

```

56 // Monotone chain Algorithm O(n log(n))
57 struct pt {
58     double x, y;
59 };
60
61 int orientation(pt a, pt b, pt c) {
62     double v = a.x*(b.y-c.y)+b.x*(c.y-a.y)+c.x*(a.y-b.y);
63     if (v < 0) return -1; // clockwise
64     if (v > 0) return +1; // counter-clockwise
65     return 0;
66 }
67
68 bool cw(pt a, pt b, pt c, bool include_collinear) {
69     int o = orientation(a, b, c);
70     return o < 0 || (include_collinear && o == 0);
71 }
72 bool ccw(pt a, pt b, pt c, bool include_collinear) {
73     int o = orientation(a, b, c);
74     return o > 0 || (include_collinear && o == 0);
75 }
76
77 void convex_hull(vector<pt>& a, bool include_collinear = false) {
78     if (a.size() == 1)
79         return;
80
81     sort(a.begin(), a.end(), [](pt a, pt b) {
82         return make_pair(a.x, a.y) < make_pair(b.x, b.y);
83     });
84     pt p1 = a[0], p2 = a.back();
85     vector<pt> up, down;
86     up.push_back(p1);
87     down.push_back(p1);
88     for (int i = 1; i < (int)a.size(); i++) {
89         if (i == a.size() - 1 || cw(p1, a[i], p2, include_collinear)) {
90             while (up.size() ≥ 2 && !cw(up[up.size()-2], up[up.size()-1], a[i],
include_collinear))
91                 up.pop_back();
92             up.push_back(a[i]);
93         }
94         if (i == a.size() - 1 || ccw(p1, a[i], p2, include_collinear)) {
95             while (down.size() ≥ 2 && !ccw(down[down.size()-2],
down[down.size()-1], a[i], include_collinear))
96                 down.pop_back();
97             down.push_back(a[i]);
98         }
99     }
100
101     if (include_collinear && up.size() == a.size()) {
102         reverse(a.begin(), a.end());
103         return;
104     }
105     a.clear();
106     for (int i = 0; i < (int)up.size(); i++)
107         a.push_back(up[i]);
108     for (int i = down.size() - 2; i > 0; i--)
109         a.push_back(down[i]);
110 }

```