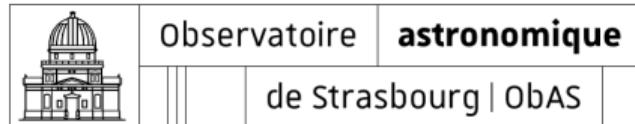




# Modified gravity under scrutiny – testing MOND with pairs of SDSS MaNGA galaxies

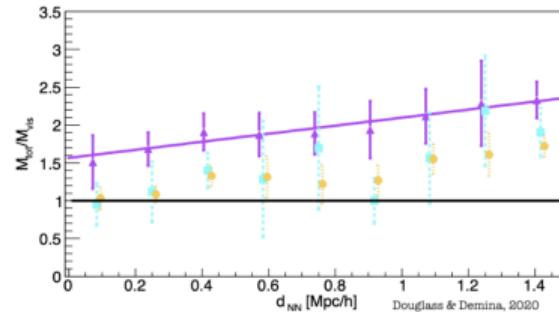
Özgen Tunç Türker

Supervisors  
Oliver Müller & Benoit Famaey



# Goal of The Project

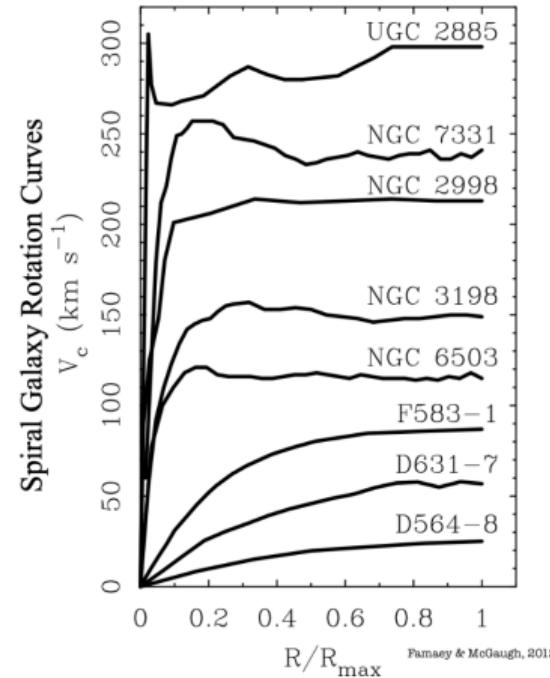
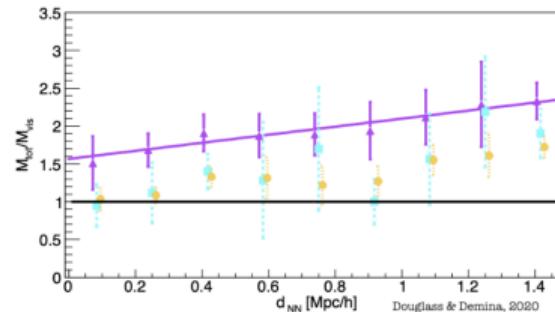
## A Systematic Behaviour



# Goal of The Project

## Observed by Galaxy Rotation Curves

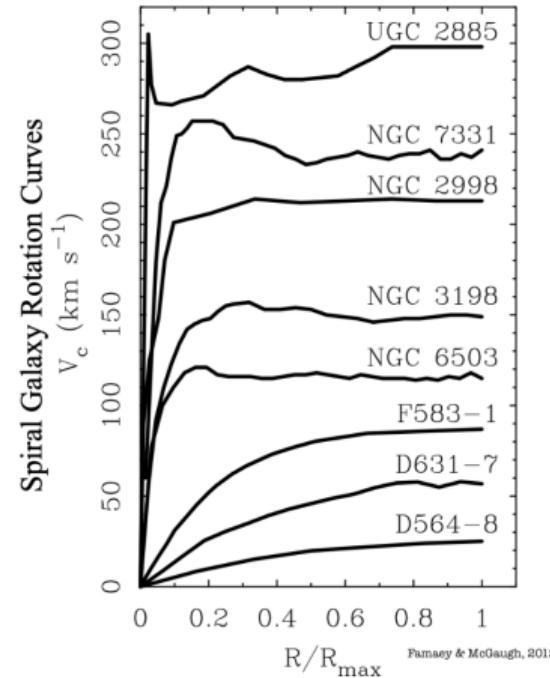
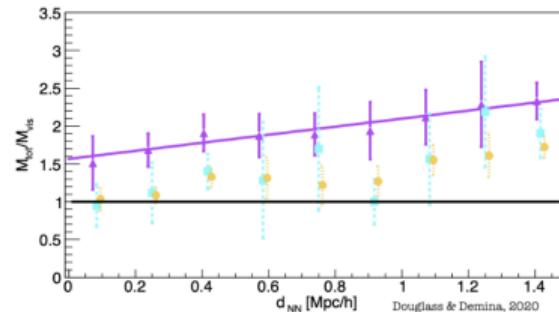
### A Systematic Behaviour



# Goal of The Project

Observed by Galaxy Rotation Curves

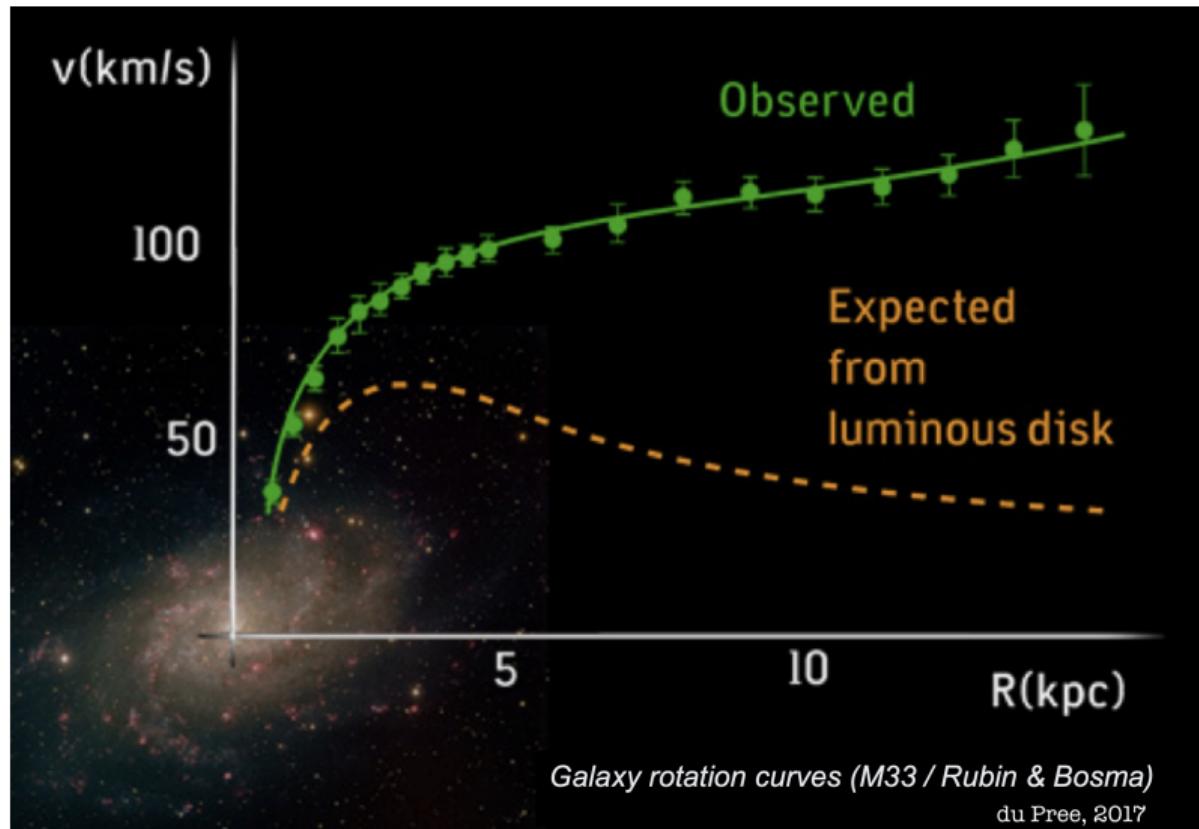
A Systematic Behaviour



Is it explainable in Modified Gravity Context?

# **Missing Mass: Dark Matter & It's Challenges**

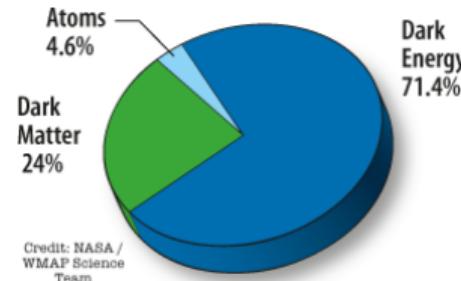
# Missing Mass Problem



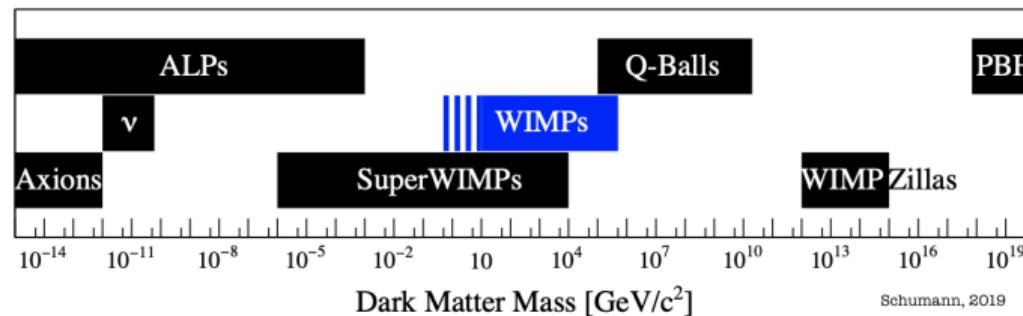
- ▶ 1930s
- ▶ Dynamic vs. Content
- ▶ Unvisible Matter
- ▶ Rubin & Bosma
- ▶ late '70s

# Dark Matter Puzzle

## Dark Matter: Cold & Non-Baryonic

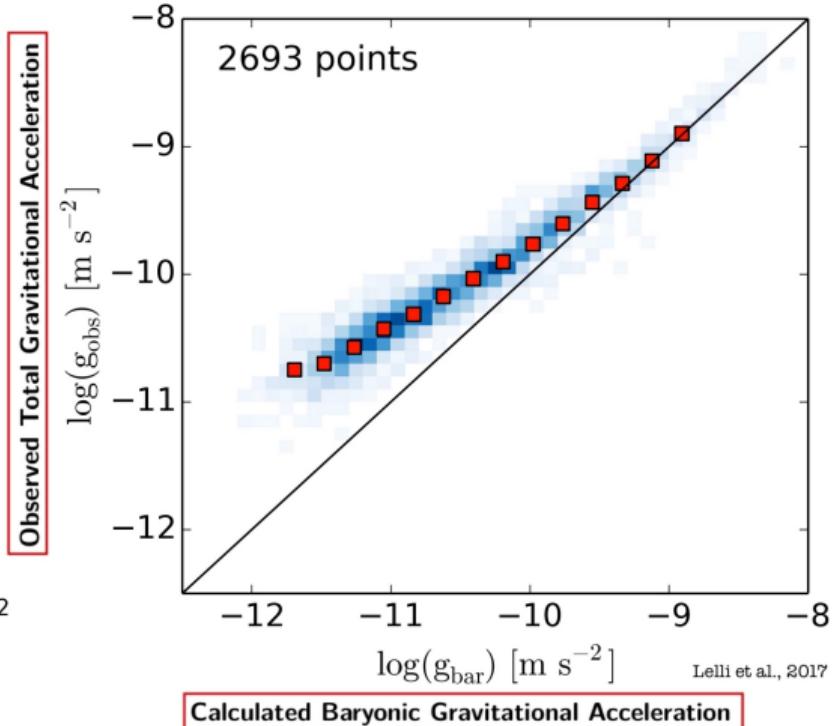
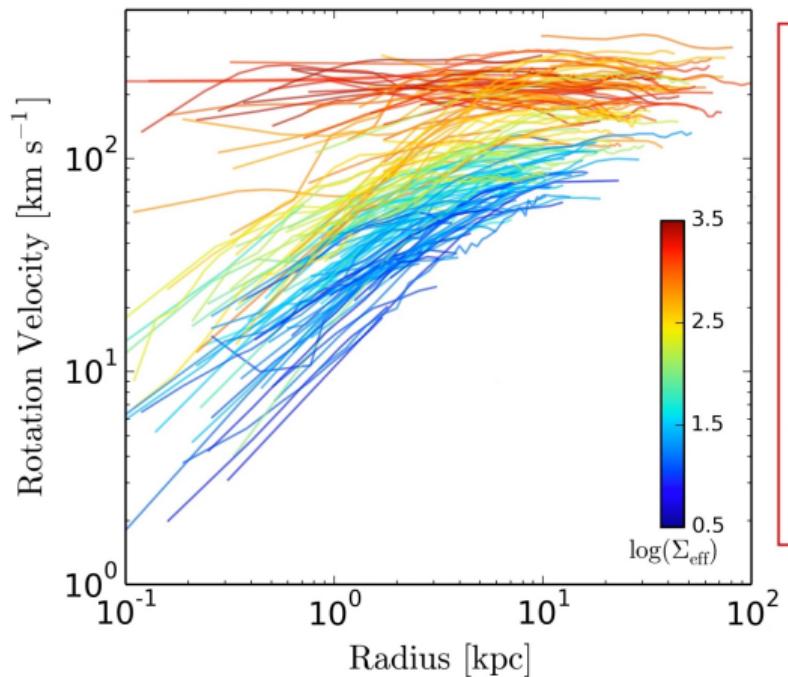


