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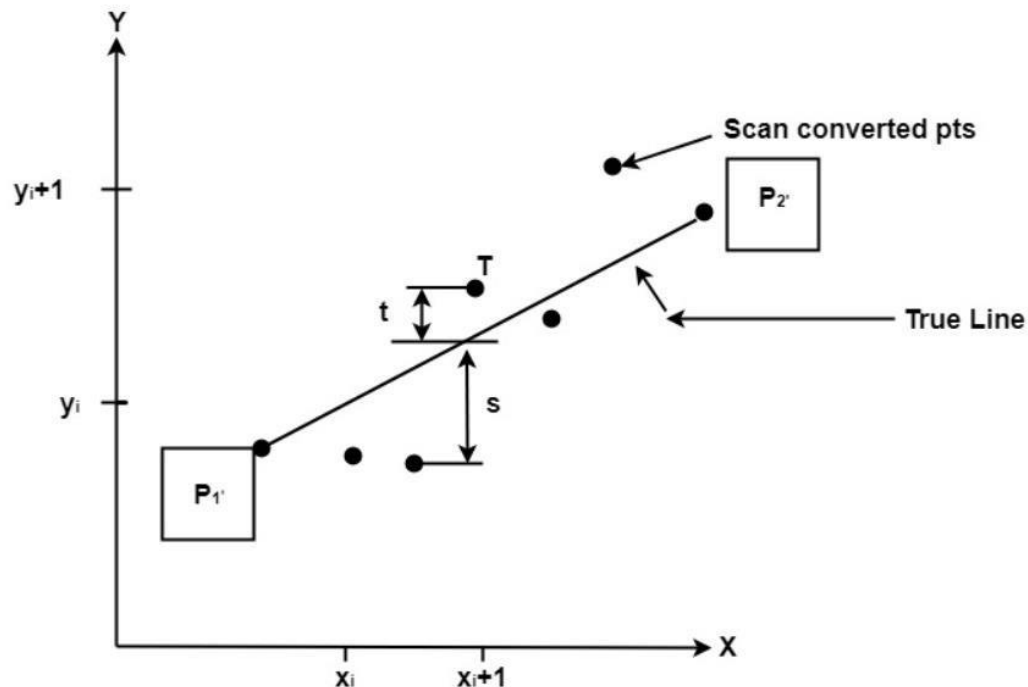
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1. Write a program to implement Bresenham's line drawing algorithm.

1.1. Explanation

Bresenham's line algorithm is used for scan converting a line. It was developed by Bresenham. It is an efficient method because it involves only integer addition, subtractions, and multiplication operations. These operations can be performed very rapidly so lines can be generated quickly.

In this method, next pixel selected is that one who has the least distance from true line. The method works as follows: Assume a pixel $P_1'(x_1', y_1')$, then select subsequent pixels as we work our way to the right, one pixel position at a time in the horizontal direction toward $P_2'(x_2', y_2')$. Once a pixel is chosen at any step, the next pixel is 1. Either the one to its right (lower-bound for the line) 2. One top its right and up (upper-bound for the line) The line is best approximated by those pixels that fall the least distance from the path between P_1', P_2' .



1.2. Code

```
# Write a program to implement Bresenham's line drawing algorithm.
```

```
import matplotlib.pyplot as plt
```

```
def drawline(x1,x2,y1,y2):
```

```
    dy=y2-y1 dx=x2-
```

```
    x1 m=dy/dx x=[]
```

```
    y=[] p=(2*dy)-dx
```

```

xnext=x1
ynext=y1
x.append(xnext)
y.append(ynext)
while(xnext<x2 or
ynext<y2): if(m<1):
xnext=x1+1
    if(p<0):
        ynext=y1
        p=p+(2*dy)
    else:
        ynext=y1+1 p=p+(2*(dy-
        dx))
    else:
        ynext=y1+1
        if(p<0):
            xnext=x1
            p=p+(2*dx)
        else:
            xnext=x1+1 p=p+(2*(dx-
            dy))
x.append(xnext)
y.append(ynext)
x1=xnext
y1=ynext print("x
coordinates are :-
",x) print("y

```

coordinates are :-

",y) plt.plot(x,y)

X1=int(input("Enter X Coordinate of Starting point of line : "))

Y1=int(input("Enter Y Coordinate of Starting point of line : "))

X2=int(input("Enter X Coordinate of Ending point of line : "))

Y2=int(input("Enter Y Coordinate of Ending point of line : "))

drawline(X1,X2,Y1,Y2)

1.3. Output

```
Enter X Coordinate of Starting point of line : 20
Enter Y Coordinate of Starting point of line : 120
Enter X Coordinate of Ending point of line : 70
Enter Y Coordinate of Ending point of line : 160
x coordinates are :- [20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70]
y coordinates are :- [120, 121, 122, 122, 123, 124, 125, 126, 126, 127, 128, 129, 130, 130, 131, 132, 133, 134, 134, 135, 136, 137, 138, 138, 139, 140, 141, 142, 142, 143, 144, 145, 146, 146, 147, 148, 149, 150, 150, 151, 152, 153, 154, 154, 155, 156, 157, 158, 159, 160]
```

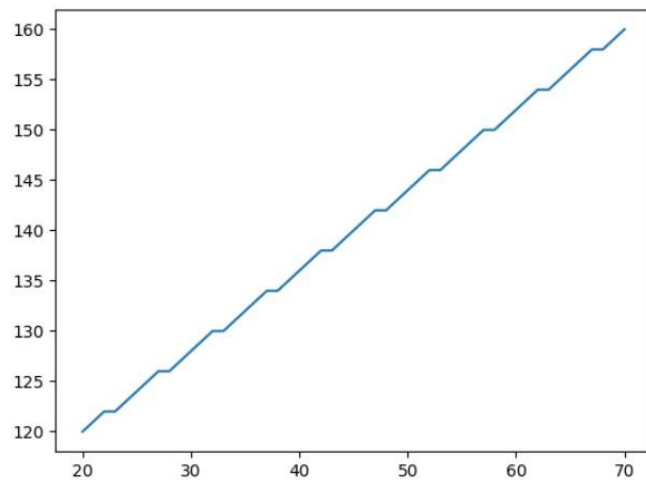
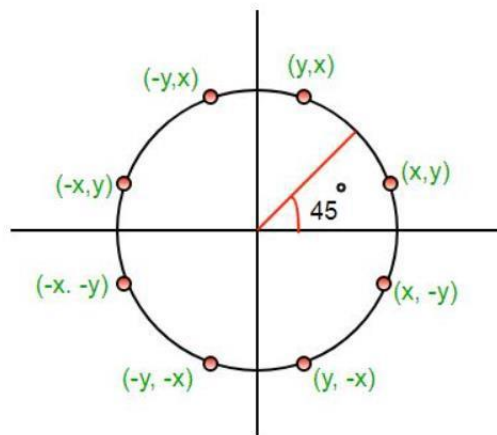


