



Welcome To My Presentation

My Presentation Topic is
Design an NFA with $\Sigma = \{0, 1\}$ in
which double '1' is followed by
double '0'



Presented By

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Outline

- ❑ Symbol, Alphabet
- ❑ Strings, Languages
- ❑ What is NFA?
- ❑ Formal Definition of NFA
- ❑ How to use an NFA?
- ❑ Problem Solve
- ❑ Application of NFA

Symbol, Alphabet

➤ Symbol :

Symbol is the basic building block of Theory of computation.

Example :

a, b, c, d,, z

0, 1, 2, 3, 4, 5, ..., 9

letter, digits, etc.

➤ Alphabet

An alphabet is a finite, non-empty set of symbols which denote by Σ (sigma).

Examples :

Binary: $\Sigma = \{0,1\}$

All lower case letters: $\Sigma = \{a,b,c,..z\}$.

Alphanumeric: $\Sigma = \{a-z, A-Z, 0-9\}$

Strings, Languages

□ Strings :

- A string or word is a finite sequence of symbols chosen from Σ
- Length of a string w , denoted by “ $|w|$ ”, is equal to the number of (non- ϵ) characters in the string.

Example: $w=0001,1010,101010$.

□ Languages :

Languages is the collections of strings which can be finite and infinite.

- *L is said to be a language over alphabet Σ , only if $L \subseteq \Sigma^*$*
- this is because Σ^* is the set of all strings (of all possible length including 0) over the given alphabet Σ

Examples:

Let L be *the* language of all strings consisting of n 0's followed by n 1's:

$$L = \{\epsilon, 01, 0011, 000111, \dots\}$$

Let L be *the* language of all strings of with equal number of 0's and 1's:

$$L = \{\epsilon, 01, 10, 0011, 1100, 0101, 1010, 1001, \dots\}$$

What is NFA?

- NFA stands for non-deterministic finite automata. It is easy to construct an NFA than DFA for a given regular language.
- The finite automata are called NFA when there exist many paths for specific input from the current state to the next state.
- Every NFA is not DFA, but each NFA can be translated into DFA.
- NFA is defined in the same way as DFA but with the following two exceptions, it contains multiple next states, and it contains ϵ transition.

Formal Definition of NFA

- A NFA is defined by the 5-tuple:

$$\{Q, \Sigma, q_0, F, \delta\}$$

- Here,

- Q : finite set of states
- Σ : finite set of the input symbol
- q_0 : initial state
- F : final state
- δ : a transition function, which is a mapping between $Q \times \Sigma \Rightarrow$ subset of Q

How to use an NFA?

- Input: a word w in Σ^*
- Question: Is w acceptable by the NFA?
- Steps:
 - Start at the “start state” q_0
 - For every input symbol in the sequence w do
 - Determine all possible next states from all current states, given the current input symbol in w and the transition function
 - If after all symbols in w are consumed, the current state is one of the accepting states (F) then *accept* w ;
 - Otherwise, *reject* w .

Problem Solve

❑ Question :

Design an NFA with $\Sigma = \{0,1\}$ in which double '1' is followed by double '0'.

❑ Solve

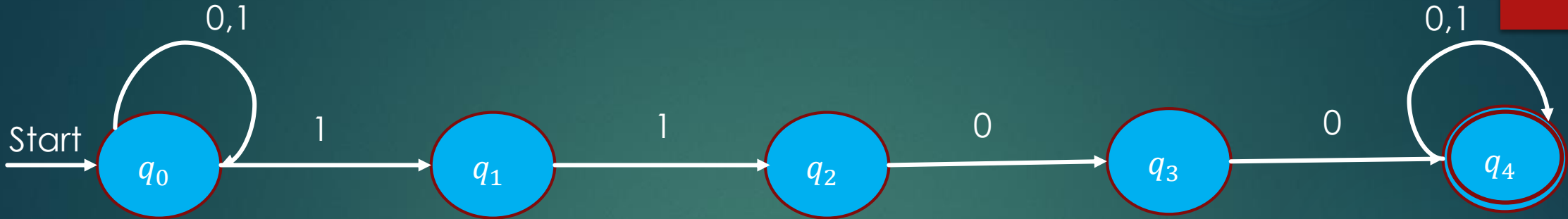
Here,

$L(M) = \{w \mid w \text{ which double '1' is followed by double '0'}\}$

$L = \{1100, 0001100, 11001100, \dots\}$.

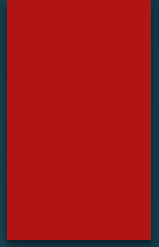
- A finite set of states, $Q = \{q_0, q_1, q_2, q_3, q_4\}$
- A finite set of input symbols, $\Sigma = \{0,1\}$
- Start state = q_0
- Set of accepting states, $F = \{q_4\}$
- δ is the transition function where $\delta: Q \times \Sigma \rightarrow 2^Q$

Problem Solve



δ Transition Table		
States	$Q \times \Sigma \rightarrow 2^Q$ 0	$Q \times \Sigma \rightarrow 2^Q$ 1
q_0	q_0	q_0, q_1
q_1	\emptyset	q_2
q_2	q_3	\emptyset
q_3	q_4	\emptyset
$*q_4$	q_4	q_4

Application of NFA



- ▶ It is important because NFAs can be used to reduce the complexity of the mathematical work required to establish many important properties in the theory of computation.
- For example, it is much easier to prove closure properties of regular languages using NFAs than DFAs.



Thank you!