Content of the universe today



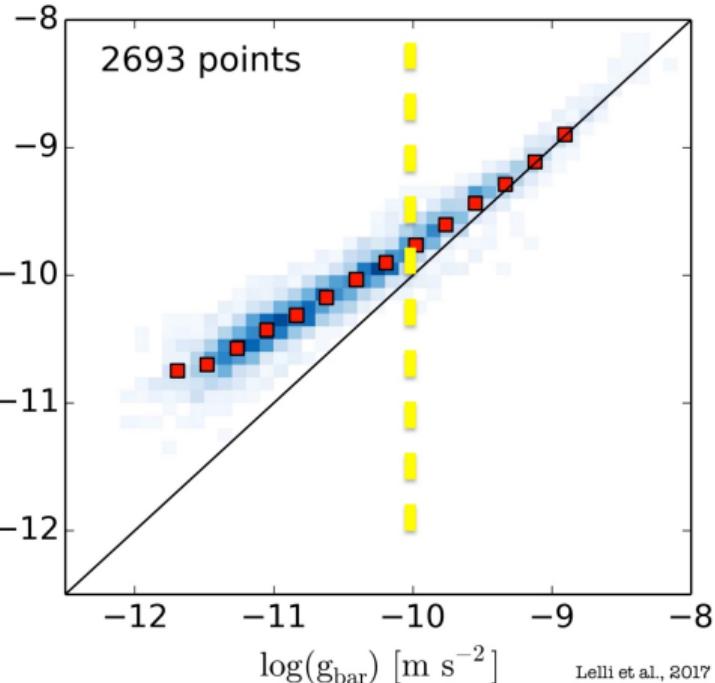
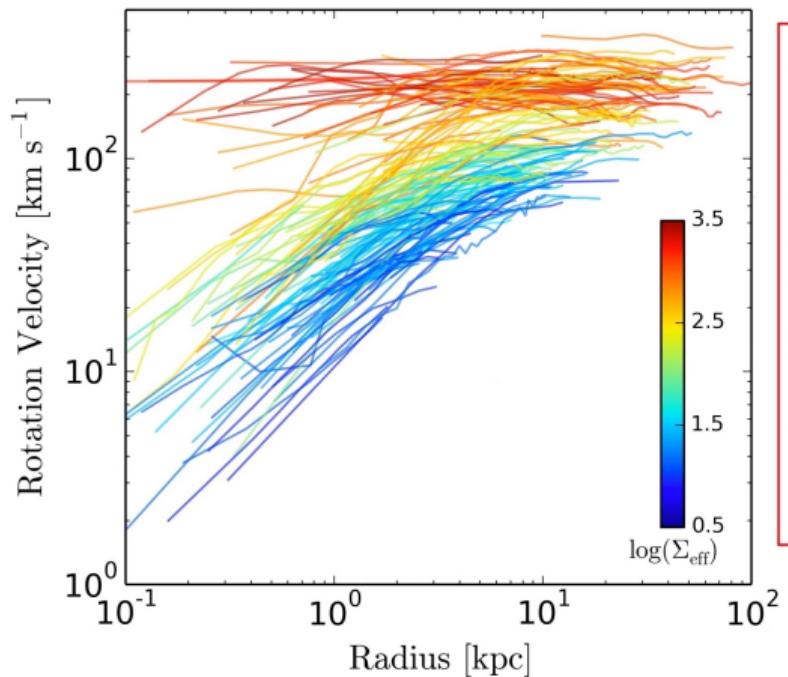
Different dark matter candidates on a many order of magnitude mass range.

# The Radial Acceleration Relation



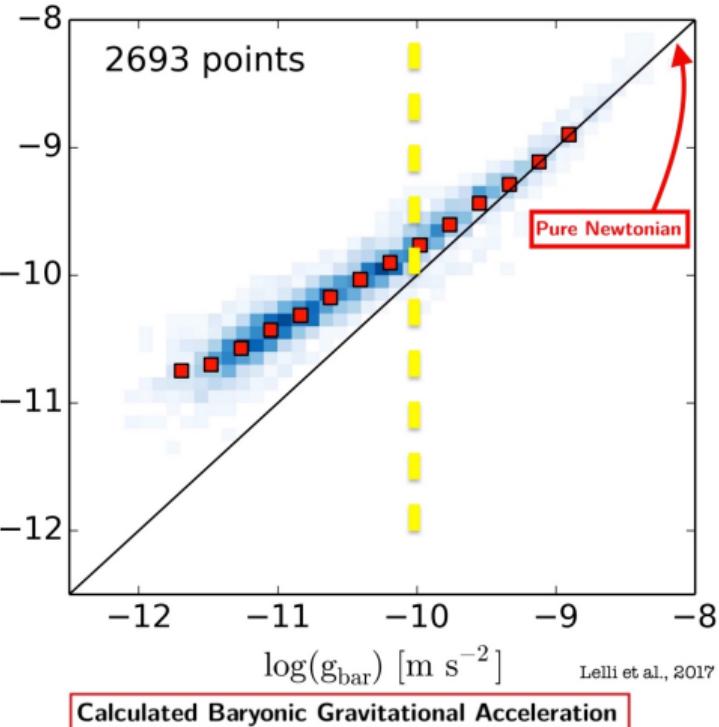
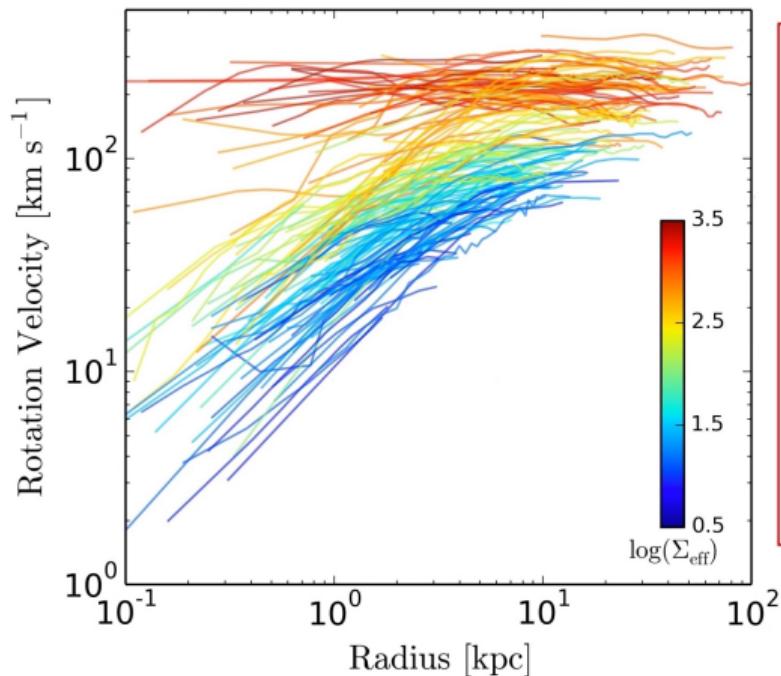
Why do mass discrepancies correlate with acceleration?

# The Radial Acceleration Relation



Why do mass discrepancies correlate with acceleration?

# The Radial Acceleration Relation



Why do mass discrepancies correlate with acceleration?

# An alternative World: Modified Newtonian Dynamics

# Introduction to MOND

- Mordehai Milgrom in 1983 (~ Dark Matter gets widely accepted.)

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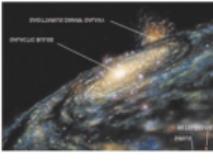
- ▶ Milgrom's law:

$$g \mu\left(\frac{g}{a_0}\right) = g_N$$

$$\mu\left(\frac{g}{a_0}\right) \rightarrow 1 \quad \text{for } g \gg a_0 \quad \& \quad \mu\left(\frac{g}{a_0}\right) \rightarrow \frac{g}{a_0} \quad \text{for } a_0 \gg g$$

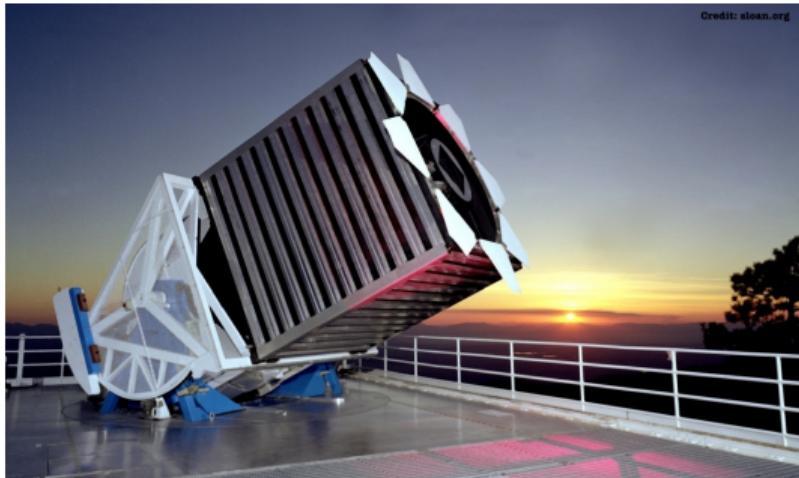
# External Field Effect (EFE)

- ▶ MOND breaks fundamental principle of **GR**: Strong Equivalence Principle.
- ▶ When the galaxy is not **isolated** then **total acceleration** matters

<b>Newtonian Regime</b> $g_{in} > a_0$  $M = \frac{RV^2}{G}$ e.g., surface of the Earth	<b>MOND Regime</b> <b>isolated systems</b> $g_{in} < a_0$  $M = \frac{V^4}{a_0 G}$ e.g., remote dwarf Leo 1
<b>External Field Dominant Newtonian Regime</b> $g_{in} < a_0 < g_{ex}$  $M = \frac{RV^2}{G}$ e.g., globular Cluster M13	<b>non-isolated systems</b> <b>External Field Dominant Quasi-Newtonian Regime</b> $g_{in} < g_{ex} < a_0$  $M = \frac{g_{ex} RV^2}{a_0 G}$ e.g., nearby Sgr dwarf

# **SDSS & MaNGA**

# SDSS & MaNGA

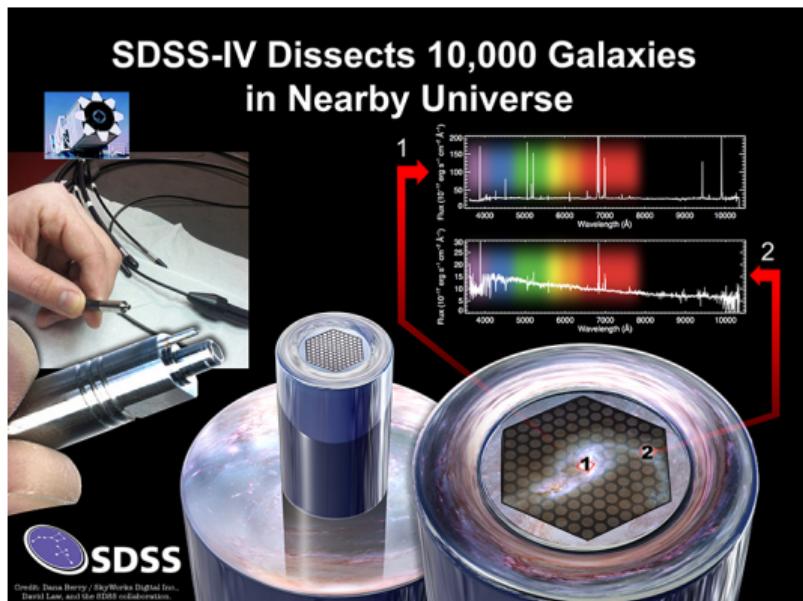


*Sloan Digital Sky Survey at Apache Point Observatory in New Mexico, United States*