Figure 1. The output of Bresenham's line drawing algorithm

2. Write a program to implement mid-point circle drawing algorithm.

2.1. Explanation

The mid-point circle drawing algorithm is an algorithm used to determine the points needed for rasterizing a circle. We use the mid-point algorithm to calculate all the perimeter points of the circle in the first octant and then print them along with their mirror points in the other octants. This will work because a circle is symmetric about its centre. The algorithm is very similar to the Mid-Point Line Generation Algorithm. Here, only the boundary condition is different. For any given pixel (x, y) , the next pixel to be plotted is either $(x, y+1)$ or $(x-1, y+1)$. This can be decided by following the steps below. 1. Find the mid-point p of the two possible pixels i.e $(x-0.5, y+1)$ 2. If p lies inside or on the circle perimeter, we plot the pixel $(x, y+1)$, otherwise if it's outside we plot the pixel $(x-1, y+1)$



2.2. Code

Write a program to implement mid-point circle drawing algorithm.

```
from graphics import *
```

```
import time def
```

```
drawcircle(x0,y0,r):
```

```
    xi=0 yi=r
```

```
    xtemp=[]
```

```
    ytemp=[]
```

```
    p=3-(2*r)
```

```
    while(xi<=yi)
```

```
    :
```

```
        print("("xi,"",yi,"")")
```

```

xtemp.append(xi)
xtemp.append(yi)
ytemp.append(yi)
ytemp.append(xi)
xnext=xi+1 if(p<0):
    ynext=yi
    p=p+(4*xnext)+6
else:
    ynext=yi-1
p=p+(4*(xnext-ynext))+10
xi=xnext yi=ynext x1=xtemp
y1=ytemp x=[] y=[] for i in
xtemp:
    x.append(i)
    x.append(i)
    x.append(-i)
    x.append(-i)
for i in ytemp:
    y.append(i)
    y.append(-i)
    y.append(-i)
    y.append(i) win = GraphWin('Ques2: Mid Point Circle Drawing
Algorithm', 600, 480) for i in range(len(x)):

    pt =
    Point(x[i]+x0,y[i]+y0)
    pt.draw(win) time.sleep(10)
    win.close()

```

```
X0=int(input("Enter X coordinates of Center of Circle : "))
```

```
Y0=int(input("Enter Y coordinates of Center of Circle : "))
```

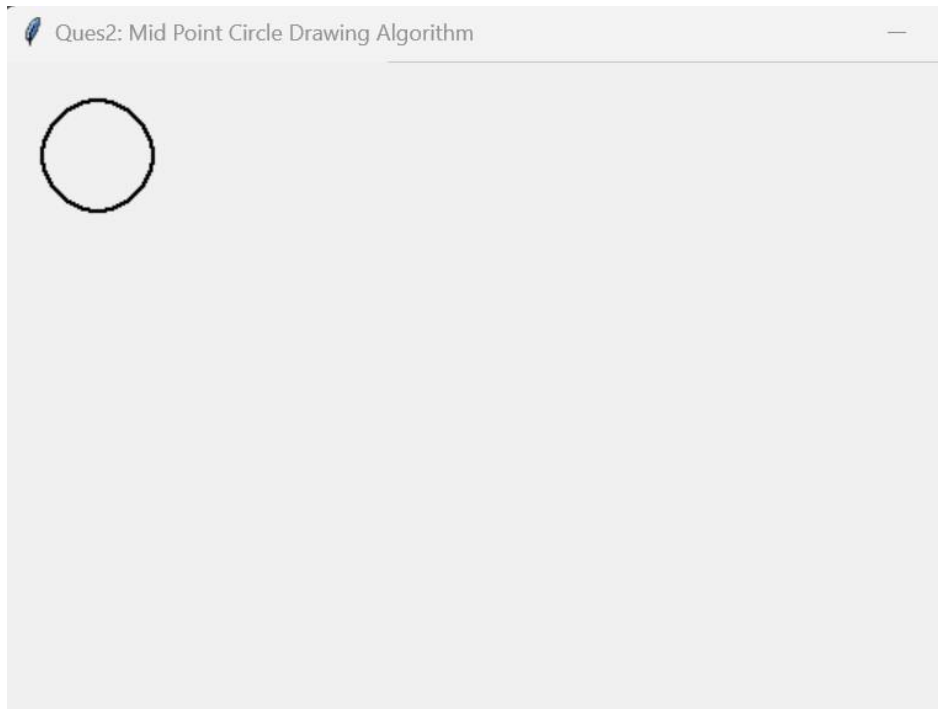
```
R=int(input("Enter Radius of Circle : "))
```

```
drawcircle(X0,Y0,R)
```

2.3. Output

```
Enter X coordinates of Center of Circle : 50
Enter Y coordinates of Center of Circle : 50
Enter Radius of Circle : 30
( 0 , 30 )
( 1 , 30 )
( 2 , 30 )
( 3 , 30 )
( 4 , 30 )
( 5 , 29 )
( 6 , 29 )
( 7 , 29 )
( 8 , 29 )
( 9 , 28 )
( 10 , 28 )
( 11 , 27 )
( 12 , 27 )
( 13 , 26 )
( 14 , 26 )
( 15 , 25 )
( 16 , 25 )
( 17 , 24 )
( 18 , 23 )
( 19 , 22 )
( 20 , 21 )
```

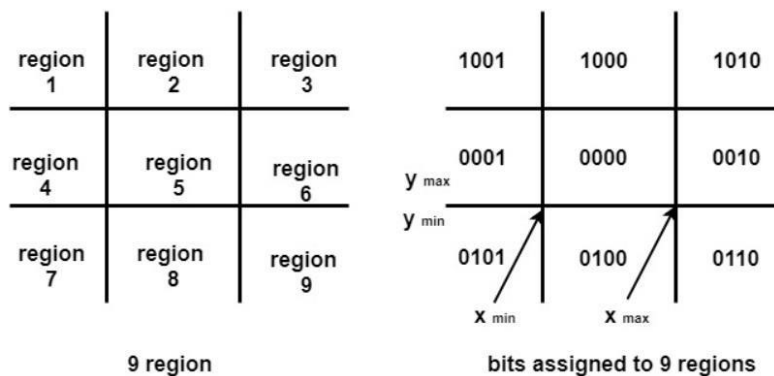
Figure 2. The output of Mid Point Circle Drawing algorithm.



