

Test cases:

input 1:  $A = [1, 3, 5]$

output 1: 8

input 2:  $A = [2, 3]$

output 2: 2

we define  $f[X, Y]$  as number of different corresponding bits in the binary representation of  $X$  &  $Y$ . for example,  $f(2, 7) = 2$ , since the binary representation of 2 & 7 are 010 and 111, respectively. The first and the third bit differ, so  $f(2, 7) = 2$ .

You are given an array of  $N$  positive integers,  $A_1, A_2, \dots, A_N$ . Find sum of  $f(A_i, A_j)$  for all pairs  $(i, j)$  such that  $1 \leq i, j \leq N$ . Return the answer modulo  $10^9 + 7$ .

$\Rightarrow$  Given

$f(x, y)$  = no. of different bits in binary of  $x$  &  $y$   
 [checking every bits  $\rightarrow TC = (N^2) \rightarrow TLE$ ]

To solve this, we can use the concept of bit manipulation - Try checking the bits of  $x$  &  $y$ .

Let's look at a particular  $k^{th}$  bit

if  $k^{th}$  bit of  $x$  is 1 &  $k^{th}$  bit of  $y$  is 0.

or vice versa

so ans = 2 for pair  $(x, y)$  &  $(y, x)$

$\hookrightarrow$  Let cnt 1 = nos having bit  $k = 1$

cnt 2 = nos having bit  $k = 0$

contribution =  $2 \times \text{cnt 1} \times \text{cnt 0}$

for  $(x, y)$  and  $(y, x)$



→ Steps to solve:

For every bit (0 → 31)

- 1) Count numbers having that bit set.
- 2) Compute pairs.
- 3) Add to answer.

→ Code:

```
#include <bits/stdc++.h>
using namespace std;
```

```
const long long MOD = 1e9 + 7;
```

```
long long totalPairs (vector<int> &A) {
```

```
    long long n = A.size();
```

```
    long long ans = 0;
```

```
    for (int bit = 0; bit < 32; bit++) {
```

```
        long long cnt1 = 0;
```

```
        for (int i = 0; i < n; i++) {
```

```
            if (A[i] & (1 << bit)) {
```

```
                cnt1++;
```

```
            }
```

```
        }
```

```
        long long contribution = (cnt1 * cnt0) % MOD;
```

```
        contribution = (2 * contribution) % MOD;
```

```
        ans = (ans + contribution) % MOD;
```

```
    }
```

```
    return ans;
```

```
}
```