- ▶ “Multi-color images of 1/3 of the sky, and spectra for more than three million astronomical objects”

- ▶ “17 simultaneous ‘integral field units’, each composed of tightly-packed arrays of optical fibers”

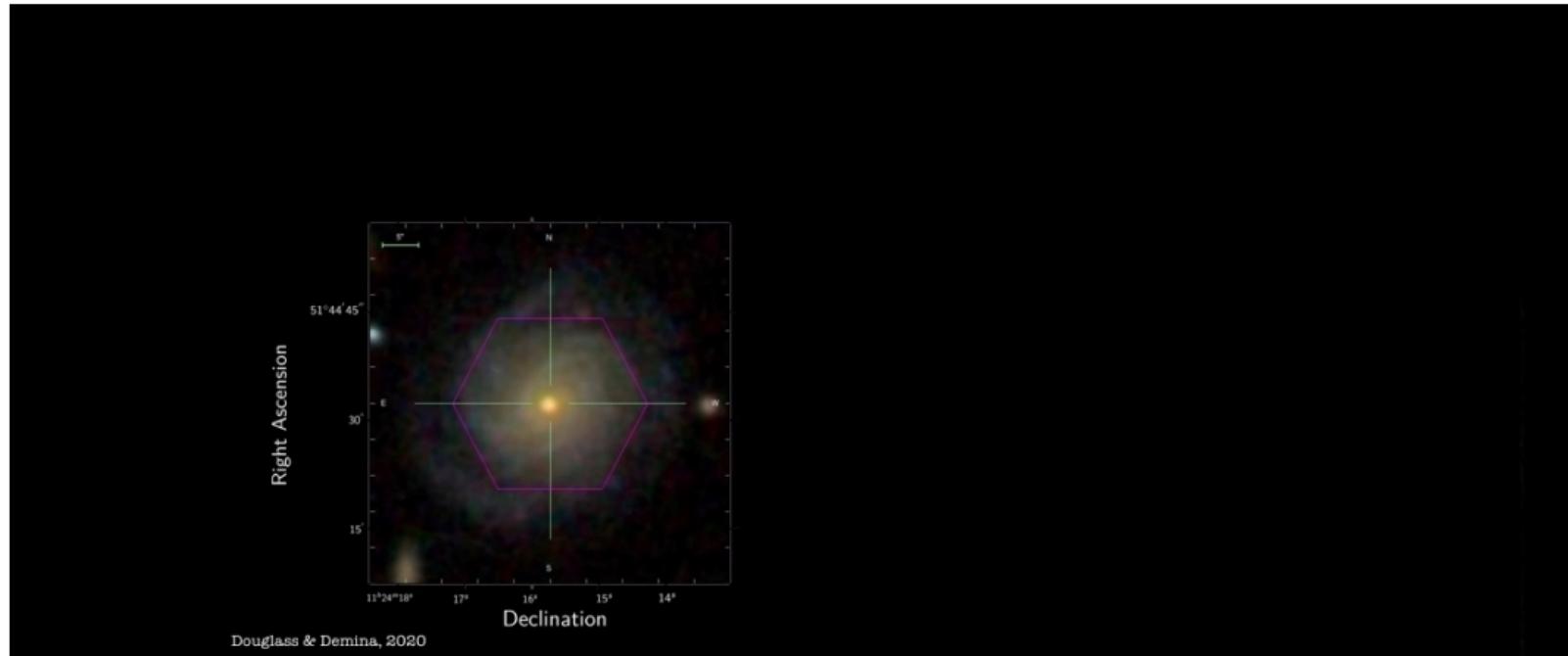
*Mapping Nearby Galaxies (MaNGA) at APO*



# Pairs of SDSS MaNGA galaxies

Dependence of the ratio of total to visible mass on observable properties of SDSS MaNGA galaxies

KELLY A. DOUGLASS<sup>1</sup> AND REGINA DEMINA<sup>1</sup>

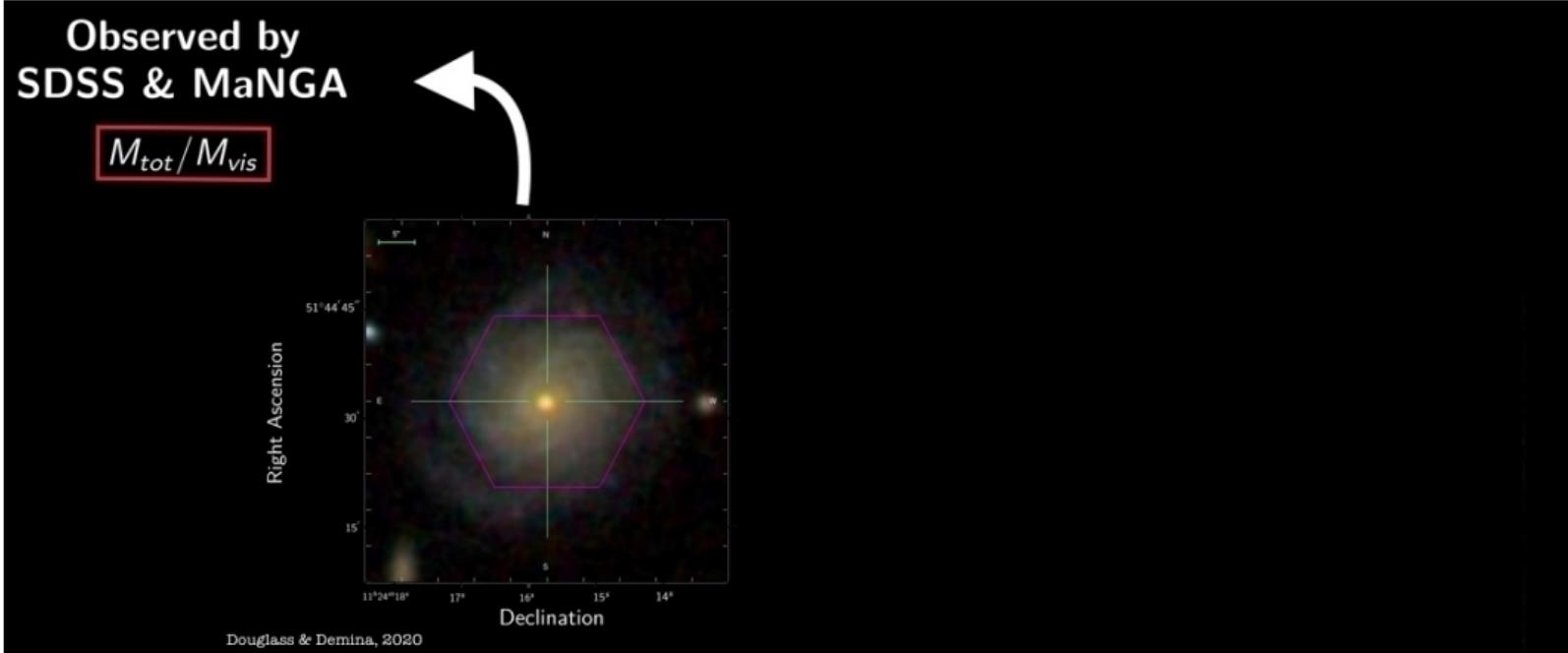


The relation between the ratio of masses and the nearest neighbor distance.

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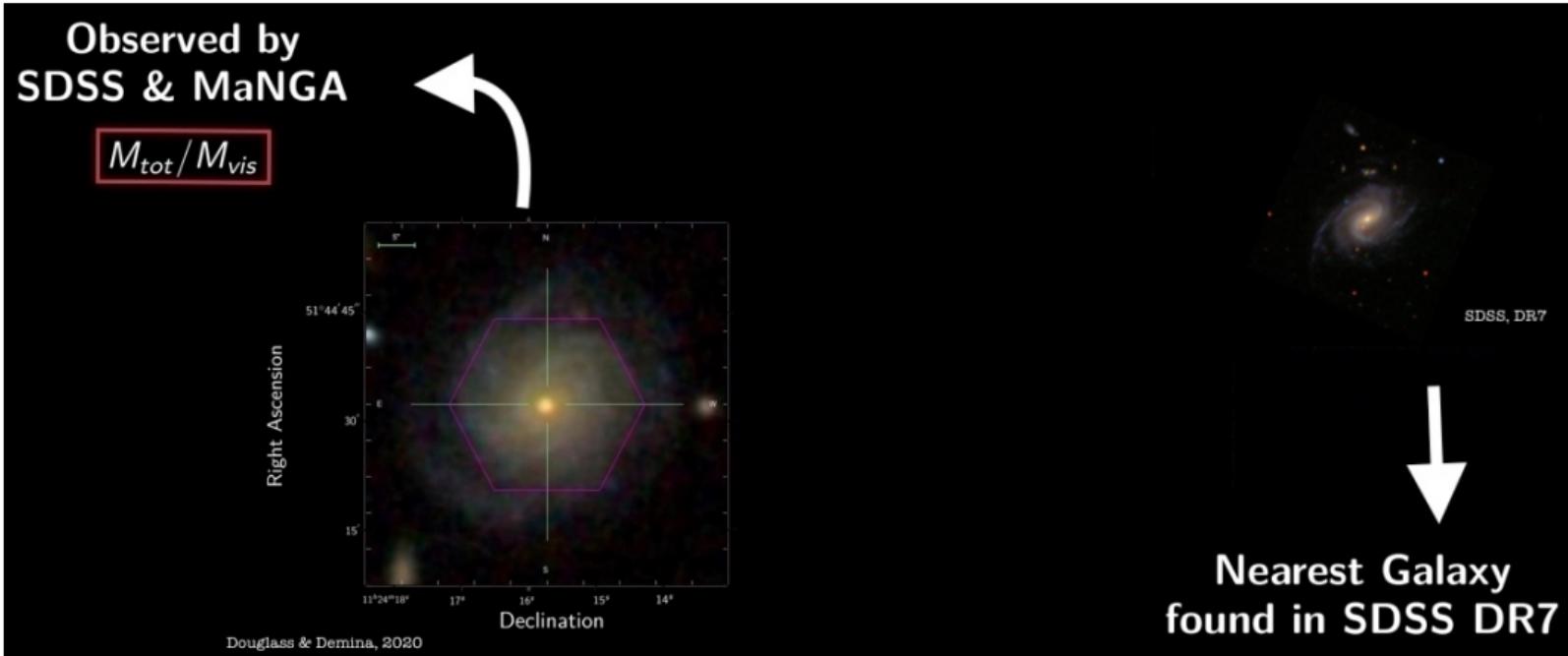


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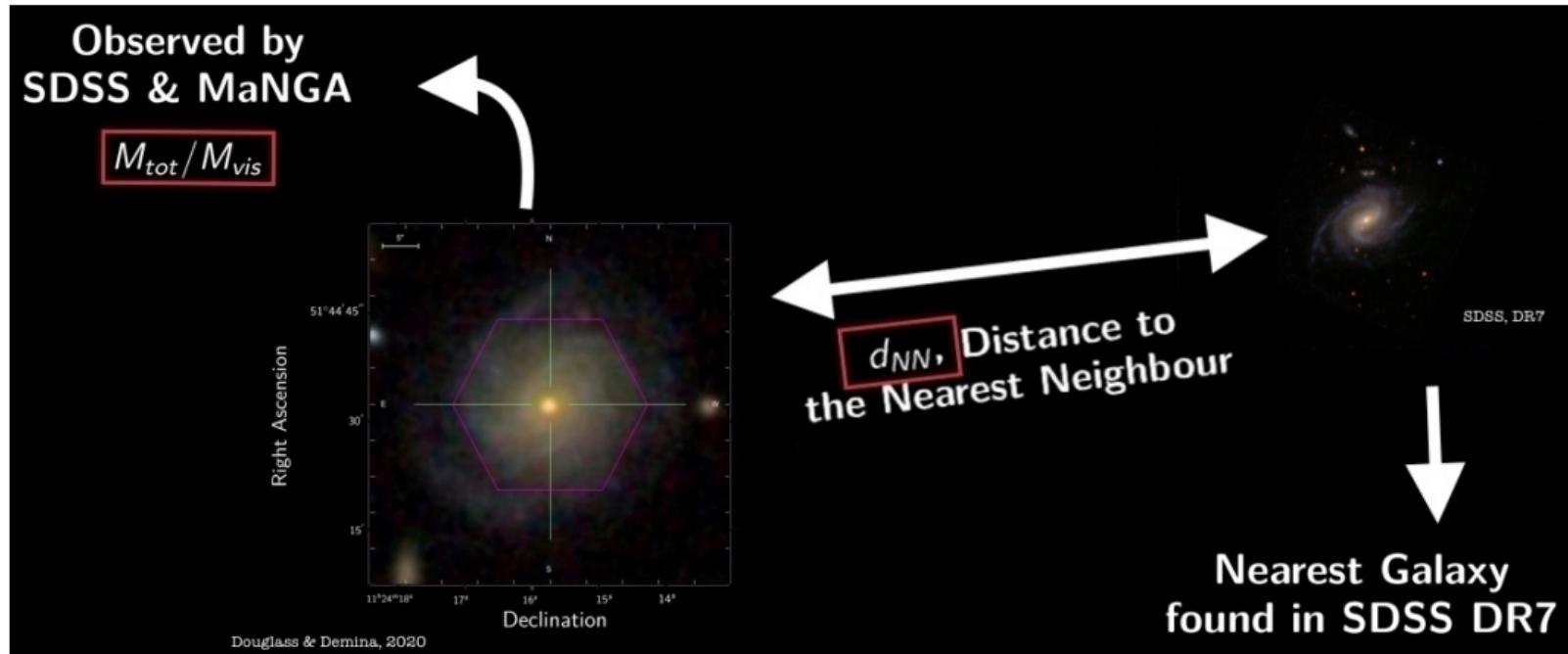


