

# KING MONGKUT'S UNIVERSITY OF TECHNOLOGY NORTH BANGKOK



## Application of PID controller to control mobile robot position

Tanawin Siriwan 6203014610060 sec 1  
College of industrial technology  
Department of Mechanical engineering Technology



Asst. prof. Dr.Chanin Joochim

## Topic

- Introduction
- Object
- Scope
- Making process
- Principle
- Test
- Problem
- Summarize

# Introduction



# Opjective

1

เพื่อศึกษาการใช้ encoder  
ในการควบคุมตำแหน่งการเคลื่อนที่ของหุ่นยนต์

2

เพื่อศึกษาการเขียนโปรแกรม Arduino  
ในการควบคุมตำแหน่งของหุ่นยนต์

3

เพื่อออกรูปแบบหุ่นยนต์ที่ควบคุม  
ตำแหน่งการเคลื่อนที่ด้วย PID

# Scope

1

ใช้ **encoder** ที่ติดอยู่กับมอเตอร์ในการอ่านค่าตำแหน่งของหุ่นยนต์

2

หุ่นยนต์สามารถเคลื่อนที่ในรูปแบบสี่เหลี่ยมจัตุรัส

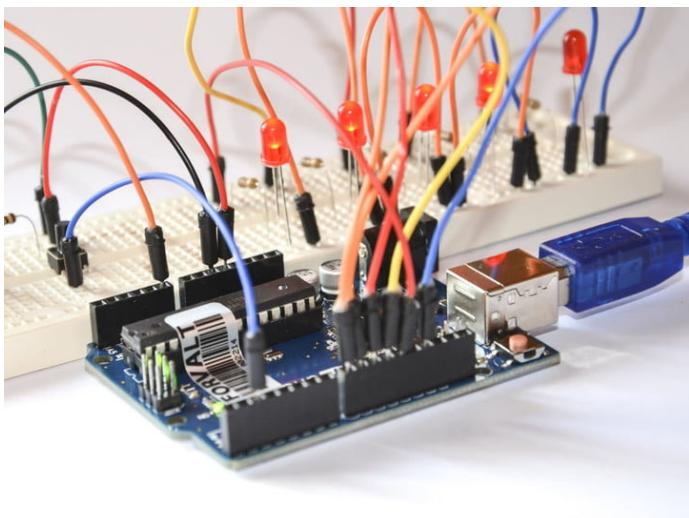
3

หุ่นยนต์สามารถเคลื่อนที่ในรูปแบบสามเหลี่ยมนูนจาก

4

พื้นที่ในการเคลื่อนที่ในพื้นราบเท่านั้น

Hard ware



Soft ware



## Hard ware



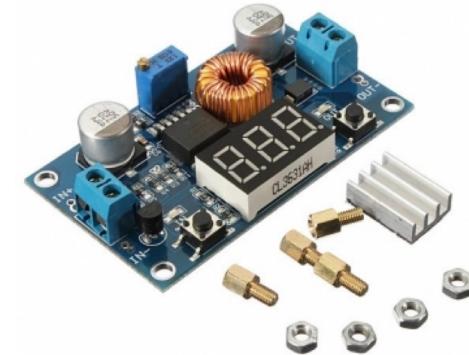
