

Quantum Information and Computing

2022 - 2023

Nguyen Xuan Tung
12/07/2022
Exercise #02

Theory

A Fortran subroutine is a block of code that performs some operation on the input variables, and as a result of calling the subroutine, the input variables are modified.

Code development

- We create a subroutine called *check_point* to perform if *DEBUG_ == TRUE* we are in 'debug mode'.
- Print the line and arg.
- We run the program *test*.
- Assign 2 real values *x* and *y*.
- If *DEBUG_ == TRUE*, print the value.

```

11
12 subroutine check_point(DEBUG, realarg, line)
13     logical    :: DEBUG ! input, if DEBUG_ == TRUE we are in 'debug mode'
14     real       :: realarg ! optional generic real argument
15     integer    :: line
16
17     if (DEBUG .eqv. .TRUE.) then
18         print *, 'LINE:', line ! print file and line
19         print *, 'arg:', realarg
20     end if
21 end subroutine check_point
22
23 #define check_real_(realarg) check_point(DEBUG, realarg, _LINE_)
24
25 program test
26     logical :: DEBUG = .TRUE.
27     real    :: x = 3.14159265359, y = 9.53562951413
28
29     ! DEBUG_ is true, this value should be printed
30     call check_real_(x)
31
32     DEBUG = .FALSE.
33     ! DEBUG_ is now false, this value should NOT be printed
34     call check_real_(y)
35
36 end program test
37
38 ! Error appears when compiling, in order to compile successful, a flag -cpp is used
39 ! gfortran -o checkpoint checkpoint.f90 -cpp
40 ! ./checkpoint
41

```

PROBLEMS OUTPUT DEBUG CONSOLE TERMINAL

```

PS D:\Physics-Data-Msc\Quantum-IC\Assignment-2> gfortran -o checkpoint checkpoint.f90 -cpp
PS D:\Physics-Data-Msc\Quantum-IC\Assignment-2> ./checkpoint
LINE:      30
arg:  3.14159274

```

Documentation and comments

- For every function and subroutine, we create a documentation and comment in order to understand the function/subroutine better.

Result

- We write function to fill the matrix with random variables.
- The matrix dimension stored in a vector of two dimensions: N, M.
- We create a module named *debug* which contains several subroutines with different functions: print matrix in the terminal, print a matrix and its lines, check for custom implemented matrix multiplication.

```
!!
!! @param[in] N : integer, number of columns in matrix
!! @param[in] M : integer, number of rows in matrix
!! @param[in] rand_range : integer, range of random numbers
!!
!! @return a matrixA = real*4, dimension(N,M), real random matrix
!!-----
function fill_no_matrix(N, M, rand_range) result(matrixA)
    integer :: N, M, rand_range
    real*4, dimension(N,M) :: matrixA
    call random_number(matrixA)
    matrixA = rand_range * matrixA
end function fill_no_matrix

!> @brief function perform matrix multiplication through a loop method
!! @param[in] matrixA = real*4, dimension(N,M), real random matrix
!! @param[in] matrixB = real*4, dimension(N,M), real random matrix
!!
!! @return a matrixC = real*4, dimension(N,M), matrixA*matrixB
!!-----
!Assume A is lhs matrix, B rhs second, C is the result matrix
!first index "i" runs slower in c_ij
function matrix_multiplication(matrixA, matrixB) result(matrixC)
    integer :: ii, jj, kk
    logical :: check
    real*4, dimension(:,) :: matrixA, matrixB
    real*4, dimension(size(matrixA,2),size(matrixB,1)) :: matrixC
```

Theory

- The Hermitian adjoint matrix, A , over a field C of complex numbers, is its complex-conjugate transpose matrix.
- The adjoint matrix A denoted as A^\dagger , where: $A^\dagger = A^{T*}$
- $*$ is denoted as conjugate
- Trace given matrix A $n \times n$, is defined: $\text{Tr}(A) = \sum_{i=1}^n a_{ii}$
- The following properties hold:
- $\text{Tr}^*(A) = \text{Tr}(A^\dagger)$
- $\text{Det}(A^\dagger) = \det A^*$

Results

- The result shows us the dimension, trace and the adjoint of the matrix generated.

```
PS D:\Physics-Data-Msc\Quantum-IC\Assignment-2> gfortran -o Derivedtypes Derivedtypes.f90
PS D:\Physics-Data-Msc\Quantum-IC\Assignment-2> ./Derivedtypes
|          (1.0000000000000000,0.0000000000000000)          (2.0000000000000000,0.0000000000000000) |
|          (3.0000000000000000,0.0000000000000000)          (4.0000000000000000,0.0000000000000000) |
Dimension:          2          2
Trace:              (5.0000000000000000,0.0000000000000000)
Adjoint:
|          (1.0000000000000000,-0.0000000000000000)          (3.0000000000000000,-0.0000000000000000) |
|          (2.0000000000000000,-0.0000000000000000)          (4.0000000000000000,-0.0000000000000000) |
```

Code development

- A module *matrices* is written, and inside it derived type data *type*, called *cmatrix*.
- After data *type*, we perform interfaces for the initialization of the *type*, the *adjoint matrix* and the *trace* computation.
- After that, we create functions to:
 - computes the trace.
 - initializes complex matrix randomly.
 - initializes complex matrix type given the 2d array.
- Then we create subroutines to prints matrix on terminal and writes matrix to file.

```
!!-----
type cmatrix
    integer, dimension(2)                :: dim      ! dimension of the matrix
    complex*16, dimension(:, :), allocatable :: element
    complex*16                           :: trace, det
end type cmatrix

interface operator(.Adj.)
    module procedure cmatrix_adjoint
end interface

interface operator(.Trace.)
    module procedure cmatrix_trace
end interface

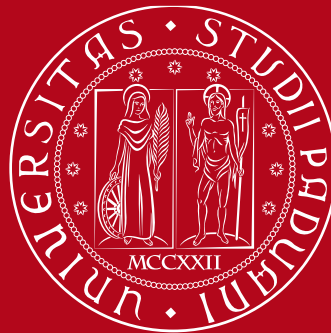
contains

> @brief computes the trace
!! @param[in] cmat = type(cmatrix), input complex matrix
!! @return trace = complex*16, trace of the complex matrix
!!-----
function cmatrix_trace(cmat) result(trace)
    integer                :: ii
    complex*16             :: trace
    type(cmatrix), intent(IN) :: cmat

    if(cmat%dim(1) == cmat%dim(2)) then ! iff the matrix is square
        trace = 0
        do ii = 1, size(cmat%element,1), 1
            trace = trace + cmat%element(ii,ii)
        end do
    else
        trace = 0
        trace = trace/trace
    end if
end function cmatrix_trace

> @brief initializes complex matrix randomly
!! @param[in] nrow = integer, number of rows of matrix
!! @param[in] ncol = integer, number of columns of matrix
!! @param[in] range = real, range of numbers: 0<=x<=range
!! @return cmat = type(cmatrix), complex matrix
!!-----
```

1222 • 2022
800
ANNI



UNIVERSITÀ
DEGLI STUDI
DI PADOVA

Thanks for the attention
