Chess Assignment

Introduction to Reinforcement Learning (Spring 2022). Source code available at: https://github.com/TwoDigitsOneNumber/IntroRL_ChessAssignment

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Abstract—We explored the use of three deep reinforcement learning methods for training agents to play a simplified version of chess. All algorithms, SARSA, Q-Learning and DQN were able to learn successful strategies. DQN was able to overcome the shortcomings of Q-Learning and provides an off-policy method with performance comparable to the on-policy method SARSA.

Index Terms—deep reinforcement learning, chess, temporal-difference methods

I. INTRODUCTION

In this assignment, we explore three different deep reinforcement learning algorithms to learn how to play a simplified version of chess, which can be thought of as a special instance of an endgame. These three algorithms are SARSA, Q-Learning and DQN¹. We will first provide a general look over our methodology (see Section II) and later discuss the result obtained in our experiments (see Section III).

The focus of this report lies on comparing these three algorithms in theory and in practise on the chess endgame environment. We further explored the impact of the hyperparameters β and γ , which represent the speed of the decaying trend for the learning rate and the discount factor respectively.

Throughout the report we indicate in footnotes which task a particular section is referring to in terms of answering the task. We do this as the solutions to certain tasks are spread throughout multiple sections, e.g. task 3 is answered in Section II and Section III. Even though this assignment was not solved in a group, we decided to also answer some of the "group only" and we stick to the numbering of the assignment in order to avoid confusion.

II. METHODS

A. Environment

This version of chess takes place on a 4 by 4 board and can be thought of as a specific version of an endgame where the agent has a king and a queen, and the opponent has only a king. Since this game can only end in a win for the agent or in a draw, it is the agent's goal to learn how to win the game and avoid draws. For all experiments considered, the agent will be given a reward of 1 for winning, 0 for drawing, and 0 for all intermediate steps.

¹SARSA serves as answer to task 3 and DQN serves as answer to task 5

This chess setting, and chess in general, fulfills the Markov property and therefore justifies the use of the temporal difference methods used in this assignment.

B. SARSA and Q-Learning²

- 1) Temporal-Difference Algorithms: SARSA and Q-Learning are two very related model-free types of temporaldifference (TD) algorithms for learning expected rewards, also known as Q-values, when rewards are not immediate and possibly sparse. The learning takes place via interaction with an environment through trial and error. These Q-values are in general represented by an action-value function Q and, for finitely many state-action pairs (s, a), can be considered as a Q-table where each state-action pair, (s, a), maps to a single Q-value, thus providing an estimate of the quality of any given state-action pair (s, a). In this assignment however we use neural networks to approximate the action-value function, which outputs the Q-values for all possible actions for any given state. This helps to avoid computing large Q-tables. All algorithms explored in this assignment, including DQN, require the environment to fulfill the Markov property.
- 2) On-policy vs. Off-policy: SARSA and Q-Learning address the temporal-credit-assignment problem [1], that is, trying to attribute future rewards to previous actions. These future rewards get discounted with the hyper-parameter γ (see Section III-C). Both algorithms repeatedly choose and take actions in the environment according to some policy π , e.g. an ϵ -greedy policy.

However, this is where they differ. SARSA is an on-policy algorithm, which means that consecutive actions are chosen according to the same policy π , even during the update step of the O-values, which leads to the update rule:

$$Q_{\pi}(s, a) \leftarrow Q_{\pi}(s, a) + \eta(r + \gamma Q_{\pi}(s_{t+1}, a') - Q_{\pi}(s, a))$$

for some future action a' chosen according to policy π .

Q-learning, on the other hand, is an off-policy algorithm, which means that it takes its actions a according to its policy π , but during the update steps it assumes a greedy policy, i.e. optimal play, for future actions a'. Q-Learning has the update rule:

$$Q_{\pi}(s, a) \leftarrow Q_{\pi}(s, a) + \eta(r + \gamma \max_{a'} Q_{\pi}(s_{t+1}, a') - Q_{\pi}(s, a)).$$

²Answer to task 1.

3) Advangages and Disadvantages: This leads to one of Q-Learning's major advantages: Because of Bellman's optimality equation, Q-Learning is guaranteed to learn the values for the optimal policy, i.e. $Q_*(s,a) = \max_{\pi} Q_{\pi}(s,a)$, regardless of the policy used to train it, and in a greedy stetting will take the optimal actions, at least if it was trained sufficiently. However, this can in certain cases mean that the online performance of Q-Learning will be worse than the one from SARSA, as Sutton et al. [2] demonstrate with their "gridworld" example "Cliff Walking". Our chess game is a similar situation, because a win and a draw can be very close, thus during exploration Q-Learning can accidentally create a draw because it is going for the optimum when exploiting. Q-Learning is however relatively unstable and the parameters can even diverge when it is combined with non-linear function approximators [3], making the guarantee to learn the optimal policy irrelevant.

SARSA will learn to take a safer path, because it keeps its policy in mind when updating the Q-values, i.e. it keeps in mind that it will explore in future actions. This has the advantage that SARSA in general tends to explore more than Q-Learning.

C. Experience Replay³

Experience replay is a technique proposed by Lin [4] to speed up the training process for reinforcement learning algorithms by reusing past experiences for future training. This is analogous to the human ability to remember past experiences and learn from them even after the fact. The past experiences are stored in a replay memory of fixed size at each time step t as a tuple $e_t = (s_t, a_t, r_t, s_{t+1})$. This essentially allows us to transform the learning process from online learning to minibatch learning, where a batch of experiences e_j is randomly sampled for each update step. Experience replay can only be used in combination with off-policy algorithms, because otherwise the current parameters determine the next sample and create unwanted feedback loops [3], [5].

Experience replay provides many benefits over online Q-Learning, especially when neural networks are used to approximate the action-value function. First, it enables the agent to learn from past experiences more then once, leading to increased data efficiency and faster convergence [4], [5]. Second, since for each update step past experiences are sampled randomly, the correlations between the individual actions are reduced, which then reduces the variance of the updates [5]. This leads to the experience samples e_j being closer to i.i.d. and thus guaranteeing better convergence when using optimization algorithms such as stochastic gradient descent as most convergence proofs assume i.i.d. data.

D. Deep Q-Networks $(DQN)^4$

A first version of the DQN algorithm was proposed by Mnih et al. [5] and combined experience replay with Q-learning, where a neural network was used as a non-linear function approximator for the action-value function. Mnih et al. [3] later

improved upon the method and presented the DQN algorithm, as it is known today, where they address the problem of the Q-values $Q_{\pi}(s,a)$ being correlated to the target values $y=r+\gamma\max_{a'}Q_{\pi}(s',a')$ because they are generated using the same neural network. In the DQN algorithm they separated the Q-network from the target network and only update the target network every C steps, which helps to break this correlation and combat diverging network parameters.

Since DQN uses experience replay, we essentially transform the reinforcement learning task to a supervised learning task. Therefore a suitable loss function for the neural network is needed. Mnih et al. [3] used a squared loss of the temporal-difference error, also known as delta: $\delta = y - Q_{\pi}(s, a)$.

E. Experiments

In order to address all tasks, we divided the tasks into several independent experiments. First, we conducted seeded runs⁵ for all three algorithms using seed 21 for reproducibility, which was chosen a-priori. These seeded runs serve as examples to compare the algorithm's online performance qualitatively. The seeds are used such that the weights of all neural networks are instantiated identically for all algorithms and they subsequently serve as seeds for any random number used during training. This makes sure that all agents start with the same initial conditions and that the results are reproducible (see Section V-A). All algorithms were run for 100000 episodes using identical model architecture and hyperparameters (see Section II-F).

Since the seeded runs are heavily influenced by the choice of the seed, we could end up with anything between a very lucky and well performing seed, or with a very unlucky one. Also the interpretation of the seeded runs is more difficult as we just have one run for each algorithm. Therefore, we decided to perform a simulation study and complete 30 non-seeded runs for each algorithm in order to get a better idea of how the algorithms perform on average. For computational reasons we limited these runs to 40000 episodes as we realized with test runs that by then most of the training progress has already taken place.

To analyze the impact of the hyper-parameters β and γ^6 we trained 49 agents with different combinations for β and γ but keeping all other hyper-parameters and model architecture identical. We chose SARSA for this experiment as we found it to have very low variance between its unseeded runs, which makes it an ideal candidate for comparing individual runs. These runs are seeded identically to the seeded runs mentioned above.

