

(* ДЗ Потенциальное поле *)
 (* в плоскости задано поле $F=(P(x,y), Q(x,y))$ *)
 (* три коэффициента многочлена $P(x,y)$ A,B,C *)
 (* надо определить так, чтобы поле стало потнециальным *)
 (* решить дифференциальное уравнение, то есть восстановить потенциал $U(x,y)$ *)
 (* уравнение $U(x,y)=U(1,1)$ определяет неявную функцию $y=f(x)$ *)
 (* которая решает задачу Коши с начальным условием $1=f(1)$ *)
 (* проведите касательную к решению в точке $x_0=1, y_0=1$ *)
 (* по касательной определите y_1 -- приближенное значение решения*)
 (* в точке $x_1=1+1/10$ *)
 (* продолжите построение ломаной Эйлера, рассмотрите $x_2=1+2/10, x_3=1+3/10$ *)
 (* предложите способ оценивать качество приближения *)

{= = = = = = = = =}

{vr, 1}

$$P(x,y)=9x^3 + Ax^2y + Bxy^2 + Cy^3, \quad Q(x,y)=\frac{2x^3}{3} + 8x^2y + 15xy^2 + 7y^3$$

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{vr, 2}

$$P(x,y)=8x^3 + Ax^2y + Bxy^2 + Cy^3, \quad Q(x,y)=3x^3 + 8x^2y + 9xy^2 + 3y^3$$

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{vr, 3}

$$P(x,y)=7x^3 + Ax^2y + Bxy^2 + Cy^3, \quad Q(x,y)=\frac{8x^3}{3} + 9x^2y + 18xy^2 + 9y^3$$

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{vr, 4}

$$P(x,y)=7x^3 + Ax^2y + Bxy^2 + Cy^3, \quad Q(x,y)=\frac{8x^3}{3} + 7x^2y + 12xy^2 + 3y^3$$

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{vr, 5}

$$P(x,y)=7x^3 + Ax^2y + Bxy^2 + Cy^3, \quad Q(x,y)=\frac{8x^3}{3} + 5x^2y + 18xy^2 + 4y^3$$

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{vr, 6}

$$P(x,y)=2x^3 + Ax^2y + Bxy^2 + Cy^3, \quad Q(x,y)=2x^3 + 3x^2y + 12xy^2 + 7y^3$$

{= = = = = = = = =}

{vr, 7}

$$P(x,y)=3x^3 + Ax^2y + Bxy^2 + Cy^3, \quad Q(x,y)=\frac{5x^3}{3} + 8x^2y + 18xy^2 + 7y^3$$

{= = = = = = = = =}

{vr, 8}

$$P(x,y)=5x^3 + Ax^2y + Bxy^2 + Cy^3, \quad Q(x,y)=\frac{2x^3}{3} + 5x^2y + 21xy^2 + 2y^3$$

{= = = = = = = = =}

{vr, 9}

$$P(x, y) = 9x^3 + Ax^2y + Bxy^2 + Cy^3, \quad Q(x, y) = \frac{7x^3}{3} + 9x^2y + 15xy^2 + 3y^3$$

{= = = = = = = = =}

{vr, 10}

$$P(x, y) = 9x^3 + Ax^2y + Bxy^2 + Cy^3, \quad Q(x, y) = \frac{2x^3}{3} + 7x^2y + 24xy^2 + 8y^3$$

{= = = = = = = = =}

{vr, 11}

$$P(x, y) = 9x^3 + Ax^2y + Bxy^2 + Cy^3, \quad Q(x, y) = \frac{7x^3}{3} + 8x^2y + 15xy^2 + 6y^3$$

{= = = = = = = = =}

{vr, 12}

$$P(x, y) = 4x^3 + Ax^2y + Bxy^2 + Cy^3, \quad Q(x, y) = \frac{2x^3}{3} + 5x^2y + 27xy^2 + 5y^3$$

{= = = = = = = = =}

{vr, 13}

$$P(x, y) = 3x^3 + Ax^2y + Bxy^2 + Cy^3, \quad Q(x, y) = 2x^3 + 4x^2y + 9xy^2 + 4y^3$$

