(2) 
$$H_2 + Br_2 \rightarrow 2HBr$$

(2) H<sub>2</sub> + Br<sub>2</sub> 
$$\rightarrow$$
 2HBr Rate law: -r<sub>HBr</sub> =  $\frac{k_1 C_{H_2} C_{Br_2}^{1/2}}{k_2 + \frac{C_{HBr}}{C_{Br_2}}}$ 

(3) 
$$H_2 + I_2 \rightarrow 2HI$$

Rate law: 
$$-r_{H_2} = kC_{H_2}C_{I_2}$$

# P3-11 (a)

Liquid phase reaction,

O 
$$CH_2$$
--OH

CH<sub>2</sub>--OH

CH<sub>2</sub>- CH<sub>2</sub> + H<sub>2</sub>O  $\rightarrow$  CH<sub>2</sub>--OH

A + B  $\rightarrow$  C

 $C_{AO} = 1 \text{ lbmol/ft}^3$ 
 $C_{BO} = 3.47 \text{ lbmol/ft}^3$ 

#### Stoichiometric Table:

Species	Symbol	Initial	Change	Remaining
Ethylene oxide	A	C <sub>AO</sub> =1 lbmol/ft <sup>3</sup>	- C <sub>AO</sub> X	$C_A = C_{AO}(1-X)$ = (1-X) lbmol/ft <sup>3</sup>
Water	В	$C_{BO}$ = 3.47 lbmol/ft <sup>3</sup> , $\theta_B$ = 3.47	-C <sub>AO</sub> X	$C_B = C_{AO}(\theta_B - X)$ =(3.47-X) lbmol/ft <sup>3</sup>
Glycol	С	0	C <sub>AO</sub> X	$C_C = C_{AO}X$ = $X \text{ lbmol/ft}^3$

Rate law:

$$-r_A = kC_AC_B$$

Therefore,

$$-r_A = k C_{AO}^2 (1-X)(\theta_B - X) = k(1-X)(3.47-X)$$

At 300K

$$E = 12500 \text{ cal/mol}, X = 0.9,$$

$$X = 0.9$$

 $k = 0.1 \text{dm}^3/\text{mol.s} = \frac{0.1}{1000} \times 35.315 \text{ ft}^3 / \text{lbmol.s} = 0.0035 \text{ ft}^3 / \text{lbmol.s}$ 

$$\tau_{CSTR} = \frac{C_{AO}X}{-r_A} = \frac{(1)(0.9)}{(0.0035)(1)^2(1-0.9)(3.47-0.9)} = 1000.56 \text{ s}^{-1}$$

 $k_2 = k \exp((E/R)(1/T-1/T_2)) = 0.0035 \exp((12500/1.987)(1/T-1/T_2)) = 0.071 \text{ dm}^3/\text{mol.s}$ 

$$\tau_{CSTR} = \frac{C_{AO}X}{-r_A} = \frac{(1)(0.9)}{(0.071)(1)^2(1-0.9)(3.47-0.9)} = 49.3s^{-1}$$

# P3-11 (b)

Isothermal, isobaric gas-phase pyrolysis,

$$C_2H_6$$
  $C_2H_4 + H_2$   
 $A \rightarrow B + C$ 

Stoichiometric table:

Species	symbol	Entering	Change	Leaving
$C_2H_6$	A	FAO	-F <sub>AO</sub> X	$F_A=F_{AO}(1-X)$

C <sub>2</sub> H <sub>4</sub>	В	0	+F <sub>AO</sub> X	F <sub>B</sub> =F <sub>AO</sub> X
H <sub>2</sub>	C	0	+F <sub>AO</sub> X	F <sub>C</sub> =F <sub>AO</sub> X
		F <sub>TO</sub> =F <sub>AO</sub>		$F_T = F_{AO}(1+X)$

$$\mathcal{E} = y_{ao} \, \delta = 1(1+1-1) = 1$$

$$v = v_{o}(1+\mathcal{E}X) \qquad \Rightarrow v = v_{o}(1+X)$$

$$C_{AO} = y_{AO} \, C_{TO} = y_{AO} \, \frac{P}{RT}$$

$$= \frac{(1)(6atm)}{\left(0.082 \frac{m^{3} atm}{K.kmol}\right) (1100K)} = 0.067 \text{ kmol/m}^{3} = 0.067 \text{ mol/dm}^{3}$$

$$C_{A} = \frac{F_{A}}{v} = \frac{F_{AO}(1-X)}{v_{O}(1+X)} = C_{AO} \, \frac{(1-X)}{(1+X)} \text{ mol/dm}^{3}$$

$$C_{B} = \frac{F_{B}}{v} = \frac{F_{AO}(X)}{v_{O}(1+X)} = C_{AO} \, \frac{X}{(1+X)} \text{ mol/dm}^{3}$$

$$C_{C} = \frac{F_{C}}{v} = \frac{F_{AO}(X)}{v_{O}(1+X)} = C_{AO} \, \frac{X}{(1+X)} \text{ mol/dm}^{3}$$