F. Implementation and Hyper-parameters

We implemented all algorithms from scratch according to Sutton et al. [2] (SARSA and Q-Learning⁷) and Mnih et al. [3] (DQN⁸). For the implementation see file neural_net.py

³Answer to "group only" task 2.

⁴Answer to task 5: Describing the used method.

⁵Answers to task 3 and 5.

⁶Answer to task 4.

⁷SARSA as answer to task 3 and Q-Learning as additional algorithm.

⁸Answer to task 5.

on GitHub or Listing 1. All algorithms use a neural network with 58 input neurons, 200 hidden neurons and 32 output neurons, not including the biases for the input and hidden layer. The neural network automatically adds a constant input for the bias and the hidden layer. The implementation treats the biases like any other weights and thus they are part of any matrix multiplication. We used a ReLU activation function for the hidden layer and no activation on the output layer. The weights were initialized using Glorot initialization [6], such that the weights are sampled from a normal distribution with mean 0 and variance $\frac{2}{n_{\rm in}+n_{\rm out}}$, where $n_{\rm in}$ and $n_{\rm out}$ denote to the number of input and output neurons of the respective layer. This helped preventing exploding gradients for the most part.check again with results

For all experiments we used the default hyperparameters provided in the Assignment.ipynb file unless otherwise noted (see Table I). For DQN we updated the weights of the target network after every C=10 steps, as most games take fewer steps than that. We used a replay memory of size 100000 and a batch size of 32.

Parameter	Value
Nr. input neurons	58+1
Nr. hidden neurons	200+1
Nr. output neurons	32
Initial exploration probability ϵ_0	0.2
Learning rate η	0.035
Decay rate of ϵ , β	0.00005
Discount factor γ	0.85

TABLE I: Common hyper-parameters shared by all algorithms.

III. RESULTS

A. Seeded Runs⁹

The rewards and number of moves for the seeded runs are depicted in Figures 1 and 2 respectively. Since the curves are very noisy, we smoothed them using an exponential moving average (EMA) with a weight on the most recent observation of $\alpha=0.001$.

As expected, the online performance of Q-Learning in terms of the rewards is generally lower than the rewards for SARSA but they converge slowly as ϵ decreases (Figure 1). Also in Figures 1 and 2 we can see that Q-Learning experiences instable learning behavior as both plots are a lot more noisy and at about 20000 and 90000 episodes the rewards decrease for some period. SARSA and DQN don't show this behavior.

Even though the number of steps is not punished, all agents still learn to reduce the number of steps over time, as they do not give rewards and their goal is to take actions that do. SARSA seems to do the best job at this, which perhaps is caused by its tendency to explore more and find better strategies. Q-Learning however seems to struggle to reduce the number of steps it takes.

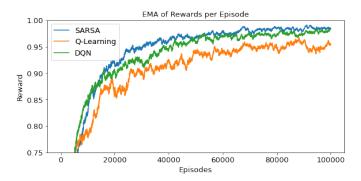


Fig. 1: Exponential moving average of the rewards achieved during training for 100000 episodes with identical hyperparameters, weight initialization and model architecture.

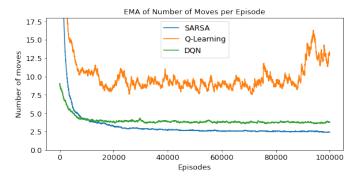


Fig. 2: Exponential moving average of the number of moves per episode achieved during training for 100000 episodes with identical hyper-parameters, weight initialization and model architecture.

As suggested by Mnih et al. [3], [5], DQN¹⁰ was able to overcome the downsides of Q-Learning which lead to an online performance which is comparable to that of SARSA in terms of reward and number of moves it achieved, and also in terms of the stability during training. It did however not learn to reduce the amounts of steps as much as SARSA.

B. Simulation Study (Non-seeded Runs)

We can confirm that the qualitative results from the seeded runs reasonably well represent the average case. The only notable exception being Q-Learning, for which most runs performed equally well to the seeded run, but some runs experienced huge increases in the number of steps, which influenced the average run dramatically, leading to an average of about 23 moves per episode after 40000 episodes.

We observed that DQN and SARSA show very comparable learning curves with DQN showing slightly faster convergence in the first 5000 episodes. SARSA showed the lowest variance in all runs and seems to be a very stable algorithm. Q-Learning on the other hand showed clear signs of divergence as for some runs the rewards consistently dropped while the number of moves consistently increased. This shows that the measures

⁹Answer to task 3 (SARSA and Q-Learning as additional algorithm) and 5 (DQN).

¹⁰Answer to task 5 for comparing DQN to SARSA and Q-Learning.

taken by Mnih et al. [3] to combat the disadvantages of Q-Learning worked and increased the stability as well as the convergence speed. We were able to verify that the gradients of the Q-Learning agents were a lot less stable than the gradients of the other agents. However, using the Glorot initialization [6] helped prevent exploding gradients from occurring.

We also found out that, unsurprisingly, the effective training time is mainly dependent on the number of steps an algorithm takes per episode. This leads to Q-Learning having by far the longest training time, especially when the parameters diverge and the number of steps increase. DQN and SARSA have relatively short training times, with SARSA being the fastest.

We can conclude that the seeded runs in our initial experiment truthfully represent the average run and therefore some level of inference is justified.

C. Hyper-parameters¹¹

Figure 3(a) depicts the rewards and number of moves per episode as a function of β and γ . We can see that the reward increases monotonically as γ is increases, suggesting that a value of $\gamma \in [0.80,1)$ should be chosen for almost all values of β . This intuitively makes sense, as we have very sparse rewards and want the agent to "backpropagate" this reward through its sequence of actions. The left plot of Figure 3 suggests that reducing γ to a value in [0.5,0.8] can teach the SARSA agent to not reduce the number of steps. Intuitively this makes sense, as the only reward will be "backpropagated" less to earlier states and thus the agent will move faster towards setting the opponent's king checkmate.

We can not see a clear relationship between β and the rewards, apart from $\beta=0$ being an inferior choice for all values of γ . In Figure 3(b) we can see that the number of steps taken by the agent decreases drastically when increasing γ from very low levels, but this effect seems larger for larger values of β . We can however see that there is a slight, but possibly insignificant, peak in the rewards around $\beta=5\cdot 10^{-3}$. In summary, for reasonably chosen values of γ the choice of β seems to not have much of an influence for training periods of around 40000 episodes.

IV. CONCLUSION

We are aware that the performance of the individual algorithms could be improved by tuning the hyper-parameters, however, this was not explicitly asked for and the focus on this assignment lies on the comparison of these algorithms from a theoretical and practical perspective.

For any deep reinforcement learning method the choice of suitable hyper-parameters for the task is crucial and can have large impacts on the training outcome. In our case, the default parameters provided to us performed very well so no need for much further consideration was necessary.

All three algorithms were able to learn to play the simplified version of chess to a very high degree even without hyper-parameter tuning. SARSA proved to be the most stable

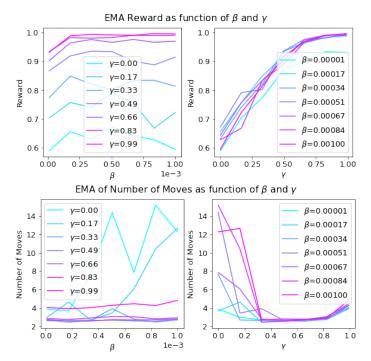


Fig. 3: Rewards and number of moves as functions of the the speed of the decaying trend β and the discount factor γ after training a SARSA agent for 40000 episodes.

algorithm, which was confirmed to be the general case with 30 non-seeded runs. Q-Learning suffers from some instabilities when training, but DQN was able to overcome all of the problems of Q-Learning and provides an off-policy method that can learn with high stability, fast convergence and a low training time comparable to SARSA. Since DQN is an off-policy method, it comes with the added advantage that it will learn an optimal policy, similar to Q-Learning.

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¹¹Answer to task 4.

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43

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A. Reproducibility

In order to reproduce the results presented in this report we provide the code on GitHub in the repositor https://github.com/TwoDigitsOneNumber/IntroRL_ChessAssignm provide a conda environment8 we environment.yaml which can be used to recreate the exact environment we used. We recommend to run the file Assignment_Train_Algorithms.ipynb before the files Assignment_Compare_Algorithms.ipynb and Assignment_Hyperparameter_Influence.ipynb54 as the latter use files generated by the former. However, even on fast hardware running the former file takes between 5-6 hours, so we provid all necessary intermediate outputs in the repository as well.

