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Q Given three integers  $n$ ,  $a$  and  $b$ , return  $n^{th}$  magical no. Since the ans may be very large return

A magical no. - if no. is divisible by either  $a$  or  $b$ .

$$n=1, a=2, b=3 \\ \text{out} = 2$$

$\Rightarrow$  Approach :

1. Creating a modulo with value  $10^9 + 7$
2. Calculating lcm of  $a$  and  $b$  with the help of GCD relation

$$\text{lcm} = (a \times b)$$

$$\text{gcd}(a, b)$$

3. Performing binary search

(start)  $s = \min(a, b)$

(end)  $e = n \times \min(a, b)$

$$\text{mid} = \frac{(s+e)}{2}$$

4. Counting magical numbers  $\leq \text{mid}$ .

$$\text{count} = \frac{\text{mid}}{a} + \frac{\text{mid}}{b} - \frac{\text{mid}}{\text{lcm}}$$

if  $\text{count} < n$  then  $s = \text{mid} + 1$

else  $\Rightarrow e = \text{mid}$ .

5. return  $\text{last \% MOD}$ .

$\Rightarrow$  Code :

```
long long gcd(long long a, long b){  
    if (b == 0) return a;  
}
```

3 return gcd(b, a%b);

long long lcm (long long a, long long b) {  
    return (a \* b) / gcd(a, b);}

3

int nthMagicalNumber (int n, int a, int b) {  
    int mod = 1000000007;

    long long low = min(a, b);

    long long high = n \* min(a, b);

    long long L = lcm(a, b);

    while (low < high) {

        long long mid = low + (high - low) / 2;

        long long count =  $\frac{mid}{a} + \frac{mid}{b} - \frac{mid}{c}$ ;

        if (count < n)

            low = mid + 1;

        else

            high = mid;

3

    return low % MOD;

3

int main () {

    cout << nthMagicalNumber(1, 2, 3);

3.

OUTPUT = 2.