Arduino DUE



DC motor driver

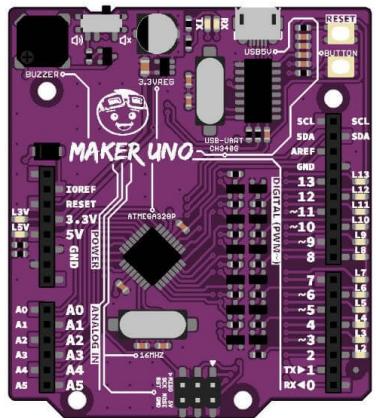


Vapcell 18650 battery  
3600mAh 3.7v

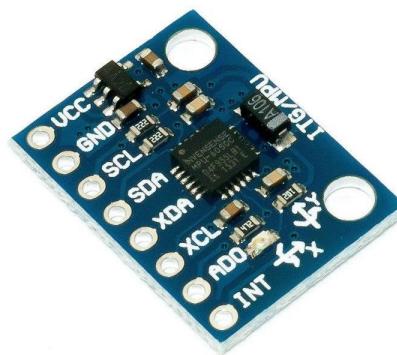


DC to DC stepdown

## Hard ware



Maker UNO



GY - 521



LCD i2c display 20 x 4

# Hard ware



Toggle switch on - off

DC motor 12V encoder



Ball wheel



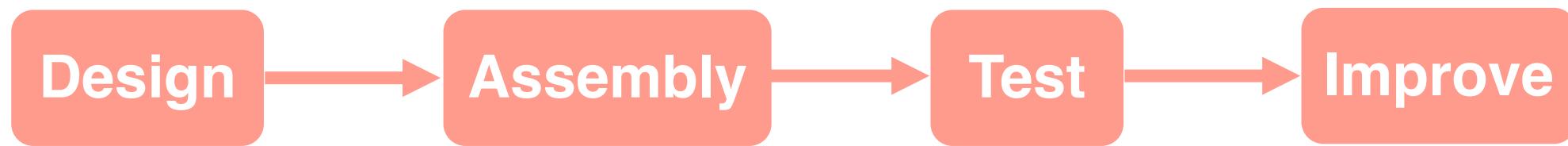
wheel



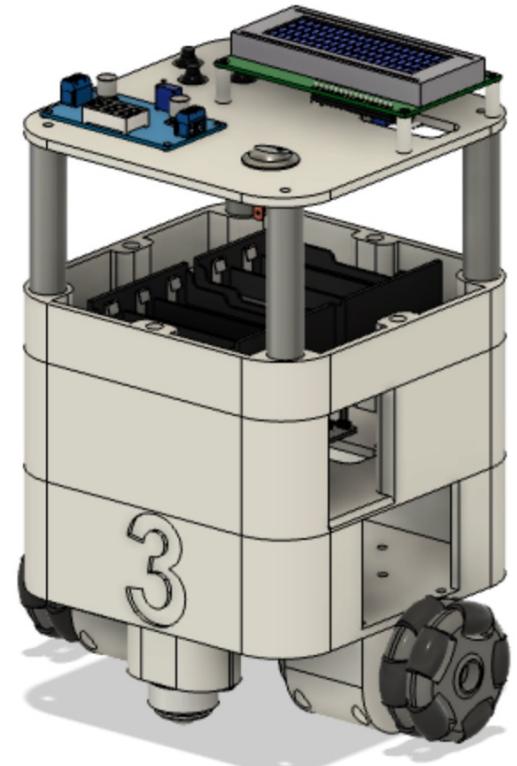
Soft ware



# Making process



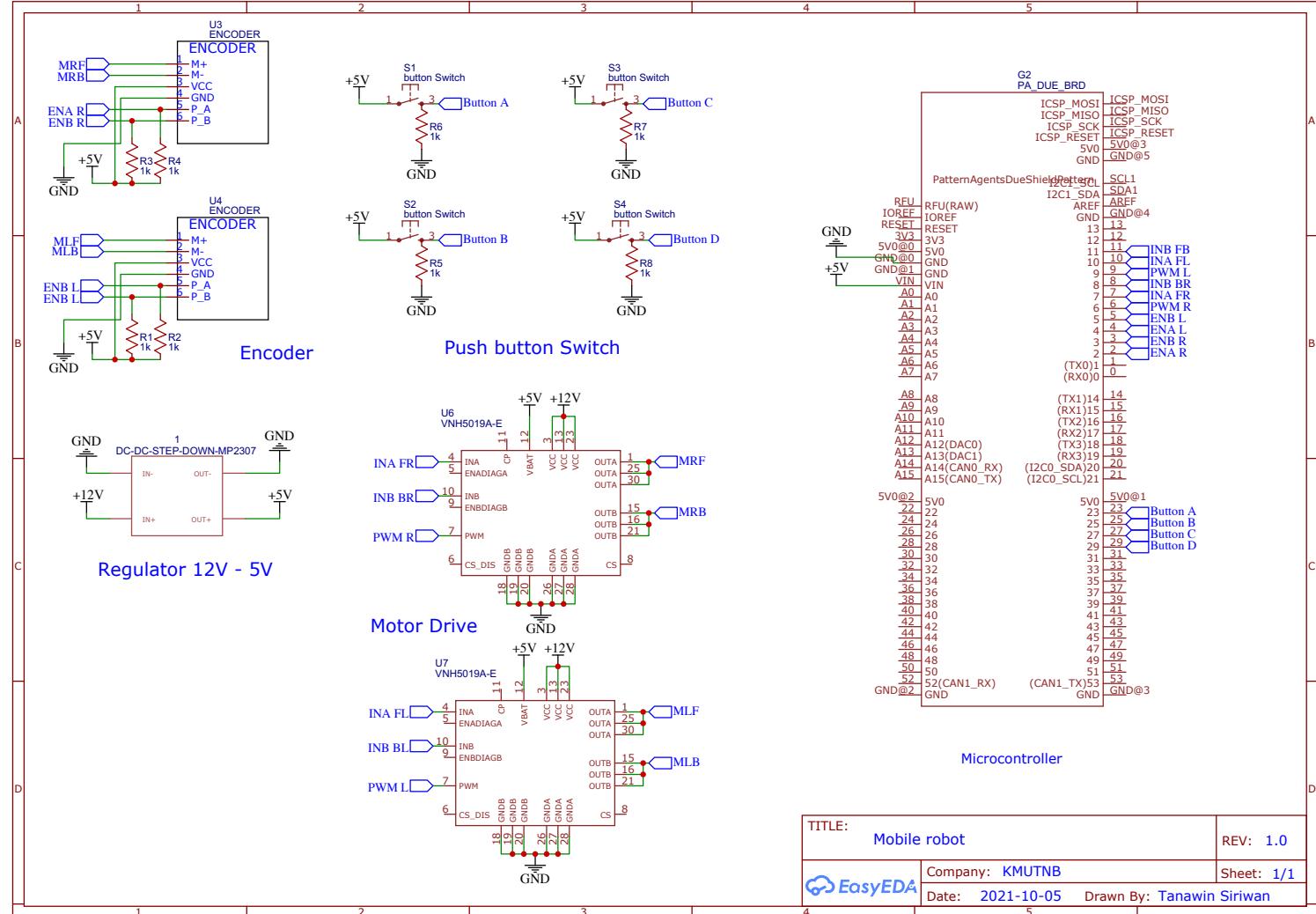
## Mechanicsm Design



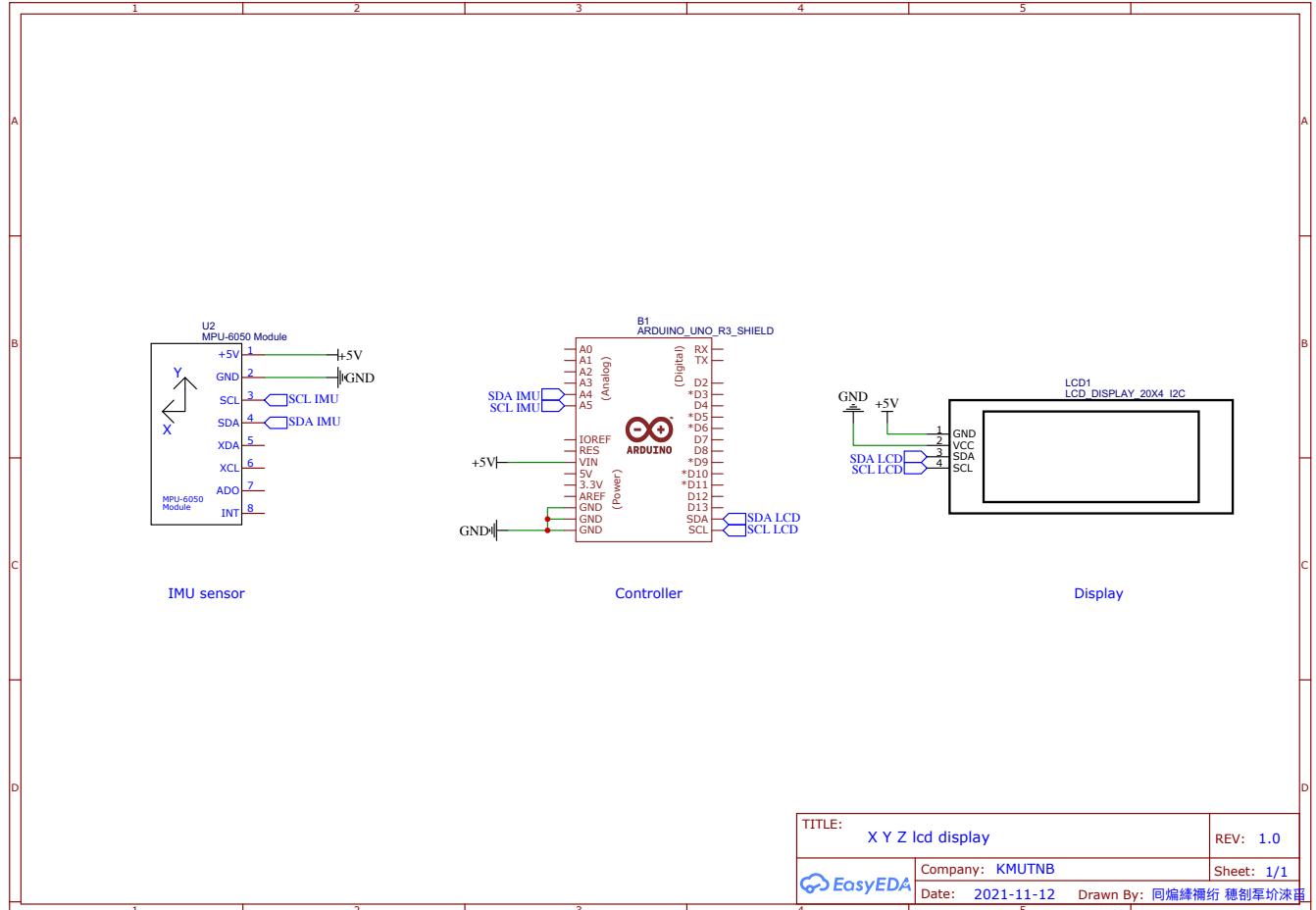
W x L x H  
145 x 220 x 330

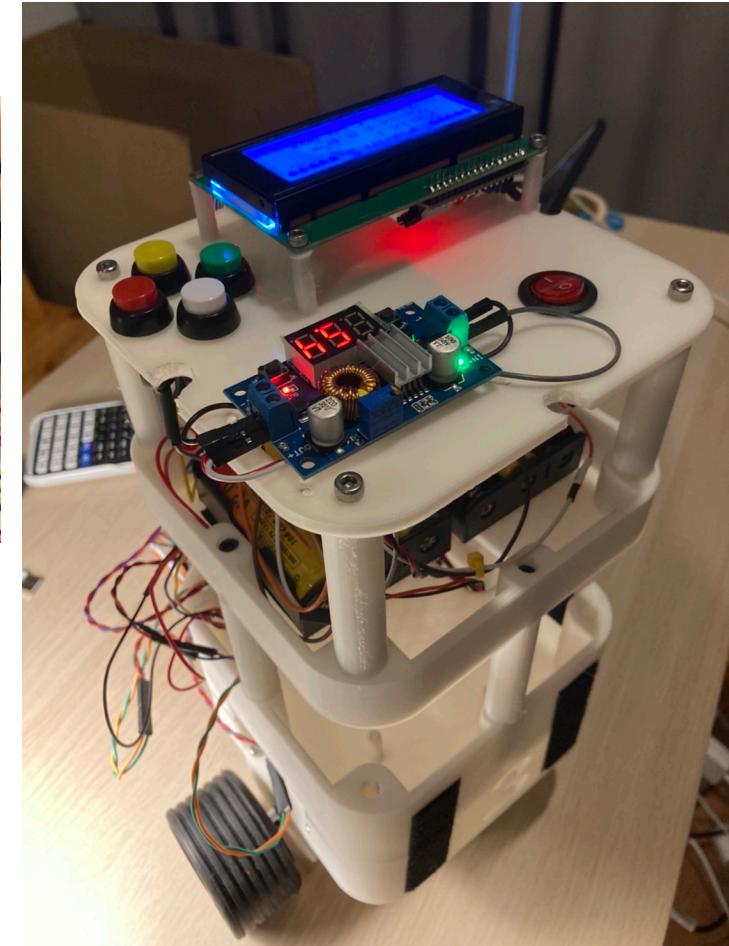
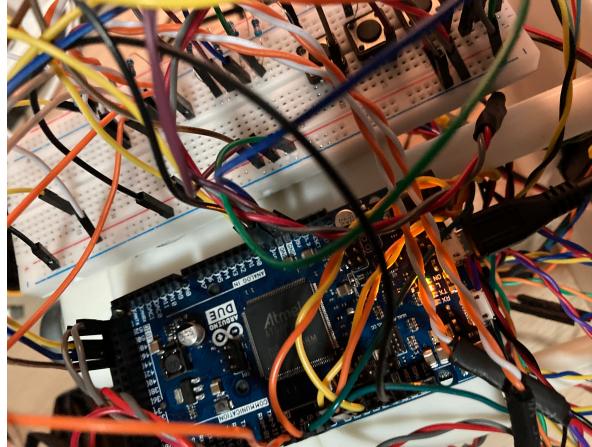
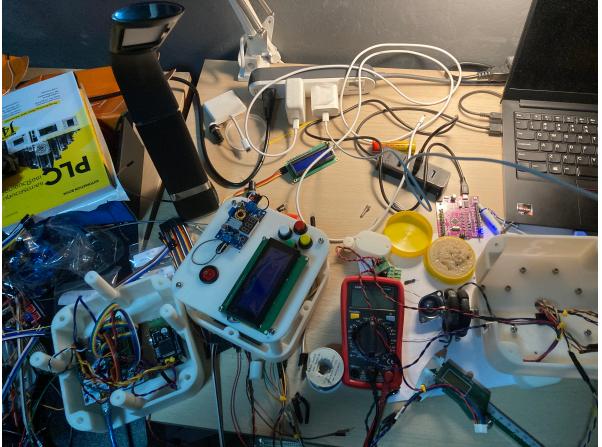
 AUTODESK®  
FUSION 360™

# Electronics Design



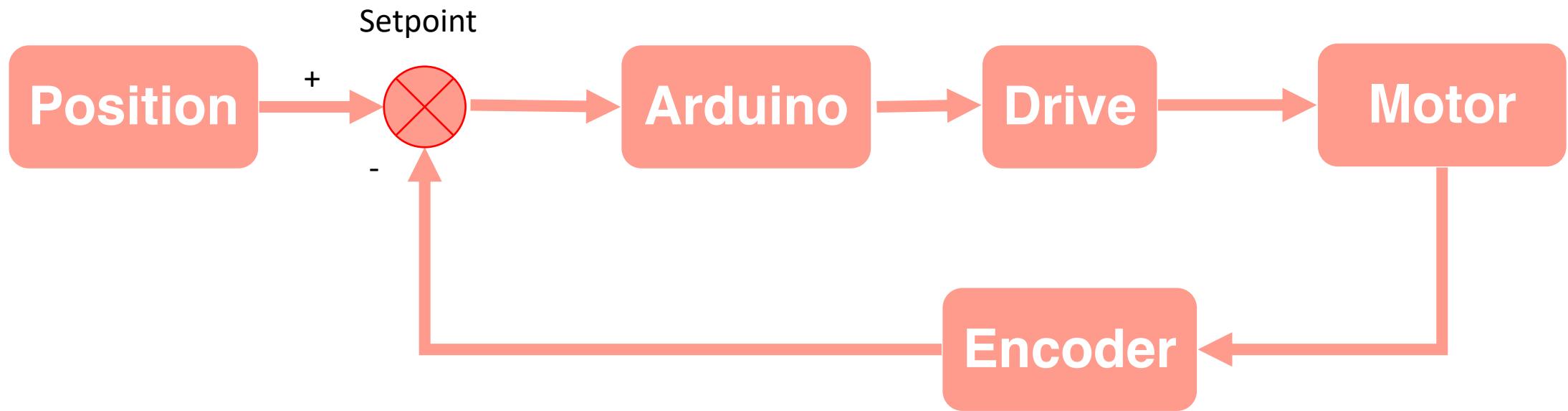
# Electronics Design





Assembly test improve

## Principle PID Robot control

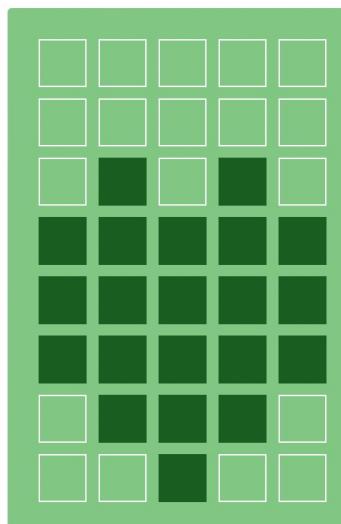
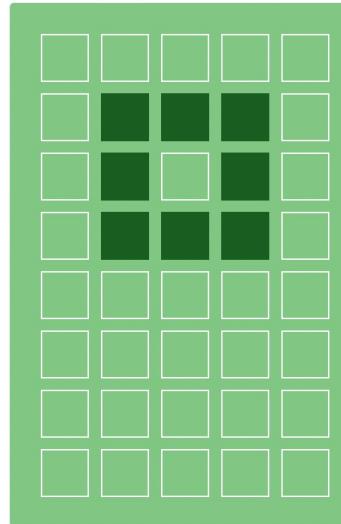