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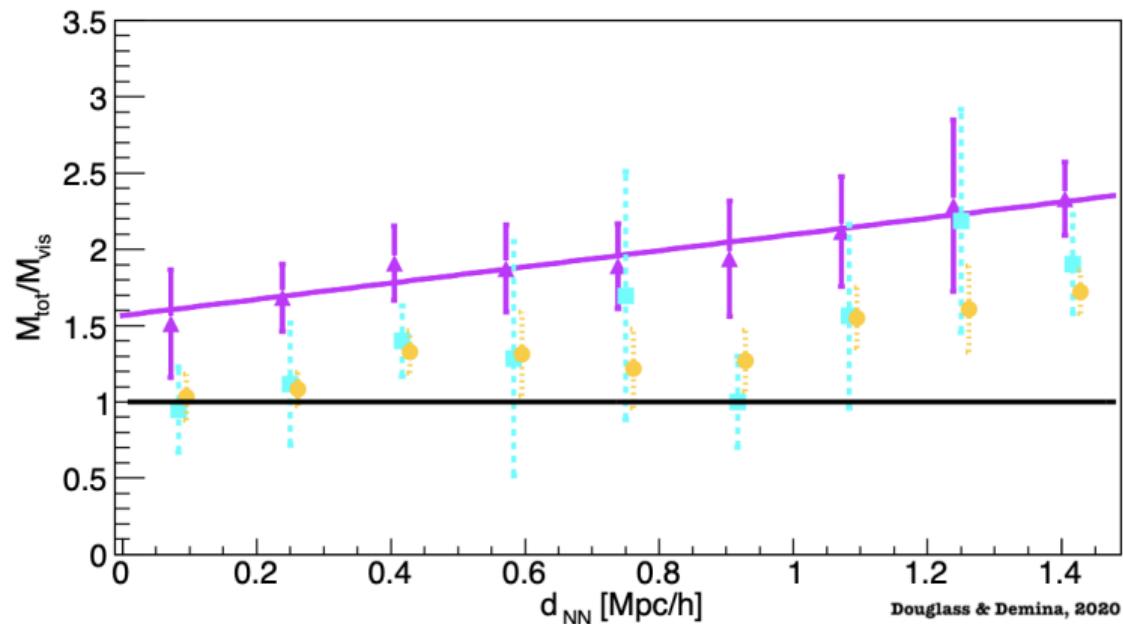


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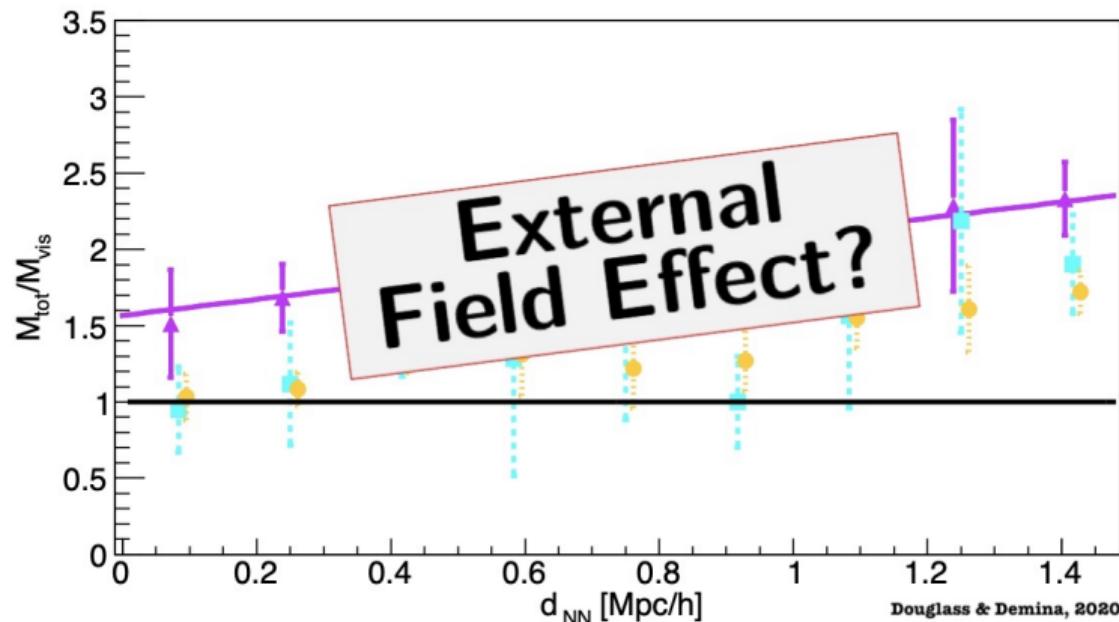


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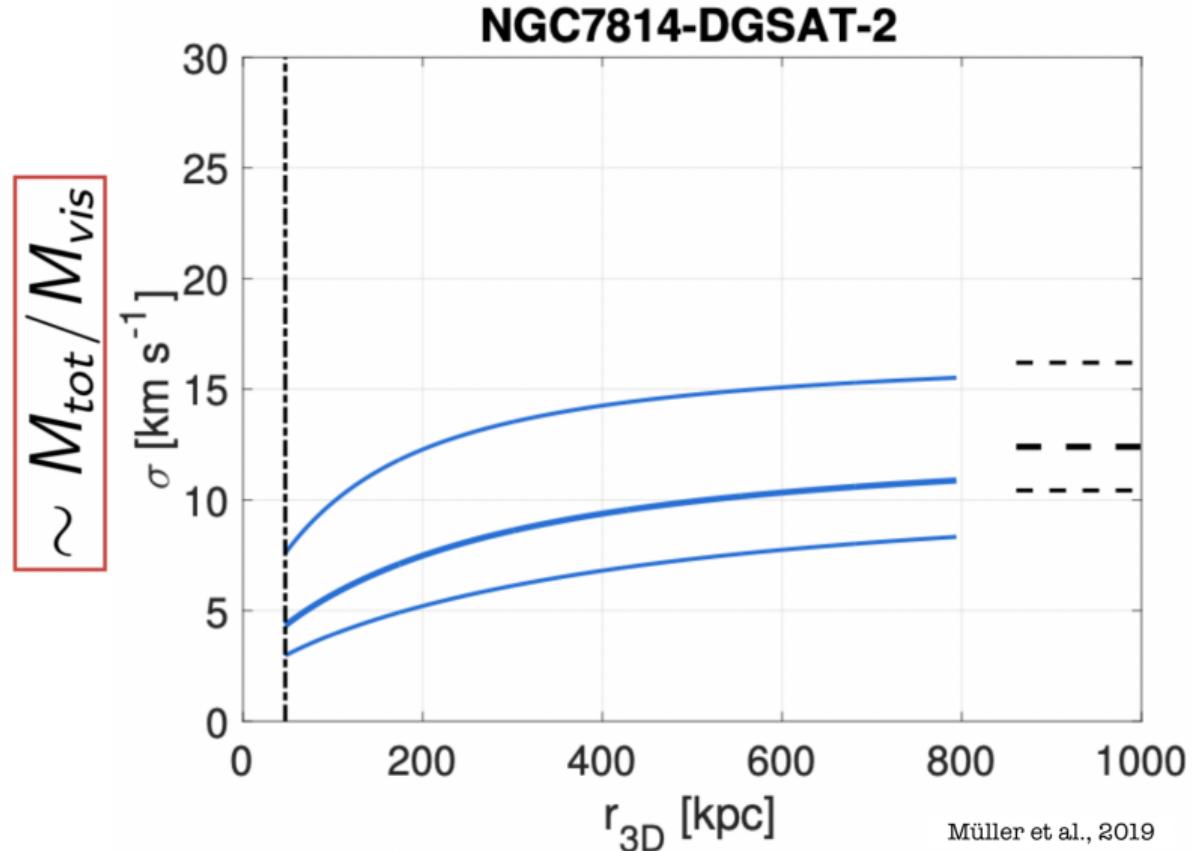
Dependence of the ratio of total to visible mass on observable properties of SDSS MaNGA galaxies

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The relation between the ratio of masses and the nearest neighbor distance.

## External Field Effect (EFE)



# Testing the External Field Effect

# Spiral Galaxies

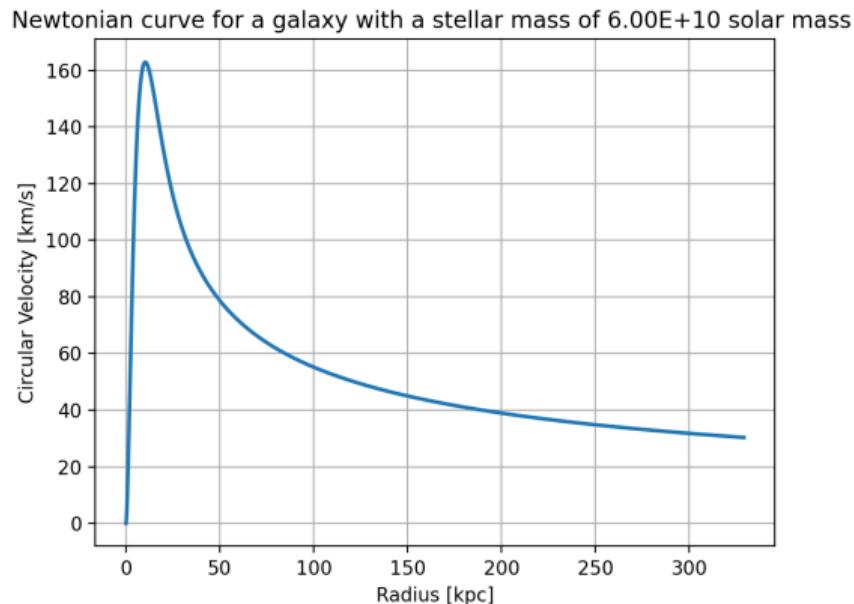
- ▶ Exponential & Infinitesimally Thin Disk