3. Write a program to clip a line using Cohen and Sutherland line clipping algorithm.

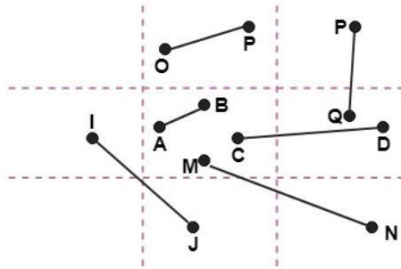
3.1. Explanation

In the algorithm, first of all, it is detected whether line lies inside the screen or it is outside the screen. All lines come under any one of the following categories: 1. Visible 2. Not Visible 3. Clipping Case 1. Visible: If a line lies within the window, i.e., both endpoints of the line lies within the window. A line is visible and will be displayed as it is. 2. Not Visible: If a line lies outside the window it will be invisible and rejected. Such lines will not display. If any one of the following inequalities is satisfied, then the line is considered invisible. 3. Clipping Case: If the line is neither visible case nor invisible case. It is considered to be clipped case. First of all, the category of a line is found based on nine regions given below. All nine regions are assigned codes. Each code is of 4 bits. If both endpoints of the line have end bits zero, then the line is considered to be visible.



The center area is having the code, 0000, i.e., region 5 is considered a rectangle window. Line AB is the visible case Line OP is an invisible case Line PQ is an invisible line Line IJ are clipping candidates Line MN are clipping candidate Line CD are clipping candidate

Following figure show lines of various types



3.2. Code

Write a program to clip a line using Cohen and Sutherland line clipping algorithm.

```
import matplotlib.pyplot as plt def
```

```
check_points(xmin,ymin,xmax,ymax,x1,y1):
```

```
    if(x1>=xmin and x1<=xmax):
```

```
        if(y1>=ymin and y1<=ymax):
```

```
            return True
```

```
        else: return
```

```
    False else:
```

```
    return False
```

```
def get_xy(xmin,ymin,xmax,ymax,x1,y1,x2,y2):
```

```
    xlist=[]
```

```
    ylist=[]
```

```
    m = (y2-y1)/(x2-x1)
```

```
    plt.ylim(ymin,ymax)
```

```
    plt.xlim(xmin,xmax)
```

```
    if(check_points(xmin,ymin,xmax,ymax,
```

```
    x1,y1) and
```

```

check_points(xmin,ymin,xmax,ymax,x2,y2):

    print(" Nothing to Clip : Line Lies in the Interaction Region")

    elif((not check_points(xmin,ymin,xmax,ymax,x1,y1)) and (not
check_points(xmin,ymin,xmax,ymax,x2,y2))):

        print(" Sorry but Line doesn't Lies in the Interaction Region")

else:

    if(check_points(xmin,ymin,xmax,ymax,x1,y1)):

        A=x1

        B=y1

        C=x2

        D=y2

    else:

        A=x2

        B=y2

        C=x1

        D=y1

    print("x1: ",A," , y1: ",B)

    xlist.append(A)

    ylist.append(B)

    if(C<=xmin):

        #left

        x=xmin y=B+(m*(xmin-

A)) elif(C>=xmax):

        #right

        x=xmax y=B+(m*(xmax-

A)) elif(D<=ymin): #bottom

        y=ymin x=((ymin-B)/m)+A

```

```

else: #top y=ymax

    x=((ymax-

    B)/m)+A

xlist.append(x) ylist.append(y) print("x2: ",x," Y2: ",y)

plt.title('Cohen Sutherland Line Clipping Algorithm By

CSC/20/35')

plt.plot(xlist,ylist)

```

```

xmin,ymin=input("Enter Lower Bound Coordinates of Interaction Area : ").split()

xmax,ymax=input("Enter Upper Bound Coordinates of Interaction Area :

").split() x1,y1=input("Enter Starting Coordinates of line : ").split()

x2,y2=input("Enter Ending Coordinates of line : ").split()

get_xy(int(xmin),int(ymin),int(xmax),int(ymax),int(x1),int(y1),int(x2),int(y2))

```

3.3. Output

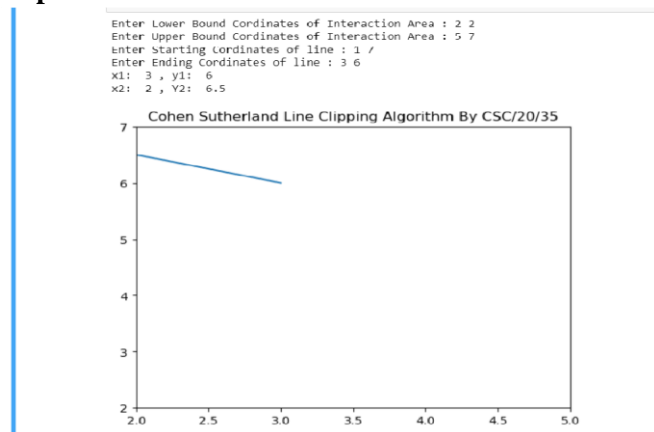


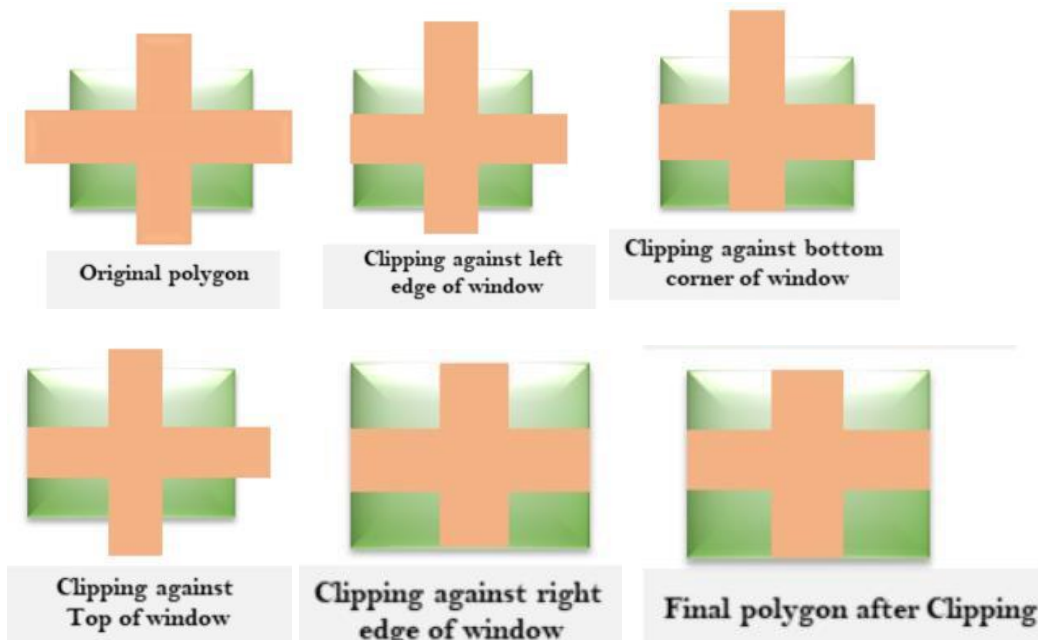
Figure 3. The output of Cohen and Sutherland Line Clipping Algorithm

4. Write a program to clip a polygon using Sutherland Hodgeman algorithm.

4.1. Explanation

It is performed by processing the boundary of polygon against each window corner or edge. First of all entire polygon is clipped against one edge, then resulting polygon is considered, then the polygon is considered against the second edge, so on for all four edges. Four possible situations while processing.