## Principle XYZ axis on LCD display

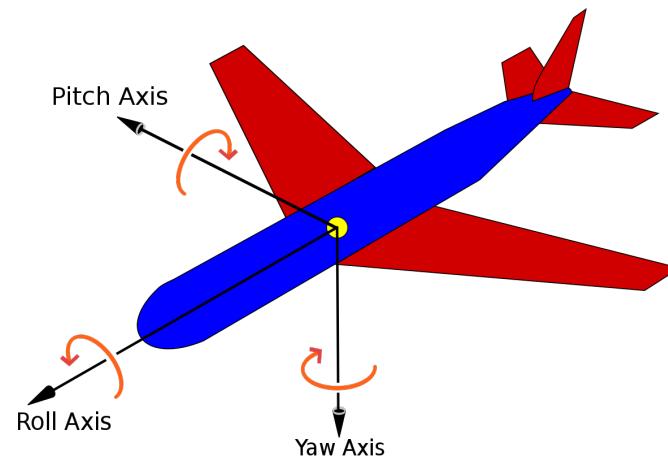
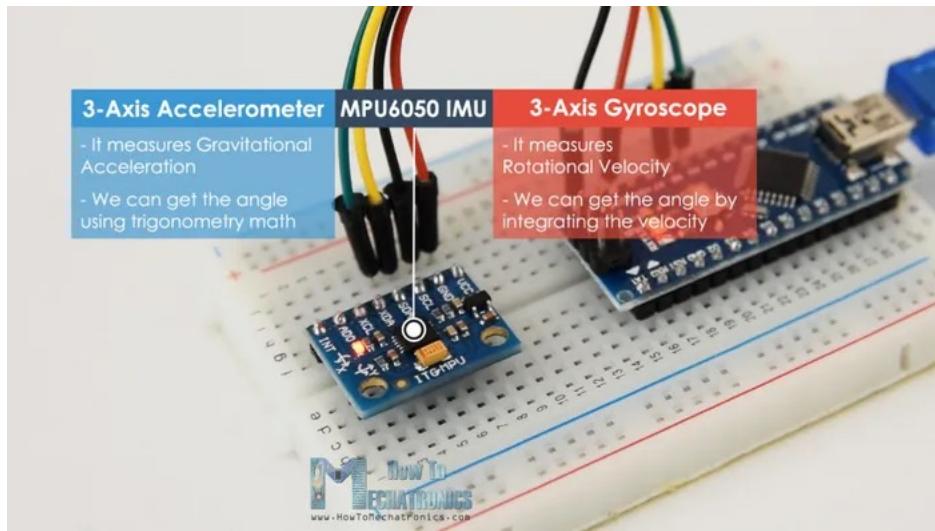


# LCD emoji

```
21 byte customChar[] = {  
22     B00000,  
23     B01110,  
24     B01010,  
25     B01110,  
26     B00000,  
27     B00000,  
28     B00000,  
29     B00000  
30 };  
31  
32 byte customChar_Hart[] = {  
33     B00000,  
34     B00000,  
35     B01010,  
36     B11111,  
37     B11111,  
38     B11111,  
39     B01110,  
40     B00100  
41 };
```



# GY-521 Module



# XYZ axis on display

```
63 void loop() {  
64     mpu.update();  
65     if ((millis() - timer) > 333) { // print data every 333ms  
66         Serial.print("X : ");  
67         Serial.print(mpu.getAngleX()); //get X axis  
68         Serial.print("\tY : ");  
69         Serial.print(mpu.getAngleY()); //get Y axis  
70         Serial.print("\tZ : ");  
71         Serial.println(mpu.getAngleZ()); //get Z axis  
72         timer = millis();  
73     }  
74     lcd.setCursor(0, 0);lcd.write(1);lcd.write(1);lcd.write(1);lcd.write(1);lcd.setCursor(5, 0); lcd.print("Tanawin S.");lcd.write(1);lcd.write(1);lcd.write(1);lcd.write(1);  
75     lcd.setCursor(3, 1); lcd.print("Xasix : "); lcd.print(mpu.getAngleX()); lcd.write(0); lcd.print(" ");  
76     lcd.setCursor(3, 2); lcd.print("Yasix : "); lcd.print(mpu.getAngleY()); lcd.write(0); lcd.print(" ");  
77     lcd.setCursor(3, 3); lcd.print("Zasix : "); lcd.print(mpu.getAngleZ()); lcd.write(0); lcd.print(" ");  
78 }  
79 }
```



# Mode selector

```
if ( millis() - last_time_X > period_X) {  
    last_time_X = millis();  
    if (state_modeREC == 1) {  
        stat_A = 1 ;  
    }  
    //Serial.print(stat_A);Serial.print(",");  
}  
if ( millis() - last_time_Y > period_Y) {  
    last_time_Y = millis();  
    if (state_modeTRI == 1) {  
        stat_B = 1;  
    }  
    //Serial.print(stat_B);Serial.print(",");  
}  
if ( millis() - last_time_Z > period_Z) {  
    last_time_Z = millis();  
    if (state_mode == 1) {  
        stat_C = 1;  
    }  
}  
Serial.print(stat_A); Serial.print(","); Serial.print(stat_B); Serial.println(","); Serial.print(stat_C);
```

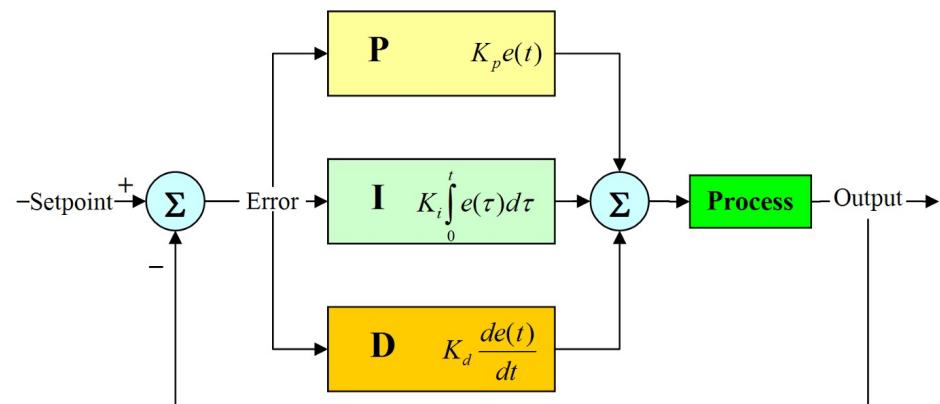
```
void readButtonA() {  
    state_modeREC = digitalRead(47);  
}  
  
void readButtonB() {  
    state_modeTRI = digitalRead(49);  
}  
  
void readButtonC() {  
    state_mode = digitalRead(51);  
}
```

## Mode selector

```
switch (stat_C) {                                /*Condition robot mode*/  
    case 1 : Triangle(); break;                  /*Robot triangle form*/  
  
}  
switch (stat_B) {                                /*Condition robot mode*/  
    case 1 : Rectangle(); break;                 /*Robot rectangular form*/  
}  
switch (stat_A) {                                /*Condition robot mode*/  
    case 1 : linear(); break;                   /*Robot linear form*/  
}
```

# PID Controller

$$u(t) = K_p e(t) + K_i \int_0^t e(\tau) d\tau + K_d \frac{d}{dx} e(t)$$



# PID block diagram

```
previous_error = setpoint - actual_position
integral = 0
start:
    error = setpoint - actual_position
    integral = integral + (error*dt)
    derivative = (error - previous_error)/dt
    output = (Kp*error) + (Ki*integral) + (Kd*derivative)
    previous_error = error
    wait(dt)
    goto start
```

## pseudocode

# PID tuning

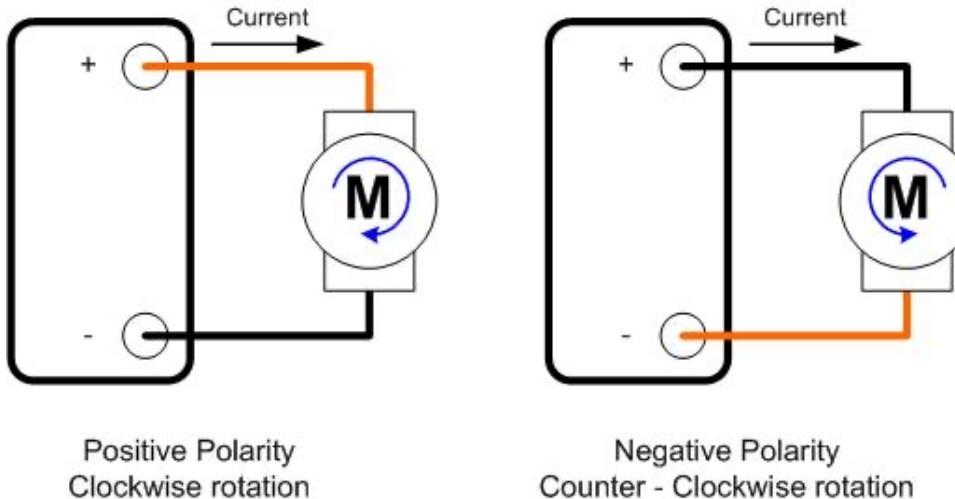
```
*****RIGHT wheel PID Tuning*****
//Define Variables we'll be connecting to
double input_R = 0, output_R = 0, setpoint_R = 0;

//Specify the links and initial tuning parameters
double kp_R = 0.5, ki_R = 0.006 , kd_R = 0;
PID myPID_R(&input_R, &output_R, &setpoint_R, kp_R, ki_R, kd_R, DIRECT);

//turn the PID RIGHT on
myPID_R.SetMode(AUTOMATIC);
myPID_R.SetSampleTime(1);
myPID_R.SetOutputLimits(-100, 100);

452 void comput_R() {
453     setpoint_R = A;                      /*modify to fit motor and encoder right*/
454     input_R = encoderPos_R ;             /*data form encoder right*/
455     myPID_R.Compute();                  /*calculate output*/
456     pwmOut_R(output_R);                /*drive motor drive module*/
457     Serial.print(setpoint_R);           /*mornitor of motor right*/
458     Serial.print(" ");
459     Serial.println(encoderPos_R);       /*mornitor motor right position*/
```