$$\Sigma(R) = \Sigma(0)e^{-R/R_d}$$

$$M(R) = M_b \left[ 1 - e^{-R/R_d} \left( 1 + \frac{R}{R_d} \right) \right]$$

$$V_c^2(R) = \frac{GM_d}{R_d} 2y^2 [I_0(y)K_0(y) - I_1(y)K_1(y)]$$

where  $y = 2R/R_d$



# Spiral Galaxies

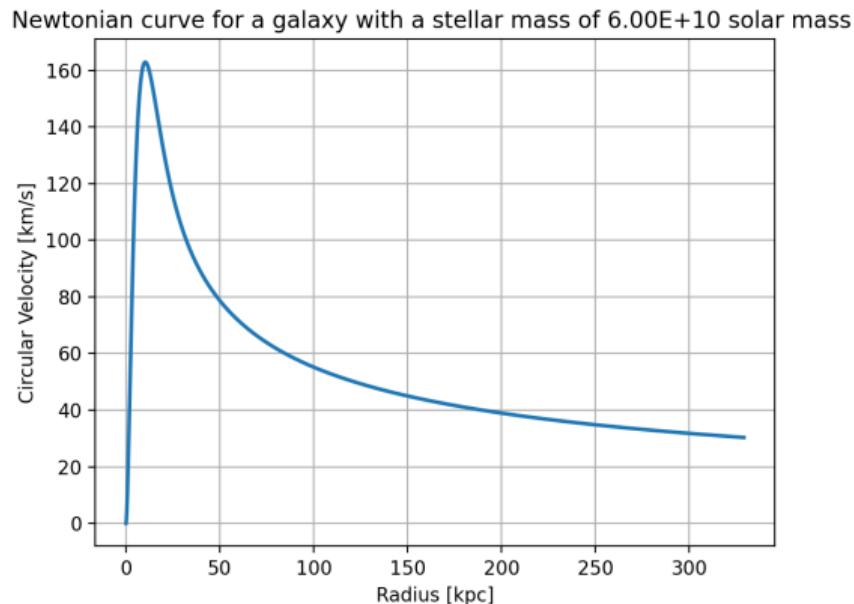
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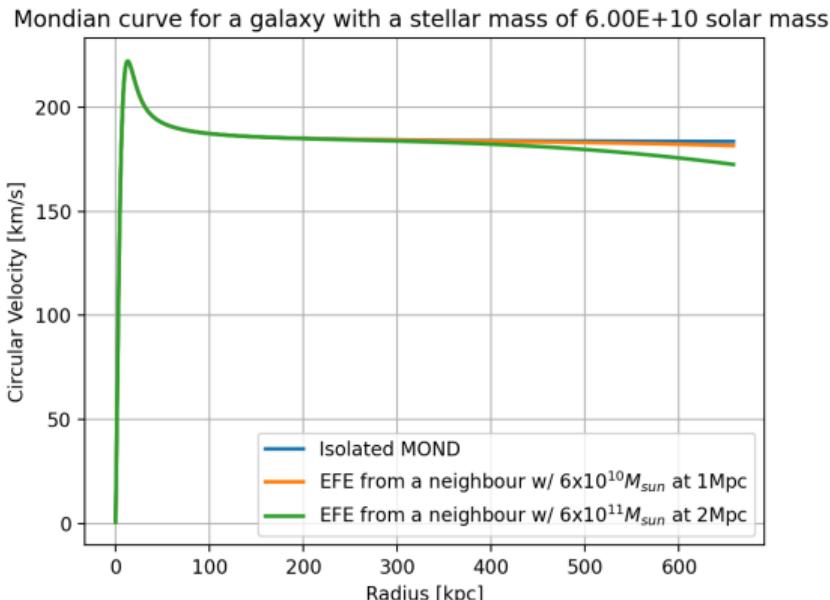
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# EFE Formulation



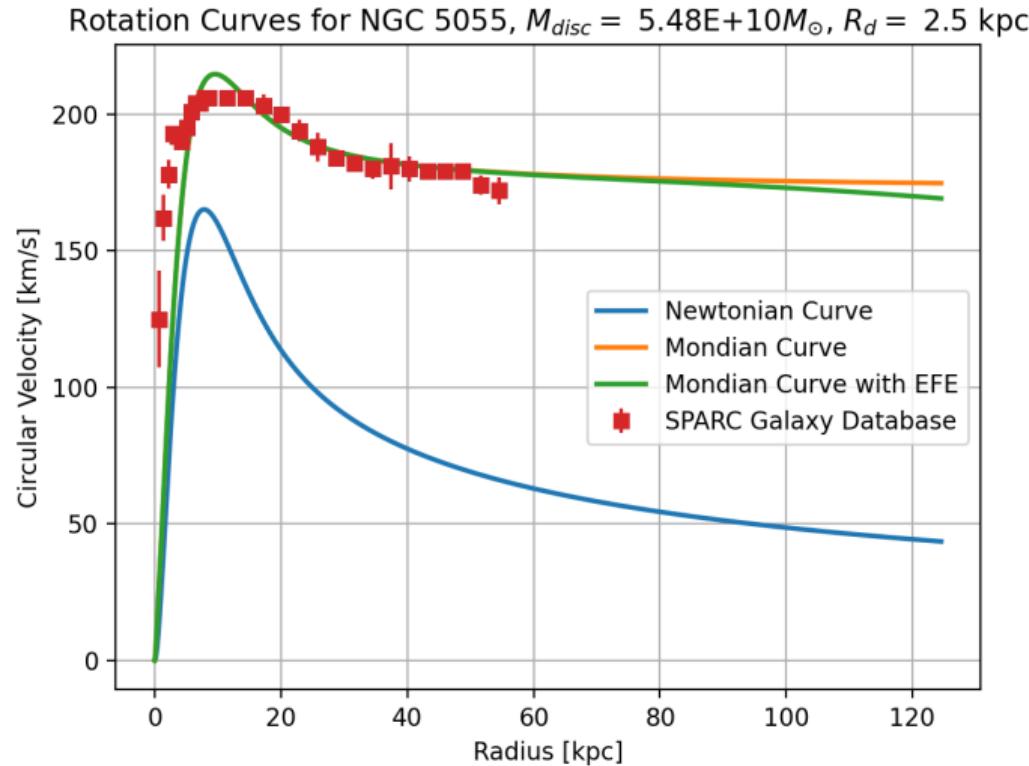
## ► EFE formulation

$$V_{\text{rot}}(r) = \sqrt{g_r(r)r}$$

$$g_r(r) = \begin{cases} \nu \left( \frac{g_{N_i} + \frac{g_{N_e}^2}{3g_{N_i}(r)}}{a_0} \right), & g_{N_i}(r) > g_{N_e} \\ \nu \left( \frac{g_{N_e} + \frac{g_{N_i}(r)^2}{3g_{N_e}}}{a_0} \right), & g_{N_i}(r) < g_{N_e} \end{cases}$$

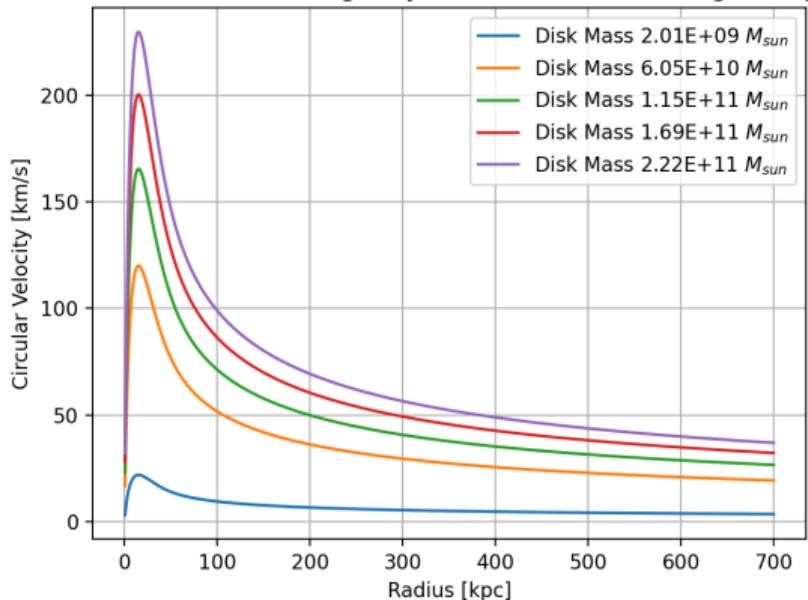
$$\nu(x) = \left( \frac{1}{4} + \frac{1}{x} \right)^{0.5} + \frac{1}{2}$$

