

**INFO 6205**  
**Program Structures & Algorithms**  
**Fall 2020**  
**Assignment No5**

At first, I write the code in the ParSort.java, and run the Main. And I get this:

```
Degree of parallelism: 7
cutoff: 510000      10times Time:1687ms
cutoff: 520000      10times Time:815ms
cutoff: 530000      10times Time:751ms
cutoff: 540000      10times Time:748ms
cutoff: 550000      10times Time:746ms
cutoff: 560000      10times Time:758ms
cutoff: 570000      10times Time:768ms
cutoff: 580000      10times Time:752ms
cutoff: 590000      10times Time:750ms
cutoff: 600000      10times Time:801ms
cutoff: 610000      10times Time:785ms
cutoff: 620000      10times Time:767ms
cutoff: 630000      10times Time:767ms
cutoff: 640000      10times Time:788ms
cutoff: 650000      10times Time:775ms
cutoff: 660000      10times Time:785ms
cutoff: 670000      10times Time:782ms
cutoff: 680000      10times Time:796ms
cutoff: 690000      10times Time:801ms
cutoff: 700000      10times Time:780ms
cutoff: 710000      10times Time:821ms
cutoff: 720000      10times Time:796ms
cutoff: 730000      10times Time:745ms
cutoff: 740000      10times Time:726ms
cutoff: 750000      10times Time:718ms
cutoff: 760000      10times Time:721ms
cutoff: 770000      10times Time:723ms
cutoff: 780000      10times Time:717ms
cutoff: 790000      10times Time:724ms
cutoff: 800000      10times Time:734ms
cutoff: 810000      10times Time:724ms
cutoff: 820000      10times Time:717ms
cutoff: 830000      10times Time:719ms
cutoff: 840000      10times Time:718ms
cutoff: 850000      10times Time:721ms
cutoff: 860000      10times Time:719ms
cutoff: 870000      10times Time:717ms
cutoff: 880000      10times Time:739ms
cutoff: 890000      10times Time:742ms
cutoff: 900000      10times Time:747ms
cutoff: 910000      10times Time:1034ms
cutoff: 920000      10times Time:790ms
cutoff: 930000      10times Time:765ms
cutoff: 940000      10times Time:809ms
cutoff: 950000      10times Time:774ms
cutoff: 960000      10times Time:769ms
cutoff: 970000      10times Time:780ms
cutoff: 980000      10times Time:781ms
cutoff: 990000      10times Time:768ms
cutoff: 1000000     10times Time:772ms
```

It seems that the code runs well and the it performs better when the cutoff is around 750,000.

Therefore, I change the code in the Main.java:

```
int[] array = new int[4000000];
System.out.println("Array size: " + array.length);
ArrayList<Long> timeList = new ArrayList<>();
for (int j = 4; j < 45; j++) {
    ParSort.cutoff = 50000 * j;
```

