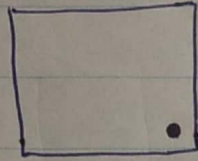


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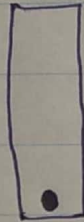
Homework 3

① a Structuring Element:



Operation: Erosion

⑥ Structuring Element:





Operation: Erosion


⑦ Structuring Element:
Step 1:



Operation: opening [Erosion followed by Dilation]

Step 2: 
Operation: Erosion.

⑧ Step 1: Structuring Element 
Operation: ~~Dilation~~ Dilation

Step 2: Structuring Element 
Operation: Closing [Dilation followed by Erosion]

② $P_1(z)$ = represents the probability P_1 of object
 $P_2(z)$ = represents the probability P_2 of Background

Using the line equation $y = mx + c$ where m = slope,
and c = y-intercept

Let us assume that $P_1(z)$ and $P_2(z)$ are equal
to get optimal threshold

$$P_1(z) = P_2(z)$$

The line passing through the point $(4, 0.5)$ and
 $(1, 0)$

$$y = \frac{0 - 0.5}{1 - 4} x + c$$

$$y = \frac{x}{6} + c$$

Applying the values of $(x, y) = (1, 0)$

$$0 = \frac{1}{6} + c$$

$$c = \underline{\underline{-1/6}}$$

$$\therefore y = \frac{x}{6} - \frac{1}{6} \Rightarrow x - 6y = 1 \quad \text{--- (1)}$$

Line passing through $(1, 1)$ and $(2, 0)$

$$y = \frac{0-1}{2-1} x + c$$

$$y = -x + c$$

Applying $(x, y) = (2, 0)$

$$0 = -2 + c$$

$$c = 2$$

$$\therefore x + y = 2 \quad \text{--- (2)}$$

Solving (1) & (2)

$$x + 6y = 1$$

$$x + y = 2$$

$$-7y = -1$$

$$y = 1/7$$

$$x = 13/7$$

Therefore $z = 13/7$ is the optimal threshold value b/w object and background pixels assuming that $p_1(z) = p_2(z)$

3) a) (i) $y = x - 2$

given this line lets find a perpendicular distance from origin to the given line
 $y = (1)x + (-2)$ ——— (1)

So here $m = 1$ and $c = -2$, any line \perp to this line will have m_2 such that
 $m_1 \cdot m_2 = -1$
 $(1) \cdot m_2 = -1$
 $m_2 = -1$

$y = -x + k$, but $k = 0$ as the line passes through origin.
 $\therefore y = -x$ ——— (2)

Solve (1) & (2)

$$\begin{array}{r} y = x - 2 \\ y = -x \\ \hline 0 = 2x - 2 \end{array}$$

$$x = 1$$

$$y = -1$$

So $(1, -1)$ is the point where \perp meets the line $y = x - 2$

$$d = \sqrt{x^2 + y^2}$$

$$\beta = \tan^{-1}(y/x)$$

$$d = \sqrt{(1)^2 + (-1)^2}$$

$$\beta = \tan^{-1}(-1/1)$$

$$d = \sqrt{2}$$

$$\beta = -\pi/4$$

The equation of the line in (r, θ) form is

$$r = \frac{d}{\cos(\theta - \beta)}$$

$$r = \frac{\sqrt{2}}{\theta + \pi/4}$$

$$\text{or } r = \frac{\sqrt{2}}{\theta + 45}$$

$$(ii) y = 1 - x/2$$

$$y = (-1/2)x + 1 \longrightarrow (1)$$

\therefore \perp^r line to this will have

$$m_2 = 2$$

The \perp^r line is given by

$$y = 2x \longrightarrow (2)$$

Solving ① & ② $x = 2/5$ $y = 4/5$

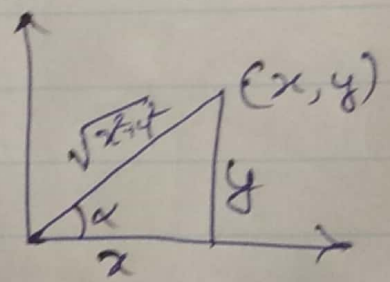
$$d = \sqrt{(2/5)^2 + (4/5)^2} = 2/\sqrt{5}$$

$$\beta = \tan^{-1}(y/x) = \tan^{-1}(2) \approx 63.41^\circ$$

$$\therefore r = \frac{2}{\sqrt{5} \cos(90 - 63.41^\circ)}$$

⑥ $x \cos \theta + y \sin \theta = p$

$$\frac{x}{\sqrt{x^2+y^2}} \cos \theta + \frac{y}{\sqrt{x^2+y^2}} = \frac{p}{\sqrt{x^2+y^2}}$$



$$\cos \alpha \cos \theta + \sin \alpha \sin \theta = p / \sqrt{x^2 + y^2}$$

$$\cos(\alpha - \theta) = p / \sqrt{x^2 + y^2}$$

$$\sin(90 - (\alpha - \theta)) = p / \sqrt{x^2 + y^2}$$

$$\sin(\theta - (\alpha - 90^\circ)) = p / \sqrt{x^2 + y^2}$$

$$f = \left(\sqrt{x^2 + y^2} \right) \sin \left(\theta - \underline{(\alpha - 90^\circ)} \right) \quad (1)$$

Compare to standard form of sinusoidal wave

$$y = A \sin(Bx - c)$$

Hence it follows a sinusoidal function.

Thus here

$$\text{Amplitude} = A = \sqrt{x^2 + y^2}$$

$$\text{Period} = \frac{2\pi}{B} = 2\pi$$

$$\text{phase angle} = (\alpha - 90)$$

→ As it can be proved, amplitude and point (x, y) are directly related. They are directly proportional

→ Here period of the sinusoidal is a constant $= 2\pi$ and doesn't change with (x, y)

→ Phase angle is directly affected by α i.e. the angle subtended by (x, y) at origin (0,0)