# Newtonian & MONDian Rotation Curves of NGC 5055

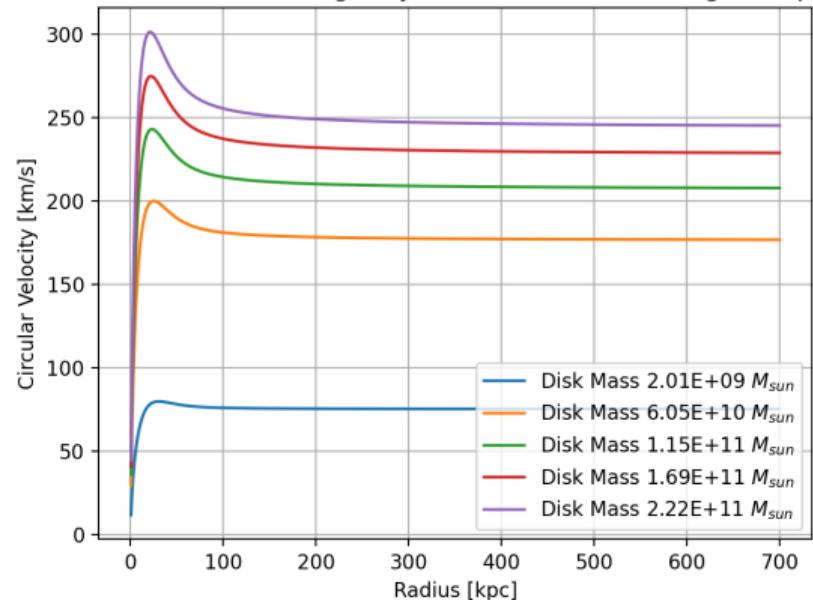


# Rotation Curves with Different Disk Mass

Newtonian curve for a galaxy with a Radius Scale Length: 7 kpc

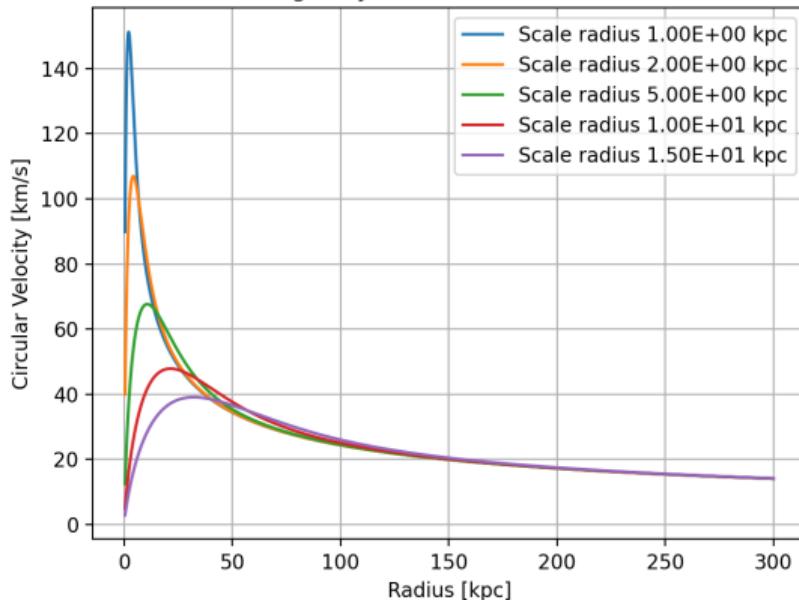


Mondrian curve for a galaxy with a Radius Scale Length: 7 kpc

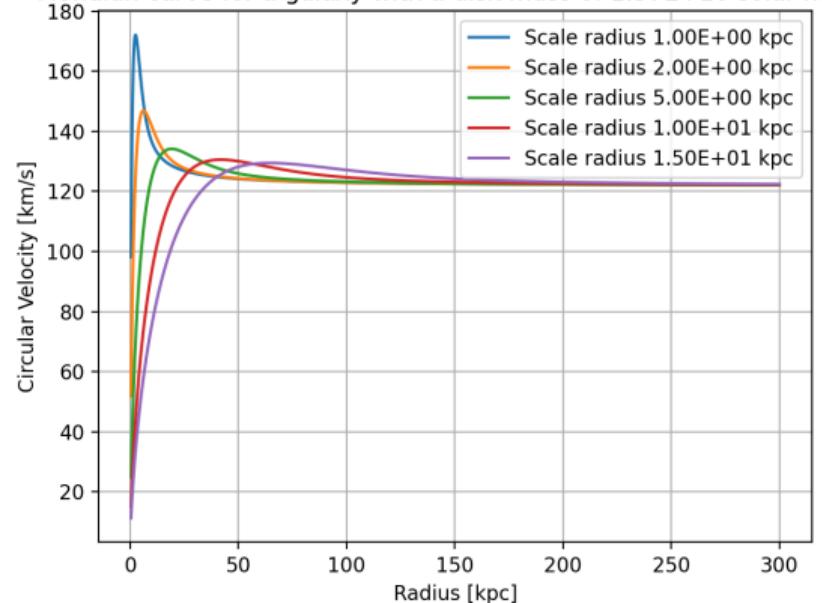


# Rotation Curves with Different Radius Scale Length

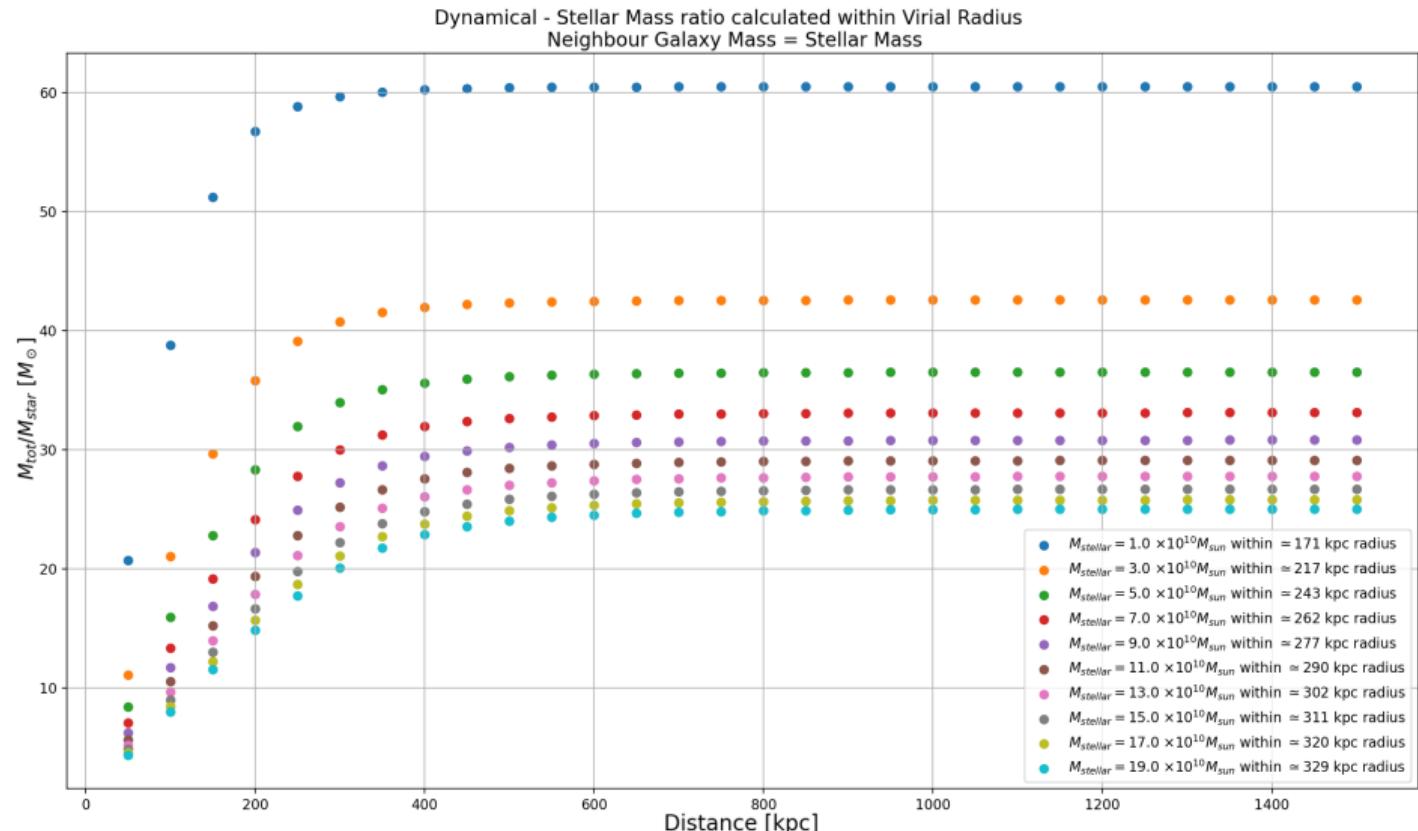
Newtonian curve for a galaxy with a disk mass of 1.37E+10 solar mass



Mondian curve for a galaxy with a disk mass of 1.37E+10 solar mass

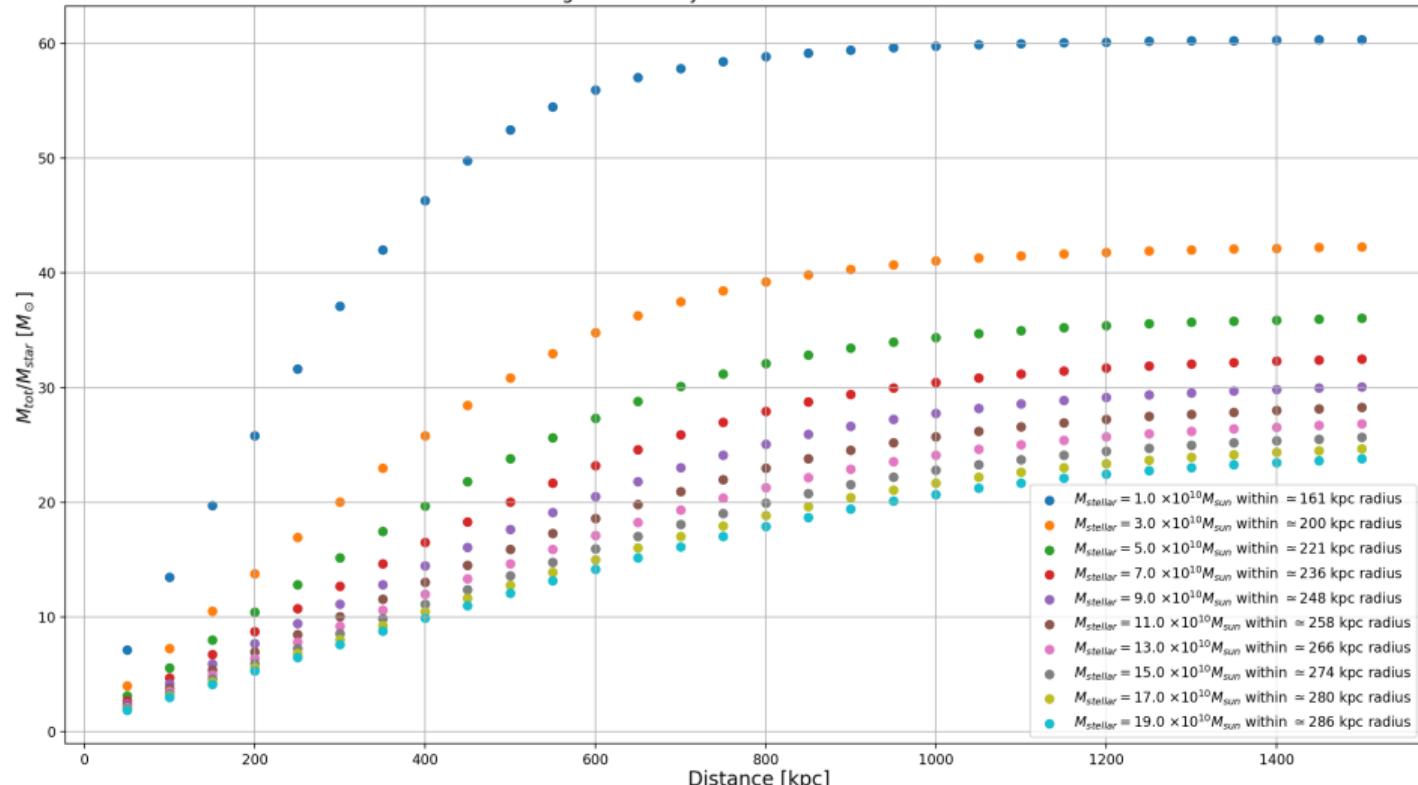


# External Field Effect on Dynamical Properties

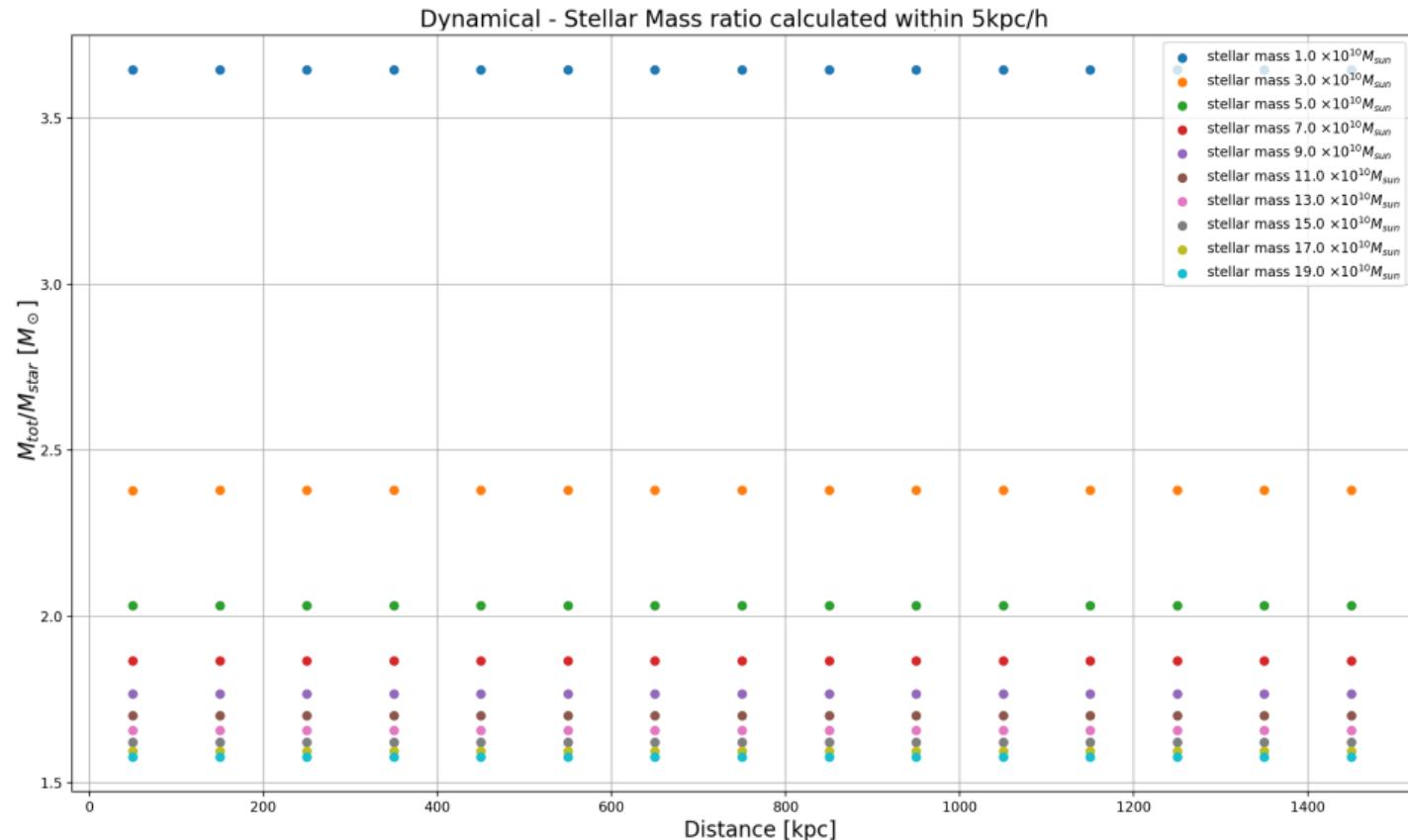


# External Field Effect on Dynamical Properties

Dynamical - Stellar Mass ratio calculated within Virial Radius  
Neighbour Galaxy Mass =  $10 \times$  Stellar Mass



# External Field Effect on Dynamical Properties



# Results

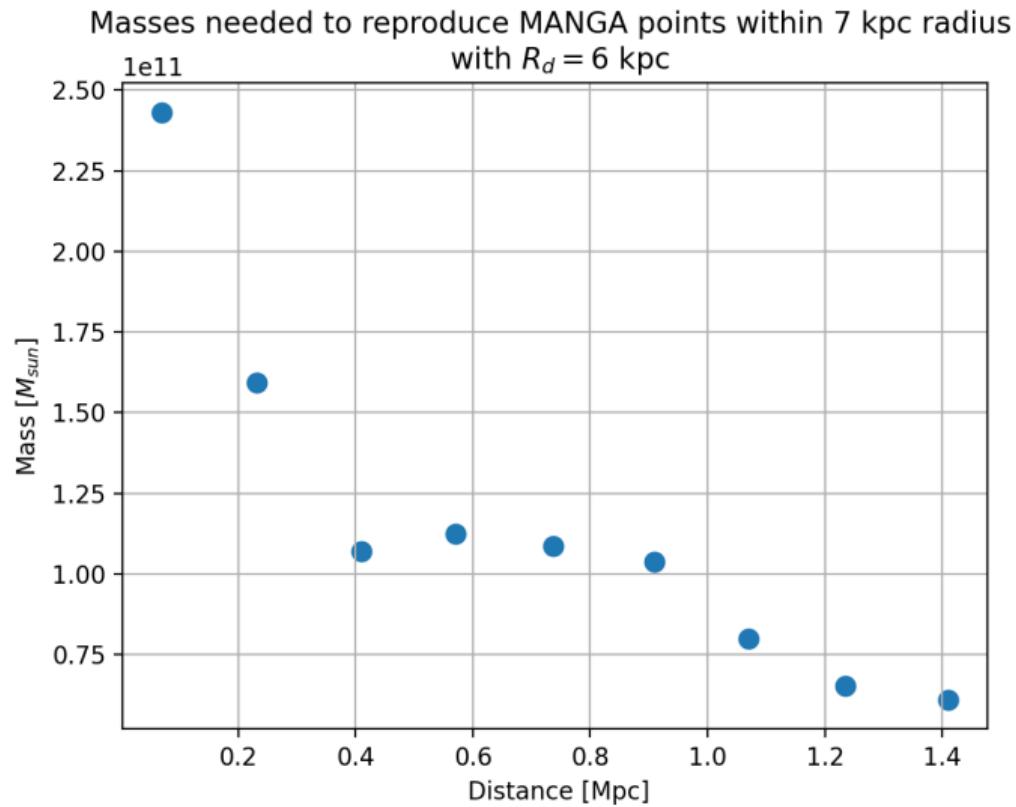
## **Result 1:**

External Field Effects dynamics at outskirts of galaxies.