Rate law:

$$-r_A = kC_A$$
  $= kC_{AO} \frac{(1-X)}{(1+X)} = 0.067 k \frac{(1-X)}{(1+X)}$ 

If the reaction is carried out in a constant volume batch reactor, =>(  $\mathcal{E}=0$ )  $C_A = C_{AO}(1-X) \text{ mol/dm}^3$   $C_B = C_{AO} \text{ X mol/dm}^3$   $C_C = C_{AO} \text{ X mol/dm}^3$ 

# P3-11 (c)

Isothermal, isobaric, catalytic gas phase oxidation,

$$C_2H_4 + \frac{1}{2}O_2 \rightarrow C_2H_4O$$

$$A + \frac{1}{2}B \rightarrow C$$

Stoichiometric table:

Species	Symbol	Entering	Change	Leaving
$C_2H_4$	A	F <sub>AO</sub>	-F <sub>AO</sub> X	$F_A=F_{AO}(1-X)$
O <sub>2</sub>	В	F <sub>BO</sub>		$F_B=F_{AO}(\theta_B-X)$
C <sub>2</sub> H <sub>4</sub> O	С	0	+F <sub>AO</sub> X	F <sub>C</sub> =F <sub>AO</sub> X

$$\theta_{B} = \frac{F_{BO}}{F_{AO}} = \frac{\frac{1}{2}F_{AO}}{F_{AO}} = \frac{1}{2} \qquad y_{AO} = \frac{F_{AO}}{F_{TO}} = \frac{F_{AO}}{F_{AO} + F_{BO}} = \frac{2}{3}$$

$$\varepsilon = y_{AO}\delta = \frac{2}{3}\left(1 - \frac{1}{2} - 1\right) = 0.33$$

$$C_{AO} = y_{AO}C_{TO} = y_{AO} \frac{P}{RT} = \frac{2}{3} \frac{(6atm)}{(0.082 \frac{atm.dm^3}{mol.K})} (533K) = 0.092 \frac{mol}{dm^3}$$

$$C_A = \frac{F_A}{v} = \frac{F_{AO}(1-X)}{v_O(1+\varepsilon X)} = \frac{C_{AO}(1-X)}{(1-0.33X)} = \frac{0.092(1-X)}{(1-0.33X)}$$

$$C_B = \frac{F_B}{v} = \frac{F_{AO}\left(\theta_B - \frac{X}{2}\right)}{v_O(1+\varepsilon X)} = \frac{0.046(1-X)}{(1-0.33X)}$$

$$C_C = \frac{F_C}{v} = \frac{F_{AO}X}{v_O(1+\varepsilon X)} = \frac{0.092(X)}{(1-0.33X)}$$

If the reaction follow elementary rate law

Rate law: 
$$-r_A = kC_A C_B^{0.5}$$
  $\Rightarrow -r_A = k \left\{ \frac{0.092(1-X)}{(1-0.33X)} \right\} \left\{ \frac{0.046(1-X)}{(1-0.33X)} \right\}^{0.5}$ 

## P3-11 (d)

Isothermal, isobaric, catalytic gas phase reaction in a PBR

$$C_6H_6 + 2H_2 \rightarrow C_6H_{10}$$
  
A + 2B  $\rightarrow$  C

Stoichiometric table:

Species	Symbol	Entering	Change	Leaving
Benzene	A	FAO	-F <sub>AO</sub> X	$F_A=F_{AO}(1-X)$
$H_2$	В	F <sub>BO</sub> =2F <sub>AO</sub>	-2F <sub>AO</sub> X	$F_B=F_{AO}(\theta_B-2X)$
C <sub>6</sub> H <sub>10</sub>	С	0	F <sub>AO</sub> X	F <sub>C</sub> =F <sub>AO</sub> X

$$\theta_{B} = \frac{F_{BO}}{F_{AO}} = \frac{2F_{AO}}{F_{AO}} = 2$$

$$y_{AO} = \frac{F_{AO}}{F_{TO}} = \frac{F_{AO}}{F_{AO} + F_{BO}} = \frac{1}{3}$$

$$\varepsilon = y_{AO}\delta = \frac{1}{3}(1 - 2 - 1) = -\frac{2}{3}$$

$$C_{AO} = C_{TO}y_{AO} = \frac{P}{RT}\left(\frac{1}{3}\right) = \frac{6atm}{\left(0.082\frac{atm.dm^{3}}{mol.K}\right)(443.2K)}\left(\frac{1}{3}\right) = 0.055mol/dm^{3}$$

$$C_{A} = \frac{F_{A}}{v} = \frac{F_{AO}(1 - X)}{v_{O}(1 + \varepsilon X)} = \frac{C_{AO}(1 - X)}{\left(1 - \frac{2}{3}X\right)} = \frac{0.055(1 - X)}{\left(1 - \frac{2}{3}X\right)}$$

$$C_{B} = \frac{F_{B}}{v} = \frac{F_{AO}(\theta_{B} - 2X)}{v_{O}(1 + \varepsilon X)} = \frac{0.11(1 - X)}{\left(1 - \frac{2}{3}X\right)}$$

$$C_{C} = \frac{F_{C}}{v} = \frac{F_{AO}X}{v_{O}(1 + \varepsilon X)} = \frac{C_{AO}X}{\left(1 - \frac{2}{3}X\right)} = \frac{0.055X}{\left(1 - \frac{2}{3}X\right)}$$

If the reaction follow elementary rate law.

$$-r_A' = kC_A C_B^2$$

$$-r_{A}' = 0.0007k \frac{\left(1 - X\right)^{3}}{\left(1 - \frac{2}{3}X\right)^{3}}$$

For a fluidized CSTR:

$$W = \frac{F_{A0}X}{-r_A}$$

$$W = \frac{F_{A0}X}{0.0007k \frac{(1-X)^3}{\left(1-\frac{2}{3}X\right)^3}}$$

$$k = 53 \frac{mol}{kgcat \min atm^3}$$
 at 300K

$$k = k_1 \exp\left(\frac{E}{R}\left(\frac{1}{T_1} - \frac{1}{T}\right)\right) = 53 \exp\left(\frac{80000}{8.314}\left(\frac{1}{300} - \frac{1}{443}\right)\right) = 1663000 \frac{mol}{kgcat \min atm^3}$$

$$F_{A0} = C_{A0} * v_0$$
  
 $v_0 = 5 \text{ dm}^3/\text{min}$ 

$$W = \frac{C_{A0}v_0X}{0.0007k\frac{(1-X)^3}{\left(1-\frac{2}{3}X\right)^3}}$$

at 
$$X = 0.8$$

W = 0.0024 kg of catalyst

## P3-15 (a)

Isothermal gas phase reaction.

$$\frac{1}{2}N_2 + \frac{3}{2}H_2 \rightarrow NH_3$$

Making H2 as the basis of calculation:

$$H_2 + \frac{1}{3}N_2 \rightarrow \frac{2}{3}NH_3$$

$$A + \frac{1}{3}B \rightarrow \frac{2}{3}C$$

Stoichiometric table:

Species	Symbol	Initial	change	Leaving
H <sub>2</sub>	A	F <sub>AO</sub>	-F <sub>AO</sub> X	$F_A=F_{AO}(1-X)$
N <sub>2</sub>	В	$F_{BO} = \theta_B F_{AO}$	-F <sub>AO</sub> X/3	$F_B=F_{AO}(\theta_B-X/3)$
NH <sub>3</sub>	C	0	+2F <sub>AO</sub> X/3	$F_{C}=(2/3)F_{AO}X$

# P3-15 (b)

$$\delta = \left(\frac{2}{3} - \frac{1}{3} - 1\right) = -\frac{2}{3}$$

$$\varepsilon = y_{AO}\delta = 0.5 \times \left(-\frac{2}{3}\right) = -\frac{1}{3}$$

$$C_{AO} = 0.5 \frac{(16.4atm)}{\left(0.082 \frac{atm.dm^3}{mol.K}\right) (500K)} = 0.2 \text{ mol/dm}^3$$

$$C_{H_2} = C_A = \frac{C_{AO}(1-X)}{(1+\varepsilon X)} = \frac{0.2(1-X)}{(1-\frac{X}{3})} = 0.1 \text{mol/dm}^3$$

$$C_{NH_3} = C_C = \frac{2}{3} \times \frac{C_{AO}(1-X)}{(1+\varepsilon X)} = \frac{2}{3} \times \frac{0.2(X)}{(1-\frac{X}{3})} = 0.1 \text{mol/dm}^3$$

