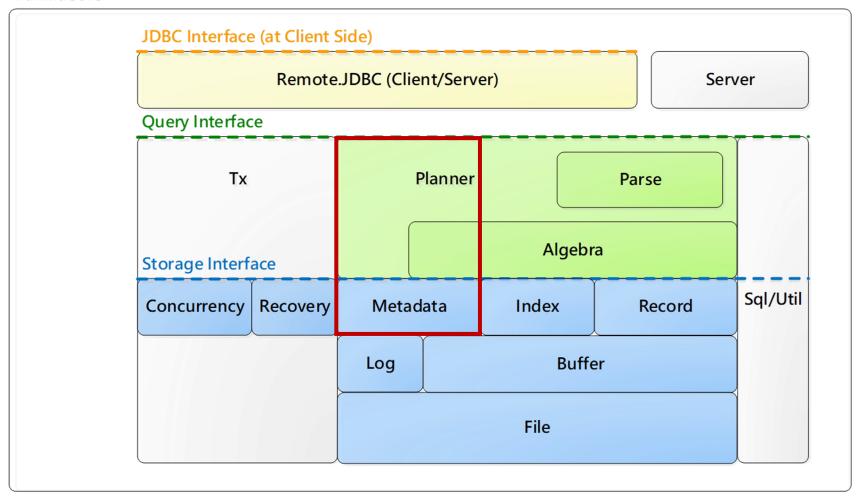
Query Optimization

Shan-Hung Wu and DataLab CS, NTHU

Where Are We?

VanillaCore



Outline

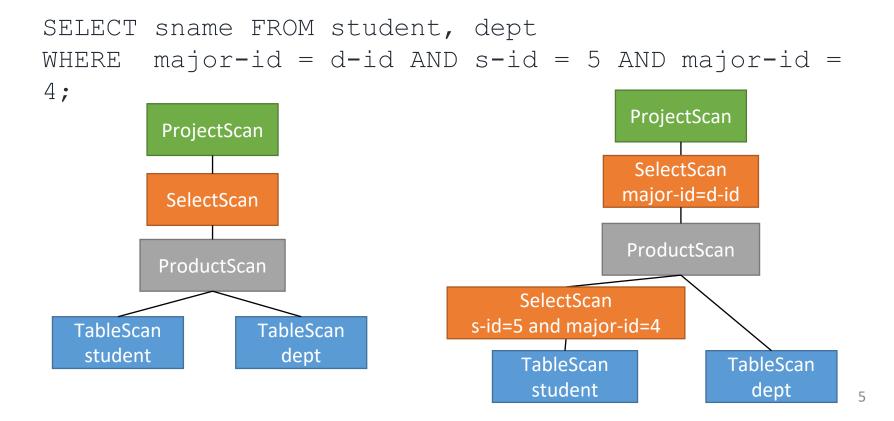
- Overview
- Cost Estimation
 - Cardinality Estimation
 - Histogram-based Estimation
 - Types of Histograms
- Heuristic Query Optimizer
 - Basic Planner
 - Pushing Select Down
 - Join Ordering
 - Heuristic Query Planner in VanillaCore
- Selinger-Style Query Optimizer

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SQL and Relational Algebra

 A SQL command can be expressed as multiple trees in relational algebra



Query Optimization

- A good scan tree can be faster than a bad one for orders of magnitude
- Query optimizer:
 - 1. Generate candidate plan trees
 - Estimate cost of each corresponding scan tree (not discussed yet)
 - 3. Pick and open the "best" one to execute query
- Goal (ideally): find the one with least cost
- Goal (in practice): avoid bad trees

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Metric for Cost

- Cost of a query?
- To user: query delay
- Low delay also implies better system throughput

Typically, I/O delay dominates query delay

Cost Estimation

- For each plan/table p, we estimate B(p)
 - #blocks accessed by the corresponding scan

- Usually, estimating B(p) requires more knowledge:
 - R(p): #records output
 - Search cost (#blocks) of index, if used
 - V(p,f): #distinct values for field f in p

Estimating B(p)