{= = = = = = = = =}

{vr, 14}

$$P(x, y) = 6x^3 + Ax^2y + Bxy^2 + Cy^3, \quad Q(x, y) = \frac{8x^3}{3} + 5x^2y + 9xy^2 + 2y^3$$

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{vr, 15}

$$P(x, y) = 9x^3 + Ax^2y + Bxy^2 + Cy^3, \quad Q(x, y) = 3x^3 + 2x^2y + 9xy^2 + 6y^3$$

{= = = = = = = = =}

{vr, 16}

$$P(x, y) = 8x^3 + Ax^2y + Bxy^2 + Cy^3, \quad Q(x, y) = \frac{8x^3}{3} + 5x^2y + 27xy^2 + 4y^3$$

{= = = = = = = = =}

{vr, 17}

$$P(x, y) = 4x^3 + Ax^2y + Bxy^2 + Cy^3, \quad Q(x, y) = 3x^3 + 6x^2y + 15xy^2 + 2y^3$$

{= = = = = = = = =}

{vr, 18}

$$P(x, y) = 7x^3 + Ax^2y + Bxy^2 + Cy^3, \quad Q(x, y) = 3x^3 + 6x^2y + 24xy^2 + 5y^3$$

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{vr, 19}

$$P(x, y) = 9x^3 + Ax^2y + Bxy^2 + Cy^3, \quad Q(x, y) = 3x^3 + 7x^2y + 15xy^2 + 7y^3$$

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{vr, 20}

$$P(x, y) = 2x^3 + Ax^2y + Bxy^2 + Cy^3, \quad Q(x, y) = \frac{8x^3}{3} + 4x^2y + 21xy^2 + 4y^3$$

{= = = = = = = = =}

{vr, 21}

$$P(x, y) = 9x^3 + Ax^2y + Bxy^2 + Cy^3, \quad Q(x, y) = \frac{8x^3}{3} + 4x^2y + 9xy^2 + 2y^3$$

{= = = = = = = = =}

{vr, 22}

$$P(x, y) = 7x^3 + Ax^2y + Bxy^2 + Cy^3, \quad Q(x, y) = 3x^3 + 3x^2y + 12xy^2 + 5y^3$$

{= = = = = = = = =}

{vr, 23}

$$P(x, y) = 4x^3 + Ax^2y + Bxy^2 + Cy^3, \quad Q(x, y) = 3x^3 + 4x^2y + 18xy^2 + 6y^3$$

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{vr, 24}

$$P(x, y) = 3x^3 + Ax^2y + Bxy^2 + Cy^3, \quad Q(x, y) = 2x^3 + 8x^2y + 6xy^2 + 8y^3$$

{= = = = = = = = =}

{vr, 25}

$$P(x, y) = 6x^3 + Ax^2y + Bxy^2 + Cy^3, \quad Q(x, y) = \frac{5x^3}{3} + 4x^2y + 24xy^2 + 9y^3$$

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{vr, 26}

$$P(x, y) = 9x^3 + Ax^2y + Bxy^2 + Cy^3, \quad Q(x, y) = x^3 + 2x^2y + 21xy^2 + 4y^3$$

{= = = = = = = = =}

{vr, 27}

$$P(x, y) = 2x^3 + Ax^2y + Bxy^2 + Cy^3, \quad Q(x, y) = 3x^3 + 7x^2y + 15xy^2 + 5y^3$$

{= = = = = = = = =}

{vr, 28}

$$P(x, y) = 3x^3 + Ax^2y + Bxy^2 + Cy^3, \quad Q(x, y) = \frac{7x^3}{3} + 2x^2y + 15xy^2 + 9y^3$$

{= = = = = = = = =}

{vr, 29}

$$P(x, y) = 8x^3 + Ax^2y + Bxy^2 + Cy^3, \quad Q(x, y) = 3x^3 + 6x^2y + 21xy^2 + 3y^3$$

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{vr, 30}

$$P(x, y) = 3x^3 + Ax^2y + Bxy^2 + Cy^3, \quad Q(x, y) = x^3 + 9x^2y + 15xy^2 + 7y^3$$

(* P = . . + A x^2 y + B x y^2 + . . . (P, Q) & (-Q, P) потенциаьны *)