Hybrid Improvement on Implicit Ranking Via BPR and WR-MF

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Abstract—Implementing a hybrid approach, both Bayesian Personalized Ranking (BPR) and Weighted Regularized Matrix Factorization (WR-MF) have been applied to movie datasets, yielding improved performance across metrics such as AUC, NDCG, Precision, and Recall. This study introduces a universal formulation that compares the highest-rated items for each user with similar items based on various similarity measures, including Overlap Coefficient, Cosine, Jaccard, Tversky Index, and Dice.

The core idea involves processing any user-item dataset with ratings, utilizing a pre-processor for the ratings, and subsequently achieving enhanced predictive results. Given that BPR and WR-MF predominantly operate on implicit feedback, the overall ranking prediction score demonstrates notable improvement when preparing datasets with implicit feedback.

Index Terms—Hybrid Recommendation, Bayes Theorem, Bayesian Prediction, Item Based Recommendation System, Content Based Recommendation System, Weighted Ranking, Matrix Factorization, AUC, NDCG, Overlap Coefficient.

I. INTRODUCTION

TEM recommendation plays a pivotal role in delivering tailored content or products to users, anticipating their preferences and needs. The fundamental objective of this task is to predict a personalized ranking among a myriad of items, such as websites, movies, stocks, cryptocurrency or products. In this paper, I delve into a prevalent scenario where implicit feedback, including user actions like clicks, acquisition or purchases, guides the recommendation process.

Common approaches to item recommendation from implicit feedback, such as matrix factorization (MF) or adaptive k-nearest-neighbor (KNN), have been designed with the aim of personalized ranking. However, an intriguing observation surfaces: these methods, despite their intended purpose, are not directly optimized for the intricate task of ranking. In response to this gap, my research uses a set of optimization criterion, termed BPR-Opt [1] and WR-MF [2], specifically tailored for personalized ranking. This criterion arises as the maximum posterior estimator derived from a Bayesian analysis of the problem.

In an effort to enhance the efficacy of BPR and WR-MF approach, I propose the incorporation of Content-Based analysis and ranking. This strategic addition aims to elevate the probability and evaluation metrics of BPR and WR-MF, further refining the accuracy and relevance of personalized recommendations. In the realm of content-based analysis, I aim to elevate the metrics of BPR and WR-MF through enhancements utilizing Jaccard, Cosine, Overlap Coefficient, Tversky Index and Dice Similarity.

II. LITERATURE REVIEW

Recommendation systems play a crucial role in sifting through vast amounts of information. Nevertheless, they frequently encounter challenges such as the cold start and sparsity problems, which hinder their overall effectiveness. Bayesian Personalized Ranking (BPR), designed to predict the relative order of user items, has traditionally been suggested to tackle these issues within ranking-based recommendation systems. However, conventional BPR methods heavily depend on implicit feedback and lack the inclusion of semantic and visual sentiment information. To bolster the efficacy of BPR, recent studies indicate that integrating diverse forms of side information, such as images, texts, videos, knowledge graphs, browsing history [3][4] and social network data, [5] can mitigate the sparsity inherent in the rating matrix.

Employing a fusion of Convolutional Neural Networks (CNN) and Bayesian Personalized Ranking (BPR) presents a promising solution to tackle the cold start problem in friend recommendation systems (BayDNN) [3]. This innovative approach leverages the capabilities of deep neural networks to effectively handle scenarios where limited or no information is available for new users or items.

In response to the constraints of existing pairwise preference learning methods and "One-Class Collaborative Filtering", MSBPR [6] introduces a novel approach. Specifically, it addresses this limitation by formulating multi-pairwise preferences, achieved through a more detailed categorization of user non-interacted items into the user's potentially favored degree, the user's disliked degree, and the uncertain degree. This enhancement provides a more nuanced understanding of user preferences, contributing to the effectiveness of the MSBPR model.