р	B(p)
TablePlan	Actual #blocks cached by StatMgr (via periodic table scanning)
ProjectPlan(c)	B(c)
SelectPlan(c)	B(c)
IndexSelectPlan(t)	IndexSearchCost(R(t), R(p)) + R(p)
ProductPlan(c1, c2)	B(c1) + (R(c1) * B(c2))
IndexJoinPlan(c1, t2)	B(c1) + (R(c1) * IndexSearchCost(R(t2), 1)) + R(p)

• B(c) is evaluated recursively down to the table level

For Any p, We Need to Estimate R(p) and Index Search Cost

- Index Search Cost:
 - HashIndex.searchCost()
 - BTreeIndex.searchCost()

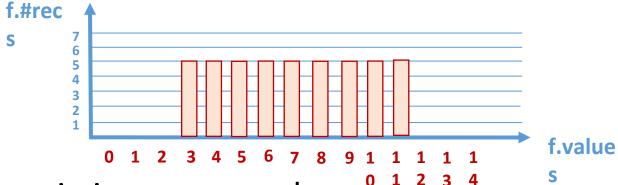
Estimating R(p) is called cardinality estimation

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Naïve Approach

- Uniform assumption
 - All values in field appear with the same probability



• Few statistics are enough:

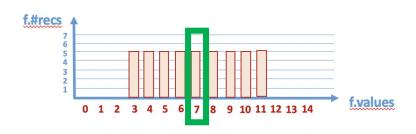
R(c)	#records in child plan c
V(c, f)	#distinct values in field f in c
Max(c, f)	Max value in field f in c
Min(c, f)	Min value in field f in c

p = Select(c, f=x)

• R(p)?

```
R(c) #records in child plan c
V(c, f) #distinct values in field f in c
Max(c, f) Max value in field f in c
Min(c, f) Min value in field f in c
```

- Selectivity(f=x): $\frac{1}{V(c,f)}$
- R(p): Selectivity(f=x) * R(c)



p = Select(c, f>x)

• R(p)?

```
R(c) #records in child plan c
V(c, f) #distinct values in field f in c
Max(c, f) Max value in field f in c
Min(c, f) Min value in field f in c
```

- Selectivity(f>x): $\frac{Max(c,f)-x}{Max(c,f)-Min(c,f)}$
- R(p): Selectivity(f>x) * R(c)

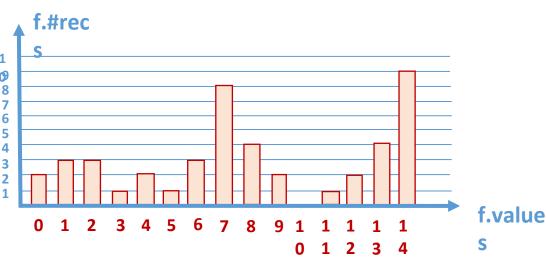


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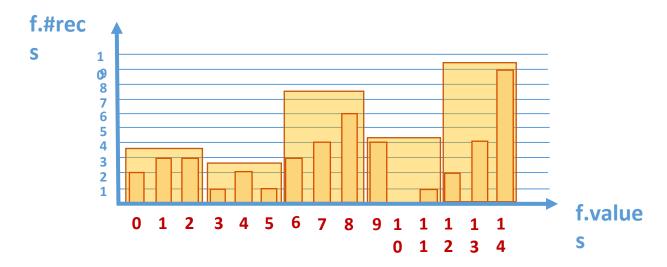
Naïve Estimation is Inaccurate

- In the real world, values in a field are seldom uniform distributed
- p = Select(c, f=14)
- Estimated R(p) = $\frac{1}{15}$ * R(c) = 3
- Actually, R(p) = 9



Histogram

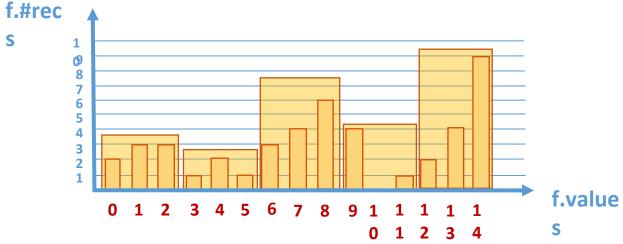
- Approximates value distribution in every field
- Partitions field values into a set of buckets



- More #buckets, more accurate approximation
 - Tradeoff between accurate and storage cost

Buckets

- Each bucket b collects statistics of a value range
 - Assumes uniform distribution of records and values in b



- R(p, f, b): #records
- V(p, f, b): #distinct values
- Range(p, f, b): value range

Cardinality Estimation

Not matter what p is, we have

$$R(p) = \sum\nolimits_{b \in p.hist.buckets(f)} R(p,f,b)$$
 for any f

Problem: how to construct the histogram?

