

10 - 8 bit binary representation

0 0 0 0 1 0 1 0

-10 = 1 0 0 0 1 0 1 0

Sign bit

-3 = 1 0 0 0 0 0 1 1

-4 = 1 0 0 0 0 1 0 0

~~1 0 0 0 0 1 1 1~~

⇒ +7

0 0 0 0 0 0 0 0 = 0

1 0 0 0 0 0 0 0 = -0

↓

-3 = 1 0 0 0 0 0 1 1

10 : 0 0 0 0 1 0 1 0

= -13

$$\rightarrow -a = 2's a = 1's a + 1 = \sim a + 1$$

$$\begin{array}{c} \xrightarrow{\quad} 0 \rightarrow 1 \\ -a = \sim a + 1 \\ \hline \end{array}$$

$$10: \quad \underline{0} \quad \underline{0} \quad \underline{0} \quad \underline{0} \quad \underline{1} \quad \underline{0} \quad \underline{1} \quad \underline{0}$$

$$\begin{array}{r} \sim 10: \quad 1 \quad 1 \quad 1 \quad 1 \quad 0 \quad 1 \quad 0 \quad 1 \\ + 1: \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad 1 \\ \hline \end{array}$$

$$\begin{array}{c} \boxed{-2} \quad 2^7 \quad 2^6 \quad 2^5 \quad 2^4 \quad 2^3 \quad 2^2 \quad 2^1 \quad 2^0 \\ -10: \quad 1 \quad 1 \quad 1 \quad 1 \quad 0 \quad 1 \quad 1 \quad 0 \\ \swarrow \text{MSB} \end{array}$$

$$128 + 64 + 32 + 16 + 4 + 2 = 246$$

$$-128 + 64 + 32 + 16 + 4 + 2 = -10$$

$$\begin{array}{c} \boxed{-2} \quad 2^7 \quad 2^6 \quad 2^5 \quad 2^4 \quad 2^3 \quad 2^2 \quad 2^1 \quad 2^0 \\ 23: \quad 0 \quad 0 \quad 0 \quad 1 \quad 0 \quad 1 \quad 1 \quad 1 \\ \hline \end{array}$$

$$\begin{array}{r} \sim 23: \quad 1 \quad 1 \quad 1 \quad 0 \quad 1 \quad 0 \quad 0 \quad 0 \\ + 1: \quad \quad \quad \quad \quad \quad \quad \quad 1 \\ \hline 1 \quad 1 \quad 1 \quad 0 \quad 1 \quad 0 \quad 0 \quad 1 \\ \hline \end{array}$$

$$-128 + 64 + 32 + 8 + 1$$

$$= -128 + 105 = -23$$

$\underline{1} \quad \underline{0} \quad \underline{0} \quad \underline{0}$ $\xrightarrow{+10} * \quad \underline{M_{an}} = \underline{+7}, \quad \underline{M_{bn}} = \underline{-8}$
 $\underline{-2^3} \quad \underline{2^2} \quad \underline{2^1} \quad \underline{2^0} \quad \rightarrow \quad [-8, +7]$

# n bits	M_{bn}	M_{an}
1		
2	$\underline{1} \quad \underline{0} \Rightarrow -2^1$	$\underline{0} \quad \underline{1} \Rightarrow 2^0$
3	$\underline{1} \quad \underline{0} \quad \underline{0} \Rightarrow -2^2$	$\underline{0} \quad \underline{1} \quad \underline{1} \Rightarrow 2^0 + 2^1 \Rightarrow 2^2 - 1$
4	$\underline{1} \quad \underline{0} \quad \underline{0} \quad \underline{0} \Rightarrow -2^3$	$\underline{0} \quad \underline{1} \quad \underline{1} \quad \underline{1} \Rightarrow 2^0 + 2^1 + 2^2 \Rightarrow 2^3 - 1$
5	$\underline{1} \quad \underline{0} \quad \underline{0} \quad \underline{0} \quad \underline{0} \Rightarrow -2^4$	$\underline{0} \quad \underline{1} \quad \underline{1} \quad \underline{1} \quad \underline{1} \Rightarrow 2^0 + 2^1 + 2^2 + 2^3 \Rightarrow 2^4 - 1$
n bits number	$\rightarrow -2^{N-1}$	$\rightarrow 2^{N-1} - 1$