Functioning as a content-based recommendation algorithm, Category-aided Multi-channel Bayesian Personalized Ranking (CMBPR) [4] seamlessly integrates users' detailed preference data by considering variances across distinct video categories and various user interactions. Empirical results underscore the effectiveness of the CMBPR video recommendation algorithm, showcasing a significantly heightened level of recommendation accuracy in comparison to traditional video recommendation algorithms. Notably, CMBPR adeptly addresses the challenges posed by the "Long Tail" effect which is niche category short videos have the potential to expand and constitute a substantial proportion of the overall recommended short videos, providing a robust solution to enhance the quality of video recommendations.

To mitigate the sparsity challenges inherent in rating systems, the VBPR model [7] underwent optimization from

various visual perspectives. This involved leveraging VGG features along with related visual attributes such as shape, color, and texture. Extracting visual features, including color and texture, from images was instrumental in enhancing the VBPR model. This optimization was built upon the foundation of the Matrix Factorization (MF) model.

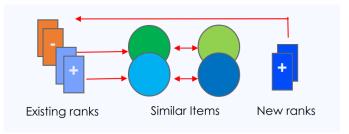
In practice, the mere observation of items by users doesn't necessarily imply a preference for those items. Moreover, when dealing with the vast majority of items that go unobserved, it is oversimplified to categorize them as purely negative feedback. Mean Bayesian Personalized Ranking algorithm (MBPR) [8] building upon the Bayesian Personalized Ranking (BPR) approach categorizes observed interactions higher or lower than the average rating as positive or negative feedback and unobserved interactions are labeled with random values within a defined range, random assignment reflects the uncertainty about whether a user prefers unobserved items For each user, the interactions are categorized based on these criteria, offering a more nuanced and probabilistic representation of user preferences compared to simplistic binary classifications.

The Listwise Bayesian Personalized Ranking (LBPR) [9] methodology is employed to calculate the likelihood of a ranking list for subsequent computation. Following the prediction of categories, Point-of-Interest (POI) candidates are filtered accordingly and ranked based on a dual strategy involving spatial influence and category ranking influence. This approach not only effectively tackles computational challenges but also enriches our comprehension of transition patterns between POIs. The outcome is a more robust and efficient next POI recommendation system within Location-Based Social Networks (LBSNs).

EBPRMF is employed for learning within each cluster, selecting Points-of-Interest (POIs) closest to the user's preferences to construct a recommendation list [10]. This list is then presented to the user. Proposed as an improved iteration, EBPRMF refines the BPRMF recommendation algorithm by adjusting the POI similarity measurement, thereby augmenting its overall accuracy. Furthermore, to enhance recommendation diversity, this enhanced version introduces spectral clustering to the conventional BPRMF recommendation algorithm.

WR-MF [11] enhances both the efficacy and efficiency of Matrix Factorization (MF) approaches in handling implicit feedback. We address two key challenges present in current methodologies. Firstly, many existing approaches tend to assign a uniform weight to unobserved feedback to mitigate computational complexity arising from the extensive space of unobserved data. However, this uniform assumption does not hold in real-world scenarios. Secondly, most methods are formulated in an offline context, lacking the adaptability required for the dynamic nature of online data. this method aims to tackle one-class collaborative filtering (OCCF) challenges through two distinct approaches: weighted low-rank approximation and negative example sampling which encompasses assigning weights to the missing data according to the popularity of the items [11].

The fundamental concept behind Weighted Regularized Matrix Factorization (WRMF) involves allocating smaller weights to unobserved instances compared to observed ones. These



By detecting positive rates corresponding items, novel rates will be added to the initial dataset, the similarity measure is responsible for matching similar items.

Fig. 1. Simple loop of novel rate addition

weights are intricately tied to the notion of confidence. Given that non-interaction with an item can stem from factors other than disliking it, negative instances carry lower confidence. This could be attributed to scenarios where a user is unaware of the item's existence or faces constraints such as its price or limited availability, making the unobserved instances a blend of negative and unknown feedback.