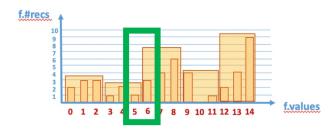
Range Selection (1/2)

- p = Select(c, f in Range)
- For each bucket b in f:
 - Selectivity = $\frac{|Range(c,f,b) \cap Range|}{|Range(c,f,b)|}$
 - Range(p,f,b) = Range(c,f,b) ∩ Range
 - V(p,f,b) = V(c,f,b) * selectivity
 - R(p,f,b) = R(c,f,b) * selectivity
- Assumptions:
 - #Records in a bucket are uniformly distributed
 - Values in a bucket are uniformly distributed

Given ∀f,b:

Range(c, f, b) V(c, f, b)

R(c, f, b)



Range Selection (2/2)

- p = Select(c, f in Range)
- For each bucket b in f' ≠ f:
 - Reduction = $\frac{\sum_{b} R(p,f,b)}{R(c)}$
 - Range(p,f',b) = Range(c,f',b)
 - R(p,f',b) = R(c,f',b) * Reduction
 - V(p,f',b) = min(V(c,f',b), R(p,f',b))
- Assumptions:
 - Values in different fields are independent with each other

Given ∀f,b:

Range(c, f, b) V(c, f, b)

R(c, f, b)

Product

- p = Product(c1, c2)
- For each (b,f) in c1:
 - Range(p,f,b) = Range(c1,f,b)
 - V(p,f,b) = V(c1,f,b)
 - R(p,f,b) = R(c1,f,b) * R(c2)
- For each (b,f) in c2:
 - Range(p,f,b) = Range(c2,f,b)
 - V(p,f,b) = V(c2,f,b)
 - R(p,f,b) = R(c2,f,b) * R(c1)

Given ∀f,b:

Range(c1, f, b) V(c1, f, b) R(c1, f, b) Range(c2, f, b) V(c2, f, b) R(c2, f, b)

Join Selection (1/2)

- * p = Select(c, f=g)or Joint(a, b, a.f=b.g)
- For each bucket b1 in f and b2 in g:
 - Range(p,f,b1) = Range(p,g,b2) = IR = Range(c,f,b1) ∩ Range(c,g,b2)

• V(p,f,b1) = V(p,g,b2) = minV = min
$$\left(\frac{|IR|*V(c,f,b1)}{|Range(c,f,b1)|'}, \frac{|IR|*V(c,g,b2)}{|Range(c,g,b2)|}\right)$$

Match rate with recs in b2

• R1 = R(c,f,b1) *
$$\frac{minV}{V(c,f,b1)}$$
 * $\frac{1}{V(c,g,b2)}$ * $\frac{R(c,g,b2)}{R(c)}$

Match rate with b2

• R2 = R(c,g,b2) *
$$\frac{minV}{V(c,g,b2)}$$
 * $\frac{1}{V(c,f,b1)}$ * $\frac{R(c,f,b1)}{R(c)}$

- R(p,f,b1) = R(p,g,b2) = min(R1, R2)
- Assumptions:
 - #Records & values in bucket are uniformly distributed
 - All values in the range having smaller number of values appear in the range having larger number of values
 - Values in different fields are independent with each other

Join Selection (2/2)

- p = Select(c, f=g)
- For each bucket b in f' ∉ {f, g}:
 - Reduction = $\frac{\sum_{b} R(p,f,b)}{R(c)}$
 - R(p,f',b) = R(c,f',b) * Reduction
 - V(p,f',b) = min(V(c,f',b), R(p,f',b))
 - Range(p,f',b) = Range(c,f',b)
- Assumptions:
 - Values in different fields are independent with each other