// n bit number $\Rightarrow [-2^{N-1}, 2^{N-1} - 1]$

// byte $\Rightarrow n=8$	$[-2^7, 2^7-1] \Rightarrow [-128, 127]$
short int $\Rightarrow n=16$	$[-2^{15}, 2^{15}-1] \Rightarrow [-32768, 32767]$
int $\Rightarrow n=32$	$[-2^{31}, 2^{31}-1] \Rightarrow [-2147483648, 2147483647]$ $\hookrightarrow [-2 \times 10^9, 2 \times 10^9]$
long int $\Rightarrow n=64$	$[-2^{63}, 2^{63}-1] \Rightarrow [-8 \times 10^{18}, 8 \times 10^{18}]$

$$\Rightarrow 2^{10} = 1024 \approx 1000 \approx 10^3$$

$$(2^{10})^3 \approx (10^3)^3$$

// Cube on both sides

$$2^{30} \approx 10^9 \Rightarrow \text{Multiply } 2 \Rightarrow 2^{31} \approx 2 \times 10^9$$

// Square on both sides

$$2^{60} \approx 10^{18} \Rightarrow \text{Multiply } 2^3 \Rightarrow 2^{63} \approx 8 \times 10^{18}$$

⇒ // Given N calculate 2^N

$N=3$

$N=10$

2^8
 $2^{10}, 1024$

$N \in [0, 62]$

power2(N) {
 N=30 $\Rightarrow 2^{30}$ ✓
 N=31 $\Rightarrow 2^{31}$ * overflow

return 1 < N
 N=60 $\Rightarrow 2^{60}$ ✓

1 < N $\Rightarrow N=61 \Rightarrow 2^{61}$ ✓

N=62 $\Rightarrow 2^{62}$ ✓

type of 1 becomes long $\Rightarrow N=63 \Rightarrow 2^{63}$ *

Python: strings

Java: BigInteger

C++: 2^{63}

1 = 0 0 0 0 0 0 0 1

1 < 1 = 0 0 0 0 0 0 1 0 = 2

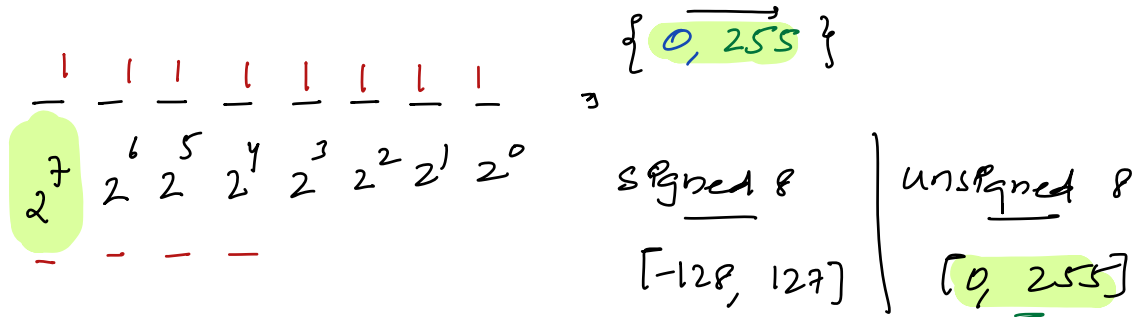
1 < 2 = 0 0 0 0 0 1 0 0 = 2^2

1 < 3 = 2^3

1 < N = 2^N

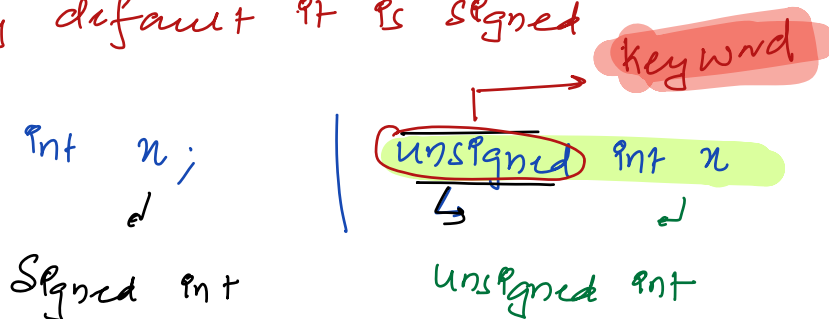
C/C++ \Rightarrow { unsigned / signed }

unsigned 8 bit Number



// unsigned MSB is +ve

By default it is signed



\Rightarrow $a - b$

$a + (-b)$

Can we get binary of $-b$?

Can we get binary of a ?

- MSB → Bit wise Operators
 - Ranges → Basic problems: check Bit (N, i)
 - Overflow → 27th Contest: 2 hrs } 4 Problems
- 2-3 days: 2 hrs

Strings	Recursion - 1	LinkedList	Subset's Subsequence
Hashing 1	Recursion - 2	Trees - 1	Problem Solving - I
Hashing 2	Stacks	Trees - 2	Problem Solving - II

- 1) Arrays -
- 2) Bits -
- 3)

① 10 days holidays

{
 ⇒ per day 10/15 to review a session Notes
 ⇒ Clear all your backlogs
 ⇒ Please watch your doubts
}

② Hackerrank : Solve topic by topic

A