1. If the first vertex is outside the window, the second vertex is inside the window. Then second vertex is added to the output list. The point of intersection of window boundary and polygon side (edge) is also added to the output line.
 2. If both vertices are inside window boundary. Then only second vertex is added to the output list.
 3. If the first vertex is inside the window and second is outside window. The edge which intersects with window is added to output list.
 4. If both vertices are outside window, then nothing is added to output list.
- Following figures show original polygon and clipping of polygon against four windows



4.2. Code

Write a program to clip a polygon using Sutherland Hodgeman algorithm.

```
def draw_graph(xlist,ylist,V,title):

    plt.plot(xlist,ylist,c="red" , label="Required
    Area") x=[] y=[] for i in V:

        x.append(i[0])

        y.append(i[1])

    plt.plot(x,y,c="blue",label="Polygon")

plt.show() def

check_points(xmin,ymin,xmax,ymax,x1,y1):
```

```

if(x1>=xmin and x1<=xmax):

    if(y1>=ymin and y1<=ymax):

        return True

    else: return

False else:

    return False def

get_xy(xmin,ymin,xmax,ymax,x1,y1,x2,y2): m =

(y2-y1)/(x2-x1)

if(check_points(xmin,ymin,xmax,ymax,x1,y1)):

    A=x1

    B=y1

    C=x2

    D=y2

else:

    A=x2

    B=y2

    C=x1

    D=y1

print("x1: ",A," y1: ",B)

print("x2: ",C," y2: ",D)

if(C<=xmin):

    #left

    x=xmin y=B+(m*(xmin-

A)) elif(C>=xmax):

    #right

    x=xmax

    y=B+(m*(xmax-A))

```

```

elif(D<=ymin):
    #bottom y=ymin
    x=((ymin-B)/m)+A
else: #top y=ymax
    x=((ymax-
    B)/m)+A
return (x,y);

def clip_using_sutherland_hongeman(x1,y1,x2,y2,V):
    check=[]
    v1=[] for
    i in V:
        check.ap
        pend(che
        ck_point
        s(x1,y1,x
        2,y2,i[0],
        i[1]))
        print(che
        ck)
        print(V)
        for i in
        range(len
        (check)-
        1):
            if(check[i]==False):

```

```

        if(check[i+1]==True): print("Outside to inside")

        x,y=get_xy(x1,y1,x2,y2,V[i][0],V[i][1],V[i+1][0],V[i+1][1])

        v1.append((x,y)) else:

            print("outside to outside")

    elif(check[i]):

        if(check[i+1]==True):

            print("Inside to Inside")

            v1.append((V[i][0],V[i][1])) else:

                print("Inside to outside")

v1.append((int(V[i][0]),int(V[i][1])))

x,y=get_xy(x1,y1,x2,y2,V[i][0],V[i][1],V[i+1][0],V[i+1][1])

v1.append((x,y)) print(v1) xlist=[x1,x1,x2,x2,x1]

ylist=[y1,y2,y2,y1,y1] draw_graph(xlist,ylist,v1,"Cropped Data is : ")

import matplotlib.pyplot as plt from shapely.geometry import Polygon

x1,y1=input("Enter Lower bound of Cropped Area : ").split()

x2,y2=input("Enter Upper bound of Cropped Area : ").split()

xlist=[int(x1),int(x1),int(x2),int(x2),int(x1)]

ylist=[int(y1),int(y2),int(y2),int(y1),int(y1)] count=int(input("Enter

Number of vertices in a Polygon : ")) V=[] print("Start entering Points

: ") for i in range(count): print("Enter Coordinates of ",i+1," Vertex :

") x,y=input().split()

    V.append((int(x),int(y)))

V.append((V[0][0],V[0][1]))

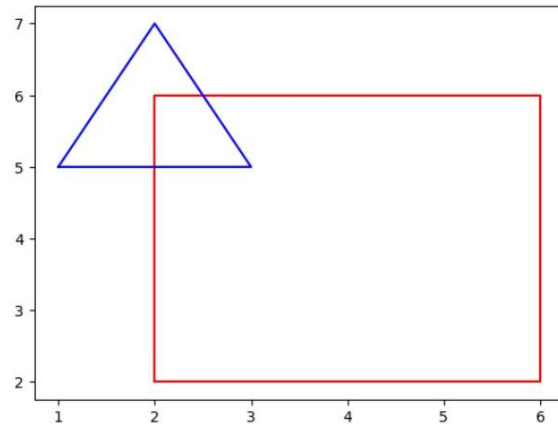
draw_graph(xlist,ylist,V,"Actual Data is : ")

V1=clip_using_sutherland_hongeman(int(x1),int(y1),int(x2),int(y2),V)

```


4.3. Output

```
Requirement already satisfied: shapely in c:\users\vikas\anaconda3\lib\site-packages (2.0.1)
Requirement already satisfied: numpy>=1.14 in c:\users\vikas\anaconda3\lib\site-packages (from shapely) (1.21.5)
Enter Lower bound of Cropped Area : 2 2
Enter Upper bound of Cropped Area : 6 6
Enter Number of vertices in a Polygon : 3
Start entering Points :
Enter Coordinates of 1 Vertex :
1 5
Enter Coordinates of 2 Vertex :
2 7
Enter Coordinates of 3 Vertex :
3 5
```



```
[False, False, True, False]
[(1, 5), (2, 7), (3, 5), (1, 5)]
outside to outside
Outside to inside
x1: 3 , y1: 5
x2: 2 , y2: 7
Inside to outside
x1: 3 , y1: 5
x2: 1 , y2: 5
[(2, 7.0), (3, 5), (2, 5.0)]
```

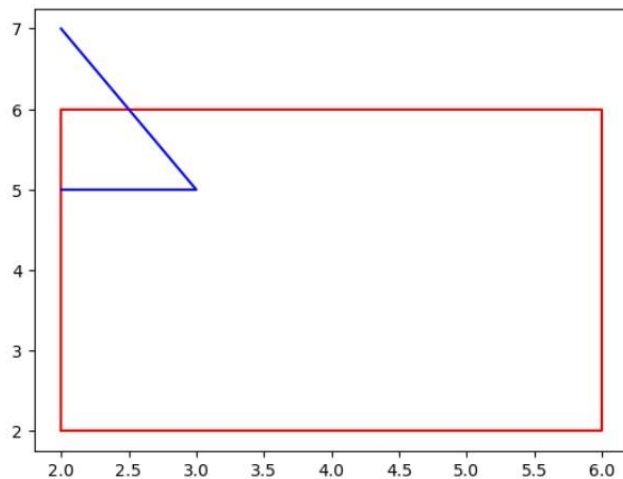
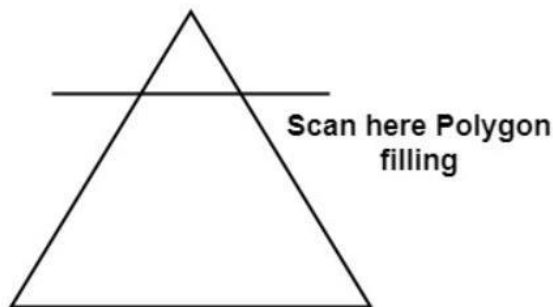


Figure 4. The output of Sutherland Hodgeman algorithm.

