

## Normalization

Reason 3: Why do we need normalization?

Student info table :-

(PK) (id)	student name	age	branch code	Branch name	HOD name
1	A	18	101	IT	XYZ
2	B	19	101	IT	XYZ
3	C	18	101	IT	XYZ
4	D	21	102	EC	PQR
5	E	20	102	EC	PQR
6	F	19	103	MECH	ABC

Redundancy of data.

Idea 3: In the table student info we have tried to store entire data about student.

Result 3: Entire branch data of a branch must be repeated for every student of the branch.

Redundancy: When the same data is stored multiple times, unnecessarily in the database.

Disadvantage :-

- ① Insertion, deletion and modification anomalies (problems).
- ② Inconsistency (data)
- ③ Increase in database size and increase in time (to search the required data).

Insertion anomalies :- When certain data (attribute) cannot be inserted into db, without the presence of other data.

Ex 3:- If we want to insert civil department details of classmate

and still none of the students have joined, then we will not be able to insert the department details itself.

Deletion anomaly :- if we want to delete the unwanted data, and if that deletion causes deletion of necessary data.

Eg:- student id 6 left the college and was the only student who joined much. By deleting student id 6, we also lose much dept data which is necessary.

Update/modification anomaly :- When we want to update a single piece of data, but it must be done at all the places where it is repeated.

Eg:- changing the FC had name from 'PQR' to 'MNO', it should be done at all places. If missed even at single occurrence leads to data inconsistency.

How do we normalize

- 1 paragraph contains 1 idea. Similarly 1 table should contain info about 1 entity.
- Normalization (decomposition of table) of table is done on the basis of Functional dependencies.

Sid	Sname	age	discode	lensnm	host-name
1	A	19	101	IT	XYZ
2	B	18	101	IT	XYZ
3	C	18	101	IT	XYZ
4	D	20	102	EC	PQR
5	E	19	102	EC	PQR
6	F	20	103	MECH	KLM

stud\_info

branch\_info

Sid	Sname	age	discode	discode	lensnm	host-name
1	A	18	101	101	IT	XYZ
2	B	19	101	102	EC	PQR
3	C	18	101	103	MECH	KLM
4	D	21	102			
5	E	20	102			
6	F	19	103			

Notations used in normalization.

- ① Prime attributes and non-prime attributes
- ② Partial functional dependency
- ③ Fully Functional dependency
- ④ Transitive functional dependency.

Consider the given FD:-

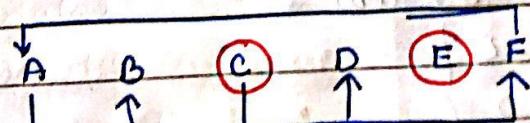
$R(A, B, C, D, E, F)$

$C \rightarrow F$

$F \rightarrow A$

$EC \rightarrow D$

$A \rightarrow B$



$$(FC)^+ = \{E, C, D, F, A, B\} - CK$$

$R(A, B, C, D, E, F)$	
E.C	A.B.D.F
Candidate key & Prime attributes	non-prime attributes

- ② Fully Functional dependency  
 Partial Functional dependency  
 Transitive Functional dependency.

② Fully Functional dependency:

$X \rightarrow Y$ , if  $y$  is said to be fully FD on  $X$  if it cannot be determined by any subset of  $X$ .

$$ABC \rightarrow D$$

③ Partial Functional dependency:

$X \rightarrow Y$ , if  $y$  is said to be partially FD on  $X$  if its subset can determine the value of  $Y$ .

$$ABC \rightarrow D$$

$$AB \rightarrow D \quad \{ \text{PD} \}$$

$$AC \rightarrow D \quad \{ \text{PD} \}$$

$$BC \rightarrow D \quad \{ \text{PD} \}$$

(proper subset of ABC)

$$A \rightarrow D \quad \{ \text{PD} \}$$

$$B \rightarrow D \quad \{ \text{PD} \}$$

$$C \rightarrow D \quad \{ \text{PD} \}$$

Eg.:  $AC \rightarrow P$  'P' is not Fully FD on AC.