Cost Estimation in VanillaCore

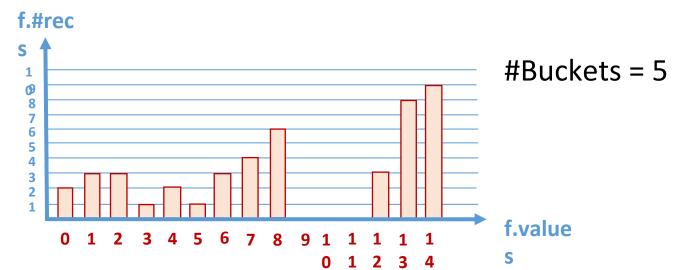
- B(p): p.blocksAccessed()
- Histogram-based cardinality estimation:
 - R(p): p.histogram().recordsOutput()
 - V(p,f): p.histogram().distinctVaues(f)
- Each plan builds its own histogram in constructor
- Important utility methods to trace:
 - SelectPlan.constantRangeHistorgram()
 - ProductPlan.productHistogram()
 - SelectPlan.joinFieldHistogram()
 - AbstractJointPlan.joinHistogram()

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Table Histogram at Lowest-Level

- Data structure that approximates value distribution
- Partitions field values into a set of buckets
- Each bucket b collects statistics of a value range
 - Assumes uniform distribution of records and values in b
- Given a fixed #buckets, how to decide bucket ranges?

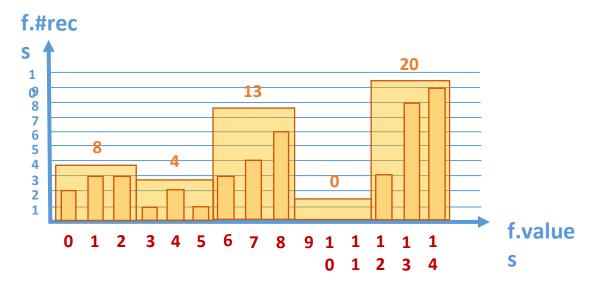


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Equi-Width Histogram

Partition strategy: all buckets have the same range

• |Range(b)| =
$$\frac{Max(p,f) - Min(p,f) + 1}{\#Buckets}$$

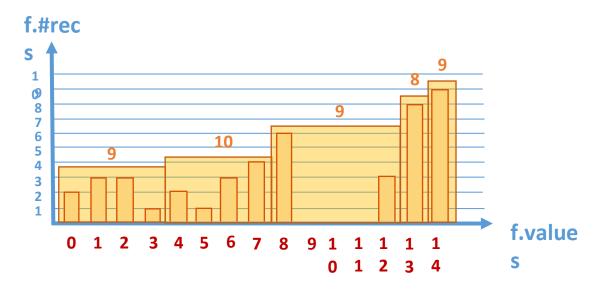


Problem: some buckets may be wasted

Equi-Depth Histogram

Partition strategy: all buckets have the same #recs

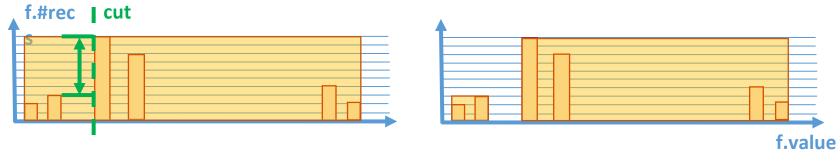
• Depth =
$$\frac{R(p)}{\#Buckets}$$



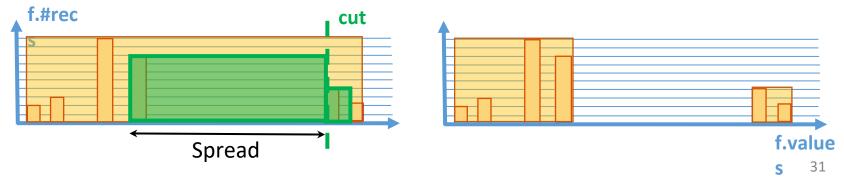
 Problem: records/values in a bucket may not be uniformly distributed

Max-Diff Histogram

- Partition strategy: split buckets at values with max.
 diff in #rec (MaxDiff(F)) or area (MaxDiff(A)):
 - #recs: uniform #records in each bucket



1. Area: uniform #records *and values* in each bucket ^s



Histogram in VanillaCore

- Table histograms are statistics metadata
 - org.vanilladb.core.storage.metadata.statistics
- Accessed (by TablePlan) via StatMgr.getTableStatInfo()