III. METHODOLOGY

To improve the performance metrics of Bayesian Personalized Ranking (BPR) and Weighted Regularized Matrix Factorization (WR-MF), a comprehensive formulation has been devised. This formulation is centered on extracting nonquantitative features from the content of items and leveraging them to establish similarity between items. The process involves selecting items with prior ratings for a specific user, considering them as potential items of interest related to the user's preferences. These selected items are then added to the list of highly ranked items for each user, thereby enhancing the recommendation system by incorporating both content-based and collaborative filtering approaches, employing Categoryaided Multi-channel Bayesian Personalized Ranking [4] integrates multi-relational feedback sampling and category-aided sampling simultaneously to address this challenge, tourist attraction recommendation system, grounded in SS and enhanced VBPR, attained a commendable level of accuracy, effectively met user expectations, and significantly mitigated issues related to data sparsity.

 $Sims(I_i,I_j)$ computes the collection of akin items, given a minimum measured similarity threshold min_s that serves as the minimum acceptable similarity level between the items I_i and I_j This function is designed to generate a list of items that exhibit a degree of similarity equal to or greater than the specified minimum threshold, offering a comprehensive overview of related items in the context of their similarity to I_i .

$$Sims(I_i, I_j) = \begin{cases} Sim(I_j, I_j) & \text{if } \geq min_s; \\ & \text{if } < min_s. \end{cases}$$

 $Sim(I_i,I_j)$ calculates the similarity between two items based on content-based metrics such as genre, tags, reviews, etc., utilizing Jaccard, Cosine, Overlap Coefficient [12], Tversky Index and Dice similarity measures.

Given $Sr(u_j)$ as the set of similar items for a particular user u_j with ranking higher than min_r , the process involves computing the collection of movies that are similar to the user's top-rated movies (those with ratings higher than min_r).

$$Sr(u_j) = \begin{cases} Sims(I_i, I_j) & \text{if } r_j \ge min_r; \\ & \text{if } r_j < min_r. \end{cases}$$

Following the computation of the list of new ratings for each user, the next step involves appending these calculated ratings into the original rating array:

$$N = \begin{bmatrix} Sr(u_1) \\ Sr(u_2) \\ \vdots \\ Sr(u_n) \end{bmatrix}$$

Encompassing both the pre-existing ratings and the newly calculated ratings, N amalgamated array serves as a comprehensive repository of user preferences, capturing the dynamics of both historical and recently generated ratings. this will be used as input variable to BPR and WR-MF algorithms for further and extended processing.

The methodology involves augmenting new ratings based on the similar items to those liked by each user. This process entails a random addition mechanism, where a shuffled list of users is employed to introduce new ratings for a specified number of items. Essentially, this approach involves updating the dataset with a pre-processed data before training the BPR and WR-MF models.

IV. APPLICATION

The hybrid model utilized the ml-1m dataset. Additional ratings were introduced into the rating data frame based on movies with similar genres, employing genre as the similarity measure. This was achieved by calculating the distance and filtering similar movies using mentioned similarity measures, with a threshold set at 0.9. The process involved iterating through each user's rankings and selecting movies with ranks exceeding 3.0 as positive feedback. This methodology essentially resembles implicit ranking, treating movies with ratings higher than 3.0 as though they have been watched.

Leveraging genres as a pivotal content medium, the extraction process involved meticulously curating a list of movies exhibiting a similarity threshold surpassing 0.9 for each user's set of rankings. Following this, a nuanced approach was implemented to append new ratings to these movies. The methodology for assigning these ratings was intricately tailored to align with the user's existing ranked values, drawing inspiration from the reference movie ranks.

This comprehensive procedure was systematically executed for the dataset comprising 1 million movies, ensuring a diverse representation across genres. To validate the robustness of the approach, the examination was extended to users randomly sampled for each movie. This iterative analysis provided a nuanced understanding of how user preferences and rankings were dynamically influenced by the intricate interplay of genres and similarity metrics within the dataset.

