

## PHYS 2311 Ch. 11 HW

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November 20, 2024

### Problem 1.

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$$I = mR^2 = (0.210)(1.25)^2 = 0.328 \text{ kg} \cdot \text{m}^2$$

$$\vec{L} = I\vec{\omega} = (0.328)(10.4) = \boxed{3.4112 \text{ kg} \cdot \text{m}^2/\text{s}}$$

### Problem 2.

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(a)

$$I = \frac{1}{2}mR^2 = \frac{1}{2}(2.8)(0.18)^2 = 0.045 \text{ kg} \cdot \text{m}^2$$

$$1500 \text{ rpm} = \frac{2\pi \text{ rad}}{60 \text{ s}} = 157.1 \text{ rad/s}$$

$$L = I\omega = (0.045)(157.1) = \boxed{7.0695 \text{ kg} \cdot \text{m}^2/\text{s}}$$

(b)

$$\omega = \omega_0 + \alpha t$$

$$0 = 157.1 + \alpha(6.0)$$

$$\alpha = \frac{-157.1}{6.0} = -26.183 \text{ rad/s}^2$$

$$\tau = I\alpha = (0.045)(26.183) = \boxed{1.178 \text{ Nm}}$$

### Problem 3.

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$$L_i = L_f$$

$$L_i = I \cdot \omega$$

$$L_f = 2I\omega_f$$

$$I\omega = 2I\omega_f$$

$$\omega_f = \frac{I\omega}{2I}$$

$$\omega_f = \frac{1}{2}\omega$$

**Problem 5.**

$$\omega_i = 0.67 \text{ rev/s} \quad \omega_f = 2.5 \text{ rev/s}$$

$$\omega_i = 4.19 \text{ rad/s} \quad \omega_f = 15.71 \text{ rad/s}$$

$$I_i = 4.9 \text{ kg} \cdot \text{m}^2$$

$$L_i = L_f$$

$$(4.9)(4.19) = I_f(15.71)$$

$$I_f = \boxed{1.317 \text{ kg} \cdot \text{m}^2}$$

The dancer lowers her moment of inertia. The simplest way to do this is by pulling in her arms to decrease her radius.

**Problem 9.**

$$L_{\text{initial}} = L_{\text{final}}$$

$$L_{\text{initial}} = I_{\text{disk}} \cdot \omega_d$$

$$L_{\text{final}} = (I_{\text{disk}} + I_{\text{rod}}) \cdot \omega_f$$

$$I_{\text{disk}} \cdot \omega_d = (I_{\text{disk}} + I_{\text{rod}}) \cdot \omega_f$$

$$I_{\text{disk}} = \frac{1}{2}MR^2$$

$$I_{\text{rod}} = \frac{1}{3}MR^2$$

$$\left(\frac{1}{2}MR^2\right) \cdot \omega_d = \left(\frac{1}{2}MR^2 + \frac{1}{3}MR^2\right) \cdot \omega_f$$

$$\frac{1}{2}MR^2 \cdot \omega_d = \frac{5}{6}MR^2 \cdot \omega_f$$

$$\frac{1}{2}(4.1) = \frac{5}{6} \cdot \omega_f$$

$$\omega_f = \boxed{2.46 \text{ rev/s}}$$

**Problem 36.**

$$\vec{L} = \vec{r} \times \vec{p}$$

$$\vec{p} = m\vec{v}$$

$$\begin{aligned}
\vec{r}_O &= d\hat{j} \\
\vec{L}_O &= \vec{r}_O \times \vec{p} = (d\hat{j}) \times (mv\hat{i}) \\
\boxed{\vec{L}_O &= mvd\hat{k}} \\
\vec{r}_{O'} &= 0 \\
\vec{L}_{O'} &= \vec{r}_{O'} \times \vec{p} = 0 \\
\vec{L}_O &= mvd\hat{k} \\
\boxed{\vec{L}_{O'} &= 0}
\end{aligned}$$

**Problem 42.**

(a)

$$\begin{aligned}
L_{\parallel} &= I \cdot \omega \\
I &= mr^2 \\
L_{\parallel} &= 2 \cdot (mr^2) \cdot \omega = 2 \cdot (0.480 \cdot 0.24^2) \cdot 4.5 = 0.249 \text{ kg} \cdot \text{m}^2/\text{s} \\
L_{\perp} &= m \cdot v \cdot h \\
v &= r \cdot \omega \\
L_{\perp} &= 2 \cdot (m \cdot r \cdot \omega \cdot h) = 2 \cdot (0.480 \cdot 0.24 \cdot 4.5 \cdot 0.42) = 0.435 \text{ kg} \cdot \text{m}^2/\text{s} \\
L &= \sqrt{L_{\parallel}^2 + L_{\perp}^2} = \sqrt{(0.249)^2 + (0.435)^2} = \boxed{0.502 \text{ kg} \cdot \text{m}^2/\text{s}}
\end{aligned}$$

(b)

$$\theta = \tan^{-1} \left( \frac{L_{\perp}}{L_{\parallel}} \right) = \boxed{60.26^\circ}$$

**Problem 48.**

$$\begin{aligned}
\ell &= 1.0 \text{ m}, \quad M = 270 \text{ g} = 0.270 \text{ kg}, \quad m_b = 3.5 \text{ g} = 0.0035 \text{ kg} \\
v_{\text{in}} &= 250 \text{ m/s}, \quad v_{\text{out}} = 140 \text{ m/s}, \quad \ell/4 = 0.25 \text{ m}, \quad L_i = 0 \\
L_{\text{initial}} &= L_{\text{final}} \\
L_{\text{initial}} &= m_b v_{\text{in}} r \\
L_{\text{initial}} &= (0.0035)(250)(0.25) = 0.21875 \text{ kg} \cdot \text{m}^2/\text{s} \\
L_{\text{bullet}} &= m_b v_{\text{out}} r = (0.0035)(140)(0.25) = 0.1225 \text{ kg} \cdot \text{m}^2/\text{s} \\
I &= \frac{1}{12} ML^2 = \frac{1}{12} (0.270)(1.0)^2 = 0.0225 \text{ kg} \cdot \text{m}^2 \\
L_{\text{stick}} &= I\omega = (0.0225)\omega
\end{aligned}$$

$$L_{\text{final}} = L_{\text{bullet}} + L_{\text{stick}} = 0.1225 + 0.0225\omega$$

$$L_{\text{initial}} = L_{\text{final}}$$

$$0.21875 = 0.1225 + 0.0225\omega$$

$$0.0225\omega = 0.21875 - 0.1225 = 0.09625$$

$$\omega = \frac{0.09625}{0.0225} = \boxed{4.28 \text{ rad/s}}$$