

Commitment-Schemes

Leonhard Applis

TH Nürnberg

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Problem(s)

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to do: What are the problems we need to adress

- A **commits** to B
- B keeps commitment, is unable to read or process it
- A reveals to B
- B can verify the commitment

TODO: Image

- ❶ **Binding:** The Values Alice put in the Commitment cannot be changed after B recieved it
- ❷ **Hiding:** Bob cannot gain any information about the message from the commitment itself

Additional for *real-life-applications*:

- ❶ Bob's are able compare commitments
- ❷ Commitments are *tradeable*

Challenge and Response

You can setup your own anonymous challenges, leaving a commitment at Bob's. If someone shows up saying he's Alice, Bob challenges to reveal the commitment.

JSON-Web-Tokens (JWT):

A payload (e.g. some account details) are encrypted to a commitment and passed to a third party.

You can verify yourself at the third-party revealing the commitment

this is done *automatic* via session or system attributes

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Hash-Based Commitments

General Concept

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- 1 Alice produces $h = \text{Hash}(m)$ and sends Bob h and Hash
- 2 Bob keeps h and Hash
- 3 Alice reveals herself by sending Bob m
- 4 Bob checks if $\text{Hash}(m) \equiv h$

Important: NEVER use actual important data as message, you send it in cleartext in Step 3.

Hiding: because of the Hash-functions **Pre-Image resistance**, it's nearly impossible to find the message m from the hash. This holds true for any Bob and any Eve.

Binding: because of the Hash-functions **collision-resistance**, it's nearly impossible to find another message m with the same hash.

Hash-Based Commitments

Problem: unlimited range - limited domain

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Usually: Bob (and Eve) are not able to *guess* m from h and $Hash$

But: if the *plausible domain* of m is known, its possible for modern computers to brute force reveal your m

Example: Alice commits to Bob about the result of a soccer game Germany vs. Brazil.

Therefore she chooses a score of 0:7 and sends Bob $h = SHA_3(str(0 : 7))$ and the Hashfunction SHA_3

Eve catches the commitment and knows the context of the soccer game. she can know try reasonable combinations of results from 0:0 up to 20:20. She only needs to try $20 \cdot 20 = 400$ results

Improved Concept:

- Alice chooses a random value s
- Alice produces $h = \text{Hash}(m, s)$ and sends h and Hash to Bob
- Bob keeps h and Hash
- Alice reveals herself by sending bob m and s
- Bob checks if $\text{Hash}(m, s) \equiv h$

Alice is anonymus. She never stated her name, used certificates, etc.
Alice can produce as many commitments for as many personas as she wants.

For increased security:

- commitments should be one-use only
- commitments should have a lifetime
- traded commitments to a third Party should revealed directly with first reveal
- messages must be chosen random

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Binary-Concept

Requirements and Definitions

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