Histogram() + Histogram(fldnames : Set<String>) ~ Histogram(dists : Map<String, Collection<Bucket>>) + Histogram(hist : Histogram) + fields() : Set<String> + buckets(fldname : String) : Collection<Bucket> + addField(fldname : String) + addBucket(fldname : String, bkt : Bucket) + setBuckets(fldname : String, bkts : Collection<Bucket>) + recordsOutput() : double + distinctValues(fldname : String) : double + toString() : String + toString(int) : String

Bucket + Bucket(valrange : ConstantRange, freq : double, distvals : double) + Bucket(valrange : ConstantRange, freq : double, distvals : double, pcts : Percentiles) + valueRange() : ConstantRange + frequency() : double + distinctValues() : double + distinctValues(range : ConstantRange) : double + valuePercentiles() : Percentiles + toString() : String + toString(int) : String

Building Histogram (1/2)

- When system starts up:
- StatMgr:
 - Scans table and calls SampledHistogramBuilder.sample()
 - When done, calls SampledHistogramBuilder.newMaxDiffHistogram()
- Histogram types:
 - MaxDiff(A): when field value is numeric
 - MaxDiff(F) : otherwise

Building Histogram (2/2)

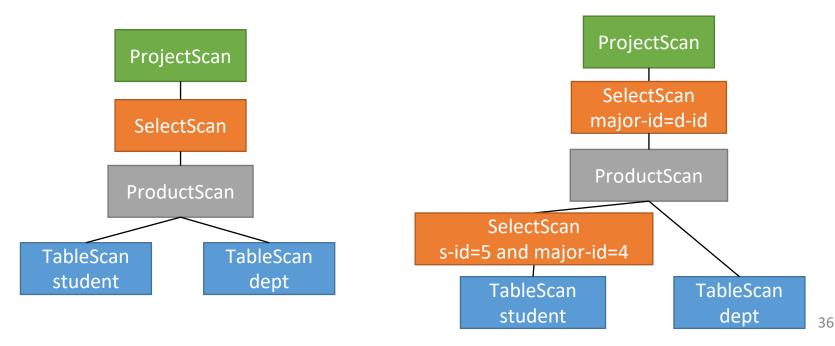
- At runtime:
- StatMgr tacks #recs updated for each table
 - QueryPlanner calls StatMgr.countRecordUpdates() after executing modify/insert/delete queries
- Rebuilds histogram in background when StatMgr.getTableStatInfo() is called
 - If #recs updated > threshold (e.g., 100)
- StatisticsRefreshTask:
 - Scans table and calls SampledHistogramBuilder.sample()
 - When done, calls SampledHistogramBuilder.newMaxDiffHistogram()

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Query Optimization

- Query optimizer:
 - 1. Generate candidate plan trees
 - 2. Estimate cost of each corresponding scan tree
 - 3. Pick and open the "best" one to execute query



In Reality...

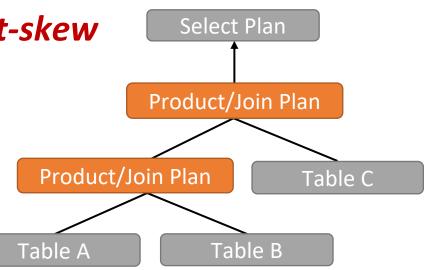
- Generating all candidate plan trees are too costly
 - #trees with n products/joins = Catalan number:

$$\frac{1}{n+1}\begin{pmatrix} 2n \\ n \end{pmatrix}$$

Compromise: consider *left-skew* candidate trees only

Query planner's goal

- Avoiding bad trees
- Not finding the best tree



Why Left-Skew Trees Only?

