JuliaBUGS

What is **BUGS**?

- Influential project that began in 1989, right here
- The first Probabilistic Programming Language
- Software for Bayesian analysis of statistical model
 - Originally with Gibbs
 - Now HMC/NUTS with JuliaBUGS, and more algorithms coming

Why Choose JuliaBUGS?

- Compatible with existing Bugs syntax
- User-friendly modelling language
- Generates the Directed Acyclic Graph (DAG)
- Works seamlessly with other Julia packages
- Supports distributed, parallel, and GPU computations*

A Simple Example - Rats

The weights of 30 young rats were measured weekly for five weeks

Rat	$x_j = 8$	$x_j = 15$	$x_j=22$	$x_j=29$	$x_j = 36$
1	151	199	246	283	320
2	145	199	249	293	354
• • •					
30	153	200	244	286	324

The Rats Model

$$Y_{ij} \sim ext{Normal}\left(lpha_i + eta_i \, (x_j - ar{x}), au_c
ight) \ lpha_i \sim ext{Normal}\left(lpha_c, au_lpha
ight) \ eta_i \sim ext{Normal}\left(eta_c, au_eta
ight)$$

BUGS Program for the Rats Model

```
model_def = @bugs("""model{
    for( i in 1 : N ) {
        for( j in 1 : T ) {
        Y[i, j] \sim dnorm(mu[i, j], tau.c)
        mu[i, j] <- alpha[i] + beta[i] * (x[j] - xbar)
        alpha[i] ~ dnorm(alpha.c,alpha.tau)
        beta[i] ~ dnorm(beta.c,beta.tau)
    tau.c \sim dgamma(0.001,0.001)
    sigma <- 1 / sqrt(tau.c)</pre>
    alpha.c \sim dnorm(0.0, 1.0E-6)
    alpha.tau \sim dgamma(0.001,0.001)
    beta.c \sim dnorm(0.0, 1.0E-6)
    beta.tau \sim dgamma(0.001,0.001)
    alpha0 <- alpha.c - xbar * beta.c
}""", false) # `false` means R-style variable names are kept
```

Workflow in JuliaBUGS

Step 1 Write the model in Julia-flavored or the original BUGS syntax, then use @bugs macro to transform it into Julia AST

```
quote
    for i = 1:N
        for j = 1:T
            $(Expr(:~, :(Y[i, j]), :(dnorm(mu[i, j], var"tau.c"))))
            mu[i, j] = alpha[i] + beta[i] * (x[j] - xbar)
        end
        $(Expr(:~, :(alpha[i]), :(dnorm(var"alpha.c", var"alpha.tau"))))
        $(Expr(:~, :(beta[i]), :(dnorm(var"beta.c", var"beta.tau"))))
    end
    $(Expr(:~, Symbol("tau.c"), :(dgamma(0.001, 0.001))))
    sigma = 1 / sqrt(var"tau.c")
    $(Expr(:~, Symbol("alpha.c"), :(dnorm(0.0, 1.0e-6))))
    $(Expr(:~, Symbol("alpha.tau"), :(dgamma(0.001, 0.001))))
    $(Expr(:~, Symbol("beta.c"), :(dnorm(0.0, 1.0e-6))))
    $(Expr(:~, Symbol("beta.tau"), :(dgamma(0.001, 0.001))))
    alpha0 = var"alpha.c" - xbar * var"beta.c"
end
```

Step 2 *Prepare data and initial values*

```
data=(
    x=[8.0, 15.0, 22.0, 29.0, 36.0],
    xbar=22, N=30, T=5,
   Y=[
        151 199 246 283 320
        145 199 249 293 354
        153 200 244 286 324
inits=(
    alpha=ones(Integer, 30) .* 250,
    beta=ones(Integer, 30) .* 6,
    var"alpha.c"=150, var"beta.c"=10, var"tau.c"=1,
    var"alpha.tau"=1, var"beta.tau"=1,
```

Step 3 Compile the model

```
model = compile(model_def, data, inits)
```

A series of functions are implemented for the <code>model</code>:

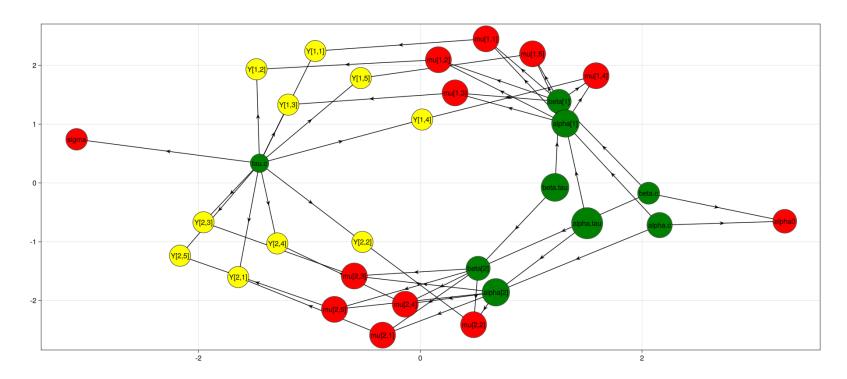
```
julia> LogDensityProblems.dimension(model) # number of parameters
65
```

and

```
julia> LogDensityProblems.logdensity(model, rand(65)) # log-density of the model
-1.2096997168777153e7
```

Visualizing the **BUGSModel** as a DAG

To visualize the Directed Acyclic Graph (DAG) underlying the BUGSModel, we can utilize standard plotting libraries. In this example, we employ Makie.jl and illustrate the DAG using only the first two rows of the rats' weights data.



