



# Welcome To My Presentation

# My Presentation Topic is

## Design an NFA in which all the string contain a substring 1100



### Presented By

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# Outline

- ❑ Symbol, Alphabet
- ❑ Strings, Languages
- ❑ What is NFA?
- ❑ Formal Definition of NFA
- ❑ How to use an NFA?
- ❑ Problem Solve
- ❑ Application of NFA

# Symbol, Alphabet

## ➤ Symbol :

Symbol is the basic building block of Theory of computation.

Example :

a, b, c, d, ....., z

0, 1, 2, 3, 4, 5, ..., 9

letter, digits, etc.

## ➤ Alphabet

An alphabet is a finite, non-empty set of symbols which denote by  $\Sigma$  (sigma).

Examples :

Binary:  $\Sigma = \{0,1\}$

All lower case letters:  $\Sigma = \{a,b,c,..z\}$ .

Alphanumeric:  $\Sigma = \{a-z, A-Z, 0-9\}$

# Strings, Languages

## □ Strings :

- A string or word is a finite sequence of symbols chosen from  $\Sigma$
- Length of a string  $w$ , denoted by “ $|w|$ ”, is equal to the number of (non-  $\epsilon$ ) characters in the string.

Example:  $w=0001,1010,101010$ .

## □ Languages :

Languages is the collections of strings which can be finite and infinite.

- *$L$  is said to be a language over alphabet  $\Sigma$ , only if  $L \subseteq \Sigma^*$*
- this is because  $\Sigma^*$  is the set of all strings (of all possible length including 0) over the given alphabet  $\Sigma$

Examples:

Let  $L$  be *the* language of all strings consisting of  $n$  0's followed by  $n$  1's:

$$L = \{\epsilon, 01, 0011, 000111, \dots\}$$

Let  $L$  be *the* language of all strings of with equal number of 0's and 1's:

$$L = \{\epsilon, 01, 10, 0011, 1100, 0101, 1010, 1001, \dots\}$$

# What is NFA?

- NFA stands for non-deterministic finite automata. It is easy to construct an NFA than DFA for a given regular language.
- The finite automata are called NFA when there exist many paths for specific input from the current state to the next state.
- Every NFA is not DFA, but each NFA can be translated into DFA.
- NFA is defined in the same way as DFA but with the following two exceptions, it contains multiple next states, and it contains  $\epsilon$  transition.

# Formal Definition of NFA

- A NFA is defined by the 5-tuple:

$$\{Q, \Sigma, q_0, F, \delta\}$$

- Here,

- $Q$  : finite set of states
- $\Sigma$  : finite set of the input symbol
- $q_0$ : initial state
- $F$  : final state
- $\delta$  : a transition function, which is a mapping between  $Q \times \Sigma \Rightarrow$  subset of  $Q$



# How to use an NFA?

- Input: a word  $w$  in  $\Sigma^*$
- Question: Is  $w$  acceptable by the NFA?
- Steps:
  - Start at the “start state”  $q_0$
  - For every input symbol in the sequence  $w$  do
    - Determine all possible next states from all current states, given the current input symbol in  $w$  and the transition function
  - If after all symbols in  $w$  are consumed, the current state is one of the accepting states ( $F$ ) then *accept*  $w$ ;
  - Otherwise, *reject*  $w$ .



# Problem Solve

## ❑ Question :

Design an NFA in which all the string contain a substring 1100.

## ❑ Solve

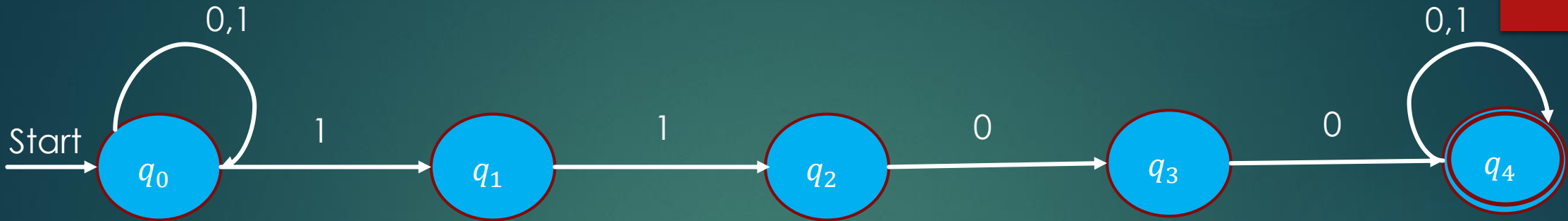
Here,

$L(M) = \{ w \mid w \text{ which double '1' is followed by double '0' } \}$

$L = \{ 1100, 0001100, 11001100, \dots \}$ .

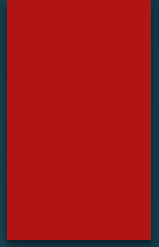
- A finite set of states,  $Q = \{ q_0, q_1, q_2, q_3, q_4 \}$
- A finite set of input symbols,  $\Sigma = \{ 0, 1 \}$
- Start state =  $q_0$
- Set of accepting states,  $F = \{ q_4 \}$
- $\delta$  is the transition function where  $\delta: Q \times \Sigma \rightarrow 2^Q$

# Problem Solve



$\delta$ Transition Table		
States	$Q \times \Sigma \rightarrow 2^Q$ 0	$Q \times \Sigma \rightarrow 2^Q$ 1
$q_0$	$q_0$	$q_0, q_1$
$q_1$	$\emptyset$	$q_2$
$q_2$	$q_3$	$\emptyset$
$q_3$	$q_4$	$\emptyset$
$*q_4$	$q_4$	$q_4$

# Application of NFA



- ▶ It is important because NFAs can be used to reduce the complexity of the mathematical work required to establish many important properties in the theory of computation.
- For example, it is much easier to prove closure properties of regular languages using NFAs than DFAs.



# Thank you!