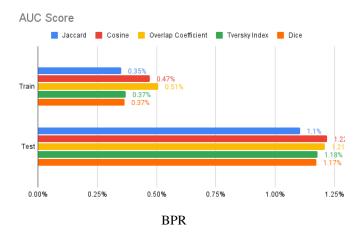


Fig. 2. Improvement of AUC score after application of the hybrid method

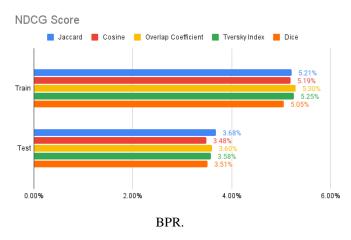


Fig. 3. Improvement of NDCG score after application of the hybrid method

V. RESULTS

1. Bayesian Personalized Ranking

As an initial note, the Amazon Movies and TV shows review dataset was employed in the BPR implementation to evaluate the method's performance on other datasets with higher sparsity. The results indicate a lower AUC score, suggesting certain limitations in BPR's predictive capabilities when applied to real data with increased sparsity.

AUC Score	Train AUC	Test AUC
Movielens_1M	0.886287	0.852563
Movies_and_TV_5	0.965592	0.773447

Implemented the Bayesian personalized ranking [1] algorithm to forecast rankings using both the pure and extended ratings data frames. Employed the AUC Score metric as a benchmark study, serving as a pivotal measure for evaluating the prediction performance.

The updated rating data frame was supplied as input to BPR. The model was trained, and the AUC score of the predictions was computed. Consequently, the ensuing table (Table. I) presents the AUC scores corresponding to various sets of input combinations for $Sr(u_i)$, aggregated across N. This analysis

provides a comprehensive overview of how different input configurations impact the AUC performance metrics.

The findings demonstrate a minor improvement, revealing a 0.51% enhancement in the prediction AUC score for the training set and a noteworthy 1.21% improvement for the test set when employing the Bayesian personalized ranking algorithm (BPR).

Notably, these positive outcomes underscore the efficacy of the BPR algorithm in refining predictive performance. Moreover, the observed gains hint at the potential for even more remarkable results by augmenting the dataset with an increased number of novel ranks. As the number of ranks expands, there is a promising prospect of further refining the algorithm's ability to capture nuanced patterns and enhance its overall predictive accuracy.

Employing the aforementioned similarity measure to identify comparable items, the subsequent chart illustrates the enhancements observed in both the AUC score and NDCG score across both the training and testing datasets. The utilization of this similarity measure has evidently led to improvements in the predictive performance, as demonstrated by the notable shifts in AUC and NDCG scores in the chart depicted in Fig(2) and Fig(3), For each similarity method, the chart values depict the percentage improvement achieved through the application of the respective similarity measurement using thr corresponding method (BPR, WR-MF), as evident from the observations, the Overlap coefficient and Cosine similarity measures exhibit superior performance in accurately matching similar items within the hybrid implementation, beyond the numerical scores, the AUC is revealed to be less reliant on the recently added ratings, making it a more robust method for predicting missing items.

2. Weighted Regularized Matrix Factorization

The revised rating data frame served as the input for WR-MF. After training the model, the Precision, Recall, and NDCG for the predictions were calculated. Subsequently, the resulting table displays the Precision, Recall, and NDCG values associated with diverse input combinations for $Sr(u_j)$, aggregated across N. This examination offers a thorough understanding of how different input configurations influence the Precision, Recall, and NDCG performance metrics.

Applying the mentioned similarity measure to identify analogous items, the subsequent chart (see Table. II) illustrates improvements observed in NDCG@k, Precision@k, and Recall@k on testing datasets. The utilization of this similarity measure has evidently resulted in enhanced predictive performance, as depicted by significant shifts in the mentioned

