

```

1  #include <bits/stdc++.h>
2  using namespace std;
3  #define ll long long
4
5  #define left p<<1 , l , (l+r)>>1
6  #define right p<<1|1 , ((l+r)>>1)+1 , r
7
8  LCA by segment tree complexity  $O(\log(n))$ :
9  struct LCA{
10     vector<int> first , occur , depth , seg;
11     vector<vector<int>> adj;
12
13     LCA(vector<vector<int>> adj , int n , int root){
14         this->adj = adj;
15         depth.assign(n+1 , 0);
16         first.assign(n+1 , 0);
17         occur.reserve(n*2);
18         dfs(root , 0);
19         seg.assign((occur.size()*4)+100 , 0);
20         build(1 , 0 , occur.size()-1);
21     }
22
23     void dfs(int u , int parent , int d = 0){
24         depth[u] = d;
25         first[u] = occur.size();
26         occur.push_back(u);
27         for(auto v : adj[u])
28             if(v!=parent){
29                 dfs(v , u , d+1);
30                 occur.push_back(u);
31             }
32     }
33
34     int build(int p , int l , int r){
35         if(l==r) return seg[p] = occur[l];
36         int c1 = build(left) , c2 = build(right);
37         if(depth[c1] < depth[c2]) seg[p] = c1; else seg[p] = c2;
38         return seg[p];
39     }
40
41     int query(int u , int v){
42         int l = first[u] , r = first[v];
43         if(l > r) swap(l , r);
44         return query(l , r , 1 , 0 , occur.size()-1);
45     }
46
47     int query (int i , int j , int p , int l , int r){
48         if(j<l || r<i) return -1;
49         if(i<=l && r<=j) return seg[p];
50         int c1 = query(i , j , left) , c2 = query(i , j , right);
51         if(c1==-1) return c2; if(c2==-1) return c1;
52         return depth[c1] < depth[c2] ? c1 : c2;
53     }
54 };

```