And I change the number of available threads(the number equals to 2, 4, 8, 16 and 32), and I run the code in each condition several times, and these are some of all the outputs:

```
"C:\Program Files\Java\jdk-14.0.1\bin\java.exe
Degree of parallelism: 2
Array size: 4000000
cutoff: 200000      10times Time:2965ms
cutoff: 250000      10times Time:2512ms
cutoff: 300000      10times Time:2323ms
cutoff: 350000      10times Time:2345ms
cutoff: 400000      10times Time:2387ms
cutoff: 450000      10times Time:2389ms
cutoff: 500000      10times Time:2292ms
cutoff: 550000      10times Time:2133ms
cutoff: 600000      10times Time:2358ms
cutoff: 650000      10times Time:2339ms
cutoff: 700000      10times Time:2263ms
cutoff: 750000      10times Time:2128ms
cutoff: 800000      10times Time:2689ms
cutoff: 850000      10times Time:2261ms
cutoff: 900000      10times Time:2282ms
cutoff: 950000      10times Time:2278ms
cutoff: 1000000     10times Time:2295ms
cutoff: 1050000     10times Time:2188ms
cutoff: 1100000     10times Time:2148ms
cutoff: 1150000     10times Time:2160ms
cutoff: 1200000     10times Time:2116ms
cutoff: 1250000     10times Time:2124ms
cutoff: 1300000     10times Time:2108ms
cutoff: 1350000     10times Time:2083ms
cutoff: 1400000     10times Time:2103ms
cutoff: 1450000     10times Time:2076ms
cutoff: 1500000     10times Time:2399ms
cutoff: 1550000     10times Time:2225ms
cutoff: 1600000     10times Time:2206ms
cutoff: 1650000     10times Time:2189ms
cutoff: 1700000     10times Time:2194ms
cutoff: 1750000     10times Time:2219ms
cutoff: 1800000     10times Time:2215ms
cutoff: 1850000     10times Time:2103ms
cutoff: 1900000     10times Time:2099ms
cutoff: 1950000     10times Time:2118ms
cutoff: 2000000     10times Time:2105ms
cutoff: 2050000     10times Time:2027ms
cutoff: 2100000     10times Time:2061ms
cutoff: 2150000     10times Time:2100ms
cutoff: 2200000     10times Time:2109ms

"C:\Program Files\Java\jdk-14.0.1\bin\java.exe
Degree of parallelism: 4
Array size: 4000000
cutoff: 200000      10times Time:3156ms
cutoff: 250000      10times Time:2036ms
cutoff: 300000      10times Time:1981ms
cutoff: 350000      10times Time:1929ms
cutoff: 400000      10times Time:1884ms
cutoff: 450000      10times Time:1762ms
cutoff: 500000      10times Time:1731ms
cutoff: 550000      10times Time:1670ms
cutoff: 600000      10times Time:1673ms
cutoff: 650000      10times Time:2104ms
cutoff: 700000      10times Time:1808ms
cutoff: 750000      10times Time:1748ms
cutoff: 800000      10times Time:1767ms
cutoff: 850000      10times Time:1689ms
cutoff: 900000      10times Time:1640ms
cutoff: 950000      10times Time:1637ms
cutoff: 1000000     10times Time:1667ms
cutoff: 1050000     10times Time:1865ms
cutoff: 1100000     10times Time:1678ms
cutoff: 1150000     10times Time:1692ms
cutoff: 1200000     10times Time:1698ms
cutoff: 1250000     10times Time:1705ms
cutoff: 1300000     10times Time:1701ms
cutoff: 1350000     10times Time:1696ms
cutoff: 1400000     10times Time:1623ms
cutoff: 1450000     10times Time:1602ms
cutoff: 1500000     10times Time:1621ms
cutoff: 1550000     10times Time:1618ms
cutoff: 1600000     10times Time:1628ms
cutoff: 1650000     10times Time:1610ms
cutoff: 1700000     10times Time:1874ms
cutoff: 1750000     10times Time:1702ms
cutoff: 1800000     10times Time:1693ms
cutoff: 1850000     10times Time:1682ms
cutoff: 1900000     10times Time:1687ms
cutoff: 1950000     10times Time:1676ms
cutoff: 2000000     10times Time:1691ms
cutoff: 2050000     10times Time:2158ms
cutoff: 2100000     10times Time:2152ms
cutoff: 2150000     10times Time:2149ms
cutoff: 2200000     10times Time:2134ms
```



```
"C:\Program Files\Java\jdk-14.0.1\bin\java.exe" "C:\Program Files\Java\jdk-14.0.1\bin\java.exe"
Degree of parallelism: 8 Degree of parallelism: 16
Array size: 4000000 Array size: 4000000
cutoff: 200000 10times Time:2063ms cutoff: 200000 10times Time:2004ms
cutoff: 250000 10times Time:1601ms cutoff: 250000 10times Time:1670ms
cutoff: 300000 10times Time:1402ms cutoff: 300000 10times Time:1568ms
cutoff: 350000 10times Time:1405ms cutoff: 350000 10times Time:1599ms
cutoff: 400000 10times Time:1421ms cutoff: 400000 10times Time:1556ms
cutoff: 450000 10times Time:1352ms cutoff: 450000 10times Time:1738ms