$A \rightarrow D$  'P' is Partially FD on AC.

$D \rightarrow P$

$$(AC)^+ = (A, C, P, D)$$

↓ subset.

$$(A)^+ = \{A, D, P\} \checkmark A \rightarrow P (PO)$$

$$(C)^+ = \{C\}$$

#### (4) Transitive Functional dependency :-

if  $x, y, z$  some set of attributes

$$x \rightarrow y$$

$$y \rightarrow z$$

$$x \rightarrow z \text{ (transitive dependency)}$$

#### Definition of Normalization and Normal Forms.

Definition :- normalization of data can be looked upon as a process of analysing the given relation schema based on their FD and Primary key, to achieve the desired properties of minimizing redundancy and minimizing the insertion, deletion and update anomalies.

Several normal forms have been proposed, each normal form minimizes the redundancy upto some extent.

The higher normal forms are only of theoretical interest but not practically applicable.

Most DB systems use normalization upto 3NF. (upto BCNF) is recommended.

Un-normalized relation

(remove multivalued attributes and composite attributes)

1NF (atomic values)

(remove partial FD)

2NF (allows only FFD)

(removes transitive FD)

3NFNormal forms

First normal form :- does not allow multi valued, complex and composite attributes

X Attribute should be atomic in nature.

Roll no	name	course
1	A	CO/CN
2	B	DBMS/OS

Roll no	name	course
1	A	CO
1	A	CN
2	B	DBMS
2	B	OS

## Second normal form :- (Partial FD removal)

$$AB \rightarrow D$$

$$B \rightarrow C$$

$$(AB)^+ = \{A, B, C, D\}$$

$AB \rightarrow$  candidate key.

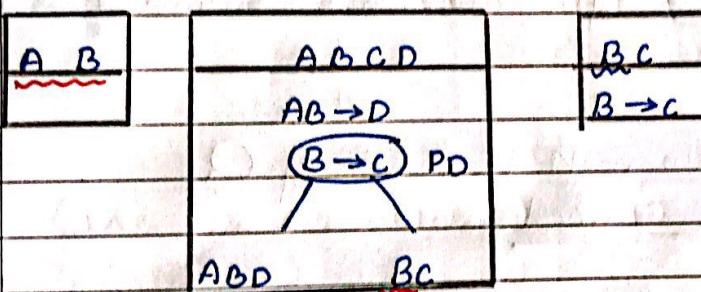
Prime attribute :- AB.

non-prime attribute :- CD.

When a non-prime attribute depends only on part of CK, then its PFD.

$$(AB)^+ = \{A, B, D, C\}$$

$$(B)^+ = \{B, C\}.$$



Total no of tables AB, ABD, BC (3 tables).

decomposition is lossless and dependency preserving.

Initial AB & ABD in 1<sup>st</sup> table  
 $AB \rightarrow$  PK of 1<sup>st</sup> table & 2<sup>nd</sup>.

$$ABD \cap BC$$

'B' → Key for 2<sup>nd</sup> table.

Third normal form :- (eliminate transitive FD)

Transitive dependency :- A FD from

$X \rightarrow Y$  is called transitive if

$X, Y \in \text{non-prime}$

① A relation is in 3NF if it is in 2NF and no transitive dependency.

Note :- To easily identify 3NF

PD :-	$P \rightarrow N_P$
	$N_P \rightarrow N_P$
	$\alpha \rightarrow \beta$

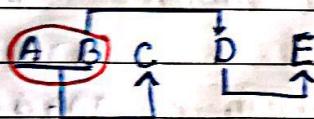
Example :-

① R(A,B,C,D,E)