5. Write a program to fill a polygon using Scan line fill algorithm.

5.1. Explanation

This algorithm lines interior points of a polygon on the scan line and these points are done on or off according to requirement. The polygon is filled with various colors by coloring various pixels. In above figure polygon and a line cutting polygon is shown. First of all, scanning is done. Scanning is done using raster scanning concept on display device. The beam starts scanning from the top left corner of the screen and goes toward the bottom right corner as the endpoint. The algorithms find points of intersection of the line with polygon while moving from left to right and top to bottom. The various points of intersection are stored in the frame buffer. The intensities of such points is kept high. Concept of coherence property is used. According to this property if a pixel is inside the polygon, then its next pixel will be inside the polygon.



5.2. Code

Write a program to fill a polygon using Scan line fill algorithm.

```
def draw_graph(V):  
    x=[] y=[]  
    for i in  
    V:  
        x.append(i[0])  
        y.append(i[1]) plt.title("Before Applying  
Scan line Algorithm")  
    plt.plot(x,y,c="blue",label="Polygon") plt.show()  
    plt.plot(x,y,c="blue",label="Polygon") return  
max(y),min(y),max(x),min(x) def get_range(V):  
    y2,y1,x2,x1=draw_graph(V  
    ) x=[] y=[] for i in  
    range(len(V)-1):
```

```

x1=V[i][0] y1=V[i][1]
x2=V[i+1][0] y2=V[i+1][1]
x3,y3=calpoints(x1,y1,x2,y2,x,y
) x=x3 y=y3

for i in range(int(len(y)/2)):
    if i!= int(len(y)/2) and i!= 0:
        plt.plot([x[i],x[y.index(y[i],i+1)]],[y[i],y[i]],c="red"
) plt.title("After Applying Scan Line algorithm") plt.show()

def calpoints(x1,y1,x2,y2,xlist,ylist):
    m=(y2-y1)/(x2-x1) c=y1-
    (m*x1) for i in range(abs(y2-
y1)*10):
        if x1<=x2:
            y=(i/10)+y1 x=(y-
            c)/m xlist.append(x)
            ylist.append(y) else:
                y=y1-(i/10) x=(y-
                c)/m xlist.append(x)
                ylist.append(y)

    return xlist,ylist
import
matplotlib.pyplot as plt from
graphics import *

count=int(input("Enter Number of vertices in a Polygon :- "))
V=[] print("Start entering Points :- ") for i in range(count):
    print("Enter Cordinates of ",i+1," Vertex :- ") x,y=input().split()

```

```

V.append((int(x),int(y)))

V.append((V[0][0],V[0][1]))

get_range(V)

```

5.3. Output

```

Enter Number of vertices in a Polygon :- 4
Start entering Points :-
Enter Coordinates of 1 Vertex :-
1 1
Enter Coordinates of 2 Vertex :-
3 5
Enter Coordinates of 3 Vertex :-
7 7
Enter Coordinates of 4 Vertex :-
5 3

```

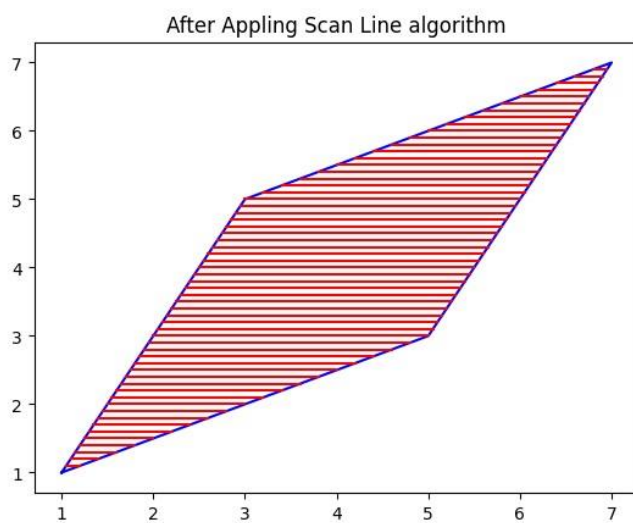
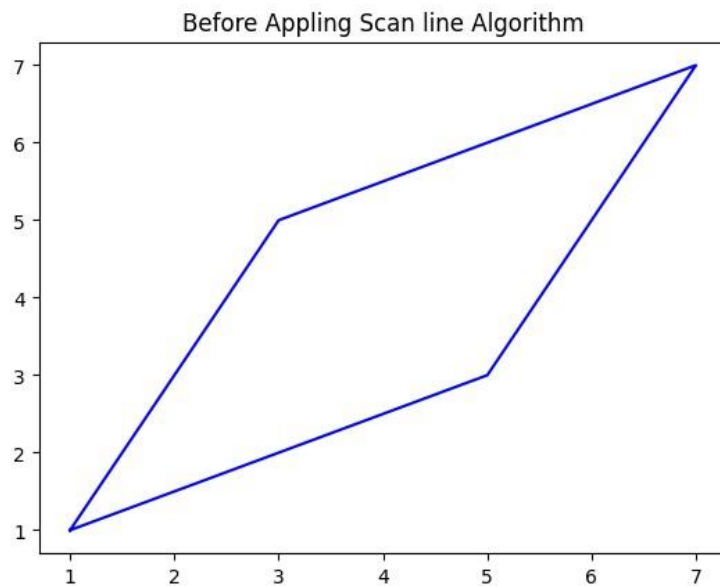


Figure 5. The output of Scan line Fill algorithm

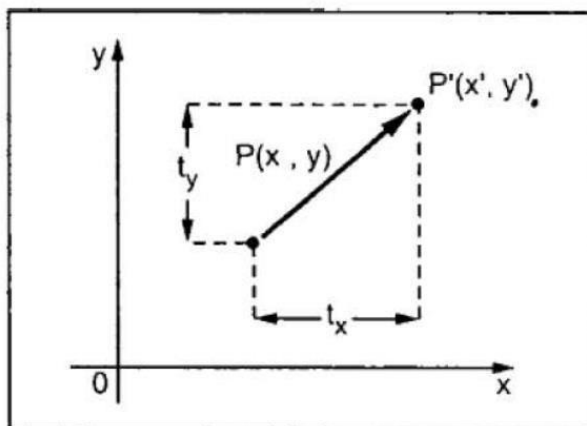
6. Write a program to apply various 2D transformations on a 2D object (use homogenous coordinates).