# P3-15 (c)

 $k_{N2} = 40 \text{ dm}^3/\text{mol.s}$ 

(1) For Flow system:

$$-r_{N_{2}} = k_{N_{2}} \left[ C_{N_{2}} \right]^{\frac{1}{2}} \left[ C_{H_{2}} \right]^{\frac{3}{2}}$$

$$= 40 \left( C_{AO} \right)^{2} \left[ \frac{\left( 1 - \frac{X}{3} \right)}{\left( 1 - \frac{X}{3} \right)} \right]^{\frac{1}{2}} \left[ \frac{\left( 1 - X \right)}{\left( 1 - \frac{X}{3} \right)} \right]^{\frac{3}{2}}$$

$$-r_{N_{2}} = 8.3 \left[ \frac{\left( 1 - X \right)}{\left( 1 - \frac{X}{3} \right)} \right]^{\frac{3}{2}}$$



(2) For batch system, constant volume.

$$-r_{N_2} = k_{N_2} \left[ C_{N_2} \right]^{\frac{1}{2}} \left[ C_{H_2} \right]^{\frac{3}{2}}$$

$$= 40 \left( C_{AO} \right)^2 \left[ \left( 1 - \frac{X}{3} \right) \right]^{\frac{1}{2}} \left[ \left( 1 - X \right) \right]^{\frac{3}{2}}$$

$$-r_{N_2} = 1.6 \left[ 1 - \frac{X}{3} \right]^{\frac{1}{2}} \left[ 1 - X \right]^{\frac{3}{2}}$$











Edit

Annotate

Fill & Sign

Convert

ΑII

Let A = ONCB $B = NH_3$  C = Nibroanaline D = Ammonium Chloride

$$A + 2B \longrightarrow C + D$$

$$-r_A = kC_A C_B$$

3-14



P3-13 (b)

Species	Entering	Change	Leaving
A	F <sub>A0</sub>	- F <sub>A0</sub> X	F <sub>A0</sub> (1-X)
В	$F_{B0} = \Theta_B F_{A0}$ =6.6/1.8 $F_{A0}$	-2 F <sub>A0</sub> X	$F_B = F_{A0}(\Theta_B - 2X)$
С	0	F <sub>A0</sub> X	$F_C = F_{A0}X$
D	0	F <sub>A0</sub> X	$F_D = F_{A0}X$

### P3-13 (c)

For batch system, C<sub>A</sub>=N<sub>A</sub>/V

$$-r_A = kN_AN_B/V^2$$

### P3-13 (d)

$$-r_A = kC_AC_B$$

$$F_{A} = \frac{N_{A}}{V} = \frac{N_{A}}{V_{0}} = \frac{N_{A0}}{V_{0}} (1 - X) = C_{A0} (1 - X), \quad C_{A} = \frac{F_{A}}{V} = \frac{F_{A}}{V_{0}} = C_{A0} (1 - X)$$

$$F_{A} = \frac{N_{B}}{V_{0}} = \frac{N_{A}}{V_{0}} = \frac{N_{A0}}{V_{0}} (1 - X) = C_{A0} (1 - X), \quad C_{A} = \frac{F_{A}}{V_{0}} = \frac{F_{A}}{V_{0}} = C_{A0} (1 - X)$$

$$F_{B} = \frac{N_{B}}{V} = \frac{N_{B}}{V_{0}} = \frac{N_{A0}}{V_{0}} (\theta_{B} - 2X) = C_{A0} (\theta_{B} - 2X), \quad C_{B} = \frac{F_{B}}{V_{0}} = C_{A0} (\theta_{B} - 2X)$$