cutoff: 500000 10times Time:1575ms cutoff: 500000 10times Time:1586ms
cutoff: 550000 10times Time:1368ms cutoff: 550000 10times Time:1556ms
cutoff: 600000 10times Time:1373ms cutoff: 600000 10times Time:1561ms
cutoff: 650000 10times Time:1350ms cutoff: 650000 10times Time:1547ms
cutoff: 700000 10times Time:1342ms cutoff: 700000 10times Time:1425ms
cutoff: 750000 10times Time:1249ms cutoff: 750000 10times Time:1762ms
cutoff: 800000 10times Time:1268ms cutoff: 800000 10times Time:1529ms
cutoff: 850000 10times Time:1242ms cutoff: 850000 10times Time:1534ms
cutoff: 900000 10times Time:1241ms cutoff: 900000 10times Time:1548ms
cutoff: 950000 10times Time:1617ms cutoff: 950000 10times Time:1514ms
cutoff: 1000000 10times Time:1372ms cutoff: 1000000 10times Time:1434ms
cutoff: 1050000 10times Time:1544ms cutoff: 1050000 10times Time:1669ms
cutoff: 1100000 10times Time:1535ms cutoff: 1100000 10times Time:1651ms
cutoff: 1150000 10times Time:1537ms cutoff: 1150000 10times Time:1680ms
cutoff: 1200000 10times Time:1573ms cutoff: 1200000 10times Time:1678ms
cutoff: 1250000 10times Time:1483ms cutoff: 1250000 10times Time:1955ms
cutoff: 1300000 10times Time:1447ms cutoff: 1300000 10times Time:1760ms
cutoff: 1350000 10times Time:1500ms cutoff: 1350000 10times Time:1752ms
cutoff: 1400000 10times Time:1479ms cutoff: 1400000 10times Time:1746ms
cutoff: 1450000 10times Time:1467ms cutoff: 1450000 10times Time:1778ms
cutoff: 1500000 10times Time:1466ms cutoff: 1500000 10times Time:1783ms
cutoff: 1550000 10times Time:1765ms cutoff: 1550000 10times Time:1734ms
cutoff: 1600000 10times Time:1546ms cutoff: 1600000 10times Time:1698ms
cutoff: 1650000 10times Time:1526ms cutoff: 1650000 10times Time:1665ms
cutoff: 1700000 10times Time:1534ms cutoff: 1700000 10times Time:1644ms
cutoff: 1750000 10times Time:1547ms cutoff: 1750000 10times Time:1684ms
cutoff: 1800000 10times Time:1529ms cutoff: 1800000 10times Time:1690ms
cutoff: 1850000 10times Time:1499ms cutoff: 1850000 10times Time:1928ms
cutoff: 1900000 10times Time:1449ms cutoff: 1900000 10times Time:1763ms
cutoff: 1950000 10times Time:1434ms cutoff: 1950000 10times Time:1738ms
cutoff: 2000000 10times Time:1447ms cutoff: 2000000 10times Time:1756ms
cutoff: 2050000 10times Time:1927ms cutoff: 2050000 10times Time:2215ms
cutoff: 2100000 10times Time:1925ms cutoff: 2100000 10times Time:2240ms
cutoff: 2150000 10times Time:1928ms cutoff: 2150000 10times Time:2228ms
cutoff: 2200000 10times Time:1935ms cutoff: 2200000 10times Time:2262ms
```

```

Degree of parallelism: 32
Array size: 4000000
cutoff: 200000      10times Time:2242ms
cutoff: 250000      10times Time:1850ms
cutoff: 300000      10times Time:1711ms
cutoff: 350000      10times Time:1641ms
cutoff: 400000      10times Time:1762ms
cutoff: 450000      10times Time:1703ms
cutoff: 500000      10times Time:1789ms
cutoff: 550000      10times Time:1592ms
cutoff: 600000      10times Time:1573ms
cutoff: 650000      10times Time:1642ms
cutoff: 700000      10times Time:1695ms
cutoff: 750000      10times Time:1475ms
cutoff: 800000      10times Time:1428ms
cutoff: 850000      10times Time:1435ms
cutoff: 900000      10times Time:1428ms
cutoff: 950000      10times Time:1716ms
cutoff: 1000000     10times Time:1543ms
cutoff: 1050000     10times Time:1645ms
cutoff: 1100000     10times Time:1684ms
cutoff: 1150000     10times Time:1748ms
cutoff: 1200000     10times Time:1781ms
cutoff: 1250000     10times Time:1756ms
cutoff: 1300000     10times Time:1755ms
cutoff: 1350000     10times Time:2035ms
cutoff: 1400000     10times Time:1760ms
cutoff: 1450000     10times Time:1756ms
cutoff: 1500000     10times Time:1790ms
cutoff: 1550000     10times Time:1761ms
cutoff: 1600000     10times Time:1773ms
cutoff: 1650000     10times Time:1716ms
cutoff: 1700000     10times Time:1656ms
cutoff: 1750000     10times Time:1659ms
cutoff: 1800000     10times Time:1673ms
cutoff: 1850000     10times Time:1675ms
cutoff: 1900000     10times Time:1658ms
cutoff: 1950000     10times Time:1968ms
cutoff: 2000000     10times Time:1750ms
cutoff: 2050000     10times Time:2247ms
cutoff: 2100000     10times Time:2237ms
cutoff: 2150000     10times Time:2239ms
cutoff: 2200000     10times Time:2241ms