B. Code Excerpts

```
61
                                                             62
   # import libraries
                                                             63
    from types import MethodDescriptorType
                                                             64
    import numpy as np
                                                             65
    from tqdm.notebook import tqdm
                                                             66
    import os
                                                             67
    import json
                                                             68
    import time
                                                             69
8
    import random
                                                             70
Q
    from collections import namedtuple, deque
                                                             71
10
                                                             72.
11
    # import from files
                                                             73
    from Chess_env import *
                                                             74
13
                                                             75
14
15
                                                             77
16
    # ==== Epsilon-greedy Policy =====
                                                             78
17
    def EpsilonGreedy_Policy(Qvalues, allowed_a, epsilon<sup>79</sup>
80
18
                                                             81
19
                                                             82
20
        returns: tuple
21
            an action in form of a one-hot encoded
                                                             84
                 vector with the same shapeensions as
                                                             85
                                                             86
22
            an action as decimal integer (0-based)
                                                             87
23
                                                             88
24
        Assumes only a single state, i.e. online
                                                             89
            learning and NOT (mini-)batch learning.
                                                             90
25
                                                             91
26
        # get the Qvalues and the indices (relative of
                                                             92
             all Qvalues) for the allowed actions
                                                             93
27
        allowed_a_ind = np.where(allowed_a==1)[0]
                                                             94
28
        Qvalues_allowed = Qvalues[allowed_a_ind]
                                                             95
29
                                                             96
30
                                                             97
31
                       — epsilon greedy –
                                                             98
32
        # draw a random number and compare it to epsilon ^{99}
33
                                                            100
34
        rand_value = np.random.uniform(0, 1, 1)
                                                            101
35
        if rand_value < epsilon: # if the random number ^{102}
36
             is smaller than epsilon, draw a random
                                                            103
             action
             action_taken_ind_of_allwed_only = np.random 104
37
                 randint(0, len(allowed_a_ind))
                                                            105
38
        else: # greedy action
             action_taken_ind_of_allwed_only = np.argmax\( \frac{106}{107} \)
39
                 Qvalues_allowed)
                                                            108
40
41
        # get index of the action that was chosen (
             relative to all actions, not only allowed) 110
```

```
ind of action taken = allowed a ind[
         action_taken_ind_of_allwed_only]
                  – create usable output –
    # get the shapeensions of the Qvalues
    N_a, N_samples = np.shape(Qvalues) # N_samples
        must be 1
    # initialize all actions of binary mask to 0
    A_{binary_mask} = np.zeros((N_a, N_{samples}))
    # set the action that was chosen to 1
    A_binary_mask[ind_of_action_taken ,:] = 1
    return A_binary_mask, ind_of_action_taken
# ==== activation functions and it's derivatives
# relu and its derivative
def relu(x):
    return np.maximum(0,x)
def heaviside(x):
    return np. heaviside (x,0)
# sigmoid and its derivative
def sigmoid(x):
    return 1 / (1 + np.exp(-x))
def gradient_sigmoid(x):
    return sigmoid(x) * (1 - sigmoid(x))
# tanh and its derivative
def tanh(x):
    return np.tanh(x)
def gradient_tanh(x):
    return 1 - np.tanh(x)**2
# identity and its derivative
def identity(x):
    return x
def const(x):
    return np.ones(x.shape)
def act_f_and_gradient(activation_function="relu"):
    if activation_function == "relu":
        return relu, heaviside
    elif activation_function == "sigmoid":
    return sigmoid, gradient_sigmoid
elif activation_function == "tanh":
        return tanh, gradient_tanh
    else: # identity and constant 1
        return identity, const
# ==== Replay Memory for Experience Replay (with
    DQN) =====
Transition = namedtuple('Transition', ("state", "
action", "reward", "next_state", "done"))
class ReplayMemory(object):
    def __init__(self, capacity):
         self.memory = deque(maxlen=capacity)
    def push(self, *args):
```

```
111
             self.memory.append(Transition(* args))
                                                                           distribution, shape: (K+1, D+1)
112
                                                          161
                                                                       # self.W1 = np.random.randn(self.K+1, self.D
113
         def sample(self, batch_size):
                                                                           +1) # standard normal distribution,
             # if less data than batch size, return all
114
                                                                           shape: (K+1, D+1)
                 data
                                                          162
             if len(self) < batch_size:</pre>
                                                                       # self.W2 = np.random.randn(self.O, self.K
115
                                                         163
116
                 batch_size = len(self)
                                                                           +1)/np.sqrt(self.K+1) # standard normal
                                                                            distribution, shape: (O, K+1)
117
             return random.sample(self.memory, batch size
                                                                       # glorot/xavier normal initialization
                                                         164
                 )
118
                                                                       self.W2 = np.random.standard_normal((self.O,
                                                         165
                                                                            self.K+1) *np. sqrt(2/(self.K+1 + self.
119
         def __len__(self):
120
             return len (self.memory)
                                                                           O)) # standard normal distribution,
121
                                                                           shape: (O, K+1)
                                                                       # self.W2 = np.random.randn(self.O, self.K
122
                                                         166
123
                                                                           +1) # standard normal distribution,
124
                                                                           shape: (O, K+1)
125
    # ===== Neural Network ======
                                                         167
                                                                       if self.method == "dqn":
126
                                                         168
                                                                           self.W1_target = np.copy(self.W1)
127
    class NeuralNetwork(object):
                                                         169
128
                                                         170
                                                                           self.W2_target = np.copy(self.W2)
129
         def __init__(self, N_in, N_h, N_a,
                                                         171
             activation_function_1="relu",
                                                         172
             activation_function_2=None, method="
                                                         173
                                                                   def forward(self, x, target=False):
             qlearning", seed=None, capacity=100_000,
                                                        C174
             =100):
                                                                       x has shape: (D+1, 1) (constant bias 1 must
                                                         175
130
                                                                           be added beforehand added)
131
             activation functions: "relu", "sigmoid", "176
                                                                       target: if True, use the weights of the
                 tanh", None
                                                                           target network
             methods: "qlearning", "sarsa", "dqn"
                                                         177
132
133
                                                         178
                                                                       returns:
134
             self.D = N_in # input dimension (without 179)
                                                                           last logits (i.e. Qvalues) of shape (O,
                 bias)
                                                                               1)
             self.K = N_h
                             # nr hidden neurons (without180
                 bias)
             self.O = N_a
                           # nr output neurons (letter 182
                                                                       if target == True:
136
                 , not digit 0)
                                                         183
                                                                           W1 = np.copy(self.W1_target)
137
                                                         184
                                                                           W2 = np.copy(self.W2_target)
138
             # store method and seed
                                                         185
                                                                       else:
139
             self.method = method
                                                         186
                                                                           W1 = np.copy(self.W1)
140
             self.seed = seed
                                                         187
                                                                          W2 = np.copy(self.W2)
141
                                                         188
             if self.method == "dqn":
                                                                       # forward pass/propagation
142
                                                         189
                                                                       a1 = W1 @ x
143
                 self.capacity = capacity
                                                         190
144
                                                         191
                                                                       h1 = self.act_f_1(a1)
                 self.replay_memory = ReplayMemory(
                                                         192
                                                                       h1[0,:] = 1 # set first row (bias to second
                     capacity)
145
                 self.C = C
                                                                            layer) to 1 (this ignores the weights
146
                                                                           for the k+1th hidden neuron, because
147
             # set activation function and gradient
                                                                           this should not exist; this allows to
                 function
                                                                           only use matrix multiplication and
148
             self.act_f_1_name = activation_function_1
                                                                           simplify the gradients as we only need 2
149
             self.act_f_2_name = activation_function_2
                                                                            instead of 4)
             self.act_f_1, self.grad_act_f_1 =
                                                         193
150
                                                                       a2 = W2 @ h1
                 act_f_and_gradient(activation_function_194