$AB \rightarrow C$

$B \rightarrow D$

$D \rightarrow E$



1<sup>st</sup> step :-

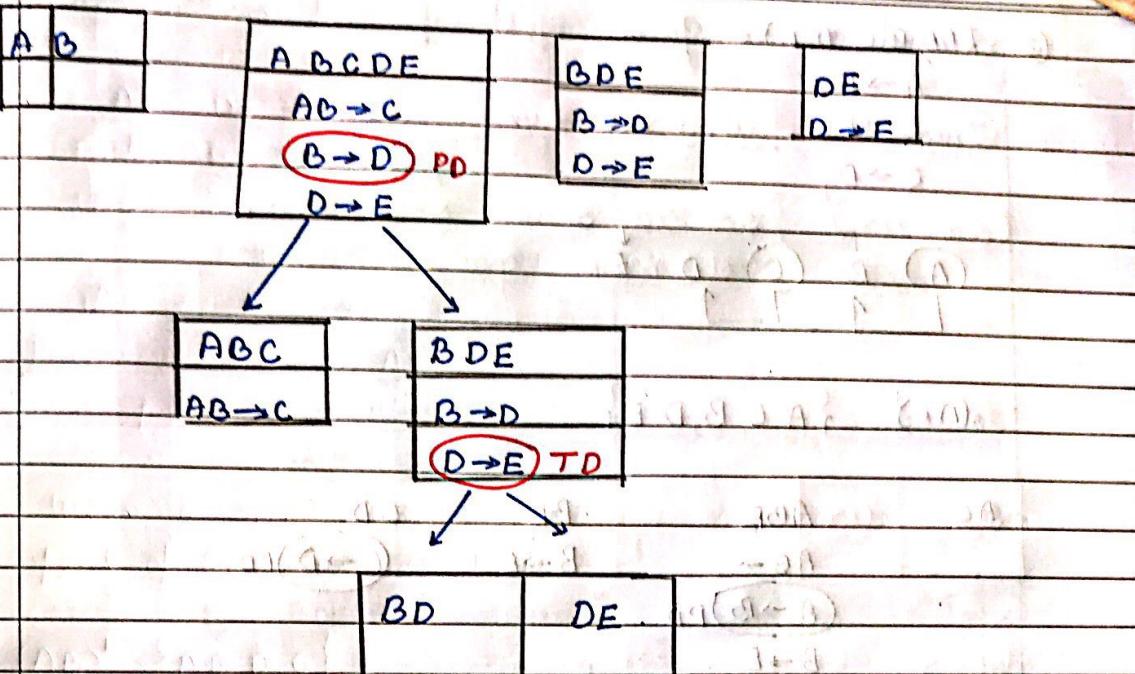
$(AB)^+ = (A, B, C, D, E) \checkmark$  candidate key - 1<sup>st</sup> table.

2<sup>nd</sup> step :-

$(AB)^+ = \{A, B, C, D, E\}$

$(B)^+ = \{B, D, E\}$

$(D)^+ = \{D, E\}$



(no of tuples : ) AB ABC BD DE.

given tuples are in 3NF.

② R(A,B,C,D,E)

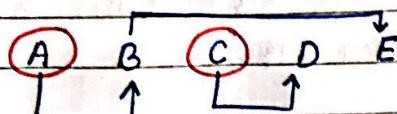
 $A \rightarrow B$  $B \rightarrow E$  $C \rightarrow D$ 

④ R(A,B,C,D,F,G,H,I,J)

 $AB \rightarrow C$  $A \rightarrow DE$  $B \rightarrow FG$  $F \rightarrow GH$  $D \rightarrow IJ$ 

③ R(A,B,C,D,E,F,G,H,I,J)

 $AB \rightarrow C$  $A \rightarrow DE$  $B \rightarrow F$  $F \rightarrow GH$  $D \rightarrow IJ$

(2)  $R(A, B, C, D, E)$  $A \rightarrow B$  $B \rightarrow E$  $C \rightarrow D$ 

$$(AC)^+ = \{A, C, B, D, E\}$$

$AC$	$ABE$	$BE$	$CD$
$AB \Leftarrow$	$B \rightarrow F$	$(C \rightarrow D)$ PD	
$(A \rightarrow B)$ PD			
$B \rightarrow E$			

$AC$	$ABE$	$CD$	$BE$	$(2^{\text{nd}} \text{ normal form})$
$A \rightarrow B$				
$(B \rightarrow E)$ TD				

AC    AB    BE    CD. (4-tuples are in 3NF)

$$AC \cap AB$$

$$AC \cap BE$$

$$ABC \cap CD$$

$$ABCDEF$$

losses and dependency preserving.