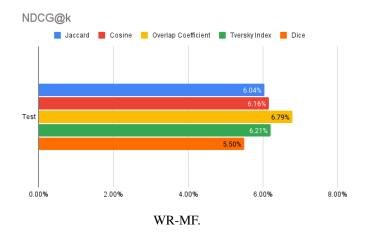


Fig. 4. Improvement of NDCG score after application of the hybrid method

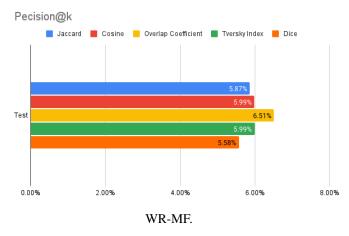


Fig. 5. Improvement of precision after application of the hybrid method

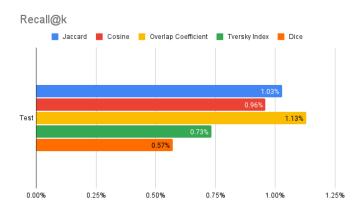
evaluation metrics in Fig(4), Fig(6), and Fig(5). As discerned from the observations, the Overlap coefficient and Cosine similarity measures outperform in accurately matching similar items within the hybrid implementation. Going beyond numerical scores, it is noteworthy that WR-MF exhibits a greater dependence on initial data for implicit prediction compared to BPR. Consequently, precision improves more significantly in WR-MF than in BPR.

The findings demonstrate a good improvement, revealing a 6.79% enhancement in the prediction NDCG@k, 6.51% for Precision@k and 1.13% of increment in Recall@k assessed on the test set when employing the Weighted Regularized Matrix Factorization (WR-MF).

Set -	AUC		NDCG			Recall			
	Prec1	Prec2	Imp	NDCG1	NDCG2	Imp	Recall1	Recall2	imp
Test	0.29687	0.35556	5.87%	0.33593	0.39632	6.04%	0.13444	0.14473	1.03%
Test	0.29759	0.35748	5.99%	0.33655	0.39812	6.16%	0.13396	0.143549	0.96%
Test	0.29716	0.36228	6.51%	0.33703	0.40489	6.79%	0.13561	0.14691	1.13%
Test	0.29814	0.35807	5.99%	0.33648	0.39856	6.21%	0.13567	0.143	0.73%
Test	0.29688	0.35263	5.58%	0.33552	0.39056	5.50%	0.13458	0.14028	0.57%
	Test Test Test Test	Test 0.29687 Test 0.29759 Test 0.29716 Test 0.29814	Rest Prec1 Prec2 Test 0.29687 0.35556 Test 0.29759 0.35748 Test 0.29716 0.36228 Test 0.29814 0.35807	Set Prec1 Prec2 Imp Test 0.29687 0.35556 5.87% Test 0.29759 0.35748 5.99% Test 0.29716 0.36228 6.51% Test 0.29814 0.35807 5.99% Test 0.29688 0.35263 5.58%	Set Prec1 Prec2 Imp NDCG1 Test 0.29687 0.35556 5.87 % 0.33593 Test 0.29759 0.35748 5.99 % 0.33655 Test 0.29716 0.36228 6.51 % 0.33703 Test 0.29814 0.35807 5.99 % 0.33648	Set Prec1 Prec2 Imp NDCG1 NDCG2 Test 0.29687 0.35556 5.87% 0.33593 0.39632 Test 0.29759 0.35748 5.99% 0.33655 0.39812 Test 0.29716 0.36228 6.51% 0.33703 0.40489 Test 0.29814 0.35807 5.99% 0.33648 0.39856 Test 0.29688 0.35263 5.58% 0.33552 0.39056	Set Prec1 Prec2 Imp NDCG1 NDCG2 Imp Test 0.29687 0.35556 5.87% 0.33593 0.39632 6.04% Test 0.29759 0.35748 5.99% 0.33655 0.39812 6.16% Test 0.29716 0.36228 6.51% 0.33703 0.40489 6.79% Test 0.29814 0.35807 5.99% 0.33648 0.39856 6.21% Test 0.29688 0.35263 5.58% 0.33552 0.39056 5.50%	Set Prec1 Prec2 Imp NDCG1 NDCG2 Imp Recall1 Test 0.29687 0.35556 5.87 % 0.33593 0.39632 6.04% 0.13444 Test 0.29759 0.35748 5.99 % 0.33655 0.39812 6.16% 0.13396 Test 0.29716 0.36228 6.51 % 0.33703 0.40489 6.79% 0.13561 Test 0.29814 0.35807 5.99 % 0.33648 0.39856 6.21% 0.13567 Test 0.29688 0.35263 5.58 % 0.33552 0.39056 5.50% 0.13458	Set Prec1 Prec2 Imp NDCG1 NDCG2 Imp Recall1 Recall2 Test 0.29687 0.35556 5.87 % 0.33593 0.39632 6.04% 0.13444 0.14473 Test 0.29759 0.35748 5.99 % 0.33655 0.39812 6.16% 0.13396 0.143549 Test 0.29716 0.36228 6.51 % 0.33703 0.40489 6.79% 0.13561 0.14691 Test 0.29814 0.35807 5.99 % 0.33648 0.39856 6.21% 0.13567 0.143 Test 0.29688 0.35263 5.58 % 0.33552 0.39056 5.50% 0.13458 0.14028