                                                                       h2 = self.act_f_2(a2)
                                                         195
                                                                       return a1, h1, a2, h2
151
             self.act_f_2, self.grad_act_f_2 =
                                                         196
                 act_f_and_gradient(activation_function_1297
                                                                   def backward(self, R, x, Qvalues, Q_prime, a1,
                                                         198
152
                                                                       h1, a2, gamma, future_reward,
153
                                                                       action_binary_mask):
154
             # initialize the weights and biases and set199
                 grobal seed
                                                         200
                                                                       backward for methods "qlearning" and "sarsa"
             np.random.seed(self.seed)
                                                         201
155
                                                                       x has shape (D+1, 1) (constant bias 1 must
156
                                                         202
                                                                           be added beforehand)
157
             # self.W1 = np.random.randn(self.K+1, self.D
                 +1)/np.sqrt(self.D+1) # standard norm203
                                                                       set future_reward=True for future reward
                  distribution, shape: (K+1, D+1)
                                                                           with gamma>0, False for immediate reward
158
             # glorot/xavier normal initialization
             # self.W1 = np.random.randn(self.K+1, self 2004
                                                                       Q_prime must be chosen according to the
159
                                                                          method on x_prime (on- or off-policy)
                 +1)*np.sqrt(2/ (self.D+1 + self.K+1)) #
                  standard normal distribution, shape: 2805
                 +1, D+1
160
             self.W1 = np.random.standard_normal((self.K207
                                                                       # backward pass/backpropagation
                 +1, self.D+1))*np.sqrt(2/(self.D+1 + 208
                                                                       # compute the gradient of the square loss
                 self.K+1)) # standard normal
                                                                           with respect to the parameters
```

```
209
                                                           270
210
             # ==== compute TD error (aka delta) ===== 271
                                                                        # gradient of loss wrt W2
211
                                                           272
                                                                         self.dL_dW2 = self.dL_da2 @ h1.T
             # make reward of shape (O, 1)
                                                           273
212
                                                           274
                                                                        # gradient of loss wrt W1
213
             R_rep = np.tile(R, (self.O, 1))
                                                                         self.dL_dW1 = ( (self.W2.T @ self.dL_da2) *
214
                                                           275
             if future_reward: # future reward
215
                  delta = R_rep + gamma*Q_prime - Qvalues
                                                                             self.grad_act_f_1(a1) ) @ x.T
                      \# \rightarrow shape (O, 1)
             else: # immediate reward
                                                           2.77
216
217
                  delta = R_rep - Qvalues # -> shape (O278
                                                           279
                                                                    def update_parameters(self, eta):
                      1)
218
                                                           280
219
             # update only action that was taken, i.e.
                                                           281
                                                                        # gradient clipping
                  all rows apart from the one
                                                           282
                                                                        # dL_dW1_norm = np.linalg.norm(self.dL_dW1)
                  corresponding to the action taken (
                                                           283
                                                           284
                                                                         \begin{tabular}{ll} \# & if & dL_dW1\_norm >= & self.gradient\_clip: \\ \end{tabular} 
                  action index) are 0
220
             delta = delta*action_binary_mask
                                                           285
                                                                               self.dL_dW1 = self.gradient_clip *
221
                                                                             self.dL_dW1 / dL_dW1_norm
222
                                                           286
223
             self.compute_gradients(delta, a1, h1, a2,
                                                          x287
                                                                        # dL_dW2_norm = np.linalg.norm(self.dL_dW2)
224
                                                           288
                                                                        # if dL_dW2_norm >= self.gradient_clip:
             self.update_parameters(self.eta)
225
                                                           289
                                                                               self.dL_dW2 = self.gradient_clip *
226
                                                                             self.dL_dW2 / dL_dW2_norm
227
         def backward_dqn(self, batch, gamma):
                                                           290
228
                                                           291
                                                                         # update W1 and W2
229
             backward for method "dqn"
                                                           292
                                                                         self.W2 = self.W2 + eta * self.dL_dW2
230
                                                           293
                                                                         self.W1 = self.W1 + eta * self.dL_dW1
231
                                                           294
             # ==== compute targets y and feature matr 295
232
                                                           296
                  X =====
233
                                                           297
234
             # turn batch into individual tuples, numpy 298
                                                                    def train(self, env, N_episodes, eta, epsilon_0,
                  arrays, or lists
                                                                          beta, gamma, alpha=0.001, gradient_clip=1,
235
             states = batch.state
                                                                         batch_size=32, run_number=None):
236
             rewards = np.array(list(batch.reward))
                                                           299
             actions = np.array(list(batch.action))
237
                                                           300
                                                                        alpha is used as weight for the exponential
238
             next_states = list(batch.next_state)
                                                                             moving average displayed during training
239
             dones = np.array(list(batch.done))
240
                                                           301
                                                                         batch_size is only used for the DQN method.
241
             # compute targets y and feature matrix X
                                                           302
             y = np.zeros((self.O, len(dones)))
242
                                                           303
                                                           304
243
             for j in np.arange(len(dones)):
                                                                        # add training hyper parameters
244
                  if dones[j]: # if done, set y_j = r_j
                                                           305
                                                                         self. N_episodes = N_episodes
245
                                                           306
                     y[actions[j], j] = rewards[j]
                                                                         self.eta = eta
246
                                                           307
                                                                         self.epsilon_0 = epsilon_0
                      # compute Q_prime
247
                                                           308
                                                                         self.beta = beta
248
                      Q_target = self.forward(next_states09
                                                                         self.gamma = gamma
                          j], target=True)[-1]
                                                                         self.alpha = alpha
                                                           310
249
                                                                         self.gradient_clip = gradient_clip
                      y[actions[j], j] = rewards[j] +
                                                           311
                                                           312
                                                                         self.batch_size = batch_size
                          gamma*np.max(Q_target)
250
                                                           313
251
                                                           314
252
             # convert states to feature matrix X
                                                                        training_start = time.time()
                                                           315
253
             X = np.hstack((states))
                                                           316
254
                                                           317
255
                                                           318
256
             # ===== compute TD error (aka delta) ===== 319
                                                                             # initialize histories for important
257
                                                                                 metrics
             a1, h1, a2, Qvalues = self.forward(X)
258
                                                           320
                                                                             self.R_history = np.full([self.
                                                                                 N_episodes, 1], np.nan)
259
             delta = y - Qvalues # -> shape (O,
                                                           321
                                                                             self.N_moves_history = np.full([self.
                  batch size)
                                                                                 N_episodes, 1], np.nan)
260
261
             self.compute_gradients(delta, a1, h1, a2, X322
                                                                             self.dL_dW1_norm_history = np.full([self
262
             self.update_parameters(self.eta)
                                                                                  . N_episodes , 1], np.nan)
263
                                                           323
                                                                             self.dL_dW2_norm_history = np.full([self
264
                                                                                 . N_episodes, 1], np.nan)
         def compute_gradients(self, delta, a1, h1, a2, 324
265
                                                           325
                                                                             # progress bar
266
             # ==== compute gradient of the loss with 326
                                                                             episodes = tqdm(np.arange(self.
                  respect to the weights =====
                                                                                 N_episodes), unit="episodes")
267
                                                                             ema_previous = 0
268
             # common part of the gradient TODO: check 328
                  dimensions
                                                           329
                                                                             n_steps = 0
269
             self.dL_da2 = delta * self.grad_act_f_2(a2)30
```