(3)  $R(A, B, C, D, E, F, G, H, I, J)$ 

$$AB \rightarrow C$$

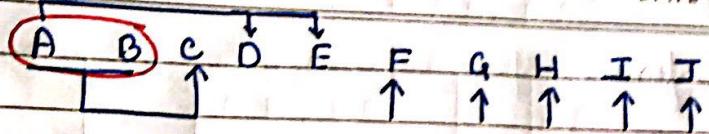
$$A \rightarrow DE$$

$$B \rightarrow F$$

$$F \rightarrow GH$$

$$D \rightarrow IJ$$

classmate



$$(AB)^+ = \{ A, B, C, D, E, F, G, H, I, J \}$$

AB      ABCDEFGHIJ      BFGH      FGH      OIJ  
 $AB \rightarrow C$   
 $A \rightarrow DE$  PD  
 $B \rightarrow F$  PD  
 $F \rightarrow GH$   
 $D \rightarrow IJ$

AB      ABC      ADEIJ      BFGH      FGH      OIJ      (2<sup>nd</sup> NF)

AB      ABC       $A \rightarrow DE$        $B \rightarrow F$   
 $D \rightarrow IJ$        $F \rightarrow GH$   
ADE      OIJ      BF      FGH

AB      ABC      ADE      OIJ      BF      FGH      (3<sup>rd</sup> NF)

④ Table form questions.

Student course details :-

Sid	cid	sname	sal	cname	cost	marks	grade

First normal form.

Sid	cid	SPN	SMN	SN	SDate	Smon	Syear	cname	cost	marks	grade

Second normal form.

Find the candidate key.

$(\text{sid}, \text{cid})^+ = \{\text{sid}, \text{cid}, \text{sname}, \text{salale}, \text{ename},$   
 $\text{cost}, \text{marks}, \text{grade}\}$

table 1

<u>sid</u>	<u>cid</u>
1	1

table 2

<u>sid</u>	<u>sname</u> (FN/MN/LN)	<u>salale</u> (D/MN)
1	A	1000

table 3

<u>cid</u>	<u>ename</u>	<u>cost</u>
1	B	1000

table 4

<u>sid</u>	<u>cid</u>	<u>marks</u>	<u>grade</u>
1	1	100	A



third normal form

values

<u>sid</u>	<u>cid</u>

table 2

<u>sid</u>	<u>sname</u>	<u>sdob</u>

table 3

<u>cid</u>	<u>cname</u>	<u>cost</u>

table 4

<u>sid</u>	<u>cid</u>	<u>marks</u>

table 5

<u>marks</u>	<u>grads</u>



BCNF :- in the above 3NF tables sid cid, sid, cid, marks are the determinants of student, course, marks, grads. These determinants are keys as well. Since determinants are the keys the given table is in BCNF.

## Detailed explanation of the problem.

- ① Determinant :- a determinant is that attribute of an entity which determines the value of other attributes.

Eg:- marks determines grade and hence the marks attribute is the determinant, represented as :-

$$\text{marks} \rightarrow \text{grade}$$

\* all determinants are not keys, however all keys are determinants.

Eg:- marks is a determinant but it is not a key because marks cannot determine the name, dob of a student.

On the contrary 'sid' is a determinant which can determine all the attributes and hence is called the key.

∴ Key is a determinant, that determines all attributes.

- ② Partial functional dependency :- when the key attribute of an entity does not completely determine an attribute then it is said that, the attribute is partially functionally dependent on the key attribute, in other words if the key attribute is a candidate key and if an attribute is not dependent on all the components of the candidate key then it is said

to be partially functionally dependent on the key attributes.

Eg:- in the above identified candidate keys i.e. (sid, sid) an attribute Sname depends only on Sid and Surname depends on sid. (So just part of the key).

- ③ Total functional dependency :- when all key attributes of an entity completely determine the attributes then it is said that the attribute is totally functionally dependent on the key attribute, in other words if the key is a candidate key and if an attribute depends on all the components of the candidate key then it is said that the attribute is totally functionally dependent on the CK.

