

Accretion in binary systems

Ilia Kosenkov, 2017-12-01 @ Tuorla



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 - Different stars end evolution timescales \rightarrow transfer through L_1
 - Mass ejection in the form of stellar wind \rightarrow wind accretion
- Parameters of a binary can evolve with time (e.g. angular momentum loss)

Roche geometry

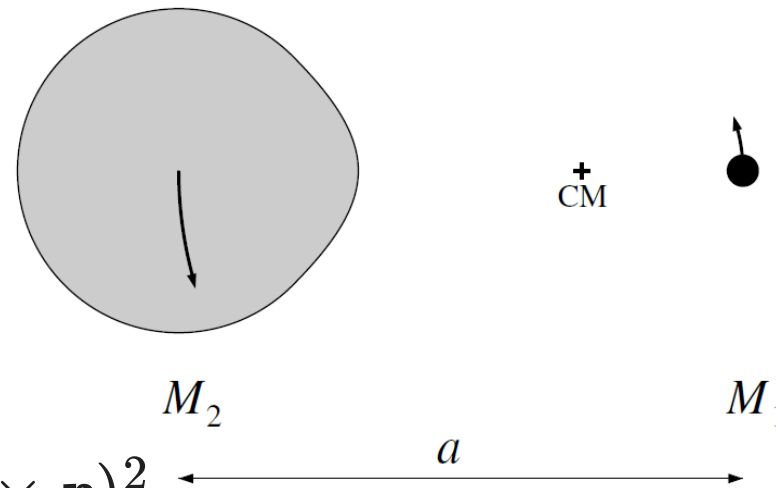
Kepler's law $4\pi^2 a^3 = GMP^2$

$$q = \frac{M_2}{M_1} \quad m = \frac{M}{M_\odot}, \text{ and}$$

$$|\omega| = \left[\frac{GM}{a^3} \right]^{\frac{1}{2}} \frac{\partial \mathbf{v}}{\partial t} + (\mathbf{v} \cdot \nabla) \mathbf{v} =$$

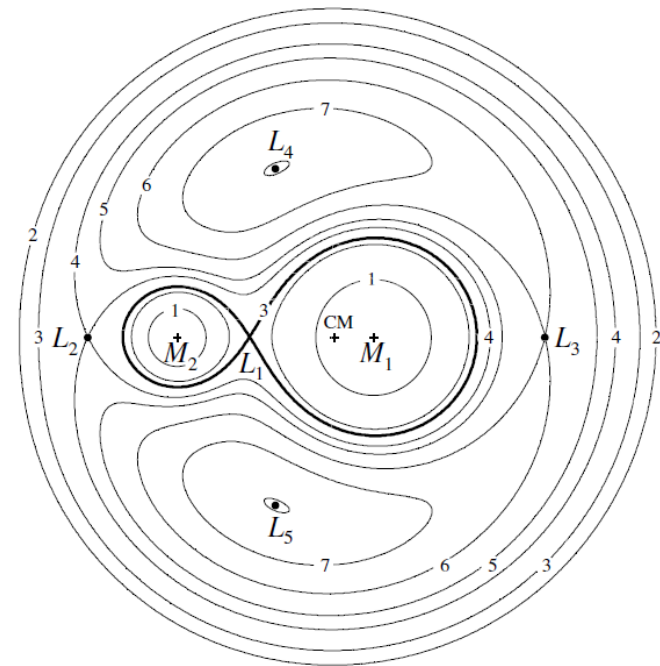
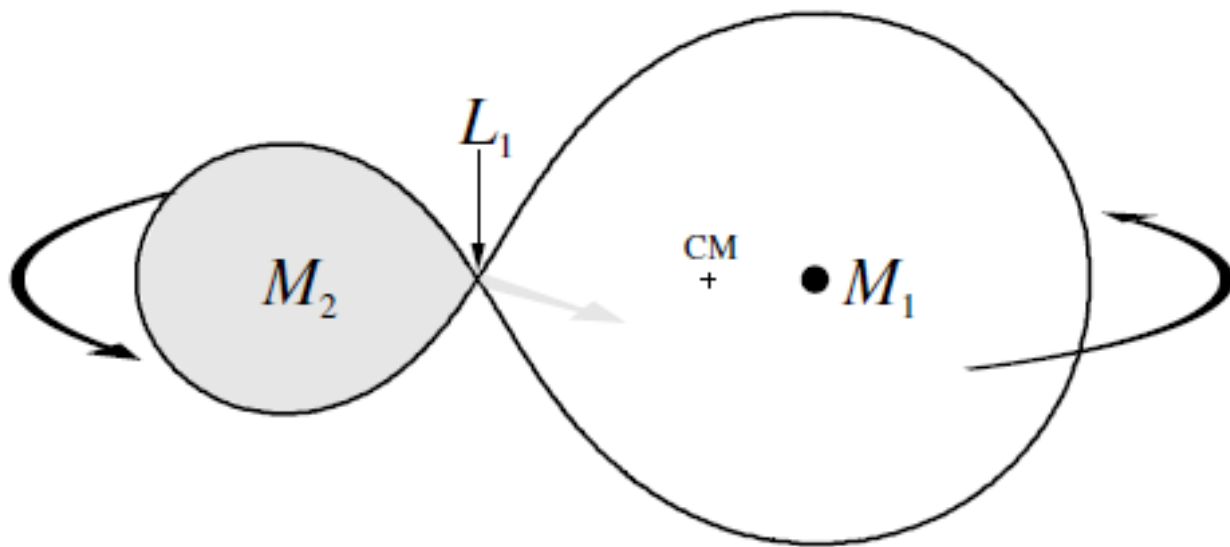
$$= -\nabla \Phi_R - 2\omega \times \mathbf{v} - \frac{1}{\rho} \nabla P$$

