



**Universität  
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## Introduction to Artificial Intelligence Exercise Sheet 7

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## Exercise 7.1

(a) Predicates: Properties of objects that we are interested in; can be true or false:

Let  $B = \{\text{Krämerbrücke, Schmiedbrücke, Honigbrücke, Holzbrücke, Grüne Brücke, Köttelbrücke, Hohe Brücke}\}$  be the set of bridges.

$$V = \{\text{crossedAtLeastOnce}(b) \mid \forall b \in B\} \cup \{\text{crossedAtMostOnce}(b) \mid \forall b \in B\}$$

(b) Initial state (only predicates which are true are listed, because of closed-world assumption):

$$I = \bigwedge_{b \in B} \text{crossedAtMostOnce}(b), \forall b \in B$$

(c) Goal state (both predicates have to be true in order to ensure that each Bridge is crossed exactly once):

$$G = \bigwedge_{b \in B} (\text{crossedAtLeastOnce}(b) \wedge \text{crossedAtMostOnce}(b)), \forall b \in B$$

(d) A is a finite set of actions  $a = \langle \text{pre}, \text{eff} \rangle$  with  $\text{pre}(a)$  and  $\text{eff}(a)$

$$A = \{\text{crossFirstTime}(b), \text{crossAgain}(b)\}, \forall b \in B$$

action  $a$   $\text{crossFirstTime}(b)$ :

$$\text{pre}(\text{crossFirstTime}(b)) = \neg \text{crossedAtLeastOnce}(b) \wedge \text{crossedAtMostOnce}(b)$$

$$\text{eff}(\text{crossFirstTime}(b)) = \text{crossedAtLeastOnce}(b) \wedge \text{crossedAtMostOnce}(b)$$

When the action  $\text{crossFirstTime}(b)$  is executed exactly once for every bridge the Goal state is reached.

action  $\text{crossAgain}(b)$ :

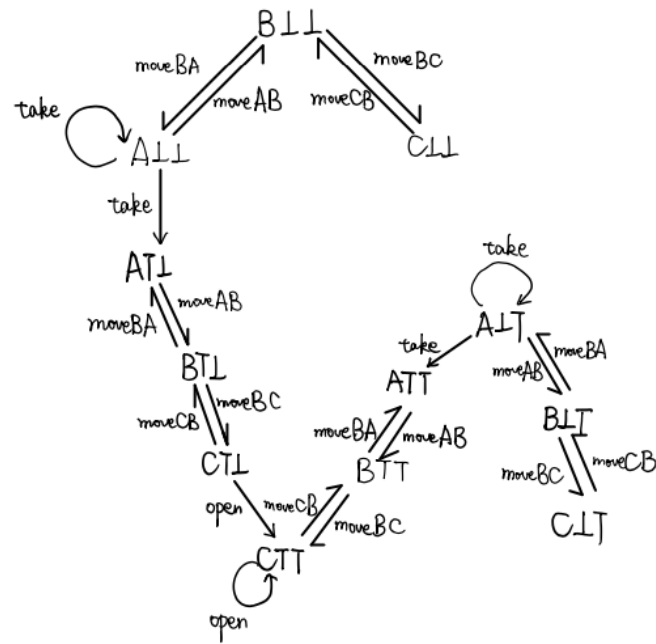
$$\text{pre}(\text{crossAgain}(b)) = \text{crossedAtLeastOnce}(b)$$

$$\text{eff}(\text{crossAgain}(b)) = \text{crossedAtLeastOnce}(b)$$

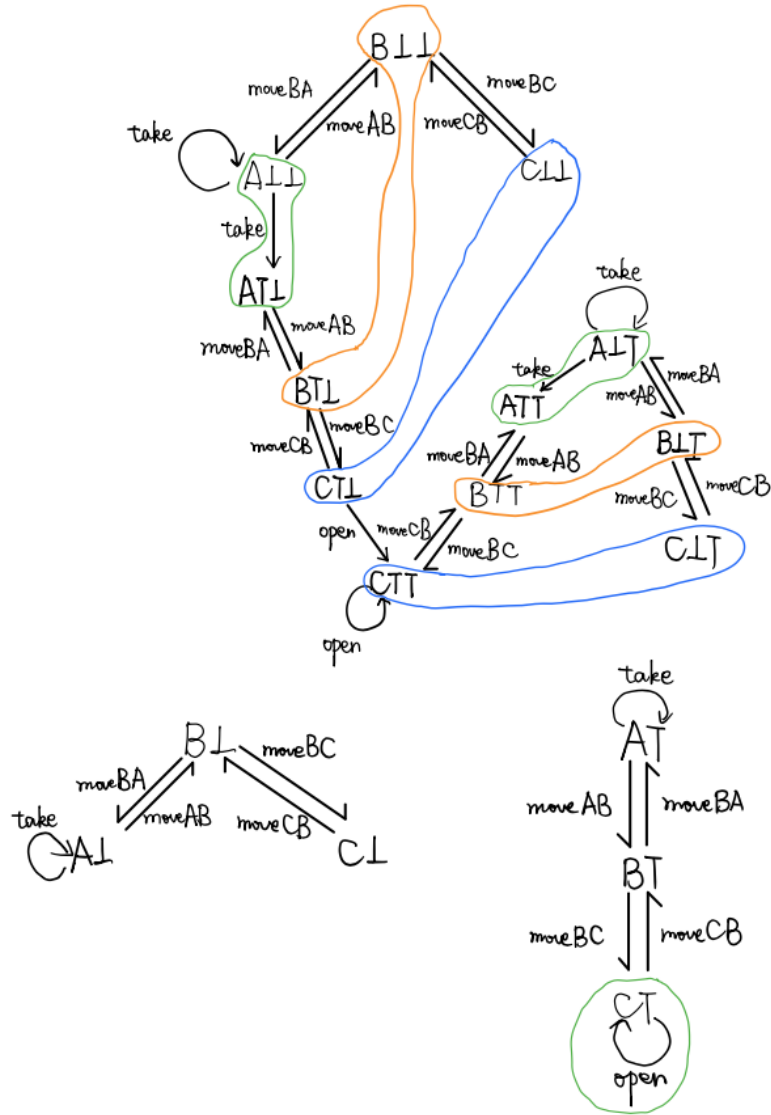
We can ignore  $\text{crossedAtMostOnce}$  in the action  $\text{crossAgain}(b)$  as its state is irrelevant for this action, i.e.  $\text{crossedAtMostOnce} \rightarrow \text{false}$  when crossing the same bridge numerous times.