Eg:- (sid, sid)  $\rightarrow$  marks.

- ④ Transitive functional dependency :- If an attribute of an entity depends on the key attribute indirectly through another attribute, then it is said that the attribute is transitively functionally dependant on the key attribute.

(cid, sid)  $\rightarrow$  marks.

marks  $\rightarrow$  grade.

FD that can be derived :-

cid, sid  $\rightarrow$  marks

Sid  $\rightarrow$  Sname, dob.

marks  $\rightarrow$  grade

Sid  $\rightarrow$  Sname, post, name

classmate

⑧ Convert the table upto BCNF.

<u>Proj no</u>	<u>Proj name</u>	<u>Empno</u>	<u>Empname</u>	<u>Rate category</u>	<u>hourly rate</u>
1023	Networking	101	Ellement	A	60
		102	Pauline	B	50
		103	Charles	C	40
1050	DB	101	Ellement	A	60
		107	David	B	50

↓  
1. first normal form

<u>Proj no</u>	<u>Proj name</u>	<u>Empno</u>	<u>Empname</u>	<u>Rate category</u>	<u>hourly rate</u>
1023	Networking	101	Ellement	A	60
1023	Networking	102	Pauline	B	50
1023	Networking	103	Charles	C	40
1050	DB	101	Ellement	A	60
1050	DB	107	David	B	50

↓  
2. second normal form

Partial dependency.

tab 1: Proj no    Empno

tab 2: Empno    Empname    Rate category    hourly rate

table 3 :-	<u>projno</u>	<u>program</u>



Third normal form :-

(Transitive dependency)

table 1 :-	<u>projid</u>	<u>empno</u>

table 2 :-	<u>empno</u>	<u>empname</u>

table 3 :-	<u>projno</u>	<u>program</u>

table 4 :-	<u>note category</u>	<u>hourly note</u>



all determinants are super keys so in BCNF.

FD :-  $\text{projid} \rightarrow \text{program}$ .

$\text{empid} \rightarrow \text{empno}$ .

$\text{note category} \rightarrow \text{hourly note}$

③ Consider the following relation

car-sale ( car#, date sold, salesman#, commission%, discount amt )

assume that a car may be sold by multiple salesperson and hence ( car#, salesman# ) is the PK  
additional dependencies are :-

$\text{date sold} \rightarrow \text{discount amt}$

$\text{salesman\#} \rightarrow \text{commission\%}$

Based on the given primary key is this relation in 1NF, 2NF or 3NF. Why or why not how would you successfully normalize it completely

car#	date-sold	salesman#	commission %	discount amt
------	-----------	-----------	--------------	--------------

(composite attribute)

so split into day, month and year

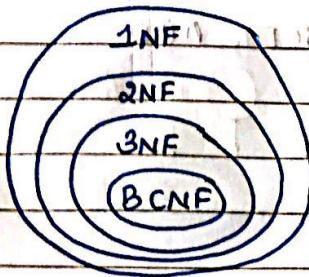
Second normal form (Partial dependencies)

table 1 :-	salesman#	car#			
table 2 :-	car#	date-sold	month	year	discount-amt
table 3 :-	salesman#	commission %			

3<sup>rd</sup> NF.

table 1 :-	salesman#	car#			
table 2 :-	car#	date-sold	month-sold	year-sold	
table 3 :-	salesman#	commission %			
table 4 :-	date-sold	discount amt			

How to identify normal form.



- ① BCNF is checked first (shortcut)

$$X \rightarrow Y$$

↓

Should be a superkey.

- ② Third NF

$$X \rightarrow Y$$

↓

Should be a superkey or 'Y' should be prime.

Problems :-

- ① R(A, B, C, D, E, F, G, H)

$$AB \rightarrow C$$

candidate key :- AB

$$A \rightarrow DE \text{ (PD)}$$

$$B \rightarrow F \text{ (PD)}$$

$$F \rightarrow GH \text{ (TD)}$$

FD is in 1<sup>st</sup> NF.