# Motor Direction

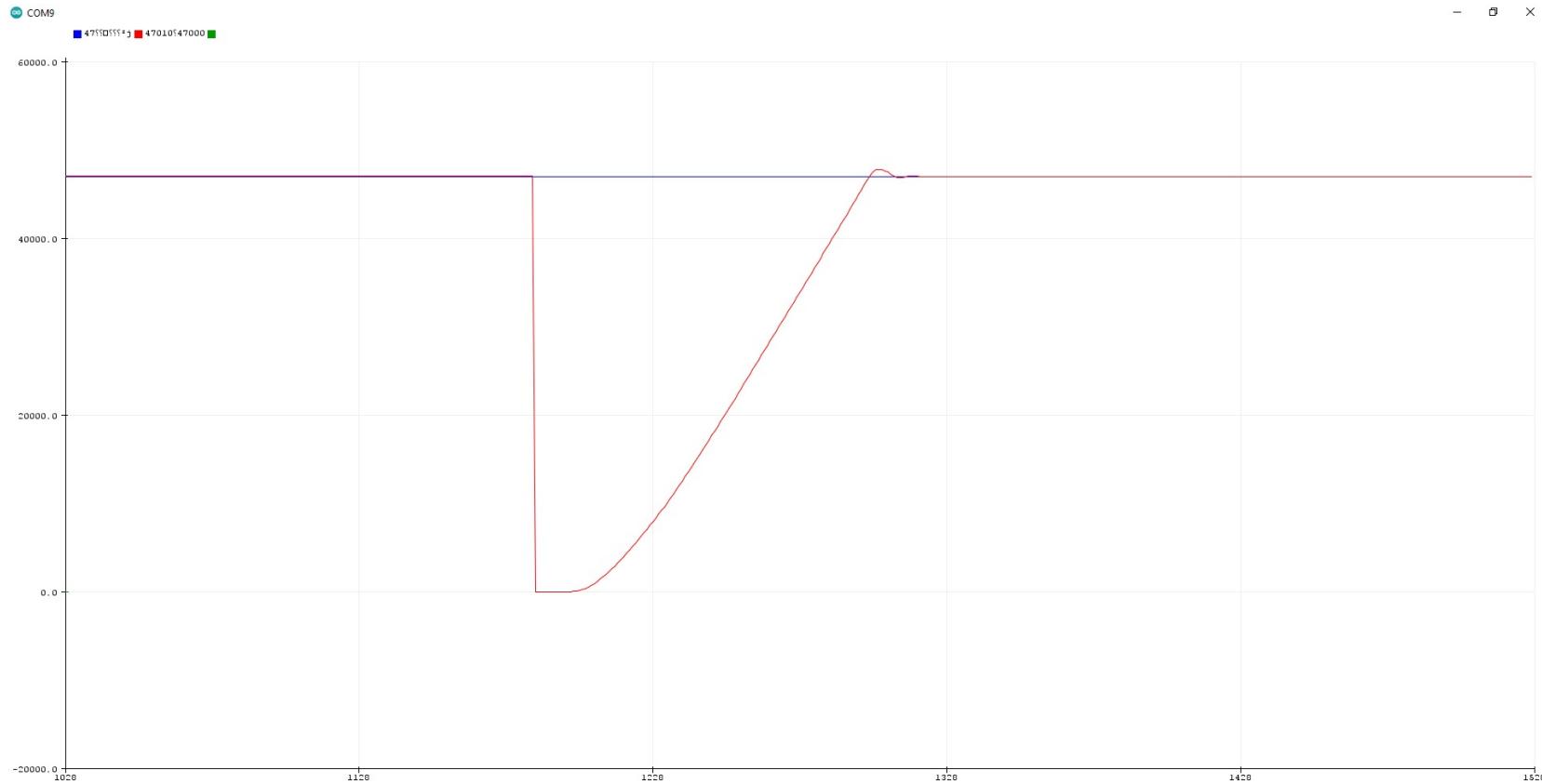


```
474 //*****Motor RIGHT direction*****  
475 void pwmOut_R(int out) {  
476   if (out > 0) {  
477     analogWrite(PWM_R, out);           /*drive motor right CW*/  
478     digitalWrite(inA_R, HIGH);  
479     digitalWrite(inB_R, LOW);  
480   }  
481   else {  
482     analogWrite(PWM_R, abs(out));    /*drive motor right CCW*/  
483     digitalWrite(inA_R, LOW);  
484     digitalWrite(inB_R, HIGH);  
485   }  
486 }  
487  
488 //*****Motor left direction*****  
489 void pwmOut_L(int out) {  
490   if (out > 0) {  
491     analogWrite(PWM_L, out);         /*drive motor left CW*/  
492     digitalWrite(inB_L, HIGH);  
493     digitalWrite(inA_L, LOW);  
494   }  
495   else {  
496     analogWrite(PWM_L, abs(out));   /*drive motor left CCW*/  
497     digitalWrite(inB_L, LOW);  
498     digitalWrite(inA_L, HIGH);  
499   }  
500 }
```

# Graph

Motor driving go to setpoint position

- Setpoint
- Motor encoder



# Encoder

```
103 //initialize the variables we're linked to  
104 Serial.begin(115200);  
105 pinMode(PWM_R, OUTPUT);  
106 pinMode(inA_R, OUTPUT);  
107 pinMode(inB_R, OUTPUT);  
108  
109 pinMode(ENCA_R, INPUT);  
110 pinMode(ENCB_R, INPUT);  
111 attachInterrupt(digitalPinToInterrupt(ENCA_R), readEncoder_R, RISING);  
112  
113 pinMode(PWM_L, OUTPUT);  
114 pinMode(inA_L, OUTPUT);  
115 pinMode(inB_L, OUTPUT);  
116  
117 pinMode(ENCA_L, INPUT);  
118 pinMode(ENCB_L, INPUT);  
119 attachInterrupt(digitalPinToInterrupt(ENCA_L), readEncoder_L, RISING);
```

```
594 void readEncoder_R() {  
595     int b = digitalRead(ENCB_R);  
596     if (b > 0) {  
597         encoderPos_R++;  
598     }  
599     else {  
600         encoderPos_R--;  
601     }  
602 }  
603  
604 /*  
605     Encoder motor left  
606 */  
607 void readEncoder_L() {  
608     int b = digitalRead(ENCB_L);  
609     if (b > 0) {  
610         encoderPos_L++;  
611     }  
612     else {  
613         encoderPos_L--;  
614     }  
615 }
```

# Encoder

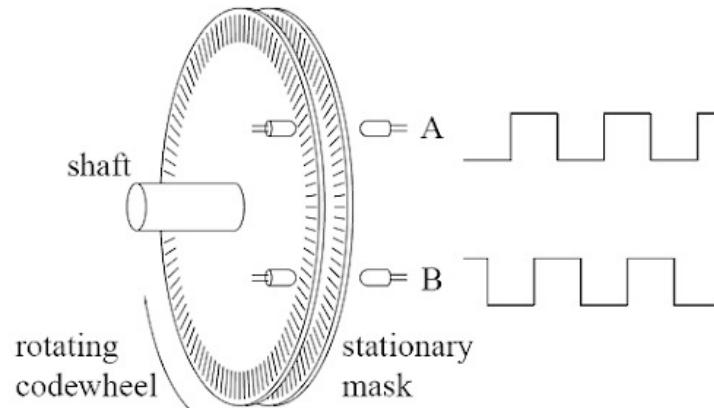


12V 0.2A

Speed : 150 RPM

Gear ratio 1:78

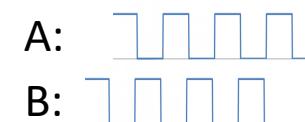
360P



$$\begin{aligned} \text{Pulse at main shaft} &= 78 * 360 = 28080 \text{ pulse} \\ \text{Circumference} &= \pi * D = \pi * 58 = 182.12 \text{ mm} \\ 28080 \text{ pulse} &= 182.12 \text{ mm} \end{aligned}$$

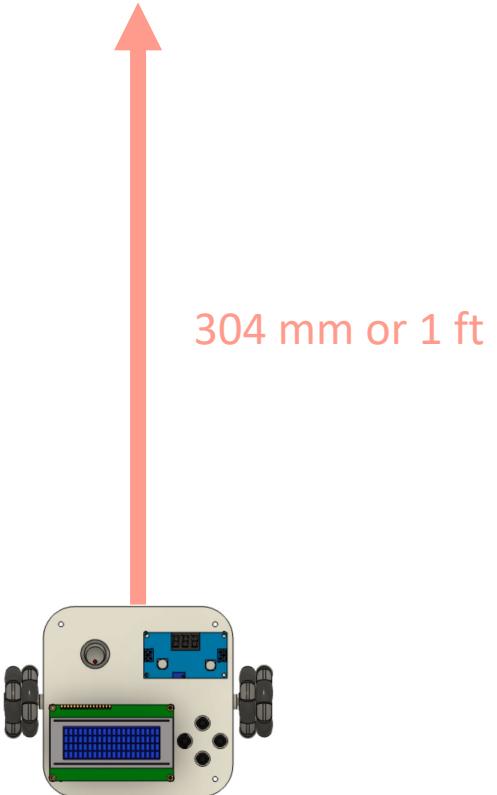
$$\text{find pulse per mm} = \frac{182.12}{28080} = 0.00648 \text{ mm}$$

