## AI1110 ASSIGNMENT 8

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# Outline

Question

Solution

## Question

#### Papoulis Chapter 7, Question 7.20

We place at random n points in the interval (0,1) and we donate by x and y the distance from the origin to the first and last point respectively. Find F(x), F(y), F(x,y).

## Solution

The event  $x \le x$  occurs if there is at least one point in the interval (0,x);

The event  $y \leq y$  occurs if all the points are in the interval(0, y).

Let 
$$A_X$$
 = at least one point in (0,  $x$ ) =  $x \le x$ 

Let  $B_Y = \text{no points in } (y, 1)$ 

= all points in 
$$(0,y) = y \le y$$

Hence for  $0 \le x \le 1$ ,  $0 \le y \le 1$ , we have:

$$F_X(x) = \Pr(A_X) = 1 - \Pr(\bar{A_X}) = 1 - (1 - x)^n$$
 (2.0.1)

$$F_Y(y) = \Pr(B_Y) = y^n$$
 (2.0.2)

Further more, we have

$$\left\{ \underset{\sim}{x} \le x, \underset{\sim}{y} \le y \right\} = A_x \cdot B_y \tag{2.0.3}$$

$$A_X B_Y + \bar{A_X} B_Y = B_Y \tag{2.0.4}$$

Case 1:  $x \le y$  then,

$$\bar{A}_X B_Y = \{ all \ points \ in \ (x, y) \}$$
 (2.0.5)

$$\implies \Pr\left(\bar{A_X}B_Y\right) = (y - x)^n \tag{2.0.6}$$

Case 2: x > y then,

$$\bar{A_X}B_Y = \{\phi\} \tag{2.0.7}$$

Therefore, we have 
$$F_{XY}(x,y) = \Pr(A_X B_Y) = \begin{cases} y^n - (y-x)^n & x \leq y \\ y^n & x > y \end{cases}$$



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