- ② R(A, B, C, D, E)

$$CE \rightarrow D$$

candidate key :- CE

$$D \rightarrow B \text{ (TD)}$$

$$C \rightarrow A \text{ (PD)}$$

FD is in 1<sup>st</sup> NF.

DATE [ ]

③  $R(A, B, C, D, E, F)$

$AB \rightarrow C$  (P0) CK:- BCD, ABD  
 $DC \rightarrow AE$  (PD)  
 $F \rightarrow F$  ✓

1<sup>st</sup> NF.

④  $R(A, B, C, D, E, G, H, I)$

$AB \rightarrow C$  CK:- ABD  
 $BD \rightarrow EF$   
 $AD \rightarrow GH$   
 $A \rightarrow I$

1<sup>st</sup> NF.

⑤  $R(ABCDE)$

$AB \rightarrow CD$  ✓ CK:- AB, BD, BC

$D \rightarrow A$  ✓ (prime attribute)

$BC \rightarrow DE$  ✓

3<sup>rd</sup> NF

⑥  $R(A, B, C, D, E)$

$BC \rightarrow ADE$  BC, GD  
 $D \rightarrow B$  (prime attribute)

1<sup>st</sup> NF. 3<sup>rd</sup> NF.

(8)  $R(U, W, X, Y, Z)$ 

$$\begin{array}{l} \downarrow \\ X \rightarrow Y \vee (P_D) \quad CK: UW, XW \\ Y \rightarrow Z \\ Z \rightarrow Y \\ UW \rightarrow X \checkmark (BCNF) \end{array}$$

$$\begin{array}{l} \downarrow \\ X \rightarrow Y \quad [2^{\text{nd}} NF] \\ \downarrow \\ \text{Part of } CK \quad \text{non-prime} \\ 1^{\text{st}} NF. \end{array}$$

(8)  $R(A, B, C, D, E, F)$ 

$$\begin{array}{ll} ABC \rightarrow D \quad (BCNF) & CK: ABD, ACD \\ ABD \rightarrow E & BCNF \times \\ CD \rightarrow F \quad (P_D) & 3NF \times \\ CDF \rightarrow B & \\ BF \rightarrow D & \end{array}$$

1NF

(9)  $R(A, B, C)$ 

$$\begin{array}{lll} A \rightarrow B & & \\ B \rightarrow C & A, B, C & \\ C \rightarrow A & & \end{array}$$

BCNF  $\checkmark$

(10)  $R(A, B, C, D, E, F)$ 

CK:-

 $A \rightarrow BCDEF$ 

A, BC, DEF

 $BC \rightarrow ADEF$  $DEF \rightarrow ABC$ 

BCNF ✓

(15)

(11)  $R(A, B, C)$  $AB \rightarrow C$ 

CK:- AB, BA

 $C \rightarrow A$ 3<sup>rd</sup> NF

(16)

(12)  $R(A, B, C, D, E)$  $A \rightarrow B$ 

CK:- ACD, BCD, CDE

 $BC \rightarrow E$  $DE \rightarrow A$ 3<sup>rd</sup> NF

(17)

(13)  $R(A, B, C, D, E)$  $AB \rightarrow CD$ 

CK:- AB, BC, BD.

 $D \rightarrow A$  (partial) $BC \rightarrow DE$ 

3NF

(18)

(14)  $R(W, X, Y, Z)$  $Z \rightarrow W$ 

CK:- Y, XW, XZ

 $Y \rightarrow ZX$  $XW \rightarrow Y$ 3<sup>rd</sup> NF

(15)  $R(A, B, C, D, E, F)$ 

$$\begin{array}{l} AB \rightarrow C \\ DC \rightarrow AE \\ E \rightarrow F \end{array}$$

OK!: ABD, BCD.  
INF

(16)  $R(A, B, C, D, E)$ 

$$\begin{array}{l} A \rightarrow B \\ B \rightarrow E \\ C \rightarrow D \end{array}$$

CK!: AE.  
INF  
INF

(17)  $R(V, W, X, Y, Z)$ 

$$\begin{array}{l} Z \rightarrow Y \\ Y \rightarrow X \\ X \rightarrow VV \\ VW \rightarrow Y \end{array}$$

OK!: XW  
INF

(18)  $R(A, B, C, D, E, F)$ 

$$\begin{array}{l} ABC \rightarrow D \\ ABD \rightarrow E \\ CD \rightarrow F \quad (PT) \\ CDF \rightarrow D \\ BF \rightarrow D \end{array}$$

CK!: ABD, ACD  
INF.