```

It's obvious that the algorithm works better when the number of threads equals to 8. I guess the reason is that my computer has 8 CPU, and it makes it's common pool parallelism is 7(as shown in the first picture), which is close to 8.

To confirm this, I need to change the size of array. It's reasonable to think that if the size is big enough, the treads we need might be larger. So I change the array size to 8,000,000:



Degree of parallelism: 4	Degree of parallelism: 8	Degree of parallelism: 16
Array size: 8000000	Array size: 8000000	Array size: 8000000
cutoff: 200000	10times Time:4220ms	10times Time:4387ms
cutoff: 250000	10times Time:3587ms	10times Time:4192ms
cutoff: 300000	10times Time:3674ms	10times Time:3539ms
cutoff: 350000	10times Time:3435ms	10times Time:3488ms
cutoff: 400000	10times Time:3332ms	10times Time:3513ms
cutoff: 450000	10times Time:3127ms	10times Time:3458ms
cutoff: 500000	10times Time:3441ms	10times Time:3492ms
cutoff: 550000	10times Time:2913ms	10times Time:3323ms
cutoff: 600000	10times Time:3090ms	10times Time:3263ms
cutoff: 650000	10times Time:2910ms	10times Time:3308ms
cutoff: 700000	10times Time:3157ms	10times Time:3097ms
cutoff: 750000	10times Time:2842ms	10times Time:3029ms
cutoff: 800000	10times Time:3257ms	10times Time:3376ms
cutoff: 850000	10times Time:2834ms	10times Time:3286ms
cutoff: 900000	10times Time:2783ms	10times Time:3003ms
cutoff: 950000	10times Time:3168ms	10times Time:3334ms
cutoff: 1000000	10times Time:3013ms	10times Time:3087ms
cutoff: 1050000	10times Time:2655ms	10times Time:3034ms
cutoff: 1100000	10times Time:2606ms	10times Time:3274ms
cutoff: 1150000	10times Time:3113ms	10times Time:3058ms
cutoff: 1200000	10times Time:2771ms	10times Time:2976ms
cutoff: 1250000	10times Time:2670ms	10times Time:2847ms
cutoff: 1300000	10times Time:2619ms	10times Time:3173ms
cutoff: 1350000	10times Time:3036ms	10times Time:3129ms
cutoff: 1400000	10times Time:2777ms	10times Time:3022ms
cutoff: 1450000	10times Time:2630ms	10times Time:2838ms
cutoff: 1500000	10times Time:2680ms	10times Time:2858ms
cutoff: 1550000	10times Time:2943ms	10times Time:3228ms
cutoff: 1600000	10times Time:2777ms	10times Time:3002ms
cutoff: 1650000	10times Time:2683ms	10times Time:2887ms
cutoff: 1700000	10times Time:2606ms	10times Time:2853ms
cutoff: 1750000	10times Time:2962ms	10times Time:3255ms
cutoff: 1800000	10times Time:2781ms	10times Time:3055ms
cutoff: 1850000	10times Time:2736ms	10times Time:3040ms
cutoff: 1900000	10times Time:2622ms	10times Time:2921ms
cutoff: 1950000	10times Time:2924ms	10times Time:3275ms
cutoff: 2000000	10times Time:2803ms	10times Time:3038ms
cutoff: 2050000	10times Time:3226ms	10times Time:3491ms
cutoff: 2100000	10times Time:3142ms	10times Time:3381ms
cutoff: 2150000	10times Time:3050ms	10times Time:3410ms
cutoff: 2200000	10times Time:3056ms	10times Time:3660ms

And we can see: even if the size is so this big, the algorithm still works better when the number of threads is 8 than the number is 16.