- Tend to be better than plans of other shapes
- Because many join algorithms scan right child c2 multiple times
- Normally, we don't want c2 to be a complex subtree

BasicQueryPlanner

```
public Plan createPlan(QueryData data, Transaction tx) {
     // Step 1: Create a plan for each mentioned table or view
     List<Plan> plans = new ArrayList<Plan>();
     for (String tblname : data.tables()) {
           String viewdef = VanillaDb.catalogMqr().getViewDef(tblname. tx):
           if (viewdef != null)
                plans.add(VanillaDb.newPlanner().createQueryPlan(viewdef, tx));
           else
                plans.add(new TablePlan(tblname, tx));

    Product/join order

     // Step 2: Create the product of all table plans
     Plan p = plans.remove(0);
                                                                follows what's
     for (Plan nextplan : plans)
           p = new ProductPlan(p, nextplan);
     // Step 3: Add a selection plan for the predicate
                                                                written in SQL
           p = new SelectPlan(p, data.pred());
     // Step 4: Add a group-by plan if specified
           if (data.groupFields() != null) {
                p = new GroupByPlan(p, data.groupFields(), data.aggregationFn(), tx);
     // Step 5: Project onto the specified fields
     p = new ProjectPlan(p, data.projectFields());
     // Step 6: Add a sort plan if specified
     if (data.sortFields() != null)
           p = new SortPlan(p, data.sortFields(), data.sortDirections(), tx);
     // Step 7: Add a explain plan if the query is explain statement
     if (data.isExplain())
           p = new ExplainPlan(p);
     return p;
```

Cost & Bottlenecks

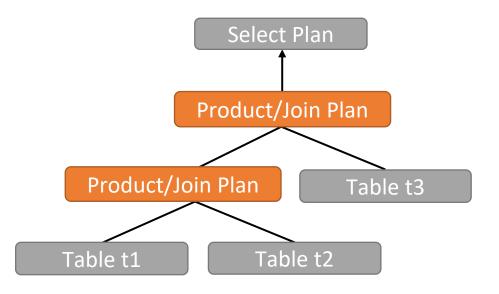
```
      SELECT
      *

      FROM
      t1, t2, t3

      WHERE
      t1.f1 = t2.f2

      AND
      t2.f3 = t3.f4

      AND
      t1.f5 = x
```



- B(root) dominated by #recs of product/join ops
 - B(Product(c1, c2)) = B(c1) + (R(c1) * B(c2))
 - B(IndexJoin(c1, c2)) = B(c1) + (R(c1) * SearchCost(...)) + ...

Optimizations

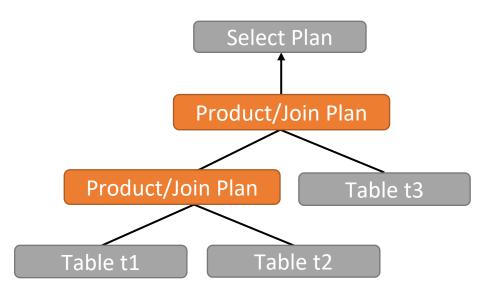
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      AND
      t1.f5 = x
```



- Goal \downarrow B(root) reduced to \downarrow R(c1)
- Heuristics:
 - Pushing Select ops down
 - Greedy Join ordering

Pushing Select Ops Down

- Execute Select ops as early as possible
- ↓R of each product/join op

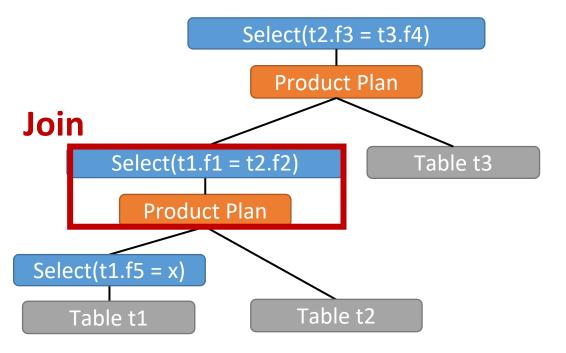
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      *

      FROM
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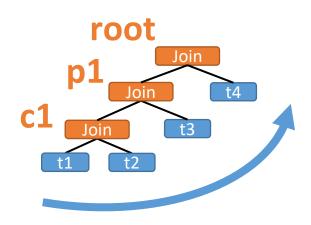
      AND
      t2.f3 = t3.f4

      AND
      t1.f5 = x
```



Greedy Join Ordering

- B(root) = B(p1) + (R(p1) * ...) + ...
 - \downarrow B(root) implies \downarrow (p1)
- B(p1) = B(c1) + (R(c1) * ...) + ...
 - \downarrow B(root) also implies \downarrow (c1)
- •
- B(root) \propto R(p1) + R(c1) + ...



