

Exercises

I. Polynomials

1. Evaluate the polynomial $p(x) = 2x^3 - 5x^2 + 8$ in $x = 2$. (hint: use `polyval`)
2. Find the roots of the polynomial $p(x) = x^3 - 5x^2 - 17x + 21$. (hint: use `roots`)

II. Graphs

1. Plot the functions $f: [0,1] \rightarrow \mathbb{R}, f(x) = e^{10x(x-1)} \sin 12\pi x$ and $f: [0,1] \rightarrow \mathbb{R}, f(x) = 3e^{5x^2-1} \cos 12\pi x$.
2. Plot the epicycloid
$$\begin{cases} x(t) = (a+b) \cos(t) - b \cos\left(\left(\frac{a}{b}+1\right)t\right) \\ y(t) = (a+b) \sin(t) - b \sin\left(\left(\frac{a}{b}+1\right)t\right) \end{cases} t \in [0, 10\pi],$$
 for a given a, b.
3. Plot, on a single graph, the function $f_1, f_2, f_3: [0, 2\pi] \rightarrow \mathbb{R}, f_1(x) = \cos x; f_2(x) = \sin x; f_3(x) = \cos 2x$.
4. Plot the graph of the function $f(x) = \begin{cases} x^3 + \sqrt{1-x}; & -1 \leq x \leq 0 \\ x^3 - \sqrt{1-x}; & 0 < x \leq 1 \end{cases}$.
5. For $x \in \{0, 1, \dots, 50\}$ plot the function $f(x) = \begin{cases} x/2 & \text{if } x = \text{even} \\ 3x + 1 & \text{if } x = \text{odd} \end{cases}$.
6. Compute $g = 1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1+1}}}}$
(Consider the general case, for a given number of fractions)
7. Plot the function $g: [-2, 2] \times [-4, 4] \rightarrow \mathbb{R}, g(x, y) = e^{-((x-\frac{1}{2})^2 + (y-\frac{1}{2})^2)}$.
(use : `meshgrid`, `mesh`).