$$\Phi_R(r) = -\frac{GM_1}{|\mathbf{r}-\mathbf{r}_1|} - \frac{GM_2}{|\mathbf{r}-\mathbf{r}_2|} - \frac{1}{2} (\omega \times \mathbf{r})^2$$





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$$\text{And period-radius relation for a lower part main sequence star } R_2 \cong 7.9 \times 10^9 P_{\text{hr}} \text{ cm}$$



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and

$$\frac{\dot{R}_2}{R_2} = \frac{2\dot{J}}{J} + \frac{2(-\dot{M}_2)}{M_2} \left(\frac{5}{6} - \frac{M_2}{M_1} \right)$$



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$-\dot{M}_2(\text{inst}) = \dot{M}_0 \exp\left[\frac{R_*-R_2}{H_*}\right] \approx 10^{-8} M_{\odot} \text{ yr}^{-1}$ for a lower main sequence stars



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$$v_{\perp} \approx b_1 \omega \approx 100 m_1^{1/3} (1 + q)^{1/3} P_{\text{day}}^{-2/3} \text{ km s}^{-1}$$

$$v_{\parallel} \lesssim c_s \approx 10 \text{ km s}^{-1} \text{ for a } 10^5 \text{ K envelope temperature}$$



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$$\frac{R_{\text{circ}}}{a} = (1 + q)[0.500 - 0.227 \lg q]^4$$

$$L_{\text{disc}} = \frac{GM_1 \dot{M}}{2R_*} = \frac{1}{2} L_{\text{acc}}$$

Accretion in close binaries: other possibilities

$$v_w \approx \left(\frac{2GM_E}{R_E} \right)^{1/2}$$

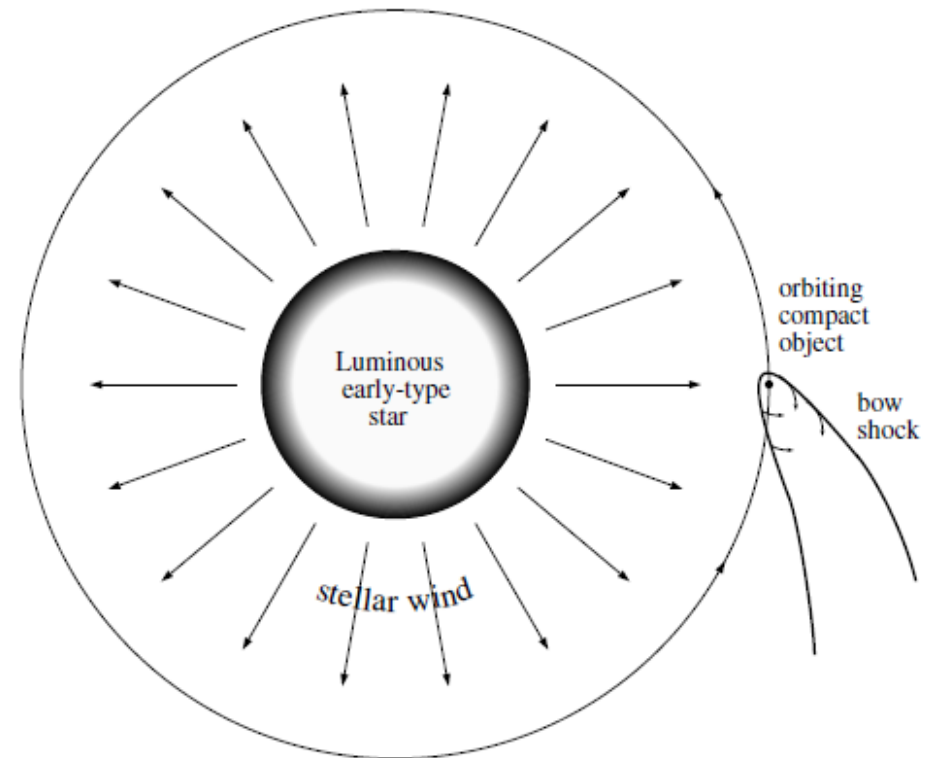
For a $10^{-5} M_\odot \text{ yr}^{-1}$ mass loss rate

$$v_w \approx \text{few} \times 10^3 \text{ km s}^{-1}$$

The wind sweeps at angle

$$\beta \approx \tan^{-1}(v_n/v_w)$$

and relative speed $v_{\text{rel}} \approx (v_n^2 + w_w^2)^{1/2}$



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Fraction of mass captured by accretor is