$$-r_A = kC_{A0}^2 \left(1 - X\right) \left(\theta_B - 2X\right)$$

$$\theta_B = \frac{C_{B0}}{C_{A0}} = \frac{6.6}{1.8} = 3.67$$

$$C_{A0} = 1.8 \frac{kmol}{m^3}$$

$$-r_A = k(1.8)^2 (1-X)(3.67-2X)$$

#### P3-13 (e)

1) At X = 0 and T = 188°C = 461 K

$$-r_{A0} = kC_{A0}^2 \theta_B = k_A C_{A0} C_{B0} = 0.0017 \frac{m^3}{kmol \min} \left( 1.8 \frac{kmol}{m^3} \right) \left( 6.6 \frac{kmol}{m^3} \right)$$

$$-r_{A0} = 0.0202 \frac{\text{kmol}}{\text{m}^3 \text{ min}}$$

2) At 
$$X = 0$$
 and  $T = 25C = 298K$ 

$$k = k_{o} \exp\left(\frac{E}{R}\left(\frac{1}{T_{o}} + \frac{1}{T}\right)\right)$$

$$k = 0.0017 \frac{m^{3}}{kmol.\min} \exp\left(\frac{11273 \frac{cal}{mol}}{1.987 \frac{cal}{mol.k}}\left(\frac{1}{461} + \frac{1}{298}\right)\right)$$

$$= 2.12 \times 10^{-6} \frac{m3}{kmol.\min}$$

$$-\tau_{AO} = kC_{AO}C_{BO} = 2.52 \times 10^{-5} \text{ kmol/m}^{3} \text{min}$$
3)
$$k = k_{0} \exp\left[\frac{E}{R}\left(\frac{1}{T_{0}} - \frac{1}{T}\right)\right]$$

$$k = 0.0017 \frac{m^{3}}{kmol \min} \exp\left[\frac{11273 \frac{cal}{mol}}{1.987 \frac{cal}{mol}}\left(\frac{1}{461K} - \frac{1}{561K}\right)\right]$$

$$k = 0.0152 \frac{m^{3}}{kmol \min}$$

$$-r_{AO} = kC_{AO}C_{BO}$$

$$-r_{A} = 0.0152 \frac{m^{3}}{kmol \min}\left(1.8 \frac{kmol}{m^{3}}\right)\left(6.6 \frac{kmol}{m^{3}}\right)$$

### P3-13 (f)

$$r_A = kC_{AO}^2(1-X)(\theta_B-2X)$$

 $-r_A = 0.1806 \frac{\text{kmol}}{\text{m}^3 \text{ min}}$ 

At X = 0.90 and T = 188C = 461K

1) at 
$$t = 188 C$$

$$-r_A = \left(0.0017 \frac{m^3}{kmol.\min}\right) \left(1.8 \frac{kmol}{m^3}\right)^2 \left(1 - 0.9\right) \left(3.67 - 2(0.9)\right)$$
$$= 0.00103 \frac{kmol}{m^3 \min}$$

At 
$$X = 0.90$$
 and  $T = 25C = 298K$ 



$$-r_{A} = \left(2.12 \times 10^{-6} \frac{m^{3}}{kmol. \min}\right) \left(1.8 \frac{kmol}{m^{3}}\right)^{2} (1-0.9)(3.67-2(0.9))$$

$$= 1.28 \times 10^{-6} \frac{kmol}{m^{3} \min}$$
3)
At X = 0.90 and T = 288C = 561K
$$-r_{A} = \left(0.0152 \frac{m^{3}}{kmol. \min}\right) \left(1.8 \frac{kmol}{m^{3}}\right)^{2} (1-0.9)(3.67-2(0.9))$$

$$= 0.00333 \frac{kmol}{m^{3} \min}$$
P3-13 (g)
$$v_{o} = 2m^{3}/\min = 0.002m^{3}/\min$$
1)For CSTR at 25C 
$$-r_{A} = 1.28 \times 10^{-6} \frac{kmol}{m^{3} \min}$$

$$V = \frac{v_{o}C_{AO}(1-X)}{-r_{A:X=0.9}}$$

$$= \frac{0.002m^{3}/\min \times 1.8kmol/m^{3} \times 0.1}{1.28 \times 10^{-6} \frac{kmol}{m^{3} \min}} = 281.25m^{3}$$
2)At 288C, 
$$-r_{A} = 0.00333 \frac{kmol}{m^{3} \min}$$

$$V = \frac{v_{o}C_{AO}(1-X)}{-r_{A:X=0.9}}$$

$$V = \frac{0.002m^{3}/\min \times 1.8kmol/m^{3} \times 0.1}{0.00333 \frac{kmol}{m^{3} \min}} = 0.108m^{3}$$