

$$\begin{pmatrix} \dot{q} \end{pmatrix} = J^+ \ddot{x}$$

$$\ddot{x} = J(q) \dot{q}$$

$N(J)$

$$\ddot{x} = \underbrace{\begin{bmatrix} J_{11} & J_{12} \end{bmatrix}}_{J(q)} \begin{bmatrix} \dot{q}_1 \\ \dot{q}_2 \end{bmatrix} = J_{11} \dot{q}_1 + J_{12} \dot{q}_2$$

$$J \dot{q} = 0$$

$$\min_{\dot{q}} \frac{1}{2} \dot{q}^T W \dot{q}$$

$$\text{sc } \dot{x} - J \dot{q} = 0$$

$$L = \frac{1}{2} \dot{q}^T W \dot{q} + \lambda^T (\dot{x} - J \dot{q})$$

$$\nabla_{\dot{q}} L = 0$$

$$W \dot{q} - J^T \lambda = 0$$

$$\nabla_{\lambda} L = 0$$

$$\rightarrow \dot{x} - J \dot{q} = 0$$

$$= \frac{1}{2} [\dot{q}_1 \quad \dot{q}_2] \begin{bmatrix} a & b \\ b & c \end{bmatrix} \begin{bmatrix} \dot{q}_1 \\ \dot{q}_2 \end{bmatrix}$$

$$\begin{bmatrix} a\dot{q}_1 + b\dot{q}_2 \\ b\dot{q}_1 + c\dot{q}_2 \end{bmatrix}$$

$$= \frac{1}{2} \left[\underset{\substack{\uparrow \\ \text{kinetic}}}{a\dot{q}_1^2} + \underset{\substack{\uparrow \\ \text{kinetic}}}{c\dot{q}_2^2} + 2\dot{q}_1\dot{q}_2 \quad \bigg| \quad b \right]$$

$$J = U \Sigma V^T$$

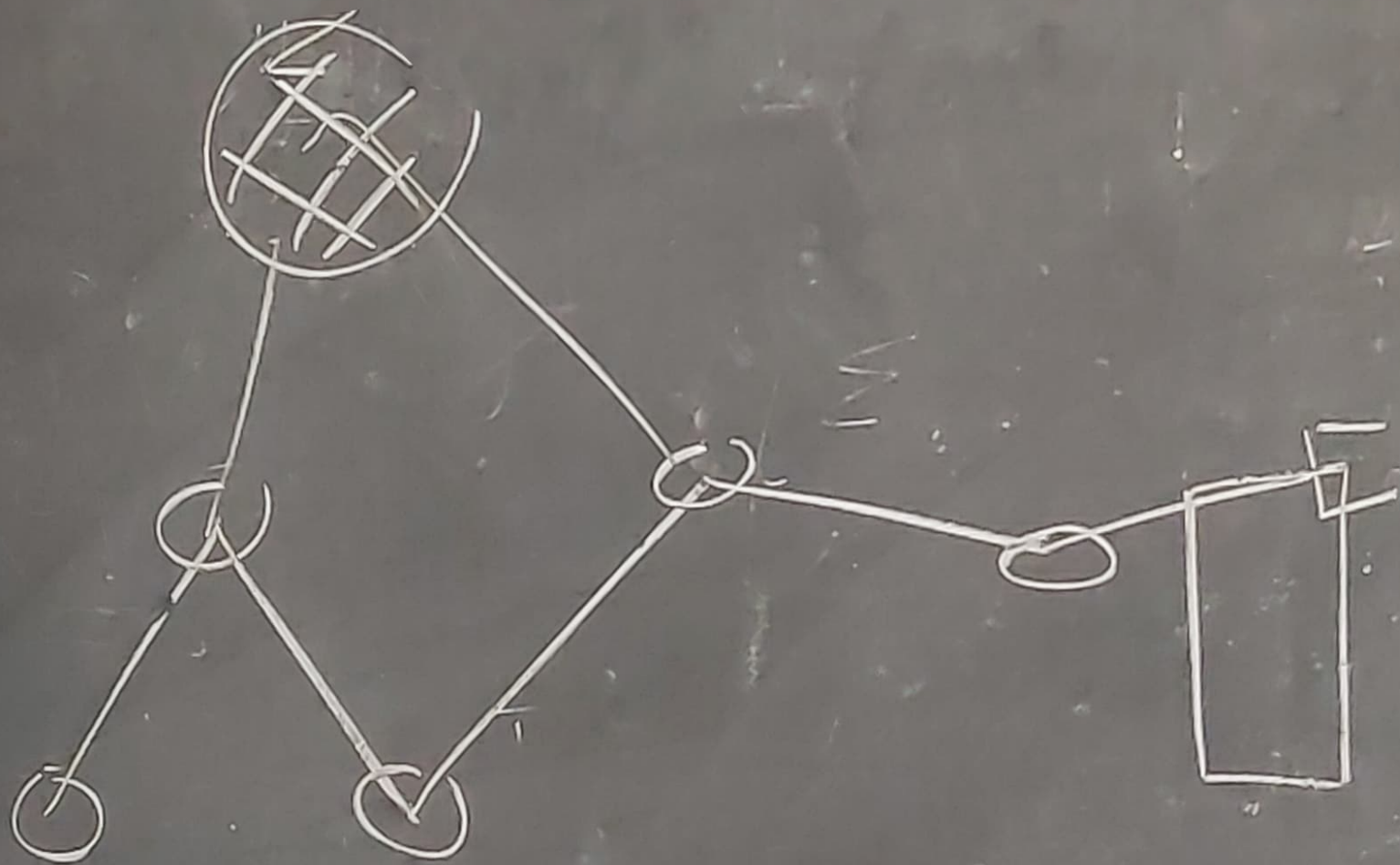
$$J^T = V \Sigma^T U^T$$

$$J_{DLS} = V \Sigma^T U^T \left[U \Sigma \Sigma^T U^T + \mu^2 U U^T \right]^{-1}$$

$$= V \Sigma^T U^T U \left[\Sigma \Sigma^T + \mu^2 I \right]^{-1} U^T$$

$$= V \left[\Sigma^T \left[\Sigma \Sigma^T + \mu^2 I \right]^{-1} \Sigma \right] U^T$$

$$\Sigma_{DLS}$$



$$J_A = \begin{bmatrix} g_{11} & g_{12} \\ -s_1 & 0 \end{bmatrix}$$

$$d\mathcal{J}_h = s_1 \dot{q}_{12}$$

$$J_A = \begin{bmatrix} J \\ J_h \end{bmatrix}$$

\uparrow
 \dot{x}_h

$$y = \cos(q_2)$$

$$\dot{y} = -s_1(q_2) \dot{q}_2$$