

Q Given three integers  $n$ ,  $a$  and  $b$ , return  $n^{\text{th}}$  magical no. Since the ans may be very large return

A magical no. - if no. is divisible by either  $a$  or  $b$ .

$$n=1, a=2, b=3$$

$$\text{out} = 2$$

⇒ Approach:

1. Creating a modulo with value  $10^9 + 7$
2. Calculating lcm of  $a$  and  $b$  with the help of GCD relation

$$\text{lcm} = \frac{(a \times b)}{\text{gcd}(a, b)}$$

3. Performing binary search  
 (start)  $s = \min(a, b)$   
 (end)  $e = n \times \min(a, b)$   
 $\text{mid} = \frac{(s+e)}{2}$

4. Counting magical number  $\leq \text{mid}$   
 $\text{count} = \frac{\text{mid}}{a} + \frac{\text{mid}}{b} - \frac{\text{mid}}{\text{lcm}}$

if  $\text{count} < n$  then  $s = \text{mid} + 1$   
 else  $\Rightarrow e = \text{mid}$ .

5. return  $\text{low} \% \text{MOD}$ .

⇒ Code:

```
long long gcd(long long a, long long b) {
    if (b == 0) return a;
    return gcd(b, a % b);
}
```

\_/\_/\_

```
return gcd(b, a%b);
```

```
}
```

```
long long lcm (long long a, long long b) {
```

```
    return (a / gcd(a,b)) * b;
```

```
}
```

```
int nthMagicalNumber (int n, int a, int b) {  
    int mod = 1000000007;
```

```
    long long low = min(a,b);
```

```
    long long high = n * min(a,b);
```

```
    long long L = lcm(a,b);
```

```
    while (low < high) {
```

```
        long long mid = low + (high - low) / 2;
```

```
        long long count = mid / a + mid / b - mid / L;
```

```
        if (count < n)
```

```
            low = mid + 1;
```

```
        else
```

```
            high = mid;
```

```
    }
```

```
    return low % MOD;
```

```
}
```

```
int main () {
```

```
    cout << nthMagicalNumber(1, 2, 3);
```

```
}
```

OUTPUT = 2.