331	for n in episodes: 369	self.replay_memory.push(X,
332	Tot it it episodes.	* * * * * * * * * * * * * * * * * * * *
		A_ind, R, X_prime, Done)
333	epsilon_f = self.epsilon_0 / (1 + 370	
	beta * n) ## DECAYING EPSILON\$71	# sample a batch of
334	Done = 0	transitions
	372	transactions = self.
	## SET DONE TO ZERO (BEGINNING	replay_memory.sample(
		1 7 = 1 1
	OF THE EPISODE)	self.batch_size)
335	i = 1 373	# turn list of transactions
		into transaction of
	## COUNTER FOR NUMBER OF ACTIONS	lists
336	374	batch = Transition(*zip(*
		· · · · · · · · · · · · · · · · · · ·
337	$S, X, allowed_a = env.$	transactions))
	Initialise_game() ## 375	
	INITIALISE GAME 376	# backward step and
338	$X = np.expand_dims(X, axis=1)$	parameter update
220	## MAKE X A77	self.backward_dqn(batch,
		* '
	TWO DIMENSIONAL ARRAY	self.gamma)
339	X = np.copy(np.vstack((np.array) 378)	
	([[1]]), X))) # add bias term 379	# update Q values indirectly by
340		updating the weights and
341	if self.method == "sarsa":	biases directly
		brases directly
342	# compute Q values for the give380	
	state 381	if Done==1: # THE EPISODE HAS
343	a1, $h1$, $a2$, $Qvalues = self$.	ENDED, UPDATEBE CAREFUL,
- 10	forward (X) # \rightarrow shape $(O,$	THIS IS THE LAST STEP OF THE
	1)	EPISODE
344	382	
345	# choose an action A using 383	if (self.method == "
343	e e e e e e e e e e e e e e e e e e e	· ·
	epsilon-greedy policy	qlearning") or (self.
346	A_binary_mask, A_ind =	method == "sarsa"):
	EpsilonGreedy_Policy(Qvalu&&4	# compute gradients and
	, allowed_a, epsilon_f) #	update weights
	_ · · · · · · · · · · · · · · · · · · ·	
	-> shape (O, 1) 385	self.backward(R, X,
347		Qvalues, None, al,
348		h1, a2, None,
349	while Done==0:	future_reward=False,
349		
	##	action_binary_mask=
	START THE EPISODE	· · · · · · · · · · · · · · · · · · ·
350	START THE EPISODE	action_binary_mask= A_binary_mask)
350 351	START THE EPISODE 386	A_binary_mask)
350 351	START THE EPISODE 386 if (self.method == "qlearning" 387	A_binary_mask) # store history
351	START THE EPISODE 386 if (self.method == "qlearning" 387 or (self.method == "dqn"): 388	A_binary_mask) # store history # todo: record max possible
	START THE EPISODE 386 if (self.method == "qlearning" 387	A_binary_mask) # store history
351	START THE EPISODE 386 if (self.method == "qlearning" 387 or (self.method == "dqn"): 388	A_binary_mask) # store history # todo: record max possible reward per episode
351 352	START THE EPISODE 386 if (self.method == "qlearning" 387 or (self.method == "dqn"): 388 # compute Q values for the given state 389	A_binary_mask) # store history # todo: record max possible reward per episode self.R_history[n] = np.copy(
351	START THE EPISODE 386 if (self.method == "qlearning" \$87 or (self.method == "dqn"): 388 # compute Q values for the given state 389 a1, h1, a2, Qvalues = self.	A_binary_mask) # store history # todo: record max possible reward per episode self.R_history[n] = np.copy(R) # reward per episode
351 352	START THE EPISODE 386 if (self.method == "qlearning")87 or (self.method == "dqn"): 388 # compute Q values for the given state 389 a1, h1, a2, Qvalues = self. forward(X) # -> shape 300	A_binary_mask) # store history # todo: record max possible reward per episode self.R_history[n] = np.copy(R) # reward per episode self.N_moves_history[n] = np
351 352 353	START THE EPISODE 386 if (self.method == "qlearning" \$87 or (self.method == "dqn"): 388 # compute Q values for the given state 389 a1, h1, a2, Qvalues = self.	A_binary_mask) # store history # todo: record max possible reward per episode self.R_history[n] = np.copy(R) # reward per episode
351 352	START THE EPISODE 386 if (self.method == "qlearning")87 or (self.method == "dqn"): 388 # compute Q values for the given state 389 a1, h1, a2, Qvalues = self. forward(X) # -> shape 300	A_binary_mask) # store history # todo: record max possible reward per episode self.R_history[n] = np.copy(R) # reward per episode self.N_moves_history[n] = np
351 352 353 354	START THE EPISODE 386 if (self.method == "qlearning" \$87 or (self.method == "dqn"): 388 # compute Q values for the given state a1, h1, a2, Qvalues = self. forward(X) # -> shape 390 O, 1)	A_binary_mask) # store history # todo: record max possible reward per episode self.R_history[n] = np.copy(R) # reward per episode self.N_moves_history[n] = np .copy(i) # nr moves per
351 352 353	START THE EPISODE 386 if (self.method == "qlearning" \$87 or (self.method == "dqn"): 388 # compute Q values for the given state 389 a1, h1, a2, Qvalues = self. forward(X) # -> shape 390 O, 1) # choose an action A using 391	A_binary_mask) # store history # todo: record max possible reward per episode self.R_history[n] = np.copy(R) # reward per episode self.N_moves_history[n] = np .copy(i) # nr moves per episode
351 352 353 354 355	START THE EPISODE 386 if (self.method == "qlearning" B87 or (self.method == "dqn"): 388 # compute Q values for the given state 389 a1, h1, a2, Qvalues = self. forward(X) # -> shape 390 O, 1) # choose an action A using 391 epsilon-greedy policy 392	A_binary_mask) # store history # todo: record max possible reward per episode self.R_history[n] = np.copy(R) # reward per episode self.N_moves_history[n] = np .copy(i) # nr moves per episode # store norm of gradients
351 352 353 354	START THE EPISODE 386 if (self.method == "qlearning" \$87 or (self.method == "dqn"): 388 # compute Q values for the given state 389 a1, h1, a2, Qvalues = self. forward(X) # -> shape 390 O, 1) # choose an action A using 391 epsilon-greedy policy 392 A_binary_mask, A_ind = 393	A_binary_mask) # store history # todo: record max possible reward per episode self.R_history[n] = np.copy(R) # reward per episode self.N_moves_history[n] = np .copy(i) # nr moves per episode # store norm of gradients self.dL_dW1_norm_history[n]
351 352 353 354 355	START THE EPISODE 386 if (self.method == "qlearning" B87 or (self.method == "dqn"): 388 # compute Q values for the given state 389 a1, h1, a2, Qvalues = self. forward(X) # -> shape 390 O, 1) # choose an action A using 391 epsilon-greedy policy 392	A_binary_mask) # store history # todo: record max possible reward per episode self.R_history[n] = np.copy(R) # reward per episode self.N_moves_history[n] = np .copy(i) # nr moves per episode # store norm of gradients
351 352 353 354 355	START THE EPISODE 386 if (self.method == "qlearning" \$87 or (self.method == "dqn"): 388 # compute Q values for the given state 389 a1, h1, a2, Qvalues = self. forward(X) # -> shape 390 O, 1) # choose an action A using 391 epsilon-greedy policy 392 A_binary_mask, A_ind = 393	A_binary_mask) # store history # todo: record max possible reward per episode self.R_history[n] = np.copy(R) # reward per episode self.N_moves_history[n] = np .copy(i) # nr moves per episode # store norm of gradients self.dL_dW1_norm_history[n]
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351 352 353 354 355	start the EPISODE if (self.method == "qlearning" \$87 or (self.method == "dqn"): 388 # compute Q values for the given state 389 al, hl, a2, Qvalues = self. forward(X) # -> shape 390 O, 1) # choose an action A using 391 epsilon-greedy policy 392 A_binary_mask, A_ind = 393 EpsilonGreedy_Policy(Qvalues, allowed_a, epsilon_f) # -> shape 394	A_binary_mask) # store history # todo: record max possible reward per episode self.R_history[n] = np.copy(R) # reward per episode self.N_moves_history[n] = np .copy(i) # nr moves per episode # store norm of gradients self.dL_dW1_norm_history[n] = np.linalg.norm(self. dL_dW1) self.dL_dW2_norm_history[n]
351 352 353 354 355 356	start the episode if (self.method == "qlearning" \$87 or (self.method == "dqn"): 388 # compute Q values for the given state 389 a1, h1, a2, Qvalues = self. forward(X) # -> shape 390 O, 1) # choose an action A using 391 epsilon-greedy policy 392 A_binary_mask, A_ind = 393 EpsilonGreedy_Policy(Qvalues, allowed_a,	A_binary_mask) # store history # todo: record max possible reward per episode self.R_history[n] = np.copy(R) # reward per episode self.N_moves_history[n] = np .copy(i) # nr moves per episode # store norm of gradients self.dL_dW1_norm_history[n] = np.linalg.norm(self. dL_dW1) self.dL_dW2_norm_history[n] = np.linalg.norm(self.
351 352 353 354 355 356	start the EPISODE if (self.method == "qlearning" \$87 or (self.method == "dqn"): 388 # compute Q values for the	A_binary_mask) # store history # todo: record max possible reward per episode self.R_history[n] = np.copy(R) # reward per episode self.N_moves_history[n] = np .copy(i) # nr moves per episode # store norm of gradients self.dL_dW1_norm_history[n] = np.linalg.norm(self. dL_dW1) self.dL_dW2_norm_history[n]
351 352 353 354 355 356	start the EPISODE if (self.method == "qlearning" \$87 or (self.method == "dqn"): 388 # compute Q values for the given state 389 al, hl, a2, Qvalues = self. forward(X) # -> shape 390 O, 1) # choose an action A using 391 epsilon-greedy policy 392 A_binary_mask, A_ind = 393 EpsilonGreedy_Policy(Qvalues, allowed_a, epsilon_f) # -> shape 394	A_binary_mask) # store history # todo: record max possible reward per episode self.R_history[n] = np.copy(R) # reward per episode self.N_moves_history[n] = np .copy(i) # nr moves per episode # store norm of gradients self.dL_dW1_norm_history[n] = np.linalg.norm(self. dL_dW1) self.dL_dW2_norm_history[n] = np.linalg.norm(self.
351 352 353 354 355 356	start the episode if (self.method == "qlearning" \$87 or (self.method == "dqn"): 388 # compute Q values for the given state 389 al, hl, a2, Qvalues = self. forward(X) # -> shape 300 O, 1) # choose an action A using 391 epsilon-greedy policy 392 A_binary_mask, A_ind = 393 EpsilonGreedy_Policy(Qvalues, allowed_a, epsilon_f) # -> shape 304 O, 1) 395	A_binary_mask) # store history # todo: record max possible reward per episode self.R_history[n] = np.copy(R) # reward per episode self.N_moves_history[n] = np .copy(i) # nr moves per episode # store norm of gradients self.dL_dW1_norm_history[n] = np.linalg.norm(self. dL_dW1) self.dL_dW2_norm_history[n] = np.linalg.norm(self. dL_dW2)
