

*Proof:* Let a three sets  $A = \{4n + 1\}_{n=1}^{\infty}$ ,  $B = \{4n + 3\}_{n=1}^{\infty}$  and  $C = A \cup B$ .  
 Since sets  $A$  and  $B$  do not intersect we can sum they to do their union:

$$4n + 1 + 4n + 3 = 8n + 4$$

Divive by 4.

$$2n + 1$$

By  $2n+1$  we can present any odd number, then a parts of which is consist in the union can present any odd number too, Q.E.D.