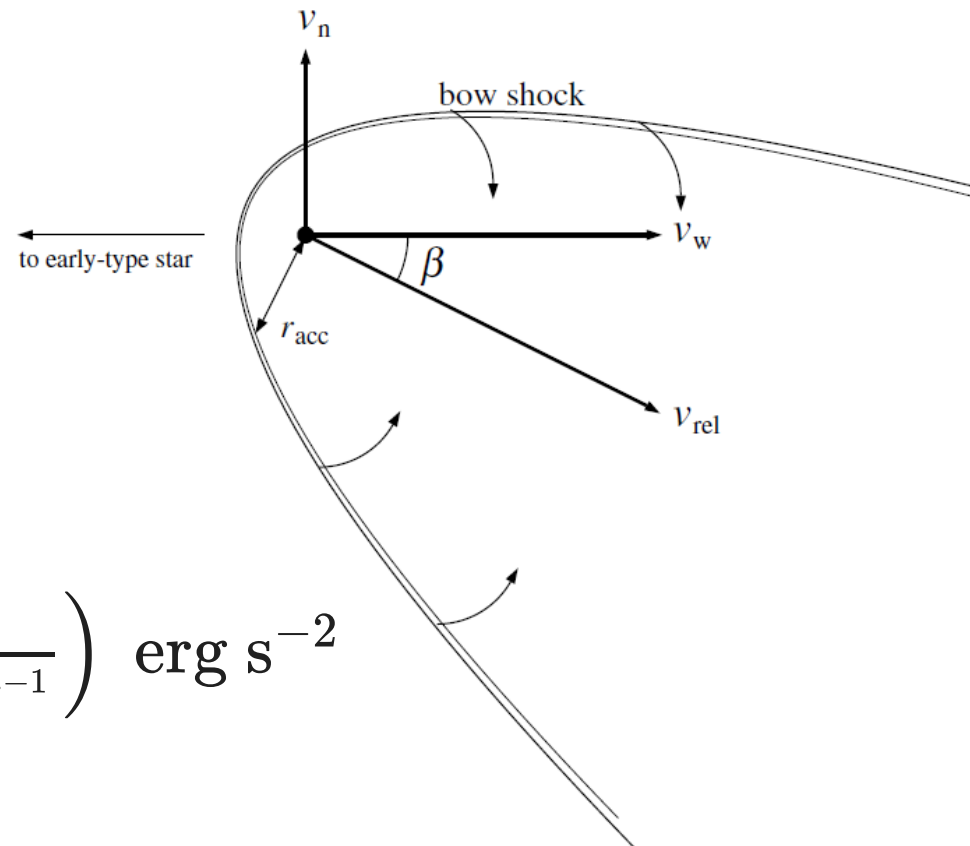
$$\frac{\dot{M}}{-\dot{M}_w} \approx \frac{1}{4} \left(\frac{M_n}{M_E} \right)^2 \left(\frac{R_E}{a} \right)^2$$

in a cylindrical region of $r \approx 2GM_n/v_{\text{rel}}^2$

which gives luminosity of the order of

$$L_{\text{acc}} \approx 10^{37} \left(\frac{\dot{M}}{-10^{-4} \dot{M}_w} \right) \left(\frac{-\dot{M}_w}{10^{-5} M_{\odot} \text{ yr}^{-1}} \right) \text{ erg s}^{-2}$$

which is mainly emitted in X-rays





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The circularization radius is $\frac{R_{\text{circ}}}{a} = \frac{M_n^3(M_n + M_E)}{16\lambda^4(a)M_E^4} \left(\frac{R_E}{a}\right)^4$ with $\lambda(r) \approx \frac{v_w^2}{v_{\text{esc}}^2} \approx 1$



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The uncertainty in λ makes it hard to estimate whether the circularization radius is large enough for a disk to form.



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- Irradiation by the luminosity resulting from accretion can further boost the process and make it self-sustainable. Can possibly stimulate wind loss.
- In supersoft binaries (accretor is WD) accretion process can be boosted by a factor of ~ 40 by steady nuclear burning at the surface.



Thank you!