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1  #include <bits/stdc++.h>
2  using namespace std;
3  #define ll long long
4
5  Useful defines:
6  #define LCM(x , y) (x*y/__gcd(x , y))
7  #define GCD(x , y) (__gcd(x , y))
8
9  GCD Applications:
10
11 //1. Euclid's: if we want the gcd of (a , b) and we can write a/b=c , a%b=d
12 // then GCD(a , b)=GCD(b , d) and the O(max(a , b));
13 int GCD(int a , int b){
14     if(b==0) return a;
15     else return GCD(b , a%b);
16 }
17
18 //2. GCD function with O(min(a , b)):
19 int GCD(int a , int b){
20     int mini = min(a , b) , ans;
21     for (int i = mini; i > 0; i--)
22     {
23         if(a%i==0 && b%i==0){
24             ans = i;
25             return ans;
26         }
27     }
28 }
29
30 //3. GCD rules:
31 // - GCD(m*a , m*b) = m * GCD(a , b)
32 // - GCD(a/m , b/m) = GCD(a , b) / m
33 // - GCD(a , b) * LCM(a , b) = a*b
34 // - GCD(0 , 0) = LCM(0 , 0) = 0
35 // - GCD(a , b , c) = GCD(a , GCD(b , c))
36 // - GCD(a , m) = 1  $\implies$  GCD(m , a*b) = GCD(m , b)
37 // - GCD(a , b) = d  $\implies$  GCD(a/d , b/d) = 1
38 // - GCD(a , b) = GCD(b , a%b)
39 // - GCD(a , a+1) = 1
40
41 //4. find three distinct positive integers a , b , c such that
42 // a+b+c=n and GCD(a , b) = c
43 void solution(){
44     int n; cin>>n;
45     if(n%2==0) cout<<n-3<<" "<<2<<" "<<1<<endl;
46     else{
47         for (int i = 2; i < n/2; i++)
48         {
49             if(__gcd(n-i-1 , i)==1){
50                 cout<<n-i-1<<" "<<i<<" "<<1<<endl;
51                 break;
52             }
53         }
54     }
55 }
56
57 //5. coPrime rules:
58 // - sum of any two coPrime number is coPrime with their product
59 // - factoring of two coPrime number is common only in number 1
60 // - if factor of a[i] = p1 * p2 * p3 then p1*p2 + p3 is coPrime with a[i]

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