So I think I can say that **the best number of threads in this algorithm on my computer is 8.**

Next, I will set the number of threads is 8 and change the size of array to find the best cutoff.

We already tested 4 million and 8 million, it looks like 750,000 is the best cutoff. To confirm this, I will test some other array size(2 million, 3 million, 5 million and 6 million):

Array size: 2000000			Degree of parallelism: 8		
cutoff: 200000	10times	Time:1184ms	Array size: 3000000		
cutoff: 250000	10times	Time:957ms	cutoff: 200000	10times	Time:1649ms
cutoff: 300000	10times	Time:813ms	cutoff: 250000	10times	Time:1210ms
cutoff: 350000	10times	Time:803ms	cutoff: 300000	10times	Time:1117ms
cutoff: 400000	10times	Time:734ms	cutoff: 350000	10times	Time:1096ms
cutoff: 450000	10times	Time:717ms	cutoff: 400000	10times	Time:1079ms
cutoff: 500000	10times	Time:738ms	cutoff: 450000	10times	Time:1003ms
cutoff: 550000	10times	Time:836ms	cutoff: 500000	10times	Time:1020ms
cutoff: 600000	10times	Time:840ms	cutoff: 550000	10times	Time:1009ms
cutoff: 650000	10times	Time:837ms	cutoff: 600000	10times	Time:1023ms
cutoff: 700000	10times	Time:836ms	cutoff: 650000	10times	Time:1004ms
cutoff: 750000	10times	Time:840ms	cutoff: 700000	10times	Time:965ms
cutoff: 800000	10times	Time:846ms	cutoff: 750000	10times	Time:938ms
cutoff: 850000	10times	Time:842ms	cutoff: 800000	10times	Time:1096ms
cutoff: 900000	10times	Time:845ms	cutoff: 850000	10times	Time:1094ms
cutoff: 950000	10times	Time:843ms	cutoff: 900000	10times	Time:1079ms
cutoff: 1000000	10times	Time:838ms	cutoff: 950000	10times	Time:1079ms
cutoff: 1050000	10times	Time:1027ms	cutoff: 1000000	10times	Time:1099ms
cutoff: 1100000	10times	Time:1042ms	cutoff: 1050000	10times	Time:1104ms
cutoff: 1150000	10times	Time:1002ms	cutoff: 1100000	10times	Time:1095ms
cutoff: 1200000	10times	Time:1038ms	cutoff: 1150000	10times	Time:1090ms
cutoff: 1250000	10times	Time:1027ms	cutoff: 1200000	10times	Time:1075ms
cutoff: 1300000	10times	Time:1033ms	cutoff: 1250000	10times	Time:1345ms
cutoff: 1350000	10times	Time:1024ms	cutoff: 1300000	10times	Time:1176ms
cutoff: 1400000	10times	Time:1036ms	cutoff: 1350000	10times	Time:1258ms
cutoff: 1450000	10times	Time:1019ms	cutoff: 1400000	10times	Time:1148ms
cutoff: 1500000	10times	Time:1051ms	cutoff: 1450000	10times	Time:1144ms
cutoff: 1550000	10times	Time:1041ms	cutoff: 1500000	10times	Time:1143ms
cutoff: 1600000	10times	Time:1033ms	cutoff: 1550000	10times	Time:1450ms
cutoff: 1650000	10times	Time:1027ms	cutoff: 1600000	10times	Time:1435ms
cutoff: 1700000	10times	Time:1320ms	cutoff: 1650000	10times	Time:1483ms
			cutoff: 1700000	10times	Time:1474ms

