Commitm Schemes

Leonharo Applis

Basics

nasn-Based

Log

Binary

Commitment-Schemes

Leonhard Applis

TH Nürnberg

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2 Hash-Based

3 Discrete Log

Introduction

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Figure: Kung Fu Hustle - Lollipop Girl

Plot Summary:

- Villain destroys village and steals girls lollipop
- Girls swears vengeance
- Girl becomes Kung Fu master
- Girl finds the villain.
 Villain recognices her by the lollipop

Commitments Basic-protocoll

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_ D:____

- A commits to B
- B keeps commitment, unable to read or process it
- A reveals to B
- B can verify the commitment

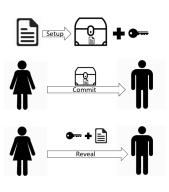


Figure: Commitments

Attributes

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- Binding: The Values Alice put in the Commitment cannot be changed after B recieved it
- Hiding: Bob cannot gain any information about the message from the commitment itself
- Viability: If both parties follow the Protocoll, Bob is always able to recover the committed value

Additional for real-life-applications:

- Bob's are able compare commitments
- 2 Commitments are tradeable

Applications

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Challenge and Response

You can setup your own anonymus challenges, leaving a commitment at Bob's. If someone show's up saying he's Alice, Bob challenges to reveal the commitment.

JSON-Web-Tokens (JWT):

A payload (e.g. some account details) are encrypted to a commitment and passed to a third party.

You can verify yourself at the third-party revealing the commitment this is done *automatic* via session or systemattributes

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Hash-Based Commitments General Concept

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- Alice produces h = Hash(m) and sends Bob h and Hash
- f 2 Bob keeps h and Hash
- Alice reveals herself by sending Bob m
- Bob checks if $Hash(m) \equiv h$

Important: NEVER use actual important data as message, you send it as cleartext in Step 3.

Fullfillment of Attributes

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Discret Log Hiding: because of the Hash-functions Pre-Image resistance, it's nearly impossible to find the message m from the hash. This holds true for any Bob and any Eve.

Binding: because of the Hash-functions collision-resistance, it's nearly impossible to find another message m with the same hash.

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Usually: Bob (and Eve) are not able to guess m from h and Hash

But: if the $plausible\ domain$ of m is known, its possible for modern computers to brute force reveal your m

Example: Alice commits to Bob about the result of a soccer game Germany vs. Brazil.

Therefore she chooses a score of 0:7 and sends Bob $h = SHA_3(str(0:7))$ and the Hashfunction SHA_3

Eve catches the commitment and knows the context of the soccer game. she can know try reasonable combinations of results from 0:0 up to 20:20. She only needs to try $20 \cdot 20 = 400$ results

Improved Concept:

- lacktriangle Alice chooses a random value s
- Alice produces h = Hash(m, s) and sends h and Hash to Bob
- \bullet Bob keeps h and Hash
- Alice reveals herself by sending bob m and s
- Bob checks if $Hash(m, s) \equiv h$

Addition

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Alice is anonymus. She never stated her name, used certificates, etc. Alice can produce as many commitments for as many personas as she wants.

For increased security:

- commitments should be one-use only
- commitments should have a lifetime
- traded commitments to a third Party should revealed directly with first reveal
- messages must be chosen random

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Discrete Logarithm - Pedersen commitment scheme $_{\mbox{\scriptsize Requirements}}$ and $_{\mbox{\scriptsize Definitions}}$

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Prerequisites: Bob needs to setup the environtment for alice, by

- choosing a large prime number p
- choosing a smaller prime number $q \in \{1..p|q \div (p-1) = 0\}$
- \circ choosing $g, v \in G_q \neq 1$
- \bullet sending Alice p, q, g, v

Now Alice can build the exact same group and subgroup like Bob. This is similar to sending the hash-function.

Implementation

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Hash Base

Discrete Log

- Alice requests p, q, g, v from Bob. Alice check that q, p are primes, q divides p-1, that g and v are valid elements.
- \bullet Alice chooses her message $m \in \{1..p\}$ and a random number $r \in \{1..q-1\}$
- Alice sends $c = g^r v^m$ to Bob (commit)
- $\bullet \ \, \text{Bob keeps} < Alice, c, < p, q, g, v >>$
- \bullet Alice can reveal herself by sending r,m to Bob. Bob checks $c=g^rv^m$

Benefits

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Major:

- Commitments always contain random parts
- No collision possible (unlike Hashfunctions)

Minor:

- tupels are smaller to store than hashes
- p, q, g, v are easily changed/renewed (you could not renew hashfunctions)

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Quadratic Residues Definitions and Setup

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Commitment to only 0,1 using quadratic residues.

A number n is **always** quadratic, if it's the product of two quadrats.

$$p^2 * q^2 = p * p * q * q = (p * q)^2$$

choose primes p,q and check for every element $x \in \mathbf{Z}_{\mathbf{n}}^*, n = p * q$

The only way to check if x is quadratic in n, is to check if its quadratic for p and q!

Quadratic Residues Jakobi-Matrizes

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Required:	Legendre-Symbol	$(\frac{x}{p})$	$= x^{p-1}$	1 mod(p)
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$(\frac{x}{p})$	$(\frac{x}{q})$	$(\frac{x}{n})$	quadratic
1	1	1	yes
1	-1	-1	no
-1	1	-1	no
-1	-1	1	no

given X and guessing we have 75% cases where it's not quadratic.

given X and $(\frac{x}{n}) = 1$ we have 50:50 Quadratic:nonQuadratic

• Alice chooses primes p, q and an element $v \in \{x \in \mathbf{Z}_n | (\frac{x}{n}) = 1\}$

- Alice commits to a bit b by choosing a random numer r and sending Bob: n, v and $c = r^2 \cdot v^b$
- Bob verifies that $(\frac{v}{n}) = 1$ and keeps it
- Alice reveals herself by sending Bob p, q, r, b
- **6** Bob verifies that p, q are primes, n = pq and $c = r^2 \cdot v^b$

If A wants to commit a quadratic residue, she chooses a quadratic v and b = 1, therefore $r^2 \cdot v^1$ will be quadratic

If a wants to commit a non-quadratic value, she chooses a nonquadratic v and b=0, therefore $r^2\cdot v^0=r^2$ which is quadratic