6.1. Explanation

Transformation means changing some graphics into something else by applying rules. We can have various types of transformations such as translation, scaling up or down, rotation, etc. When a transformation takes place on a 2D plane, it is called 2D transformation. Transformations play an important role in computer graphics to reposition the graphics on the screen and change their size or orientation.

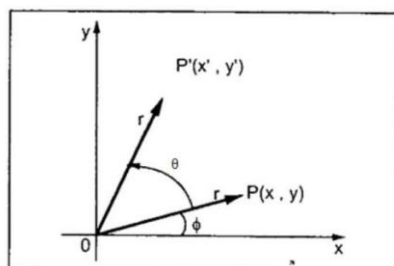
Translation

A translation moves an object to a different position on the screen. You can translate a point in 2D by adding translation coordinate (tx,ty) to the original coordinate X,Y to get the new coordinate X',Y'.



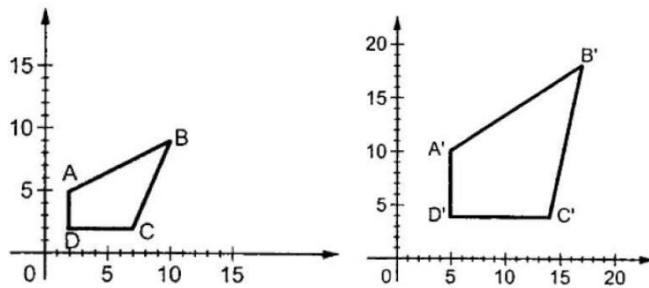
Rotation

In rotation, we rotate the object at particular angle θ from its origin. From the following figure, we can see that the point $P(X,Y)$ is located at angle ϕ from the horizontal X coordinate with distance r from the origin. Let us suppose you want to rotate it at the angle θ . After rotating it to a new location, you will get a new point $P' (X',Y')$.



Scaling

To change the size of an object, scaling transformation is used. In the scaling process, you either expand or compress the dimensions of the object. Scaling can be achieved by multiplying the original coordinates of the object with the scaling factor to get the desired result.



6.2. Code

Write a program to apply various 2D transformations on a 2D object (use homogenous coordinates).

```
import matplotlib.pyplot as plt
```

```
import numpy as np
```

```
def draw_graph(V,title):
```

```
    x=[]
```

```
    y=[]
```

```
    for
```

```
        i in
```

```
            range(le
```

```
                n(V)):
                x.append(V[i][0])
```

```
                y.append(V[i][1])
```

```
    x.append(x[0])
```

```
    y.append(y[0])
```

```
    plt.plot(x,y)
```

```
    plt.title(title)
```

```

plt.show() def
multiply_matrix(O,C):
C.append(1)
x=np.dot(O[0],C)
y=np.dot(O[1],C) return
[x,y]

```

```

def Translation(V):
    x=[] y=[] for i in
    range(len(V)):
        x.append(V[i][0])
        y.append(V[i][1]) print(" Performing Translation on
2D Object Provided : ") dx=int(input("Enter Shifting
Distance on X-axis : ")) dy=int(input("Enter Shifting
Distance on Y-axis : "))
O=[[1,0,dx],[0,1,dy],[0,0,1]]
V1=[] draw_graph(V,"Original
Graph") for i in V:
    print(i)
    V1.append(multiply_matrix(O,i))
draw_graph(V1,"Translation of 2D Object")
print(V1)
Scaling(V1)

```

```

def Scaling(V):
    x=[] y=[] for i in
    range(len(V)):

```

```

        x.append(V[i][0])

        y.append(V[i][1]) print(" Performing Scaling on

2D Object Provided : ") sx=float(input("Enter Scaling
factor of X-axis : ")) sy=float(input("Enter Scaling
factor of Y-axis : "))

O=[[sx,0,0],[0,sy,0],[0,0,1]]

V1=[] for

i in V:

    print(i)

    V1.append(multiply_matrix(O,i))

draw_graph(V1,"Scaling of 2D Object")

Rotation(V1)

def Rotation(V):

    x=[] y=[] for i in

    range(len(V)):

        x.append(V[i][0])

        y.append(V[i][1])

    print(" Performing Rotation on 2D Object Provided : ")

    sign=int(input("Enter Rotation side 0 : (Anti Clockwise), 1:(Clockwise) :

    ")) theta=int(input("Enter Rotation angle :- ")) if sign==0:

O=[[math.cos(math.radians(theta)),-math.sin(math.radians(theta)),0],[math.sin(math.radians(t
heta)),math.cos(math.radians(theta)),0],[0,0,1]] else:

O=[[math.cos(math.radians(theta)),math.sin(math.radians(theta)),0],[-math.sin(math.radians(t
heta)),math.cos(math.radians(theta)),0],[0,0,1]]

```



```

V1=[]
for
i in V:
    print(i)
    V1.append(multiply_matrix(O,i))
draw_graph(V1,"Rotation of 2D Object")

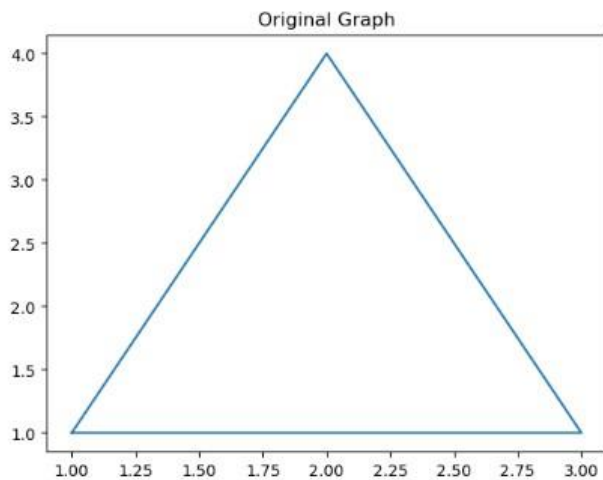
count=int(input("Enter Number of vertices of Object : "))

V=[]
for i in range(count):
    print("Enter",i+1," Vertex Coordinates : ")
    x,y=input().split()
    V.append([int(x),int(y)])
Translation(V)

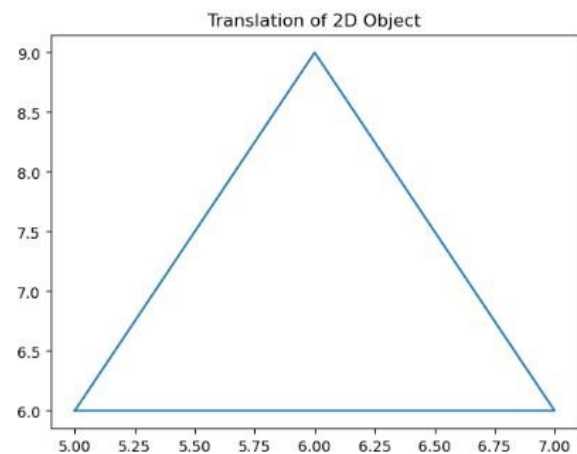
```