Degree of parallelism: 8			Degree of parallelism: 8		
Array size: 5000000			Array size: 6000000		
cutoff: 200000	10times	Time:2531ms	cutoff: 200000	10times	Time:3089ms
cutoff: 250000	10times	Time:2038ms	cutoff: 250000	10times	Time:2543ms
cutoff: 300000	10times	Time:1939ms	cutoff: 300000	10times	Time:2491ms
cutoff: 350000	10times	Time:1863ms	cutoff: 350000	10times	Time:2579ms
cutoff: 400000	10times	Time:1858ms	cutoff: 400000	10times	Time:2635ms
cutoff: 450000	10times	Time:1852ms	cutoff: 450000	10times	Time:2479ms
cutoff: 500000	10times	Time:1790ms	cutoff: 500000	10times	Time:2505ms
cutoff: 550000	10times	Time:1798ms	cutoff: 550000	10times	Time:2387ms
cutoff: 600000	10times	Time:1695ms	cutoff: 600000	10times	Time:2368ms
cutoff: 650000	10times	Time:1622ms	cutoff: 650000	10times	Time:2288ms
cutoff: 700000	10times	Time:1598ms	cutoff: 700000	10times	Time:2248ms
cutoff: 750000	10times	Time:1873ms	cutoff: 750000	10times	Time:2121ms
cutoff: 800000	10times	Time:1732ms	cutoff: 800000	10times	Time:2554ms
cutoff: 850000	10times	Time:1710ms	cutoff: 850000	10times	Time:2260ms
cutoff: 900000	10times	Time:1709ms	cutoff: 900000	10times	Time:2263ms
cutoff: 950000	10times	Time:1740ms	cutoff: 950000	10times	Time:2244ms
cutoff: 1000000	10times	Time:1744ms	cutoff: 1000000	10times	Time:2296ms
cutoff: 1050000	10times	Time:1794ms	cutoff: 1050000	10times	Time:2137ms
cutoff: 1100000	10times	Time:1709ms	cutoff: 1100000	10times	Time:2145ms
cutoff: 1150000	10times	Time:1690ms	cutoff: 1150000	10times	Time:2390ms
cutoff: 1200000	10times	Time:1693ms	cutoff: 1200000	10times	Time:2183ms
cutoff: 1250000	10times	Time:1714ms	cutoff: 1250000	10times	Time:2203ms
cutoff: 1300000	10times	Time:2245ms	cutoff: 1300000	10times	Time:2090ms
cutoff: 1350000	10times	Time:2087ms	cutoff: 1350000	10times	Time:2043ms
cutoff: 1400000	10times	Time:2076ms	cutoff: 1400000	10times	Time:2078ms
cutoff: 1450000	10times	Time:2053ms	cutoff: 1450000	10times	Time:2409ms
cutoff: 1500000	10times	Time:2074ms	cutoff: 1500000	10times	Time:2158ms
cutoff: 1550000	10times	Time:2050ms	cutoff: 1550000	10times	Time:2560ms
cutoff: 1600000	10times	Time:1941ms	cutoff: 1600000	10times	Time:2551ms
cutoff: 1650000	10times	Time:1958ms	cutoff: 1650000	10times	Time:2489ms
cutoff: 1700000	10times	Time:1942ms	cutoff: 1700000	10times	Time:2430ms
cutoff: 1750000	10times	Time:1948ms	cutoff: 1750000	10times	Time:2436ms
cutoff: 1800000	10times	Time:2225ms	cutoff: 1800000	10times	Time:2713ms
cutoff: 1850000	10times	Time:2041ms	cutoff: 1850000	10times	Time:2529ms
cutoff: 1900000	10times	Time:2016ms	cutoff: 1900000	10times	Time:2544ms
cutoff: 1950000	10times	Time:2034ms	cutoff: 1950000	10times	Time:2517ms
cutoff: 2000000	10times	Time:2022ms	cutoff: 2000000	10times	Time:2545ms
cutoff: 2050000	10times	Time:2005ms	cutoff: 2050000	10times	Time:2422ms
cutoff: 2100000	10times	Time:1953ms	cutoff: 2100000	10times	Time:2447ms
cutoff: 2150000	10times	Time:1930ms	cutoff: 2150000	10times	Time:2446ms

It's obvious that in all these four pictures, the quickest cutoff is from 700,000 to 800,000. Considering the experimental error, I believe it's fair to say that **the best cutoff is 750,000**.

## Conclusion:

On my computer:  
The cutoff should be 750,000.  
The number of threads should be 8.