351 352 353 354 355 356	start the episode if (self.method == "qlearning" \$87 or (self.method == "dqn"): 388 # compute Q values for the given state 389 al, hl, a2, Qvalues = self. forward(X) # -> shape 300 O, 1) # choose an action A using 391 epsilon-greedy policy 392 A_binary_mask, A_ind = 393 EpsilonGreedy_Policy(Qvalues, allowed_a, epsilon_f) # -> shape 304 O, 1) # take action and observe rewars96	A_binary_mask) # store history # todo: record max possible reward per episode self.R_history[n] = np.copy(R) # reward per episode self.N_moves_history[n] = np .copy(i) # nr moves per episode # store norm of gradients self.dL_dW1_norm_history[n] = np.linalg.norm(self. dL_dW1) self.dL_dW2_norm_history[n] = np.linalg.norm(self. dL_dW2) # compute exponential moving
351 352 353 354 355 356 357 358 359	start the episode if (self.method == "qlearning" \$87 or (self.method == "dqn"): 388 # compute Q values for the given state 389 al, hl, a2, Qvalues = self. forward(X) # -> shape 390 O, 1) # choose an action A using 391 epsilon-greedy policy 392 A_binary_mask, A_ind = 393 EpsilonGreedy_Policy(Qvalues, allowed_a, epsilon_f) # -> shape 394 O, 1) # take action and observe rewars96 R and state S_prime	A_binary_mask) # store history # todo: record max possible reward per episode self.R_history[n] = np.copy(R) # reward per episode self.N_moves_history[n] = np .copy(i) # nr moves per episode # store norm of gradients self.dL_dW1_norm_history[n] = np.linalg.norm(self. dL_dW1) self.dL_dW2_norm_history[n] = np.linalg.norm(self. dL_dW2) # compute exponential moving average (EMA) to
351 352 353 354 355 356	start the episode if (self.method == "qlearning" \$87 or (self.method == "dqn"): 388 # compute Q values for the given state 389 al, hl, a2, Qvalues = self. forward(X) # -> shape 390 O, 1) # choose an action A using 391 epsilon-greedy policy 392 A_binary_mask, A_ind = 393 EpsilonGreedy_Policy(Qvalues, allowed_a, epsilon_f) # -> shape 394 O, 1) # take action and observe rewars96 R and state S_prime S_prime, X_prime,	A_binary_mask) # store history # todo: record max possible reward per episode self.R_history[n] = np.copy(R) # reward per episode self.N_moves_history[n] = np .copy(i) # nr moves per episode # store norm of gradients self.dL_dW1_norm_history[n] = np.linalg.norm(self. dL_dW1) self.dL_dW2_norm_history[n] = np.linalg.norm(self. dL_dW2) # compute exponential moving average (EMA) to display during training
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351 352 353 354 355 356 357 358 359	start the episode if (self.method == "qlearning" B87 or (self.method == "dqn"): 388 # compute Q values for the given state 389 a1, h1, a2, Qvalues = self. forward(X) # -> shape 390 O, 1) # choose an action A using 391 epsilon-greedy policy 392 A_binary_mask, A_ind = 393 EpsilonGreedy_Policy(Qvalues, allowed_a, epsilon_f) # -> shape 394 O, 1) # take action and observe reward 96 R and state S_prime S_prime, X_prime, allowed_a_prime, R, Done = 397	A_binary_mask) # store history # todo: record max possible reward per episode self.R_history[n] = np.copy(R) # reward per episode self.N_moves_history[n] = np .copy(i) # nr moves per episode # store norm of gradients self.dL_dW1_norm_history[n] = np.linalg.norm(self. dL_dW1) self.dL_dW2_norm_history[n] = np.linalg.norm(self. dL_dW2) # compute exponential moving average (EMA) to display during training ema = alpha*R + (1-alpha)*
351 352 353 354 355 356 357 358 359 360	start the episode if (self.method == "qlearning" \$87 or (self.method == "dqn"): 388 # compute Q values for the given state 389 al, hl, a2, Qvalues = self. forward(X) # -> shape 390 O, 1) # choose an action A using 391 epsilon-greedy policy 392 A_binary_mask, A_ind = 393 EpsilonGreedy_Policy(Qvalues, allowed_a, epsilon_f) # -> shape 394 O, 1) # take action and observe reward 96 R and state S_prime S_prime, X_prime, allowed_a_prime, R, Done = 397 env.OneStep(A_ind)	A_binary_mask) # store history # todo: record max possible reward per episode self.R_history[n] = np.copy(R) # reward per episode self.N_moves_history[n] = np .copy(i) # nr moves per episode # store norm of gradients self.dL_dW1_norm_history[n] = np.linalg.norm(self. dL_dW1) self.dL_dW2_norm_history[n] = np.linalg.norm(self. dL_dW2) # compute exponential moving average (EMA) to display during training ema = alpha*R + (1-alpha)* ema_previous
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351 352 353 354 355 356 357 358 359 360 361	if (self.method == "qlearning" B87 or (self.method == "dqn"): 388 # compute Q values for the	# store history # todo: record max possible reward per episode self.R_history[n] = np.copy(R) # reward per episode self.N_moves_history[n] = np .copy(i) # nr moves per episode # store norm of gradients self.dL_dW1_norm_history[n] = np.linalg.norm(self. dL_dW1) self.dL_dW2_norm_history[n] = np.linalg.norm(self. dL_dW2) # compute exponential moving average (EMA) to display during training ema = alpha*R + (1-alpha)* ema_previous if n == 0: # first episode ema = R
351 352 353 354 355 356 357 358 359 360	start the episode if (self.method == "qlearning" \$87 or (self.method == "dqn"): 388 # compute Q values for the given state 389 al, hl, a2, Qvalues = self. forward(X) # -> shape 390 O, 1) # choose an action A using 391 epsilon-greedy policy 392 A_binary_mask, A_ind = 393 EpsilonGreedy_Policy(Qvalues, allowed_a, epsilon_f) # -> shape 394 O, 1) # take action and observe rewars 96 R and state S_prime S_prime, X_prime, allowed_a_prime, R, Done = 397 env.OneStep(A_ind) X_prime = np.expand_dims(X_prins 98)	A_binary_mask) # store history # todo: record max possible reward per episode self.R_history[n] = np.copy(R) # reward per episode self.N_moves_history[n] = np .copy(i) # nr moves per episode # store norm of gradients self.dL_dW1_norm_history[n] = np.linalg.norm(self. dL_dW1) self.dL_dW2_norm_history[n] = np.linalg.norm(self. dL_dW2) # compute exponential moving average (EMA) to display during training ema = alpha*R + (1-alpha)* ema_previous if n == 0: # first episode
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351 352 353 354 355 356 357 358 359 360 361 362	if (self.method == "qlearning" B87 or (self.method == "dqn"): 388 # compute Q values for the given state 389 al, hl, a2, Qvalues = self. forward(X) # -> shape 300 O, 1) # choose an action A using 391 epsilon-greedy policy 392 A_binary_mask, A_ind = 393 EpsilonGreedy_Policy(Qvalues, allowed_a, epsilon_f) # -> shape 304 O, 1) # take action and observe reward 006 R and state S_prime S_prime, X_prime, allowed_a_prime, R, Done = 397 env.OneStep(A_ind) X_prime = np.expand_dims(X_prime) , axis=1) 399 X_prime = np.copy(np.vstack((np40))	A_binary_mask) # store history # todo: record max possible reward per episode self.R_history[n] = np.copy(R) # reward per episode self.N_moves_history[n] = np .copy(i) # nr moves per episode # store norm of gradients self.dL_dW1_norm_history[n] = np.linalg.norm(self. dL_dW1) self.dL_dW2_norm_history[n] = np.linalg.norm(self. dL_dW2) # compute exponential moving average (EMA) to display during training ema = alpha*R + (1-alpha)* ema_previous if n == 0: # first episode ema = R ema_previous = ema if run_number is not None: episodes.set_description
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351 352 353 354 355 356 357 358 359 360 361 362 363 364 365 366	if (self.method == "qlearning" ß87 or (self.method == "dqn"): 388 # compute Q values for the given state	A_binary_mask) # store history # todo: record max possible reward per episode self.R_history[n] = np.copy(R) # reward per episode self.N_moves_history[n] = np .copy(i) # nr moves per episode # store norm of gradients self.dL_dW1_norm_history[n] = np.linalg.norm(self. dL_dW1) self.dL_dW2_norm_history[n] = np.linalg.norm(self. dL_dW2) # compute exponential moving average (EMA) to display during training ema = alpha*R + (1-alpha)* ema_previous if n == 0: # first episode ema = R ema_previous = ema if run_number is not None: episodes.set_description (f"Run = {run_number }; EMA Reward = {ema :.2f}") else:
351 352 353 354 355 356 357 358 359 360 361 362 363 364 365 366 367	if (self.method == "qlearning" p87 or (self.method == "dqn"): 388 # compute Q values for the given state 389 a1, h1, a2, Qvalues = self. forward(X) # -> shape 390 O, 1) # choose an action A using 391 epsilon-greedy policy 392 A_binary_mask, A_ind = 393 EpsilonGreedy_Policy(Qvalues, allowed_a, epsilon_f) # -> shape 394 O, 1) # take action and observe rewars96 R and state S_prime S_prime, X_prime, allowed_a_prime, R, Done = 397 env.OneStep(A_ind) X_prime = np.expand_dims(X_prinare) X_prime = np.copy(np.vstack((np400 array([[1]]), X_prime))) #01 add bias term 402 n_steps += 1 if self.method == "dqn": 403 404	# store history # todo: record max possible reward per episode self.R_history[n] = np.copy(R) # reward per episode self.N_moves_history[n] = np .copy(i) # nr moves per episode # store norm of gradients self.dL_dW1_norm_history[n] = np.linalg.norm(self. dL_dW1) self.dL_dW2_norm_history[n] = np.linalg.norm(self. dL_dW2) # compute exponential moving average (EMA) to display during training ema = alpha*R + (1-alpha)* ema_previous if n == 0: # first episode ema = R ema_previous = ema if run_number is not None: episodes.set_description
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351 352 353 354 355 356 357 358 359 360 361 362 363 364 365 366 367	if (self.method == "qlearning" p87 or (self.method == "dqn"): 388 # compute Q values for the given state 389 a1, h1, a2, Qvalues = self. forward(X) # -> shape 390 O, 1) # choose an action A using 391 epsilon-greedy policy 392 A_binary_mask, A_ind = 393 EpsilonGreedy_Policy(Qvalues, allowed_a, epsilon_f) # -> shape 394 O, 1) # take action and observe rewars96 R and state S_prime S_prime, X_prime, allowed_a_prime, R, Done = 397 env.OneStep(A_ind) X_prime = np.expand_dims(X_prinare) X_prime = np.copy(np.vstack((np400 array([[1]]), X_prime))) #01 add bias term 402 n_steps += 1 if self.method == "dqn": 403 404	# store history # todo: record max possible reward per episode self.R_history[n] = np.copy(R) # reward per episode self.N_moves_history[n] = np .copy(i) # nr moves per episode # store norm of gradients self.dL_dW1_norm_history[n] = np.linalg.norm(self. dL_dW1) self.dL_dW2_norm_history[n] = np.linalg.norm(self. dL_dW2) # compute exponential moving average (EMA) to display during training ema = alpha*R + (1-alpha)* ema_previous if n == 0: # first episode ema = R ema_previous = ema if run_number is not None: episodes.set_description