$$1 \text{ pulse} \approx 0.0064 \text{ mm}$$

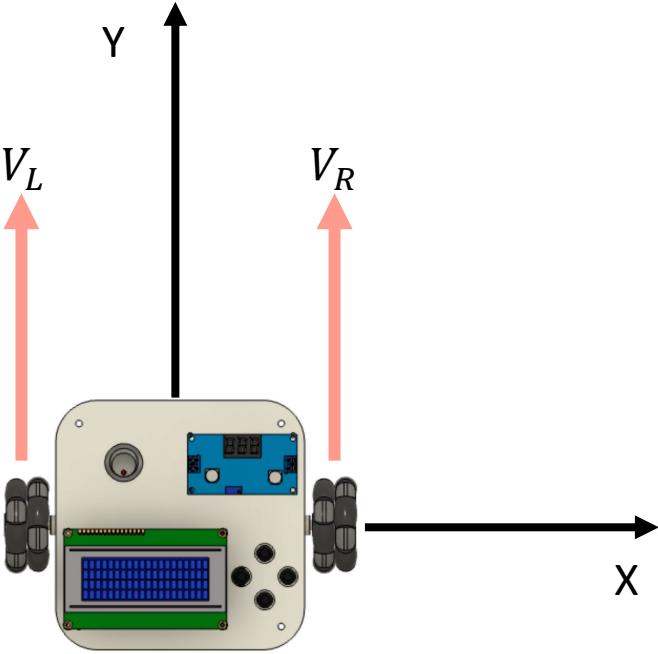


# Direct move

$$304 \text{ mm} = \frac{304\text{mm}}{0.0064} = 47500 \text{ pulse}$$

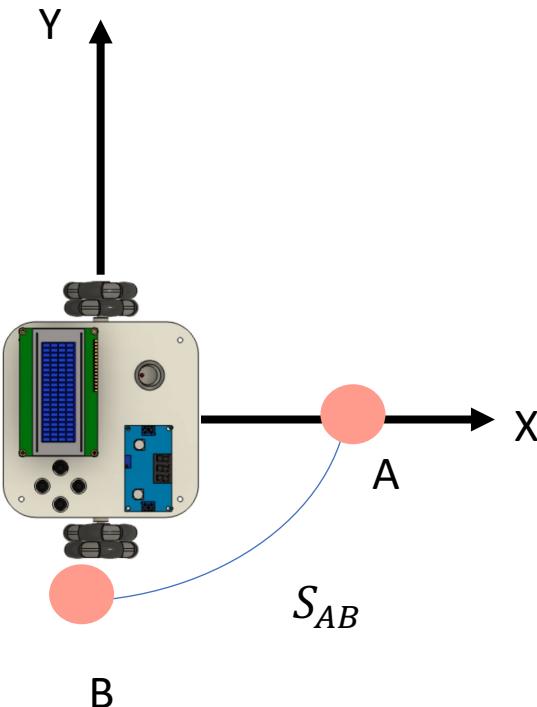


```
502 /*
503  Calculate the pluse of encoder right for command robot go to x = 0 ft, y = 1 ft
504 */
505 float pulse_RW(float pulse) {
506     int feetXX = coorX * 304;
507     float res_pulse = motor_raio * rev_pluse;
508     float tick = dimention_wheel / res_pulse;
509     pulse = feetXX / tick;
510     return pulse;
511 }
512
513 /*
514  Calculate the pluse of encoder left for command robot go to x = 0 ft, y = 1 ft
515 */
516 float pulse_LW(float pulse) {
517     int feetYY = coorY * 304;
518     float res_pulse = motor_raio * rev_pluse;
519     float tick = dimention_wheel / res_pulse;
520     pulse = feetYY / tick;
521     return pulse;
522 }
```



```
223 /*
224   Traget point 1 start robot go to x = 0 ft, y = 1 ft
225   Motor right CW direction
226   Motor left CW direction
227 */
228 void direct_drive_1() {
229   double a, b, c, d;
230   A = pulse_RW(a); B = pulse_LW(b);
231   C = A; D = B;
232   if (encoderPos_R >= A && encoderPos_L >= B) {
233     Targetpoint++;
234   }
235 }
```

## Robot turn around



$$Body = 220 \text{ mm}$$

$$r = \frac{Body}{2} = \frac{220}{2} = 110 \text{ mm}$$

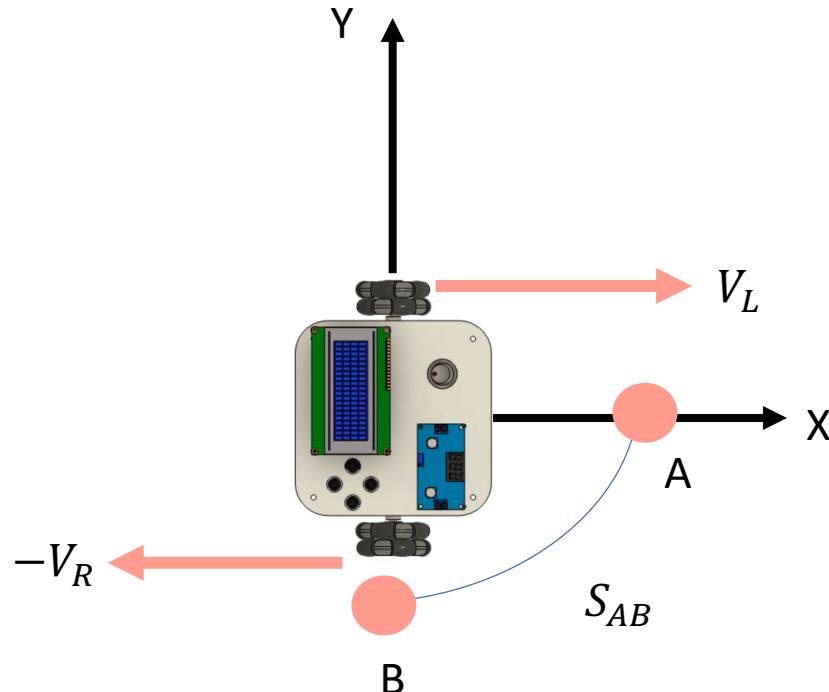
$$\theta = 90^\circ$$

$$S_{AB} = 2\pi \cdot r \cdot \frac{\theta}{360}$$

$$S_{AB} = 2\pi \cdot 110 \cdot \frac{90}{360} = 172.78 \text{ mm}$$

$$pulse = \frac{S_{AB}}{0.0064} = \frac{172.78}{0.0064} = 26996 \text{ pulse}$$

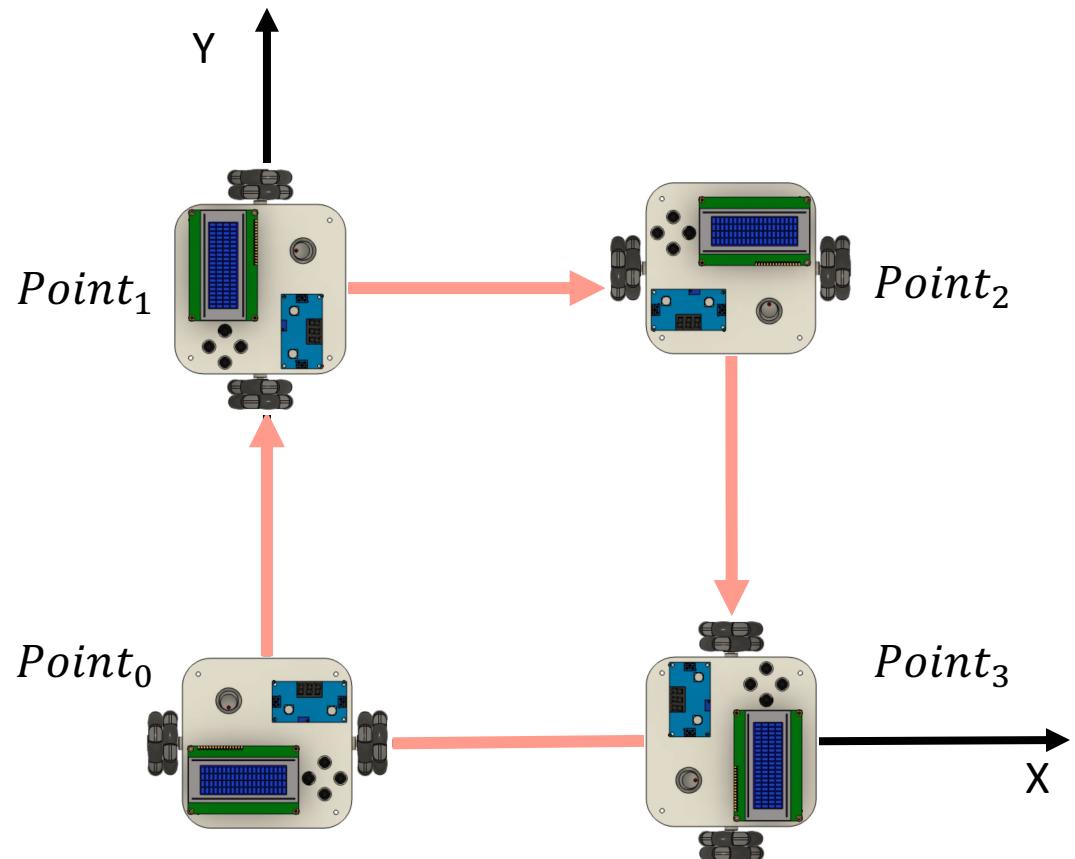
```
524 /*
525  Calculate the pluse of encoder for command robot turn around 90 degree
526 */
527 float pulse_r90(float pulse) {
528     float distance = 2 * 3.14 * (body / 2) * 0.13;
529     float res_pulse = motor_raio * rev_pluse;
530     float tick = dimention_wheel / res_pulse;
531     pulse = distance / tick;
532     return pulse;
533 }
```



```

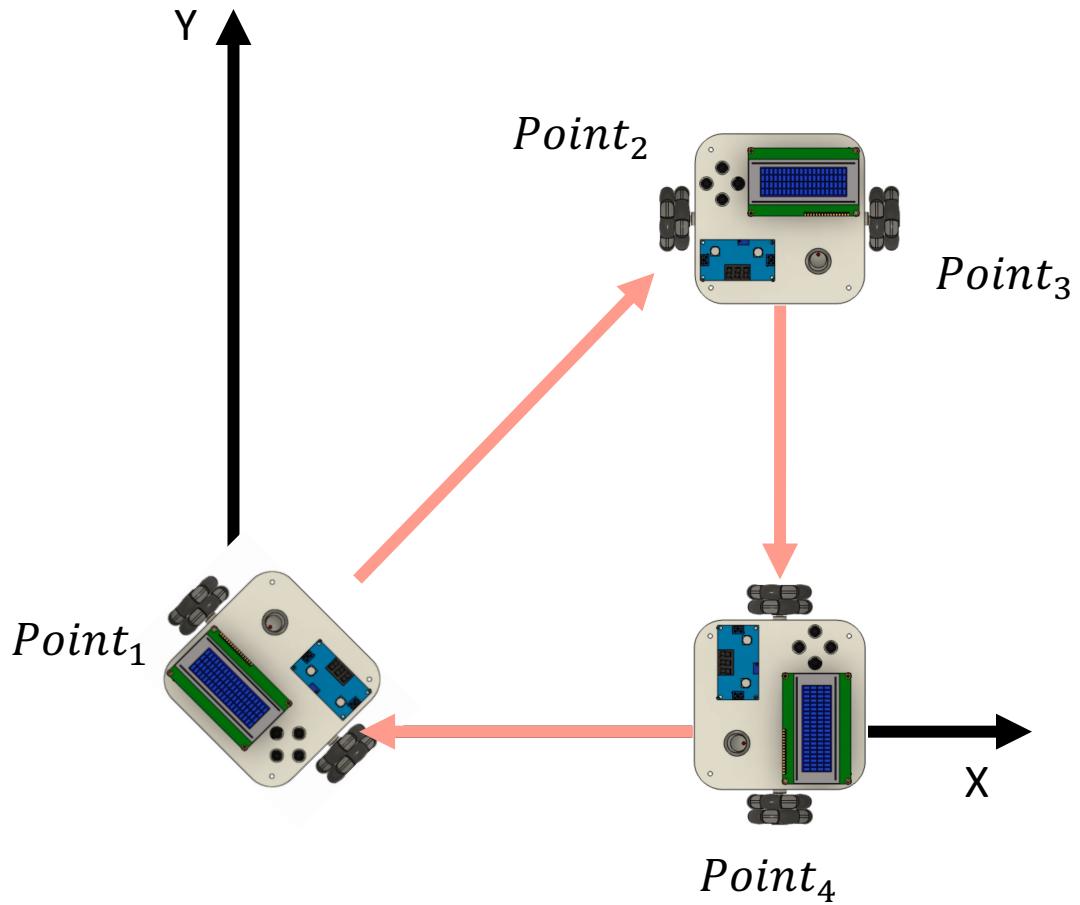
401 /*
402   Target point 5 robot turn around 90 degree
403   Motor right CCW direction
404   Motor left CW direction
405 */
406
407 void drive_Tri_90() {
408   double a, b;
409   Set_tri_R[4] = A = Set_tri_R[3] - pulse_r90(a) - 4500; Set_tri_L[4] = B = Set_tri_L[3] + pulse_r90(b) + 4000;
410   if (encoderPos_R <= A && encoderPos_L >= B) {
411     Targetpoint++;
412   }
413 }
```