 Greedy Join ordering: repeatedly add table to the "trunk" that result in lowest R(trunk)

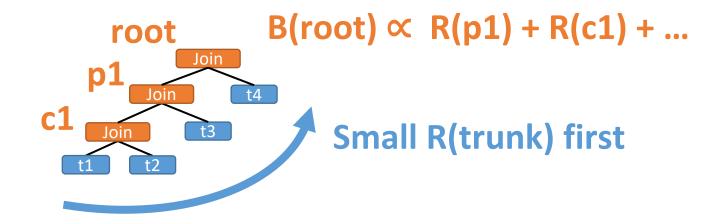
HeuristicPlanner in VanillaCore

```
public Plan createPlan(QueryData data, Transaction tx) {
     // Step 1: Create a TablePlanner object for each mentioned table/view
     int id = 0;
     for (String tbl : data.tables()) {
          String viewdef = VanillaDb.catalogMqr().getViewDef(tbl, tx);
          if (viewdef != null)
                views.add(VanillaDb.newPlanner().createQueryPlan(viewdef, tx));
          else {
                TablePlanner tp = new TablePlanner(tbl, data.pred(), tx, id);
               tablePlanners.add(tp);
          id += 1;
     // Step 2: Choose the lowest-size plan to begin the trunk of join
     Plan trunk = getLowestSelectPlan();
     // Step 3: Repeatedly add a plan to the join trunk
     while (!tablePlanners.isEmpty() || !views.isEmpty()) {
          Plan p = getLowestJoinPlan(trunk);
          if (p != null)
                                                      Feasible Select ops applied
               trunk = p:
          else
               // no applicable join
               trunk = getLowestProductPlan(trunk)
     // Step 4: Add a group by plan if specified
     // Step 5. Project on the field names
     // Step 6: Add a sort plan if specified
     // Step 7: Add a explain plan if the query is explain statement
```

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Why not HeuristicPlanner?



- Assumption: $\downarrow R(c1)$ implies $\downarrow R(p1)$)
- May not be true: joint rate also matters
- Exhaustively searching the best join order?
 - #Candidates: O(n!) for n joins (e.g., 8! = 40320)

Selinger-Style Optimizer



- Recursion:
 - B*({t1, t2, t3})= min(B*({t1, t2} ⋈ t3), B*({t1, t3} ⋈ t2), B*({t2, t3} ⋈ t1))
- Sub-optimality:
 - If B*({t1, t2}) = B(t1 ⋈ t2) <= B(t2 ⋈ t1)
 - Then $B^*(\{t1, t2\} \bowtie t3) = B(t1 \bowtie t2 \bowtie t3) <= B(t2 \bowtie t1 \bowtie t3)$
- We can use dynamic programming to avoid repeating computations

Selinger Optimizer Example (1/3)

- Consider 3 relations to join: X, Y, Z
- Step 1: compute the B(t) of each table t
 - with proper selection ops

1-Set	Best Plan	R
{X}	Index Select Plan	10
{Y}	Table Plan	30
{Z}	Select Plan	20

Selinger Optimizer Example (2/3)

- Step 2: compute the cost of 2-way join
 - Estimate all left-deep permutation using the singlerelation cost just cached

• B({X} ⋈ Y): 159



• B({Y} ⋈ X): 189

Because the $R(X \bowtie Y)$, $R(Y \bowtie X)$ is the same, we can only keep one in K-set

1-Set	Best Plan	Cost
{X}	Index Select Plan	10
{Y}	Table Plan	30
{Z}	Select Plan	20

2-Set	Best Plan	Cost
{X, Y}	X⋈Y	159
{X, Z}	$Z\bowtie X$	98
{Y, Z}	Z⋈Y	77

Selinger Optimizer Example (3/3)

- Step 3: compute the cost of 3-way join
 - Estimate all left-deep tree permutation using the 2set costs
- E.g. {X, Y, Z} =
 - B({X, Y} ⋈ Z)=259
 - B({X, Z} ⋈ Y)=100