DATE


Gate Questions

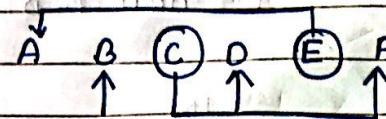
(19)  $R(A, B, C, D, E, F)$

$$C \rightarrow F$$

$$E \rightarrow A$$

$$EC \rightarrow D$$

$$A \rightarrow B.$$



$$(CE)^+ = \{C, F, F, A, B, D\}$$

1NF

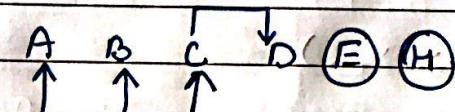
(20)  $R(A, B, C, D, E, H)$

$$A \rightarrow B$$

$$BC \rightarrow D$$

$$E \rightarrow C \text{ (PD)}$$

$$D \rightarrow A.$$



$$(EH)^+ = \{E, H, C\} \times$$

$$(AEH)^+ = \{A, E, H, D, C, D\} \checkmark$$

$$(BEH)^+ = \{B, E, H, C, D, A\} \checkmark$$

$$(CEH)^+ = \{C, E, H\} \times$$

$$(DEH)^+ = \{D, E, H, A, C, B\} \checkmark$$

AEH, BEH, DEH.

1NF

(21)  $R(A, B, C, D, E, P, G)$  $AB \rightarrow CD$  $DE \rightarrow P$  $C \rightarrow E$  $P \rightarrow C$  $B \rightarrow G$ .A B C D E P G  
↑↑↑↑↑↑ $(AB)^+ = \{A, B, C, D, E, G, P\} \checkmark$ 

INF.

(22)  $R(A, B, C, D, E, F, G, H)$ note  
CK $CH \rightarrow G$  $A \rightarrow BC$  (PD) $B \rightarrow CFH$  $E \rightarrow A$  $F \rightarrow EG$ 

INF.

A B C D E F G H  
↑↑↑↑↑↑↑↑

AD ✓

BD ✓

CD ✗

DE ✓

DF ✓

DG ✗

DH ✗

DCG ✗

DGH ✗

DCH ✗

DCGH ✗

(23)

 $R(A; B, C, D)$  $A \rightarrow B$  $B \rightarrow C$  $C \rightarrow BD$ .

CK: A

→ when the size of CK is  
y.  
it will be in QNF.

(24)  $R(A, B, C, D, E, F)$  $AB \rightarrow CD$  $CD \rightarrow EF$  $BC \rightarrow DEF$  $D \rightarrow B$  $CE \rightarrow F$ CK:-  $AB \checkmark$  $AC X$  $AD \checkmark$  $AE X$  $AF X$  $(ACE)^+ X$  $(ACF)^+ X$  $(AEF)^+ X$  $(ACEF)^+ X$ How to normalize a table.(25)  $R(A, B, C, D, E, F, G, H, I, J)$  $AB \rightarrow C$  $A \rightarrow DE$  $B \rightarrow F$  $D \rightarrow IJ$  $E \rightarrow GH$  $(AB)^+ = \{A, B, C, D, E, F, G, H, I, J\}$ 

Table in 1NF.

 $R_1(A, B)$  $R_2(A, BC)$  $R_3(A, D, E, I, J)$  $R_4(B, F, G, H)$ 

Table in 2NF

DATE

tables in 3NF.

R<sub>1</sub> (A B)

R<sub>2</sub> (A B C)

R<sub>3</sub> (A D E)

R<sub>4</sub> (D I J)

R<sub>5</sub> (B F)

R<sub>6</sub> (E, G, H)

do not take R<sub>2</sub> (A, B)  
to count.

So, number of tables is  
(5).