# Rectangle move



```
202 void Rectangle() {  
203     comput_R();  
204     comput_L();  
205  
206     Serial.println(Targetpoint);  
207     switch (Targetpoint) {  
208         case 1 : direct_drive_1(); break;  
209         case 2 : A90_drive_1(); break;  
210         case 3 : direct_drive_2(); break;  
211         case 4 : A90_drive_2(); break;  
212         case 5 : direct_drive_3(); break;  
213         case 6 : A90_drive_3(); break;  
214         case 7 : direct_drive_4(); break;  
215         case 8 : A90_drive_4(); break;  
216     }  
217 }
```

# Triangle move

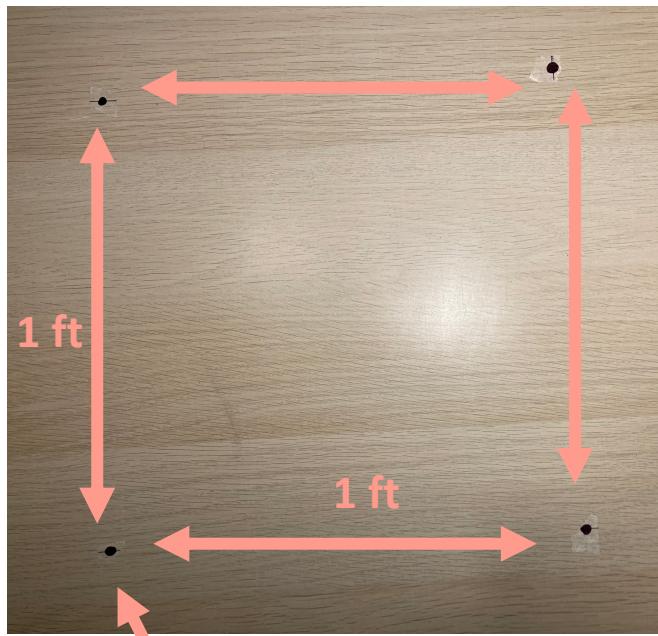


```
182 void Triangle() {  
183     comput_RO();  
184     comput_LO();  
185  
186     Serial.println(Targetpoint);  
187     switch (Targetpoint) {  
188         case 1 : drive_Tri_45(); break;  
189         case 2 : driff_drive(); break;  
190         case 3 : return_drive(); break;  
191         case 4 : back_drive(); break;  
192         case 5 : drive_Tri_90(); break;  
193         case 6 : to_home(); break;  
194         case 7 : drive_Tri_90_2(); break;  
195     }  
196 }
```

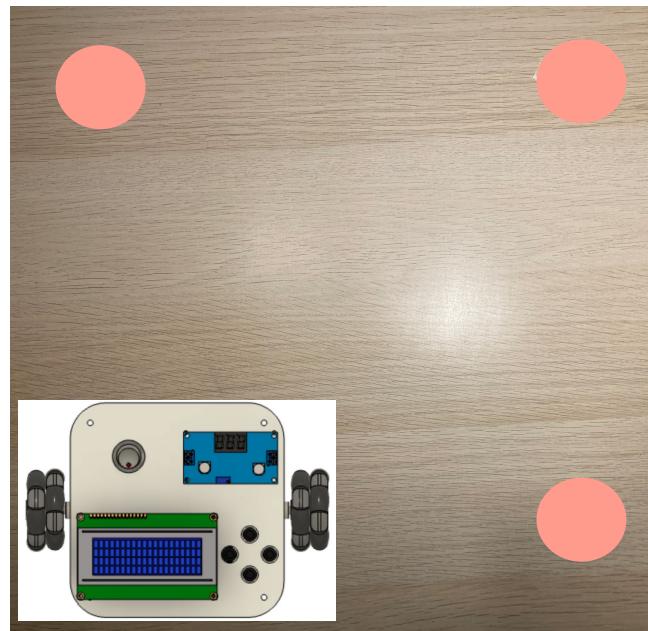
# Calibration



# Test field



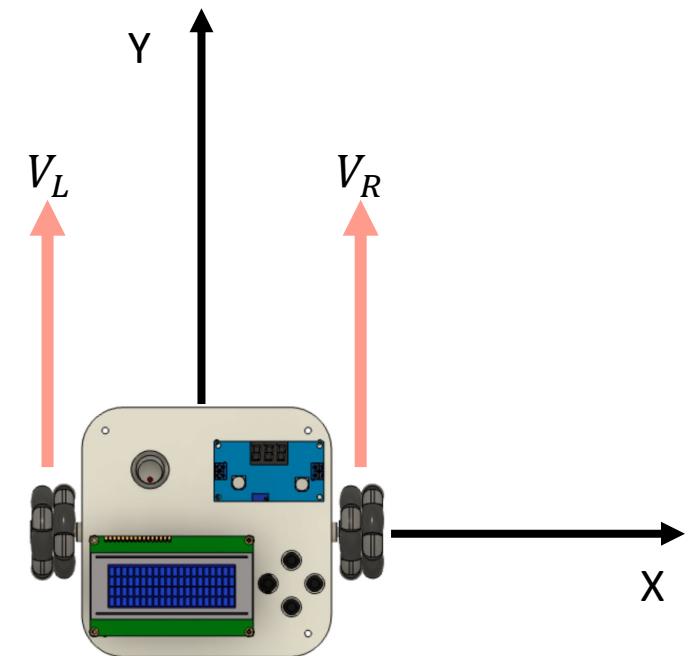
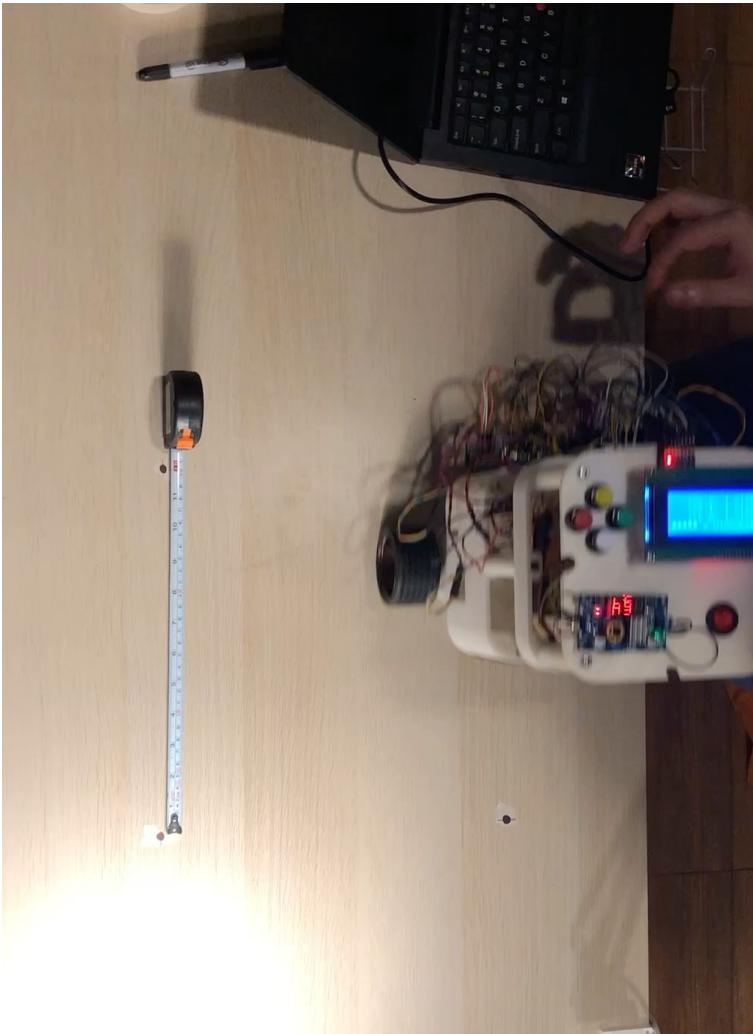
# Start point