Step 4 Transform the model to be AD-ready (only necessary for HMC/NUTS)

```
ad_model = ADgradient(:ReverseDiff, model; compile = Val(true)) # if using ReverseDiff
ad_model = ADgradient(:ForwardDiff, model) # if using ForwardDiff
```

After the transformation, we can take the gradient of the log-density function

```
julia>logp, gradients = LogDensityProblems.logdensity_and_gradient(ad_model, rand(65));

julia> gradients
65-element Vector{Float64}:
    11.027615568346802
    14.156247939871195
3288.2000788518317
...
1800.9201449927032
```

Step 5 Ready to sample!

```
n_samples = 3000; n_adapts = 1000 # number of samples and adaptation steps
initial_θ = rand(LogDensityProblems.dimension(model)) # initial values
samples_and_stats = AbstractMCMC.sample(
    ad_model,
    AdvancedHMC.NUTS(0.65),
    n_samples;
    chain_type = Chains,
    n_adapts = n_adapts,
    init_params = initial_θ,
    discard_initial = n_adapts,
)
```

Here we

- Use the AbstractMCMC interface to sample
- An McMcChains.Chain object is returned (see next slide)

The sampling results (simplified for legibility)

```
Chains MCMC chain (3000×80×1 Array{Real, 3}):
. . .
Summary Statistics
  parameters
                              std
                                       mcse
                                               ess_bulk
                                                              rhat
                   mean
                                                                     ess_per_sec
      Symbol
                Float64
                          Float64
                                    Float64
                                                    Real
                                                           Float64
                                                                         Missing
      beta.c
                 6.1856
                           0.1083
                                     0.0018
                                              3594.9367
                                                            1.0005
                                                                         missing
                                     0.0119
                                                                         missing
       sigma
                 6.0966
                           0.4802
                                              1640.5283
                                                            0.9998
      alpha0
               106.6111
                           3.5747
                                     0.0574
                                              3884.4420
                                                            1.0005
                                                                         missing
Quantiles
  parameters
                             25.0%
                                                               97.5%
                   2.5%
                                        50.0%
                                                   75.0%
      Symbol
                Float64
                           Float64
                                      Float64
                                                 Float64
                                                             Float64
      beta.c
                            6.1156
                                       6.1855
                                                   6.2578
                                                              6.3940
                 5.9663
       sigma
                 5.2499
                            5.7528
                                       6.0588
                                                   6.4025
                                                              7.1354
      alpha0
                                     106.6278
                99.8404
                          104.1624
                                                108.9566
                                                            113.6170
```

which contains all the sample values and statistics

Registering Functions and Distributions

Juliabugs has implemented most of the distributions and functions in Bugs

Users can also register their own functions and distributions by

```
JuliaBUGS.@register_primitive function myfunc(x::Float64, y::Float64)
   return x + y
end
```

alternatively,

```
function myfunc(x::Float64, y::Float64)
    return x + y
end
JuliaBUGS.register_primitive(myfunc)
```

then myfunc is ready to use in a JuliaBUGS model

Source Folder Tour

```
- ext # package extensions

    JuliaBUGSAdvancedHMCExt.jl

    JuliaBUGSGraphMakieExt.jl

    JuliaBUGSGraphPlotExt.jl

    JuliaBUGSTikzGraphsExt.jl

 src # source code
     BUGSExamples # defines examples from OpenBUGS
         BUGSExamples.jl
         Backgrounds
           — README.md
           — rats.md
         README.md
         · Volume I
          ├─ Blocker.jl
      └─ Volume II
            — BiRats.jl
            — Eyes.jl
     BUGSPrimitives # defines BUGS distributions and functions
         BUGSPrimitives.jl
        — distributions.jl
        functions.jl
     JuliaBUGS.jl
     compiler_pass.jl # compiler implementation
     graphs.jl # the DAG MetaGraph interface
    - logdensityproblems.jl # the LogDensityProblem interface
     model.jl # defines the model and log-density computation
     parser.jl # the parser of BUGS
    - utils.jl
    - variable_types.jl # defines some datatype used in the compiler
```

Current Status and Caveats

- Juliabugs is in early development. Bugs and discrepancies with Bugs may exist.
- The compiler is not optimized for large models.
- Initial compile function calls may be slow, but subsequent calls will be faster.
- Inference is supported via the LogDensityProblem interface with HMC/NUTS from AdvancedHMC.jl and MH algorithms from AdvancedMH.jl.
- We are working on exploiting the graphical structure for implementing algorithms.

Future Plans

- Optimize the compiler to handle larger models efficiently
- Extend inference support with more algorithms and more efficient implementations
- Continue testing and debugging

Collaborate with us!