405	446	# update target network
406 407	break 447	every C steps self.W1_target = np.copy(
408	else: # IF THE EPISODE IS NOT	self.W1)
400	OVER 448	self.W2_target = np.copy(
409 410	if self.method == "qlearnin449	self.W2)
	":	
411	# chose next action off451 policy 452	training_end = time.time()
412	policy 452 Q_prime = np.max(self.	<pre>self.training_time_in_seconds = training_end - training_start</pre>
	forward (X_prime) 453	
412	[-1]) 454	return None
413 414	455 elif self.method == "sarsa'456	
415	# chose next action on-457	except KeyboardInterrupt as e:
416	policy 458	# return nothing
416 417	459 a1_prime, h1_prime, 460	<pre>training_end = time.time() self.training_time_in_seconds =</pre>
,	a2_prime,	training_end - training_start
	Qvalues_prime = se461	N .
	. forward (X_prime) 462 -> shape (N_a, 1) 463	return None
418	464	
419	# chose next action and 465	<pre>def save(self, name_extension=None):</pre>
420	save it 466 A_binary_mask_prime, 467	<pre># create directory for the model name = f"{self.method}_{self.act_f_1_name}_{</pre>
120	A_ind_prime =	self.act_f_2_name}"
	EpsilonGreedy_Polic468	if name_extension is not None:
	(Qvalues_prime, 469 allowed_a_prime, 470	<pre>name += f"_{name_extension}"</pre>
	epsilon_f) 471	<pre>path = f"models/{name}"</pre>
421	472	if not os.path.isdir(path): os.mkdir(path)
422	# get Qvalue of next 473 action 474	<pre>print(f"saving to: {path}")</pre>
423	Q_prime = Qvalues_prime475	# save weights
	A_ind_prime] 476	np.save(f"{path}/W1.npy", self.W1)
424 425	477 478	$np.save(f"{path}/W2.npy", self.W2)$
426	if (self.method == "479")	# save training history
	qlearning") or (self. 480	<pre>np.save(f"{path}/training_history_R.npy",</pre>
427	method == "sarsa"): # backpropagation and 481	<pre>self.R_history) np.save(f"{path}/training_history_N_moves.</pre>
727	weight update	npy", self. N_moves_history)
428	self.backward(R, X, 482	np.save(f"{path}/
	Qvalues, Q_prime, a1, h1, a2, self.gamma	<pre>training_history_dL_dW1_norm.npy", self. dL_dW1_norm_history)</pre>
	, future_reward=Tru483	np.save(f"{path}/
	, action_binary_mask	<pre>training_history_dL_dW2_norm.npy", self.</pre>
429	=A_binary_mask) 484	dL_dW2_norm_history)
430	485	# save training parameters and other general
431	# NEXT STATE AND CO. BECOME	info
432	ACTUAL STATE 486 if self.method == "sarsa": 487	<pre>params = { "method": self.method,</pre>
433	A_binary_mask = np.copy488	"N_episodes": self.N_episodes,
42.4	A_binary_mask_prime \$9	"eta": self.eta,
434	A_ind = np.copy(490 A_ind_prime) 491	"epsilon_0": self.epsilon_0, "beta": self.beta,
435	$a1 = np.copy(a1_prime) 492$	"gamma": self.gamma,
436	$h1 = np.copy(h1_prime)$ 493	"alpha": self.alpha,
437 438	a2 = np.copy(a2_prime) 494 Qvalues = np.copy(495	<pre># "gradient_clip": self.gradient_clip , "seed": self.seed ,</pre>
	Qvalues_prime) 496	"D": self.D,
439 440	S = np.copy(S_prime) 497 X = np.copy(X prime) 498	"K": self.K,
440 441	$X = np.copy(X_prime)$ 498 allowed_a = np.copy(499	"O": self.O, "training_time_in_seconds": self.
	allowed_a_prime)	training_time_in_seconds
442	500	} if salf mathed "den":
443	i += 1 # UPDATE COUNTER FC%101 NUMBER OF ACTIONS 502	<pre>if self.method == "dqn": params["capacity"] = self.capacity</pre>
444	503	params["batch_size"] = self.batch_size
445	if (self.method == "dqn") and 604 n_steps % self.C == 0):	params["C"] = self.C
	n_steps 70 seri.C == 0):	

```
505
               with open(f"{path}/training_parameters.json"
                       "w") as f:
506
                    json.dump(params, f)
507
508
509
      \begin{tabular}{ll} def & load\_from (method , act\_f\_1 , act\_f\_2 , \\ \end{tabular} 
           name_extension=None):
          # read values and store in neural network
511
               instance
512
          name = f''\{method\}_{act_f_1}_{act_f_2}''
513
          if name_extension is not None:
514
               name += f"_{name_extension}"
515
                                                                    5
          path = f"models/{name}"
                                                                    6
517
          # print(f"loading from: {path}")
                                                                    7
518
519
          # initialize neural network
          nn = NeuralNetwork (0,0,0, activation_function_1\frac{1}{70}
520
               act_f_1, activation_function_2=act_f_2,
                                                                    11
               method=method)
                                                                    12
521
                                                                    13
522
          # network weights
                                                                    14
          nn.W1 = np.load(f"{path}/W1.npy")
nn.W2 = np.load(f"{path}/W2.npy")
523
                                                                    15
524
                                                                    16
525
                                                                    17
526
          # network training history
                                                                    18
          nn.R_history = np.load(f"{path}/
527
                                                                    19
               training_history_R.npy")
528
          nn. N_moves_history = np.load(f"{path}/
                                                                    20
               training_history_N_moves.npy
                                                                   2.1
          nn.dL_dW1\_norm\_history = np.load(f"{path}/
529
                                                                    22
               training_history_dL_dW1_norm.npy")
                                                                    23
          nn.dL\_dW2\_norm\_history = np.load(f^{**}\{path\}/
530
                                                                   24
               training_history_dL_dW2_norm.npy")
                                                                   25
531
532
          # network training parameters
          with open(f"{path}/training_parameters.json",
533
                ") as f:
                                                                   2.7
534
               params = json.load(f)
535
                                                                    28
               # set parameters to the network instance
nn.method = params["method"]
nn.N_episodes = int(params["N_episodes"])
536
537
538
539
               nn.eta = float(params["eta"])
                                                                    30
               nn.epsilon_0 = float(params["epsilon_0"])
nn.beta = float(params["beta"])
540
                                                                   31
541
                                                                    32
               nn.gamma = float (params ["gamma"])
542
                                                                    33
543
               nn.alpha = float(params["alpha"])
                                                                    34
               # nn.gradient_clip = float(params["
544
                                                                    35
                    gradient_clip^"])
545
                                                                    36
546
                    nn.seed = int(params["seed"])
547
               except:
                                                                    37
548
                    nn.seed = params["seed"]
                                                                    38
               nn.D = int(params["D"])
nn.K = int(params["K"])
549
550
                                                                   39
               nn.O = int(params["O"])
                                                                    40
               nn.training_time_in_seconds = float(params["1"
552
                    training_time_in_seconds"])
                                                                   42
553
               if nn.method == "dqn":
554
                                                                   43
                    nn.capacity = int(params["capacity"])
555
556
                    nn.batch_size = int(params["batch_size"
557
                    nn.C = int(params["C"])
                                                                   46
558
559
                                                                    47
          if nn.method == "dqn":
560
                                                                   48
561
               nn.W1_target = np.copy(nn.W1)
562
               nn.W2\_target = np.copy(nn.W2)
                                                                   49
563
564
          return nn
                                                                    50
                                                                    51
```