The Goal state won't be reached when action  $\text{crossAgain}(b)$  is used.

(a)



(b)



(c) PDB:

$$\{ \text{loc} \rightarrow B, \text{treasure} \rightarrow \perp \} = \infty$$

$$\{ \text{loc} \rightarrow A, \text{treasure} \rightarrow \perp \} = \infty$$

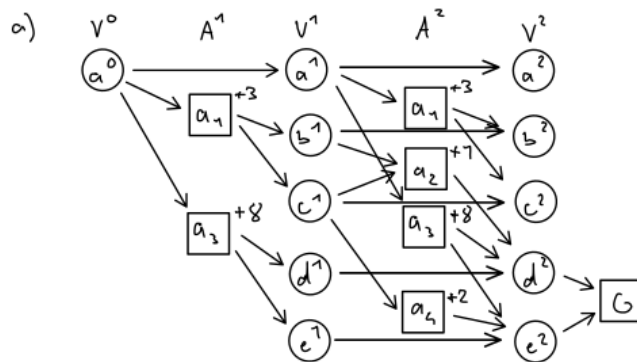
$$\{ \text{loc} \rightarrow C, \text{treasure} \rightarrow \perp \} = \infty$$

$$\{ \text{loc} \rightarrow A, \text{treasure} \rightarrow T \} = 2$$

$$\{ \text{loc} \rightarrow B, \text{treasure} \rightarrow T \} = 1$$

$$\{ \text{loc} \rightarrow C, \text{treasure} \rightarrow T \} = 0$$

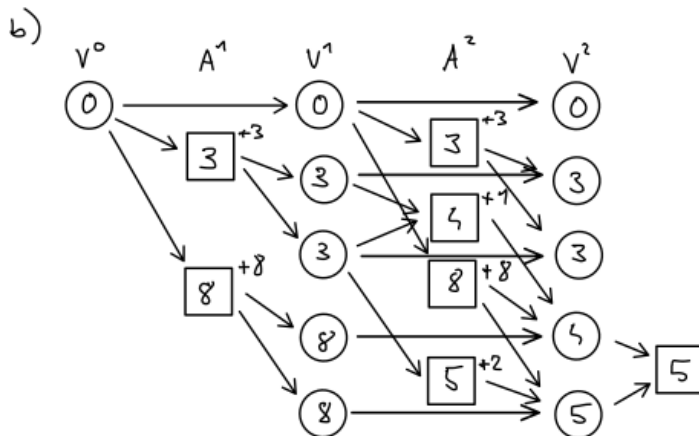
## Exercise 7.3



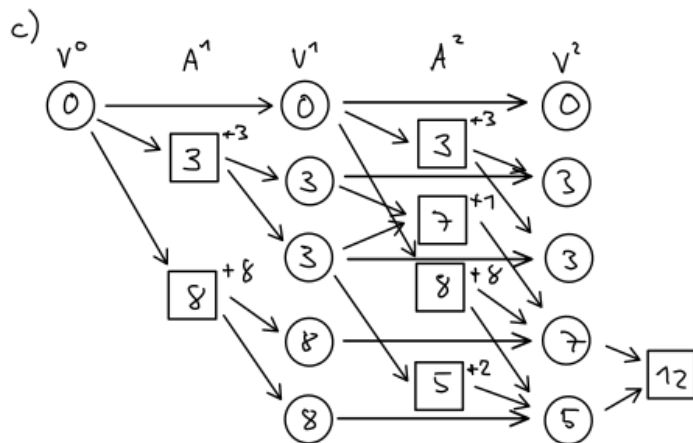
$$V^1 = V^2, A^1 \neq A^2$$

↳ RPG did not stabilize yet

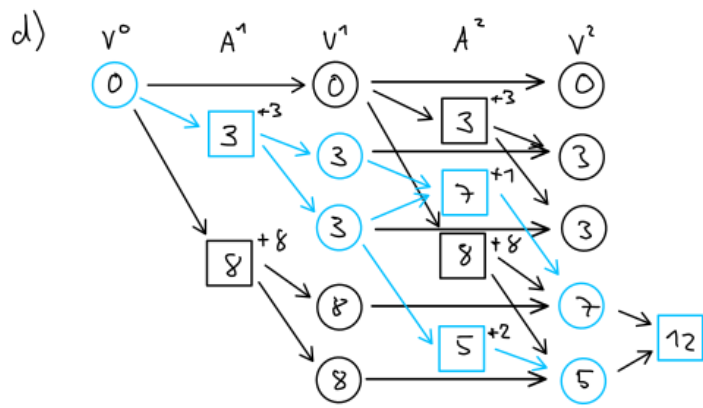
question: Would we need to "add" the goal node  $G$  on action layer  $A^2$  too?



$$h^{\max}(I) = 5, I = \{a\}$$



$$h^{\text{add}}(I) = 12$$



$$h^{FF}(\Gamma) = 3 + 1 + 2 = 6$$