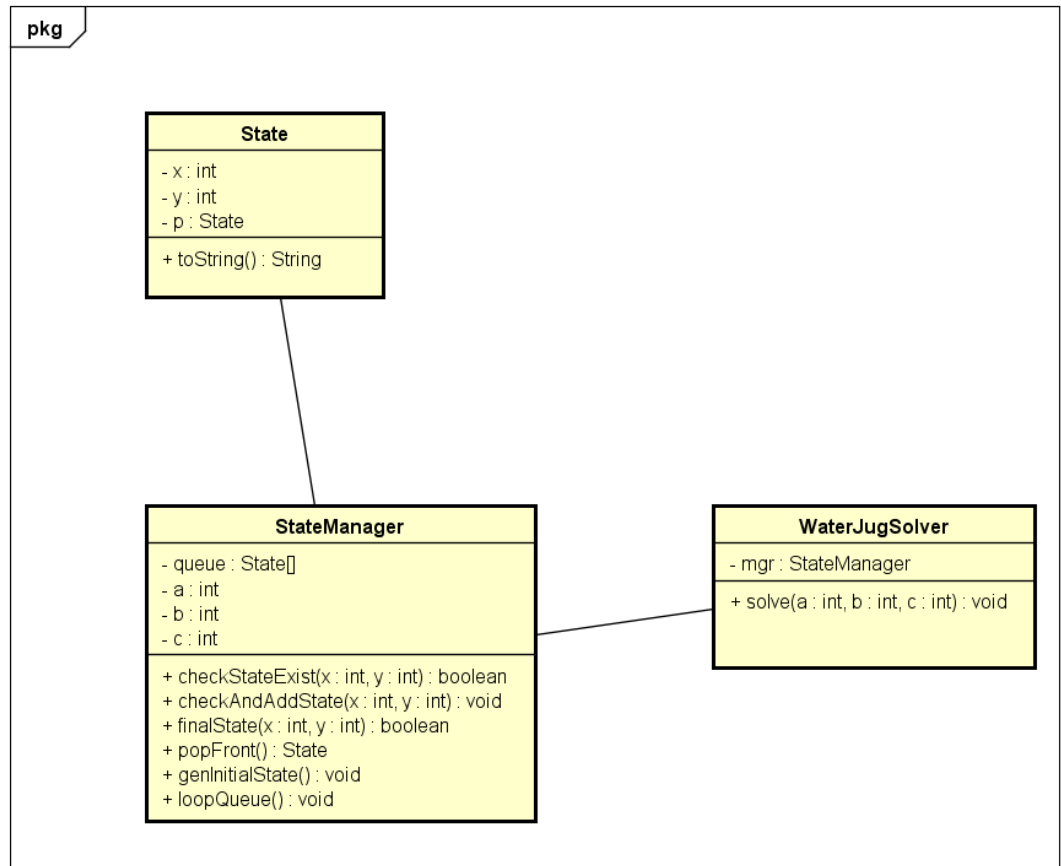
### **a. Problem description**

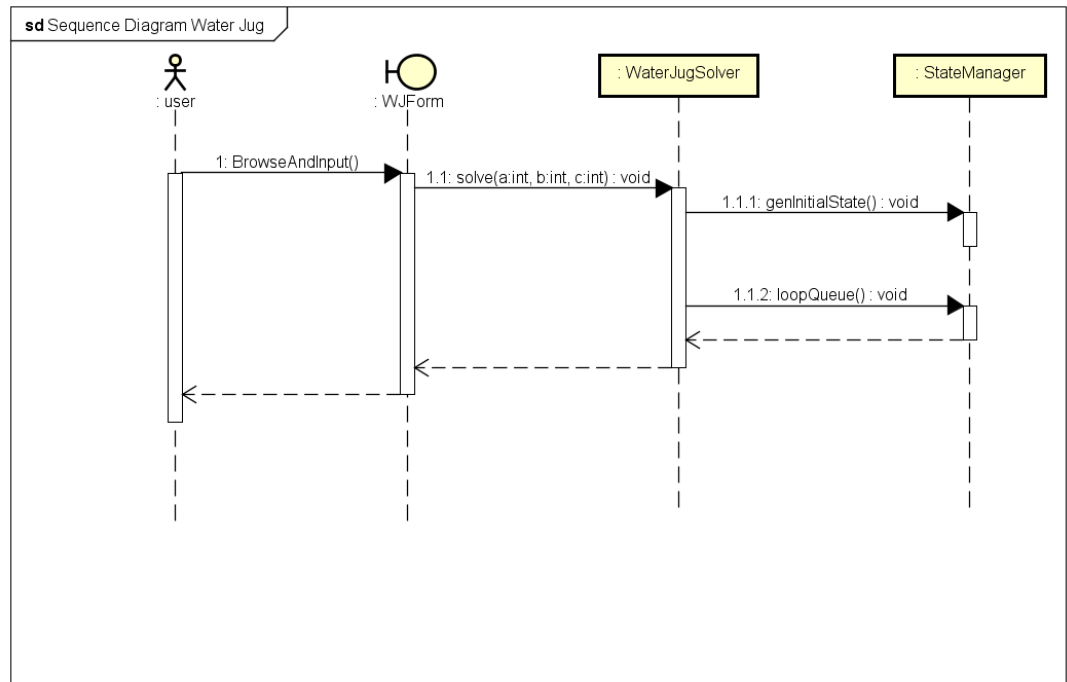
There are two jugs having capacities  $a$  and  $b$  liters. There is a tank with unlimited water. Given a target volumn  $c$  liters. Find the way to get exactly  $c$  liters water ( $a, b, c$  are positive integers).

### **b. Design**

- Use the breadth first search technique to find the optimal move path in a state transition schema. Each state is modelled by a pair  $(x, y)$  in which  $x$ , và  $y$  respectively the amount of water in the jugs 1 and 2. The initial state is  $(0, 0)$  and the target state is  $(x, c)$  or  $(c, y)$  or  $(x, y)$  with  $x+y=c$ . From the state  $(x, y)$ , neighboring states can be generated by following operations:
  - Empty the jug 1  $\rightarrow$  state  $(0, y)$
  - Empty the jug 2  $\rightarrow$  state  $(x, 0)$
  - Full fill the jug 1  $\rightarrow$  state  $(a, y)$
  - Full fill the jug 2  $\rightarrow$  state  $(x, b)$
  - Pour the jug 1 into the jug 2 until the jug 2 is full (if  $x+y \geq b$ )  $\rightarrow$  state  $(x+y-b, b)$
  - Pour the jug 1 into the jug 2 until the jug 1 is empty (if  $x+y < b$ )  $\rightarrow$  state  $(0, x+y)$
  - Pour from the jug 2 into the jug 1 until the jug 1 is full (if  $x+y \geq a$ )  $\rightarrow$  state  $(a, x+y-a)$
  - Pour from the jug 2 into the jug 1 until the jug 2 is empty (if  $x+y < a$ )  $\rightarrow$  state  $(x+y, 0)$

- method `check(int x, int y)` return true if state (x, y) has been generated
- method `final(int x, int y)` return true if state (x, y) is a final state





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## 9. DataBase

### a. Problem description

Build a data structure (database) storing profiles of staffs in an organization. Each staff has a unique ID which is a string and other personal information. The data structure allows users to perform following operations

- add(String ID, Info I): add a profile of a staff to the database
- find(String ID): find and return the profile of the staff given his/her ID
- delete(String ID): remove the profile of the staff given his/her ID

The data structure employ hashing and binary search tree techniques.

### b. Design

- Class Item represents the profiles of staffs
- Class BST represents binary search trees
- Lóp BSTNode represents nodes of the BST. It contains an Item and references to the left and right children.
- Class Dictionary represents the data structure using the hashing technique and binary search trees for separate chaining.