Listing 1: Object oriented implementation of the neural networks, which can be instantiated with specifications for the model architecture and a method: "sarsa", "qlearning" or "dqn". The training loop will adapt automatically.

```
import numpy as np
import matplotlib.pyplot as plt
def moving_average(a, n=3) :
    steps = len(a)-n
    ma = np. full(steps, np.nan)
    for i in range(steps):
        ma[i] = np.mean(a[i:i+n])
    return ma, np.arange(steps)
def exponential_moving_average(array, alpha=0.001):
    Calculate exponential moving average of an array
    ema = np.full(len(array), np.nan)
    ema[0] = array[0]
    for i in range(1, len(array)):
        ema[i] = alpha * array[i] + (1 - alpha) *
            ema[i-1]
    return ema
def save_avg_statistics(histories, method):
    # unpack histories
    R_histories = [history[0] for history in
        histories 1
    N_moves_histories = [history[1] for history in
        histories 1
    training_times = [history[2] for history in
        histories]
    layer1_gradient_norms_histories = [history[3]
        for history in histories]
    layer2_gradient_norms_histories = [history[4]
        for history in histories]
    # turn into numpy arrays
    R_histories = np.hstack(R_histories)
    N_moves_histories = np.hstack(N_moves_histories)
    training_times = np.hstack(training_times)
    layer1_gradient_norms_histories = np.hstack(
        layer1_gradient_norms_histories)
    layer2_gradient_norms_histories = np.hstack(
        layer2_gradient_norms_histories)
    # compute mean and standard deviation for each
        row of the histories
    R_{mean} = np.mean(R_{histories}, axis=1)
    R_{std} = np. std (R_{histories}, axis=1)
    N_moves_mean = np.mean(N_moves_histories, axis
        =1
    N_moves_std = np.std(N_moves_histories, axis=1)
    layer1_gradient_norms_mean = np.mean(
        layer1_gradient_norms_histories , axis=1)
    layer1_gradient_norms_std = np.std(
        layer1_gradient_norms_histories , axis=1)
    layer2_gradient_norms_mean = np.mean(
        layer2_gradient_norms_histories , axis=1)
    layer2_gradient_norms_std = np.std(
        layer2_gradient_norms_histories , axis=1)
    # save to file
```

```
52
        np.\,save\,(\,f\,"\,s\,t\,a\,t\,i\,s\,t\,i\,c\,s\,/\{\,method\,\}\_R\_mean\,.\,npy\,"\,,
             R_mean)
53
        np.save(f"statistics/{method}_R_std.npy", R_std)
54
        np.\,save\,(\,f\,"\,s\,t\,a\,t\,i\,s\,t\,i\,c\,s\,/\,\{\,method\,\}\_N\_moves\_mean\,.\,npy\,"\,,
55
              N_moves_mean)
56
        np.save(f"statistics/{method}_N_moves_std.npy",
             N_moves_std)
57
58
        np.save(f"statistics/{method}_training_times.npy
             ", training_times)
59
60
        np.save(f"statistics/{method}
              _layer1_gradient_norms_mean.npy",
             layer1_gradient_norms_mean)
61
        np.save(f"statistics/{method}
              _layer1_gradient_norms_std.npy",
             layer1_gradient_norms_std)
62
63
        np.save(f"statistics/{method}
              _layer2_gradient_norms_mean.npy",
             layer2_gradient_norms_mean)
64
        np.save(f"statistics/{method}
              _layer2_gradient_norms_std.npy",
             layer2_gradient_norms_std)
65
66
67
    def load_avg_statistics(method):
        R_{mean} = np.load(f"statistics/{method}_{R_{mean}}.
68
             npy")
69
        R_std = np.load(f"statistics/{method}_R_std.npy"
             )
        N_{moves\_mean} = np.load(f"statistics/{method})
71
             _N_moves_mean.npy")
        N_moves_std = np.load(f"statistics/{method}
72
             _N_moves_std.npy")
73
        training_times = np.load(f"statistics/{method}
74
             _training_times.npy")
75
76
        layer1_gradient_norms_mean = np.load(f"
             statistics / { method }
              _layer1_gradient_norms_mean.npy")
        layer1_gradient_norms_std = np.load(f"statistics
77
             /{method}_layer1_gradient_norms_std.npy")
78
79
        layer2_gradient_norms_mean = np.load(f"
             statistics / { method }
              _layer2_gradient_norms_mean.npy")
80
        layer2_gradient_norms_std = np.load(f"statistics
             /{method}_layer2_gradient_norms_std.npy")
81
82.
        return R_mean, R_std, N_moves_mean, N_moves_std,
              training_times, layer1_gradient_norms_mean,
              layer1_gradient_norms_std ,
             layer2_gradient_norms_mean,
             layer2_gradient_norms_std
83
84
85
    def printable_name(method):
86
        if method == "sarsa":
87
             return "SARSA"
        elif method == "qlearning":
88
             return "Q-Learning"
89
90
        elif method == "dqn":
             return "DQN"
91
92
        else:
93
             return None
```

Listing 2: Helper functions used throughout the implementation of the neural network and the notebooks, where the experiments were conducted.