1ft x 1ft



# Direct Drive test



	X	Y
1	-8	304
2	-5	304
3	-15	304
4	-2	304
5	-3	304
6	-2	304
7	4	304
8	-11	304
9	-2	304
10	4	304

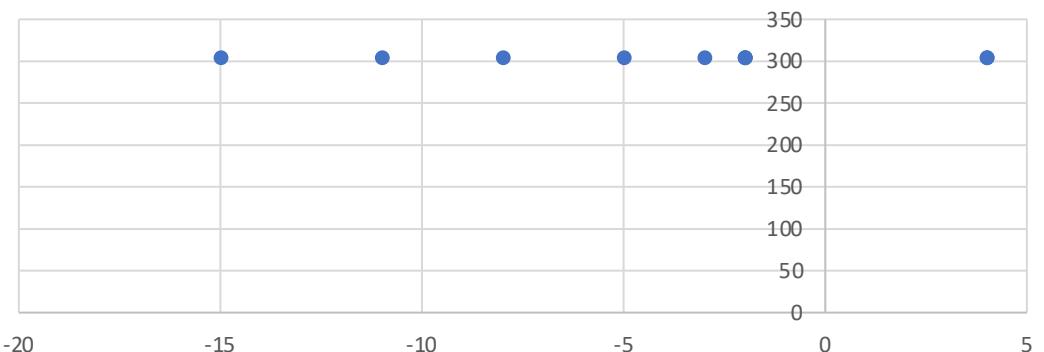
Average : X = -4 , Y = 304  
SD. : X = 6.03, Y = 0

$$Position = \sqrt{(X_{measure} - X_{origin})^2 + (Y_{measure} - Y_{origin})^2}$$

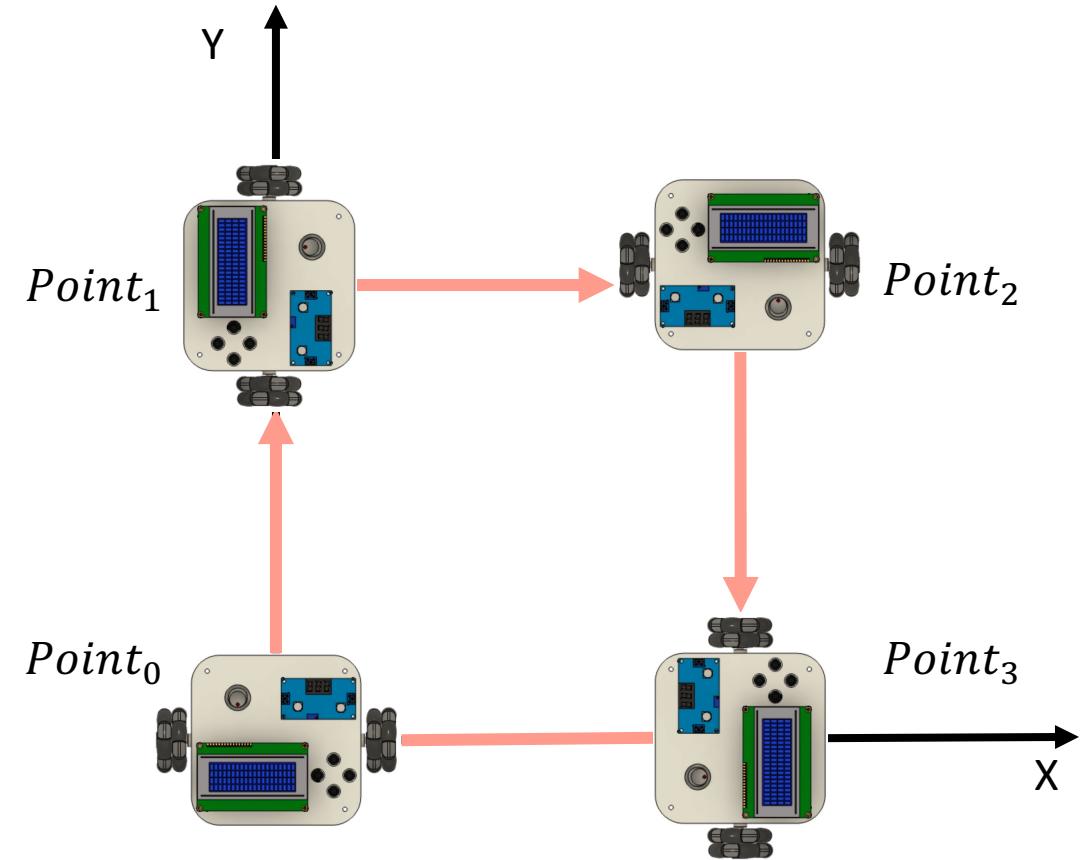
$$Position = \sqrt{(-4 - 0)^2 + (304 - 0)^2} = 304.02 \text{ mm}$$

$$\theta = \tan^{-1}(y/x) = \tan^{-1}\left(-\frac{304}{4}\right) = -89.24^\circ$$

Real Position



# Rectangle drive test



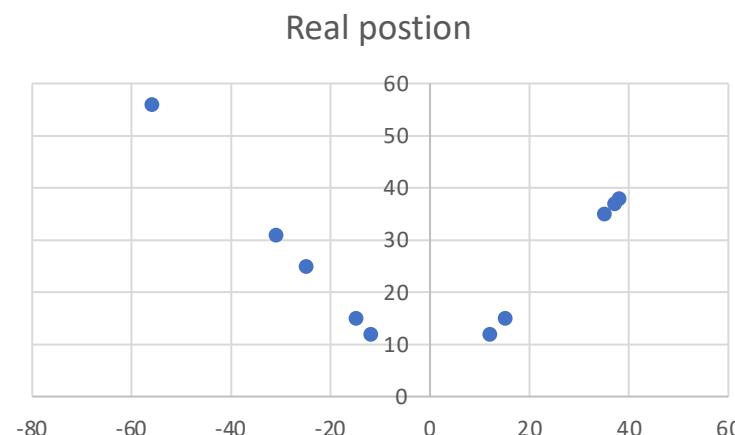
Average : X = -0.2 , Y = 27.6  
 SD. : X = 26.48, Y = 14.45

	X	Y
1	15	15
2	12	12
3	-31	31
4	-56	56
5	-25	25
6	-15	15
7	38	38
8	37	37
9	35	35
10	-12	12

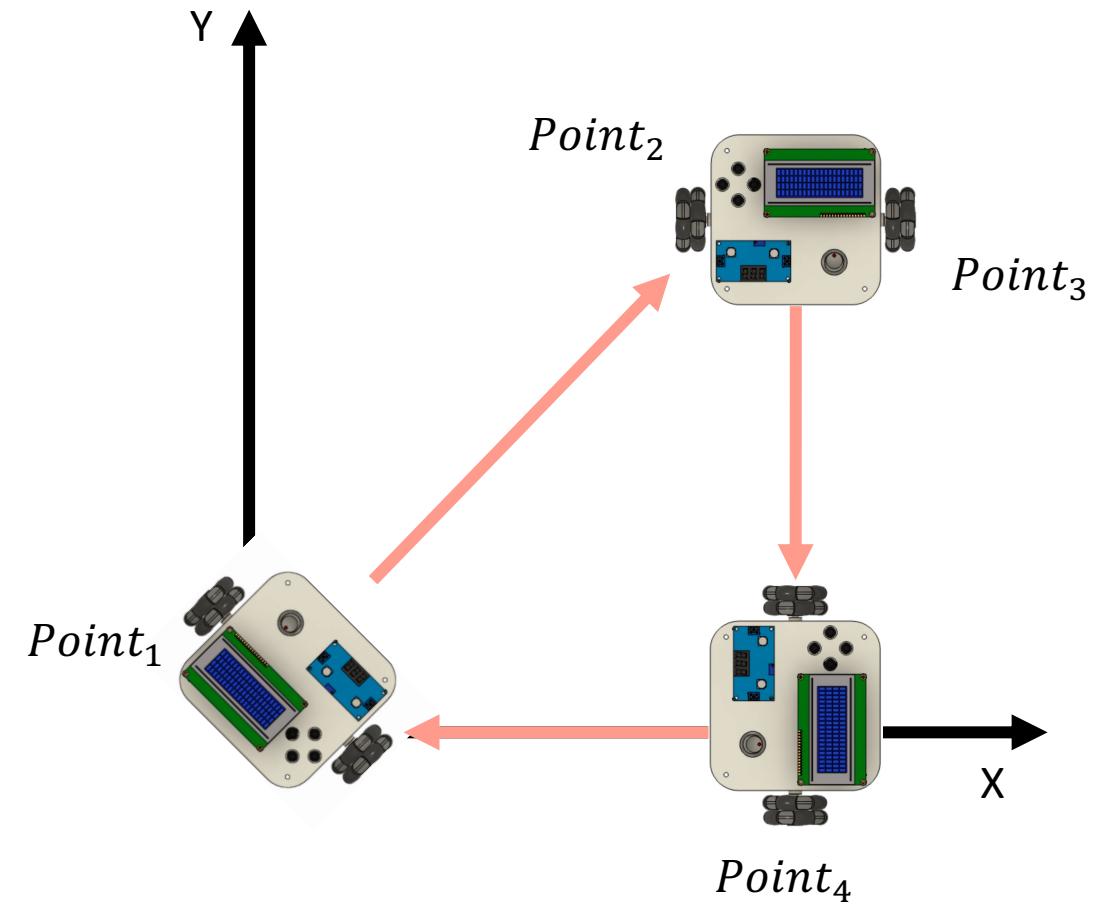
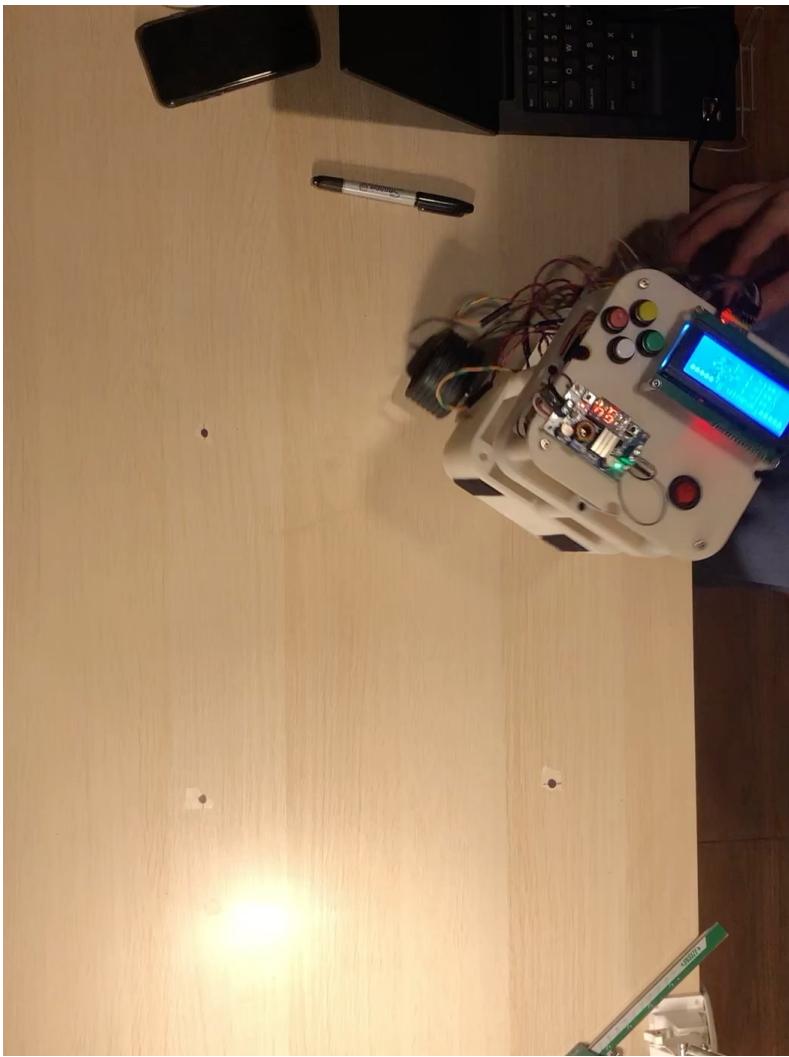
$$Position = \sqrt{(X_{measure} - X_{origin})^2 + (Y_{measure} - Y_{origin})^2}$$

$$Position = \sqrt{(-0.2 - 0)^2 + (27.6 - 0)^2} = 27.6 \text{ mm}$$

$$\theta = \tan^{-1}(y/x) = \tan^{-1}\left(-\frac{27.6}{0.2}\right) = -89.58^\circ$$