6.3. Output

```
Enter Number of vertices of Object : 3
Enter 1 Vertex Coordinates :
1 1
Enter 2 Vertex Coordinates :
3 1
Enter 3 Vertex Coordinates :
2 4
Performing Translation on 2D Object Provided :
Enter Shifting Distance on X-axis : 4
Enter Shifting Distance on Y-axis : 5
```



```
[1, 1]
[3, 1]
[2, 4]
```



```
[[5, 6], [7, 6], [6, 9]]
Performing Scaling on 2D Object Provided :
Enter Scaling factor of X-axis : 3
Enter Scaling factor of Y-axis : 4
[5, 6]
[7, 6]
[6, 9]
```

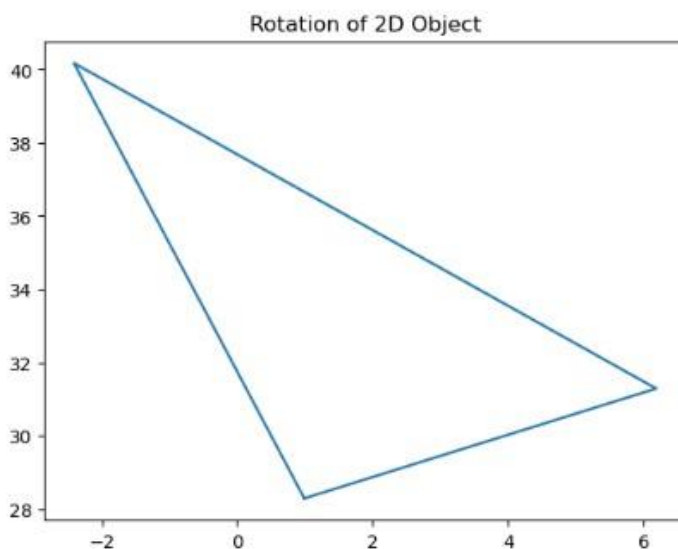
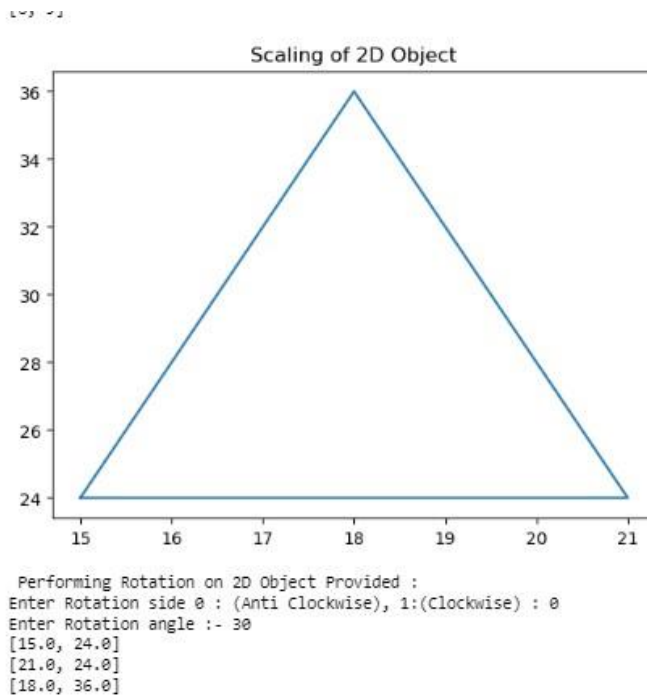


Figure 6. The output of 2D Transformation on a 2D Object.

7. Write a program to apply various 3D transformations on a 3D object and then apply parallel and perspective projection on it.

7.1. Explanation

3-D Transformation: In very general terms a 3D model is a mathematical representation of a physical entity that occupies space. In more practical terms, a 3D model is made of a description of its shape and a description of its color appearance. 3-D Transformation is the process of manipulating the view of a three-D object with respect to its original position by modifying its physical attributes through various methods of transformation like Translation, Scaling, Rotation, Shear, etc.

Properties of 3-D Transformation:

1. Lines are preserved,
2. Parallelism is preserved,
3. Proportional distances are preserved.

One main categorization of a 3D object's representation can be done by considering whether the surface or the volume of the object is represented:

Boundary-based: the surface of the 3D object is represented. This representation is also called b-rep. Polygon meshes, implicit surfaces, and parametric surfaces, which we will describe in the following, are common representations of this type.

Volume-based: the volume of the 3D object is represented. Voxels and Constructive Solid Geometry (CSG) Are commonly used to represent volumetric data.

Types of Transformations:

1. Translation
2. Scaling
3. Rotation

7.2. Code

```
# Write a program to apply various 3D transformations on a 3D object and then apply parallel
and perspective projection on it. import matplotlib.pyplot as plt import numpy as np import
math
```

```
def multiply_matrix(O,C):
```

```
    C.append(1)
    x=np.dot(O[0],C)
    y=np.dot(O[1],C)
    z=np.dot(O[2],C)
    return [x,y,z]
```

```
def Translation(V):
```

```

x=[] y=[] z=[] for i in
range(len(V)):

    x.append(V[i][0])

    y.append(V[i][1])

    z.append(V[i][2]) print(" Performing Translation on
3D Object Provided : ") dx=int(input("Enter Shifting
Distance on X-axis : ")) dy=int(input("Enter Shifting
Distance on Y-axis : ")) dz=int(input("Enter Shifting
Distance on Z-axis : "))

O=[[1,0,0,dx],[0,1,0,dy],[0,0,1,dz],[0,0,0,1]

] V1=[] for i in V:

    V1.append(multiply_matrix(O,i))

print(V1)

Scaling(V1)

```

```

def Scaling(V):

    x=[]

    y=[]

    z=[] for

    i in

    range(le

    n(V)):

        x.append(V[i][0])

        y.append(V[i][1])

        z.append(V[i][2]) print(" Performing Scaling on
3D Object Provided : ") sx=float(input("Enter Scaling
factor of X-axis : ")) sy=float(input("Enter Scaling

```

```

factor of Y-axis : ") sz=float(input("Enter Scaling
factor of Z-axis : "))

O=[[sx,0,0,0],[0,sy,0,0],[0,0,sz,0],[0,0,0,1]

] V1=[] for i in V:

    V1.append(multiply_matrix(O,i))

print(V1)

Rotation(V1)

def Rotation(V):

    x=[] y=[] z=[] for i in
    range(len(V)):

        x.append(V[i][0])

        y.append(V[i][1])

        z.append(V[i][2]) print(" Performing Rotation on 3D Object Provided : ")

    sign=int(input("Enter Rotation side 0 : (Anti Clockwise), 1:(Clockwise) :
    ")) theta=int(input("Enter Rotation angle : ")) Axis=input("Enter Rotation's
    Axis : ")

    if sign==0:

        if Axis=='x':

            O=[[1,0,0,0],[0,math.cos(math.radians(theta)),-math.sin(math.radians(theta)),0],[0,math.sin(m
            ath.radians(theta)),math.cos(math.radians(theta)),0],[0,0,0,1]] elif Axis=='y':

            O=[[math.cos(math.radians(theta)),0,math.sin(math.radians(theta)),0],[0,1,0,0],[-math.sin(mat
            h.radians(theta)),0,math.cos(math.radians(theta)),0],[0,0,0,1]] else:

            O=[[math.cos(math.radians(theta)),-math.sin(math.radians(theta)),0,0],[math.sin(math.radians
            (theta)),math.cos(math.radians(theta)),0,0],[0,0,1,0],[0,0,0,1]]

            else: if Axis=='x':