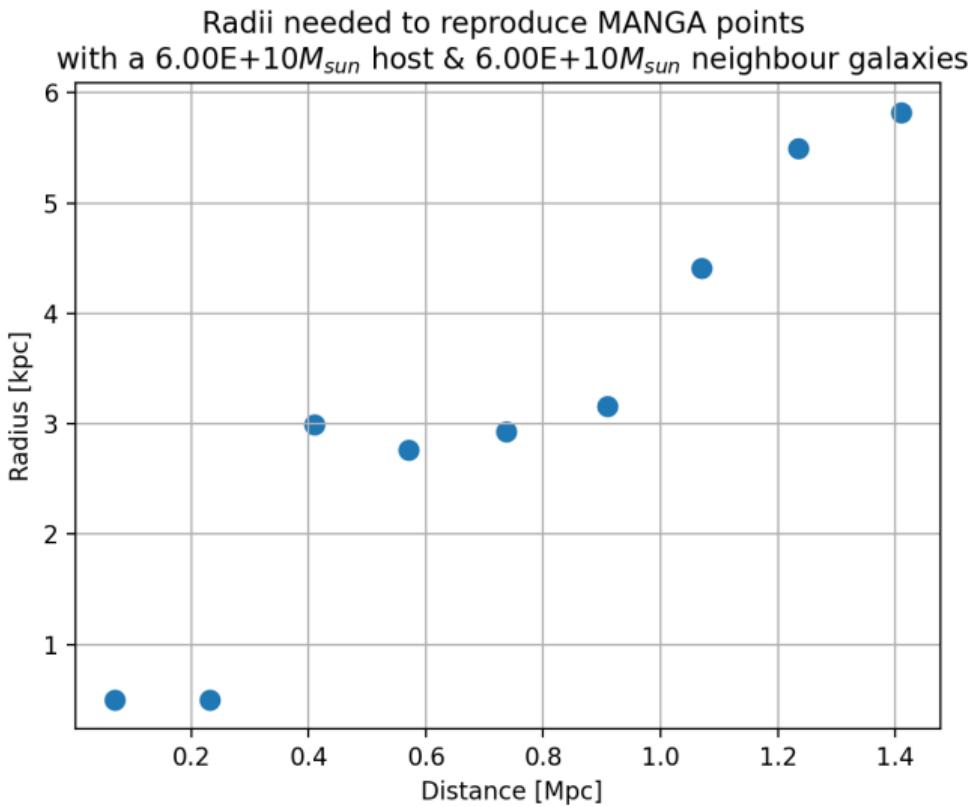
## **Result 2:**

External Field Effect has no influence on the radii considered!

# Conclusion



# Conclusion



# Results

## Result 1:

External Field Effects dynamics at outskirts of galaxies

## Result 2:

External Field Effect has no influence on the radii considered!

## Result 3:

Higher  $R_d \rightarrow$  Low Surface Density  $\rightarrow$  Higher  $M_{tot}/M_{vis}$

## References I

- [1] D. J. Chung, E. W. Kolb, and A. Riotto.  
Superheavy dark matter.  
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*arXiv preprint arXiv:2009.10083*, 2020.
- [3] T. du Pree.  
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- [5] J. L. Feng, S. Su, and F. Takayama.  
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*Physical review letters*, 96(15):151802, 2006.
- [6] A. Kusenko, V. Kuzmin, M. Shaposhnikov, and P. G. Tinyakov.  
Experimental signatures of supersymmetric dark-matter q-balls.  
*Physical Review Letters*, 80(15):3185, 1998.
- [7] F. Lelli, S. S. McGaugh, J. M. Schombert, and M. S. Pawlowski.  
One law to rule them all: the radial acceleration relation of galaxies.  
*The Astrophysical Journal*, 836(2):152, 2017.
- [8] O. Müller, B. Famaey, and H. Zhao.  
Predicted mond velocity dispersions for a catalog of ultra-diffuse galaxies in group environments.  
*Astronomy & Astrophysics*, 623:A36, 2019.

## References III

[9] M. Schumann.

Direct detection of wimp dark matter: concepts and status.

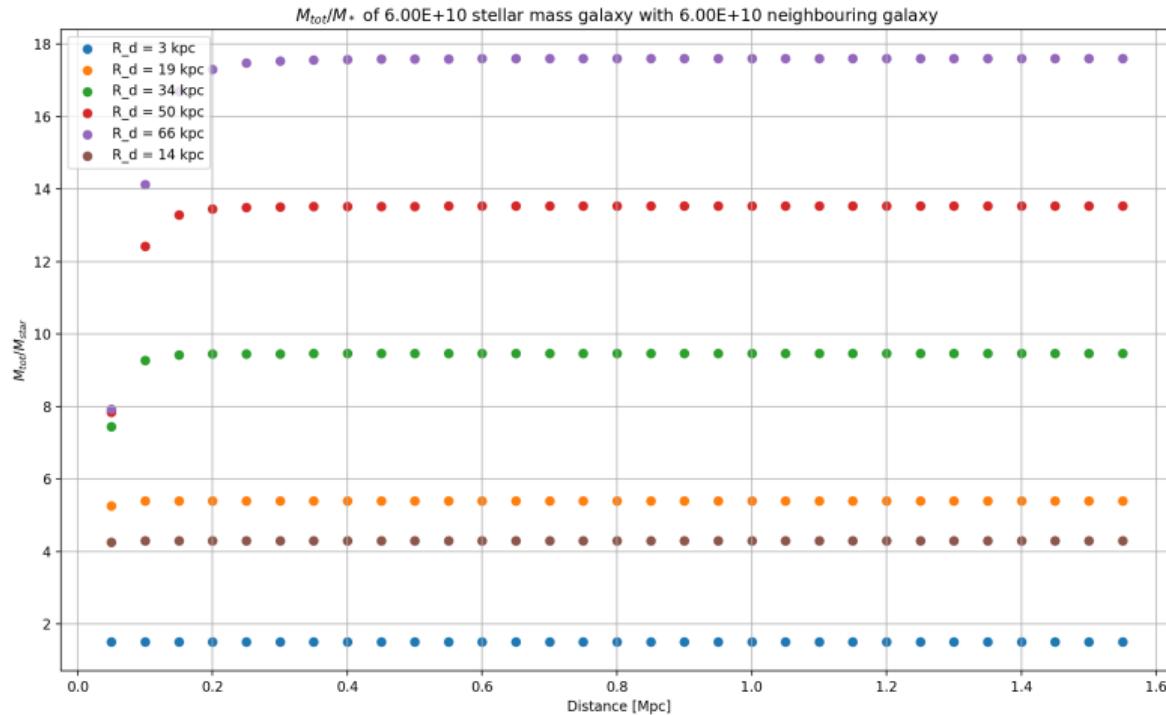
*Journal of Physics G: Nuclear and Particle Physics*, 46(10):103003, 2019.

# Where to look?

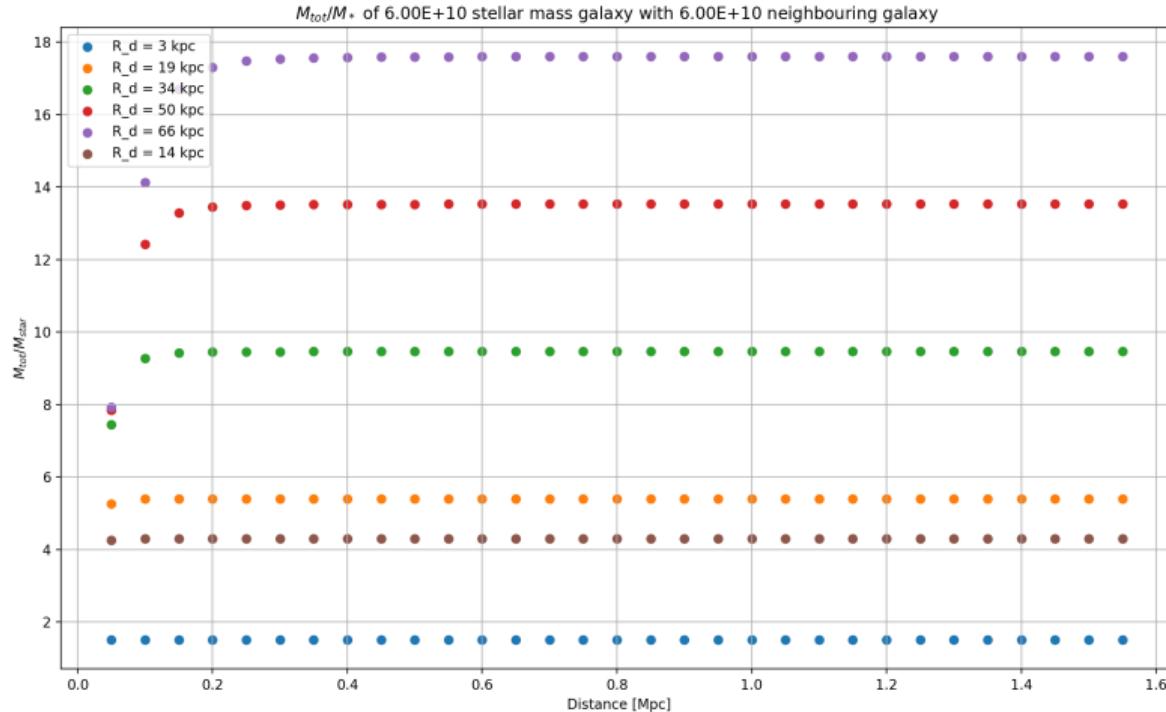
## Dwarf Spheroidals

- ▶ Dwarf Galaxies with Low Surface Brightness → Inner regions can be EFE dominant.