# Triangle drive test



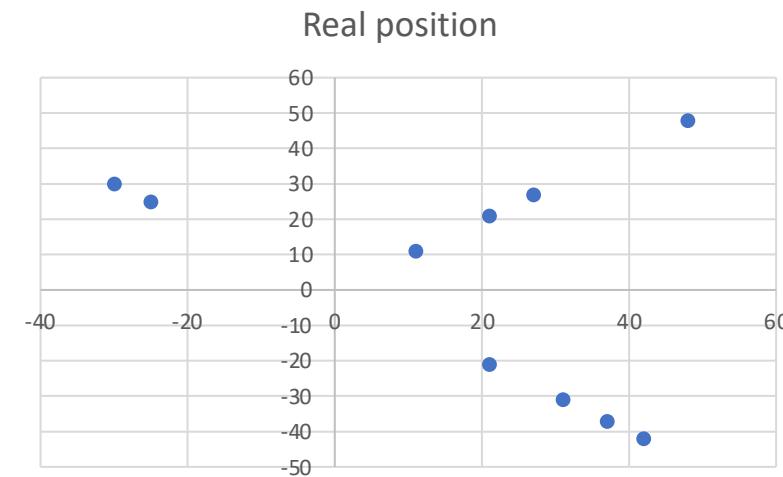
	X	Y
1	-25	25
2	-30	30
3	48	48
4	31	-31
5	42	-42
6	21	21
7	27	27
8	21	-21
9	11	11
10	37	-37

Average : X = 18 , Y = 3.1  
SD. : X = 26.47, Y = 32.58

$$Position = \sqrt{(X_{measure} - X_{origin})^2 + (Y_{measure} - Y_{origin})^2}$$

$$Position = \sqrt{(18 - 0)^2 + (3.1 - 0)^2} = 18.26 \text{ mm}$$

$$\theta = \tan^{-1}(y/x) = \tan^{-1}\left(\frac{3.1}{18}\right) = 9.77^\circ$$

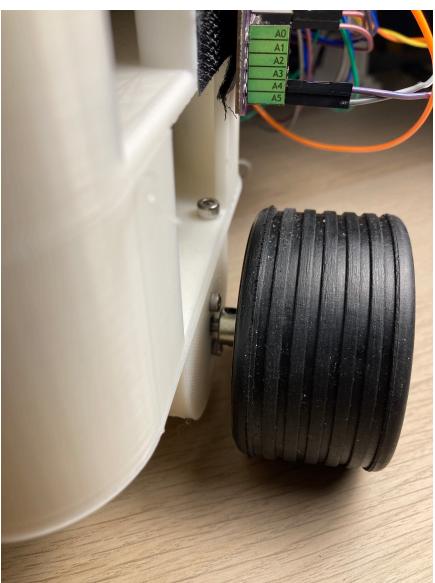


# Summarize

## Direct drive

X = -4 mm

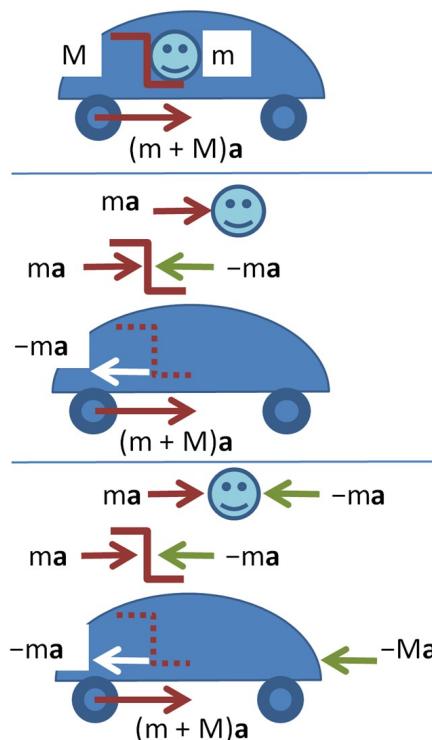
Y = 304 mm



## Rectangle drive

X = 0.2 mm

Y = -27.6 mm

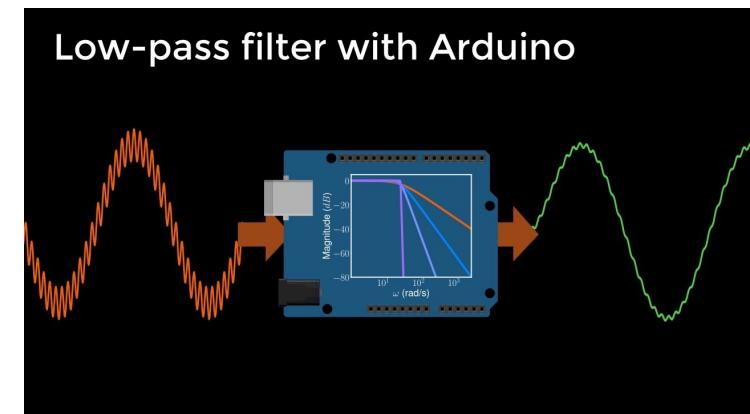


## Triangle drive

X = 18 mm

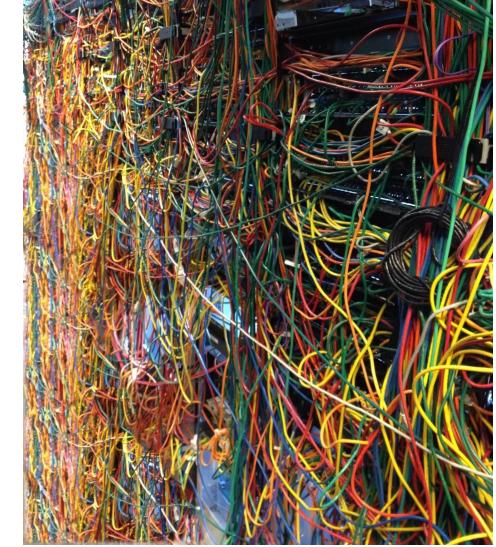
Y = -3.1 mm

## Low-pass filter with Arduino

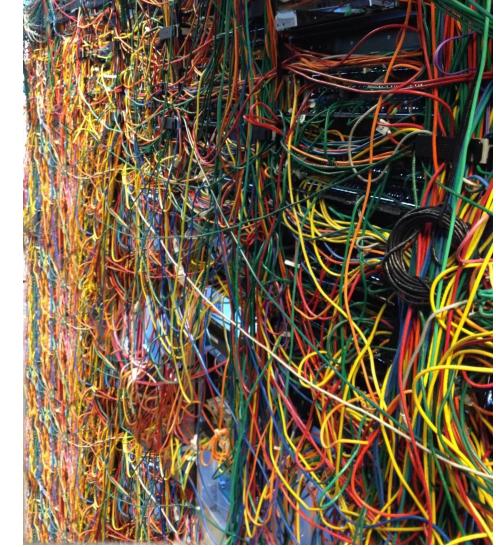




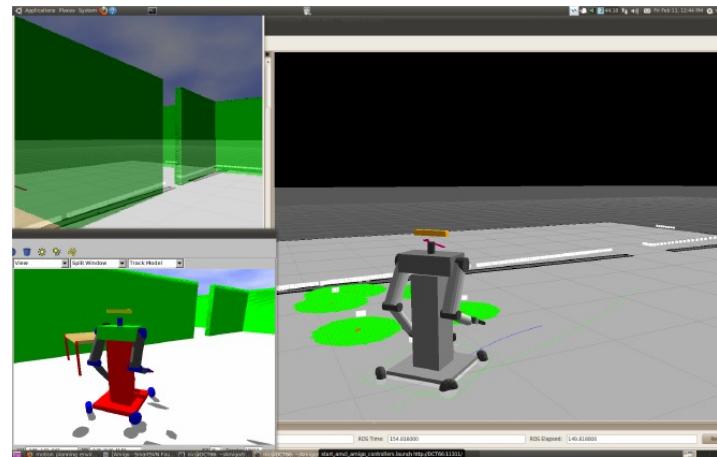
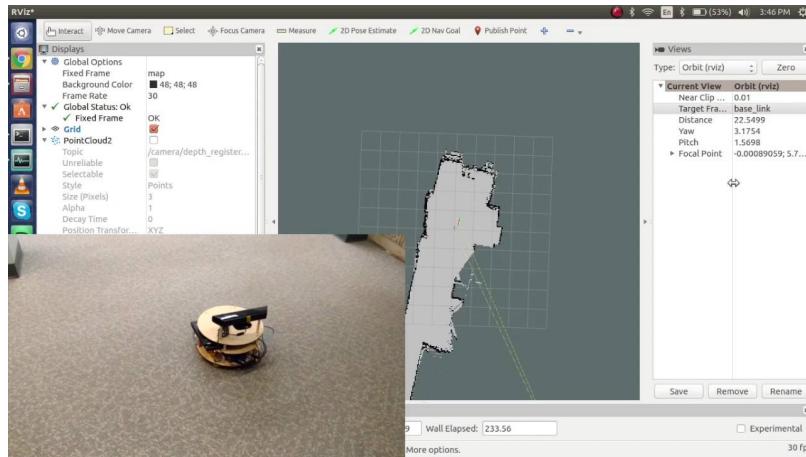
**Problem**



**Test field**



# Applied



**Question**

Thx