Similarity Measure	Set		AUC		NDCG			
Similarity Measure	Sei	AUC1	AUC2	Imp	NDCG1	NDCG2	Imp	
Jaccard	Train	0.886071	0.889586	0.35%	0.532628	0.584745	5.21%	
	Test	0.85208	0.863133	1.1%	0.340224	0.377007	3.68%	
Cosine	Train	0.885419	0.890127	0.47%	0.534402	0.586267	5.19%	
	Test	0.851683	0.863857	1.22%	0.342056	0.376879	3.48%	
Overlap Coefficent	Train	0.886287	0.891349	0.51%	0.534955	0.587915	5.30%	
	Test	0.852563	0.864642	1.21%	0.342198	0.378239	3.60%	
TverskyIndex	Train	0.886051	0.889753	0.37%	0.534571	0.587118	5.25%	
	Test	0.852189	0.86396	1.18%	0.341766	0.377536	3.58%	
Dice	Train	0.885916	0.889575	0.37%	0.534394	0.584878	5.05%	
	Test	0.851509	0.863242	1.17%	0.341764	0.37685	3.51%	
			TABLE II					

WR-MF RESULTS AND METRICS OVER TRAIN AND TEST OF ML-1M DATASET



For each similarity method, the chart values depict the percentage improvement achieved through the application of the respective similarity measurement using WR-MF.

Fig. 6. Improvement of recall after application of the hybrid method

VI. DATASET

Movie Lens 1M

The ML-1M dataset was utilized to extract detailed information, encompassing rankings, movies, user profiles, and genre classifications. This dataset stands as a valuable resource, facilitating a comprehensive exploration and analysis of the intricate relationships and patterns within the realm of movies.

Movies and TV 5 Reviews

The amazon dataset for the movies was utilized to assess BPR ranking performance, this dataset does not cover the detailed information about the movies, so the content extraction and similarity is not applicable for it.

VII. CONCLUSION

In the realm of NDCG, the performance of both Bayesian Personalized Ranking (BPR) and Weight Regularized Matrix Factorization (WR-MF) stands remarkably similar. However, an innovative approach involving the integration of preprocessed similar ratings into the dataset reveals interesting

nuances. This experimentation highlights that WR-MF demonstrates a heightened responsiveness to the newly introduced ratings, leading to a more substantial improvement compared to BPR.

While the comparative analysis underscores the enhanced sensitivity of WR-MF to the augmented dataset, it's important to consider the computational aspects. BPR, in contrast, exhibits a lower computational demand, suggesting a trade-off between sensitivity to new ratings and processing efficiency. This insight into their respective strengths and efficiencies adds valuable perspective to the evaluation of recommendation algorithms.

Based on the comprehensive iterations conducted with both WR-MF and BPR, the Overlap Coefficient emerges as the standout similarity measure. Through a thorough examination of their respective performances, the Overlap Coefficient consistently outshines other measures in capturing the similarity between items. This finding underscores the robustness and efficacy of the Overlap Coefficient in the context of recommendation systems, offering valuable insights for optimizing the similarity calculations in such algorithms.

Given that the overlap coefficient is traditionally associated with graphs, the superior performance observed in this study suggests that genre data, when transformed into graphs, can be more effectively processed and analyzed than when employing linear or matrix-based comparisons. The assumption underlying this preference for the overlap coefficient is grounded in its primary usage for social network friendship recommendations, where individuals with social similarities are often found to share similar movie-watching preferences.

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