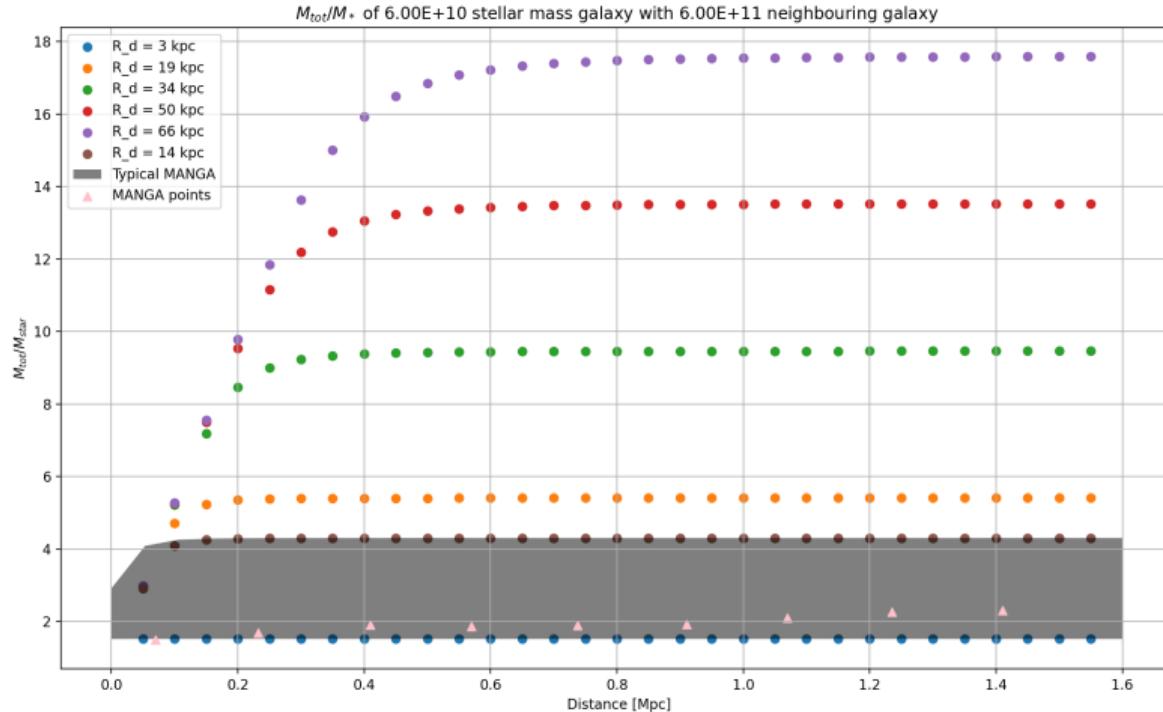
# Back-up - Milky Way Like Galaxy



# Back-up - Milky Way Like Galaxy



# Back-up - Milky Way Like Galaxy



## Back-up - Dark Matter Candidates

**Axions:** Hypothetical particle (Peccei–Quinn theory) introduced to solve *strong CP problem*.

**$\nu$ :** Heavy right-handed neutrinos

**WIMPs:** Weakly interacting massive particles

**SuperWIMPs:** Decay product of WIMPs (Feng, Su & Takayama, 2006)

**Q-Balls:** Arisen from supersymmetric extensions of the standard model, stable localised field, which carry baryon or lepton number. (Kusenko & Shaposhnikov, 1997)

**WIMPZillas:** nonthermal WIMPs, not in equilibrium when it froze out. (Kolb, Chung & Riotto, 1998)

**PBH:** Primordial black holes

# Back-up - Radial Acceleration Relation

## One Law to Rule Them All: The Radial Acceleration Relation of Galaxies

Federico Lelli<sup>1,2,5</sup>, Stacy S. McGaugh<sup>1</sup>, James M. Schombert<sup>3</sup>, and Marcel S. Pawlowski<sup>1,4,6</sup>

<sup>1</sup> Department of Astronomy, Case Western Reserve University, Cleveland, OH 44106, USA; [felli@eso.org](mailto:felli@eso.org)

<sup>2</sup> European Southern Observatory, Karl-Schwarzschild-Strasse 2, D-85748, Garching, Germany

<sup>3</sup> Department of Physics, University of Oregon, Eugene, OR 97403, USA

<sup>4</sup> Department of Physics and Astronomy, University of California, Irvine, CA 92697, USA

Received 2016 October 26; revised 2017 January 12; accepted 2017 January 12; published 2017 February 16

### Abstract

We study the link between baryons and dark matter (DM) in 240 galaxies with spatially resolved kinematic data. Our sample spans 9 dex in stellar mass and includes all morphological types. We consider (1) 153 late-type galaxies (LTGs; spirals and irregulars) with gas rotation curves from the SPARC database, (2) 25 early-type galaxies (ETGs; ellipticals and lenticulars) with stellar and HI data from ATLAS<sup>3D</sup> or X-ray data from *Chandra*, and (3) 62 dwarf spheroidals (dSphs) with individual-star spectroscopy. We find that LTGs, ETGs, and “classical” dSphs follow the same radial acceleration relation: the observed acceleration ( $g_{\text{obs}}$ ) correlates with that expected from the distribution of baryons ( $g_{\text{bar}}$ ) over 4 dex. The relation coincides with the 1:1 line (no DM) at high accelerations but systematically deviates from unity below a critical scale of  $\sim 10^{-10} \text{ m s}^{-2}$ . The observed scatter is remarkably small ( $\lesssim 0.13$  dex) and largely driven by observational uncertainties. The residuals do not correlate with any global or local galaxy property (e.g., baryonic mass, gas fraction, and radius). The radial acceleration relation is tantamount to a natural law: when the baryonic contribution is measured, the rotation curve follows, and vice versa. Including ultrafaint dSphs, the relation may extend by another 2 dex and possibly flatten at  $g_{\text{bar}} \lesssim 10^{-12} \text{ m s}^{-2}$ , but these data are significantly more uncertain. The radial acceleration relation subsumes and generalizes several well-known dynamical properties of galaxies, like the Tully–Fisher and Faber–Jackson relations, the “baryon-halo” conspiracies, and Renzo’s rule.

# Back-up - Radial Acceleration Relation

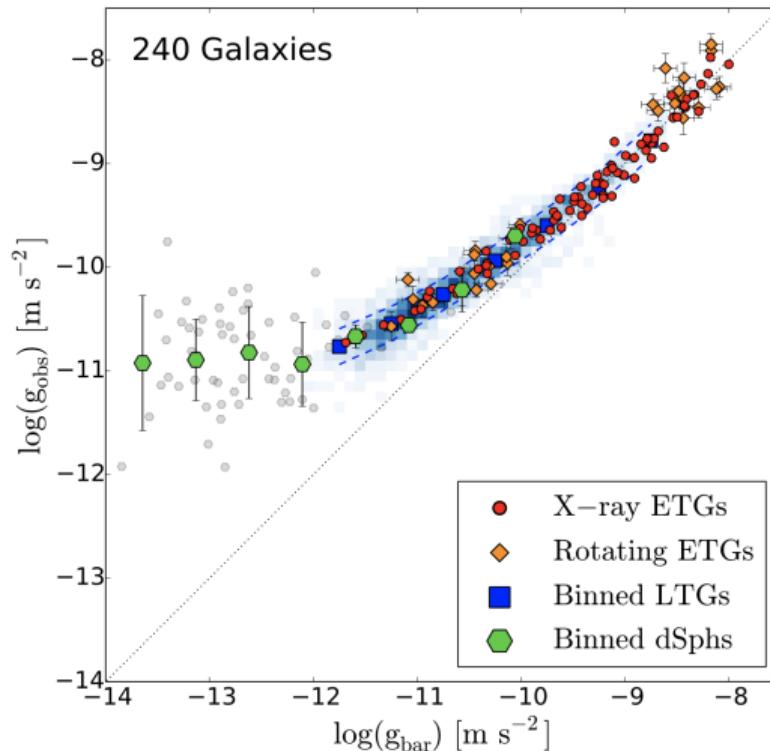
**Table 1**  
Fiducial Stellar Mass-to-light Ratios

Galaxy Component	$\Upsilon_*$
Disks of LTGs (Sa to Irr)	$0.5 M_\odot/L_\odot$
Bulges of LTGs (Sa to Sb)	$0.7 M_\odot/L_\odot$
Rotating ETGs (S0 and disk E)	$0.8 M_\odot/L_\odot$
X-ray ETGs (Giant metal-rich E)	$0.9 M_\odot/L_\odot$
Dwarf Spheroidals ( <i>V</i> -band)	$2.0 M_\odot/L_\odot$

**Note.** The values of  $\Upsilon_*$  refer to  $3.6 \mu\text{m}$  apart for dwarf spheroidals (*V*-band). We adopt a Chabrier (2003) IMF and the SPS models of Schombert & McGaugh (2014).

(Lelli et al., 2017)

## Back-up - Radial Acceleration Relation



(Lelli et al., 2017)

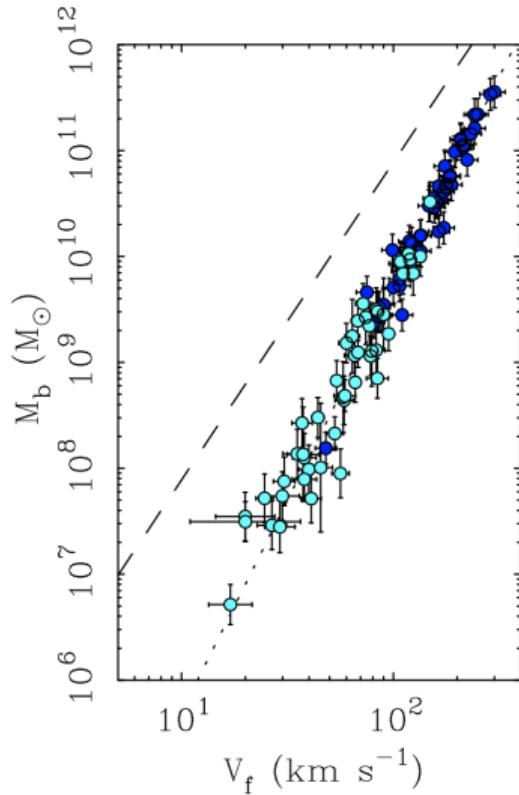
## Back-up - Some $\Lambda$ CDM Challenges

**Missing Satellite Problem:** "model predicts overabundance of dark subhalos"  
(Famaey & McGaugh, 2012)

**Local Void Challenge:** structure formation, faster than model predicts (Famaey & McGaugh, 2012)

**Cusp-Core Problem:** Do DM halos have a density profile which is constant at the small radii or steeply increasing?

## Back-up - Baryonic Tully-Fisher



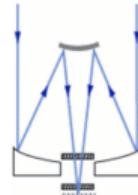
“The dotted line has slope 4 corresponding to a constant acceleration parameter,  $1.2 \times 10^{10} \text{ m s}^2$ . The dashed line has slope 3 as expected in  $\Lambda$ CDM with the normalization expected if all of the baryons associated with dark matter halos are detected.” (Famaey & McGaugh, 2012)

# Back-up - SDSS

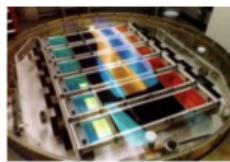
## Key Components of the Survey Telescope

### Channeling the light

The telescope's optical system is dominated by two reflecting mirrors. The focusing system includes two corrective lenses that minimize distortion. The diagram at right shows how that incoming starlight strikes the 2.5-meter primary mirror, bounces back and strikes the smaller secondary mirror, then is reflected back through a hole in the primary mirror. The light passes through the first correcting lens and then through the second lens on top of the camera. Images from the system appear in good focus from an area of sky equal to about 30 full moons.



### Making the two-dimensional image



The inner sanctum of the SDSS telescope contains what may be the most complex camera ever built. It includes 30 silicon electronic light sensors called charge-coupled devices, or **CCDs** (seen at left), that are each two inches square. Scientists encase each column of five devices in a vacuum-sealed chamber. In order to enhance sensitivity, liquid nitrogen cools each chamber to -80 degrees Celsius. Each CCD is made up of more than four million picture elements, which release electrons as light is absorbed. The electrons in turn are amplified into electronic signals that can be digitized, recorded on tape and ultimately fed into a computer. A night's observing will produce up to 200 gigabytes of data on a dozen tapes. Each of the five rows of CCDs receives the light through a different colored filter, so each row records the brightness of objects in a different color.

### Into the third dimension

A **spectrograph**, a device that disperses light into many colors so the spectrum can be recorded, analyzes the distance, composition and age of each celestial object. Astronomers drill 640 holes in an aluminum plate, with each hole corresponding to the position of a selected galaxy, quasar or star in the sky. Scientists plug the holes with optical fiber cables (right). The fibers simultaneously capture light from the 640 objects and record the results in CCDs. The plug plates are interchangeable with the CCD camera at the focal plane of the telescope. On a good night, observers will use six to nine plates.



<http://classic.sdss.org/background/telescope.html>

## Back-up - Interpolating Function

Written like this, the analogy between Milgrom's law and Coulomb's law in a dielectric medium is clear, as noted in [56]. Indeed, inside a dielectric medium, the amplitude of the electric field  $E$  generated by an external point charge  $Q$  located at a distance  $r$  obeys the following equation:

$$\mu(E)E = \frac{Q}{4\pi\epsilon_0 r^2}, \quad (9)$$

where  $\mu$  is the relative permittivity of the medium, and can depend on  $E$ . In the case of a gravitational field generated by a point mass  $M$ , it is then clear that Milgrom's interpolating function plays the role of "gravitational permittivity". Since it is smaller than 1, it makes the

(Famaey & McGaugh, 2012)

## Back-up - Acceleration