2-Set	Besi Plan	Cost
{X, Y}	X ⋈ Y	159
{X, Z}	Z I⋈ X	98
{Y, Z}	Z⋈Y	77

3-Set	Best Plan	Cost
{X, Y, Z}	$Z \bowtie X \bowtie Y$	100

Complexity (Simplified)

$$\begin{pmatrix} n \\ 1 \end{pmatrix} + \begin{pmatrix} n \\ 2 \end{pmatrix} + \dots + \begin{pmatrix} n \\ n \end{pmatrix} = O(2^n)$$

- E.g., when n=8:
- Exhaustively search: 8! = 40320 candidates
- Selinger-style planner: 2⁸=256 candidates

SelingerLikeQueryPlanner in VanillaCore

Package: org.vanilladb.core.query.planner.opt

```
private Plan getAllCombination(Plan viewTrunk) {
       long finalKev = 0:
       // for layer = 1, use select down strategy to construct
       for (TablePlanner tp: tablePlanners) {
               Plan bestPlan = null;
               if (viewTrunk != null) {
                       bestPlan = tp.makeJoinPlan(viewTrunk);
                       if (bestPlan == null)
                       bestPlan = tp.makeProductPlan(viewTrunk);
               else
                  bestPlan = tp.makeSelectPlan();
               AccessPath ap = new AccessPath(tp, bestPlan);
               lookupTbl.put(ap.getAPId(), ap);
               // compute final access path id
               finalKey += ap.getAPId();
```

```
// construct all combination layer by layer
for (int layer = 2; layer <= tablePlanners.size(); layer++) {
       Set<Long> keySet = new HashSet<Long>(lookupTbl.keySet());
       for (TablePlanner rightOne: tablePlanners) {
               for (Long key: keySet) {
                       AccessPath leftTrunk = lookupTbl.get(key);
                       // cannot join with table which (layer-1) combination already included
                       if (leftTrunk.isUsed(rightOne.getId()))
                          continue:
                       // do join
                       Plan bestPlan = rightOne.makeJoinPlan(leftTrunk.getPlan());
                       if (bestPlan == null)
                          bestPlan = rightOne.makeProductPlan(leftTrunk.getPlan());
                       AccessPath candidate = new AccessPath(leftTrunk, rightOne, bestPlan);
                       AccessPath ap = lookupTbl.get(candidate.getAPId());
                       // there is no access path contains this combination
                       if (ap == null) {
                          lookupTbl.put(candidate.getAPId(), candidate);
                       // check whether new access path is better than previous
                       else {
                               if (candidate.getCost() < ap.getCost())
                                  lookupTbl.put(candidate.getAPId(), candidate);
       // remove the elements belong to layer-1
       // because in the next layer we only need this layer's combination
```

```
    Iterate all table planners to join with all existing
(layer-1) combination to construct this layer
```

lookupTbl.remove(key);

for (Long key: keySet)

```
public class AccessPath {
       private Plan p;
       private AccessPathId apId;
       private long cost = 0;
       private ArrayList<Integer> tblUsed = new ArrayList<Integer>();
        public class AccessPathId {
               long id;
               AccessPathId(TablePlanner tp) {
                  this.id = (long) Math.pow(2,tp.getId());
               AccessPathId(AccessPath ap, TablePlanner tp) {
                  this.id = ap.getAPId()+(long) Math.pow(2,tp.getId());
               public long getID() {
                  return id:
       public AccessPath (TablePlanner newTp, Plan p) {
               this p = p:
```

- apID is the key of the lookup table
- Use sum of pow(2, tp.id) to represent the k-set in an access path

```
this.p = p;
this.tblUsed.add(newTp.getId());
this.apId = new AccessPathId(newTp);
this.cost = p.recordsOutput();

public AccessPath (AccessPath preAp, TablePlanner newTp, Plan p) {
this.p = p;
this.tblUsed.addAll(preAp.getTblUsed());
this.tblUsed.add(newTp.getId());
this.apId = new AccessPathId(preAp, newTp);

// approximate cost = previous cost + new cost
this.cost = preAp.getCost() + p.recordsOutput();
}
```

 Approximate B(root) using R(p1) + R(c1)...

Reference

- https://db.inf.unituebingen.de/staticfiles/teaching/ws1011/db2/db2 -selectivity.pdf
- https://www.cise.ufl.edu/~adobra/approxqp/histo grams2
- https://pdfs.semanticscholar.org/b024/0a44105fa0 a0967d96d109aac9f021902ebb.pdf