```

```

O=[[1,0,0,0],[0,math.cos(math.radians(theta)),math.sin(math.radians(theta)),0],[0,-math.sin(m
ath.radians(theta)),math.cos(math.radians(theta)),0],[0,0,0,1]]

    elif Axis=='y':
O=[[math.cos(math.radians(theta)),0,-math.sin(math.radians(theta)),0],[0,1,0,0],[math.sin(mat
h.radians(theta)),0,math.cos(math.radians(theta)),0],[0,0,0,1]]

    else:
O=[[math.cos(math.radians(theta)),math.sin(math.radians(theta)),0,0],[-math.sin(math.radians
(theta)),math.cos(math.radians(theta)),0,0],[0,0,1,0],[0,0,0,1]] V1=[] for i in V:

    V1.append(multiply_matrix(O,i)) print(V1)

count=int(input("Enter Number of vertices of Object : "))

V=[] for i in range(count):

    print("Enter ",i+1," Vertex Coordinates : ")

    x,y,z=input().split()

    V.append([int(x),int(y),int(z)])

Translation(V)

```

7.3. Output

```

Enter Number of vertices of Object : 3
Enter 1 Vertex Coordinates :
2 2 2
Enter 2 Vertex Coordinates :
3 3 3
Enter 3 Vertex Coordinates :
4 4 4
Performing Translation on 3D Object Provided :
Enter Shifting Distance on X-axis : 2
Enter Shifting Distance on Y-axis : 3
Enter Shifting Distance on Z-axis : 4
[[4, 5, 6], [5, 6, 7], [6, 7, 8]]
Performing Scaling on 3D Object Provided :
Enter Scaling factor of X-axis : 1
Enter Scaling factor of Y-axis : 2
Enter Scaling factor of Z-axis : 3
[[4.0, 10.0, 18.0], [5.0, 12.0, 21.0], [6.0, 14.0, 24.0]]
Performing Rotation on 3D Object Provided :
Enter Rotation side 0 : (Anti Clockwise), 1:(Clockwise) : 0
Enter Rotation angle : 90
Enter Rotation's Axis : 30
[[-10.0, 4.000000000000001, 18.0], [-12.0, 5.000000000000001, 21.0], [-14.0, 6.000000000000001, 24.0]]

```

Figure 1. The output of Bresenham's line drawing algorithm.

8. Write a program to draw Hermite /Bezier curve.

8.1. Explanation

Bezier curves are one of the parametric curves most frequently used in computer graphics and were independently developed for computer-assisted car design by two engineers, both working for French automobile companies: Pierre Bezier who was an engineer for Renault, and Paul de Casteljau, who was an engineer for Citroën. The concept of Bezier curves was discovered by the French engineer Pierre Bézier. Bezier curves are basically used in computer graphics to draw shapes, for CSS animation, and in many other places. These are the curves that are generated under the control of some other points, also called control points.

Properties of Bezier Curves: A very important property of Bezier curves is that they always pass through the first and last control points. The degree of the polynomial defining the curve segment is always one less than the number of defining polygon points. So, for example, if we have 4 control points, then the degree of the polynomial is 3, i.e., cubic polynomial. In the Bezier curves, moving a control point alters the shape of the whole curve. A Bezier curve generally follows the shape of the defining polygon. A curve is always inside the convex hull of control points.

8.2. Code

```
# Write a program to draw Hermite /Bezier curve.
```

```
import numpy as np
```

```
import matplotlib.pyplot as plt
```

```
def h00(t): return 2*t**3 -
```

```
3*t**2 + 1 def h10(t): return
```

```
t**3 - 2*t**2 + t def h01(t):
```

```
return -2*t**3 + 3*t**2 def
```

```
h11(t):
```

```
    return t**3 - t**2
```

```
P0 = np.array([0, 0])
```

```
P1 = np.array([1, 1])
```

```
V0 = np.array([1, 0]) V1 =
```

```
np.array([2, 1]) t_v =
```



```

np.linspace(0, 1, 100) Bezier_pts =
np.zeros((2, len(t_v))) for i, t in
enumerate(t_v):
    Bezier_pts[:, i] = (1-t)**3 * P0 + 3*t*(1-t)**2 * (P0 + V0) + 3*t**2*(1-t) * (P1 - V1) +
t**3 * P1
Hermite_pts = np.zeros((2, len(t_v)))
for i, t in enumerate(t_v):
    Hermite_pts[:, i] = h00(t) * P0 + h10(t) * V0 + h01(t) * P1 + h11(t) * V1
plt.plot(Bezier_pts[0], Bezier_pts[1], label="Bezier")
plt.plot(Hermite_pts[0], Hermite_pts[1], label="Hermite")
plt.scatter([P0[0], P1[0]], [P0[1], P1[1]], label="Control points")
plt.legend()

plt.show()

```

8.3. Output

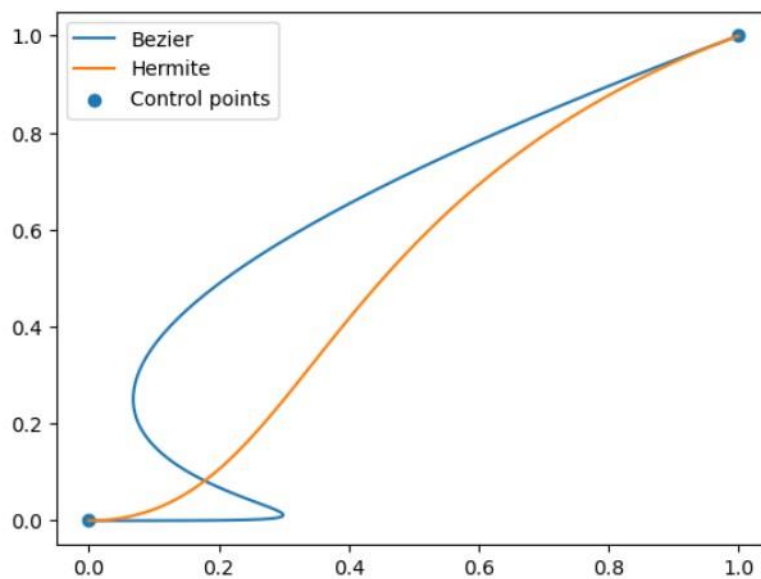


Figure 1. The output of Bresenham's line drawing algorithm.