

$$f = 1/T$$

$$\omega = 2\pi f$$

Voltage divider:

$$V_{r1} = v_i \frac{R1}{R1+R2}$$

Voltage and Current gain in decibels:

$$A_{v\text{-dB}} = 20 \log_{10}(A_{V/V})$$

$$A_{i\text{-dB}} = 20 \log_{10}(A_{A/A})$$

Power gain in decibels:

$$A_{p\text{-dB}} = 10 \log_{10}(A_{W/W})$$

The power gain in decibels is the average of the voltage and amperage gain in decibels.

Amplifier Models:

$$v_o = A_{v_o} v_i \frac{R_L}{R_L + R_o}$$

$$A_v = A_{v_o} \frac{R_L}{R_L + R_o}$$

Consider the voltage divider at the output for the load. There may also be one at the source getting into the input of the amplifier.

Amplifier Types:

Voltage: $A_{v_o} \equiv \frac{v_o}{v_i}$

Wants: $R_i \rightarrow \infty$ and $R_o \rightarrow 0$

Current: $A_{i_s} \equiv \frac{i_o}{i_s}$

Wants: $R_i \rightarrow 0$ and $R_o \rightarrow \infty$

Transconductance: $G_m \equiv \frac{i_o}{v_i}$

Wants: $R_i \rightarrow \infty$ and $R_o \rightarrow \infty$

Transresistance: $R_m \equiv \frac{v_o}{i_s}$

Wants: $R_i \rightarrow 0$ and $R_o \rightarrow 0$

Frequency Response of Amplifier

STC (single time constant) networks:

$$\tau = L / R \text{ or } \tau = CR$$

Low-pass filter with RC, voltage output is across the capacitor because it appears short at high frequencies.

High-pass filter with RC, voltage output is across the resistor.

This is opposite for inductors.

Semiconductors

Intrinsic means not doped. Group IV elements make good semiconductors because they have 4 valence electrons. At low temps, covalent bonds remain more intact and don't conduct electricity. Higher temps means more free electrons means more current.

Recombination n_i is number of free holes and electrons in a unit volume.

$$n_i = BT^{3/2} e^{-E_g/2kT}$$

B is material dependent parameter ($7.3 \times 10^{15} \text{cm}^{-3} \text{K}^{-3/2}$ for Si)

E_g is band gap energy, in Si it's 1.12 eV.

k is Boltzmann's Constant

$$(8.62 \times 10^{-5} \text{eV/K})$$

Doped semiconductors

N-type: Dope the semiconductor with a Group V element. Those have an extra electron, so now there are extra free electrons making it N-type.

If $N_D \gg n_i$ then $n_n \approx N_D$

$$n_n p_n = n_i^2$$

$$p_n = \frac{n_i^2}{N_D}$$

P-type: Dope the semiconductor with a Group III element, more holes.

If $N_D \gg n_i$ then $n_n \approx N_D$

$$p_p n_p = n_i^2$$

$$n_p = \frac{n_i^2}{N_A}$$

Drift Current

$$\text{Hole velocity } v_{p\text{-drift}} = \mu_p E \frac{cm}{s}$$

$$\mu_p = 480 \frac{cm^2}{s}$$

$$\text{Electron velocity } v_{n\text{-drift}} = -\mu_n E \frac{cm}{s}$$

$$\mu_n = 1350 \frac{cm^2}{s}$$

$$\text{Hole current: } I_p = A q p v_{p\text{-drift}}$$

$$I_p = A q p \mu_p E$$

$$J_p = \frac{I_p}{A} = q p \mu_p E$$

p is hole concentration

$$\text{Electron current: } I_n = -A q n v_{n\text{-drift}}$$

$$I_n = -A q n \mu_n E$$

$$J_n = \frac{I_n}{A} = q p \mu_n E$$

n is electron concentration q is magnitude of charge: 1.609×10^{-19}

Drift current density:

$$J = J_p + J_n$$

Diffusion Current:

$$J_p = -q D_p \frac{dp(x)}{dx} \frac{A}{cm^2}$$

$$J_n = q D_n \frac{dn(x)}{dx} \frac{A}{cm^2}$$

$$\frac{D_n}{\mu_n} = \frac{D_p}{\mu_p} = V_T$$

V_T is the thermal voltage. $V_T = 25.9 \text{mV}$

Junction Built-in Voltage:

$$V_0 = V_T \ln \left(\frac{N_A N_D}{n_i^2} \right)$$

Usually, V_0 is between 0.6 and 0.9 V.

Magnitude of Charge:

$$|Q_+| = q A x_n N_D$$

$$|Q_-| = q A x_p N_A$$

A is cross sectional area.

Width of depletion layer:

$$W = x_n + x_p = \sqrt{\frac{2\epsilon_s}{q} \left(\frac{1}{N_A} + \frac{1}{N_D} \right) V_0}$$

$$x_n = W \frac{N_A}{N_A + N_D}$$

$$x_p = W \frac{N_D}{N_A + N_D}$$

$$Q_J = A \sqrt{2\epsilon_s q \left(\frac{N_A N_D}{N_A + N_D} \right) V_0}$$

With reverse voltage V_R :

$$Q_J = A \sqrt{2\epsilon_s q \left(\frac{N_A N_D}{N_A + N_D} \right) (V_0 + V_R)}$$

Capacitance can be found by:

$$C_j = \frac{dQ_J}{dV_R} \Big|_{V_R=V_Q}$$

$$C_j = \frac{\alpha}{2\sqrt{V_0 + V_R}}$$

Where α is shown by

$$\alpha = A \sqrt{2\epsilon_s q \frac{N_A N_D}{N_A + N_D}}$$

Diffusion Capacitance:

$$Q_p = A q [p_n(x_n) - p_{n0}] L_p$$

$$Q_p = \frac{L_p^2}{D_p} I_p$$

$$\tau_p = \frac{L_p^2}{D_p}$$

$$Q = \tau_T I$$

$$C_d = \frac{dQ}{dV}$$

$$C_d = \frac{\tau_T}{V_T} I$$

Where I is the forward bias current, it is really small when the diode is reverse biased.

Depletion Capacitance:

$$C_{j0} = A \sqrt{\left(\frac{\epsilon_s q}{2} \right) \left(\frac{N_A N_D}{N_A + N_D} \right) \frac{1}{V_0}}$$

$$C_j = \frac{C_{j0}}{\left(1 + \frac{V_R}{V_0} \right)^m}$$

m is between 1/3 and 1/2

Saturation Current:

$$I_s = A q n_i^2 \left(\frac{D_p}{L_p N_D} + \frac{D_n}{L_n N_A} \right)$$

$$I = I_s (e^{V/V_T} - 1)$$

Forward Current:

$$I = I_p + I_n$$

$$I_p = A q n_i^2 \frac{D_p}{L_p N_D} (e^{V/V_T} - 1)$$

$$I_n = A q n_i^2 \frac{D_n}{L_n N_A} (e^{V/V_T} - 1)$$

Diodes:

$$V_T = \frac{kT}{q} = 25.9 \text{mV}$$

Iterative Solution:

Guess V_1 and I_1

$$I_2 = \frac{V_{DD} - V_1}{R}$$

$$V_2 = V_1 + V_T \ln \left(\frac{I_2}{I_1} \right)$$

Now use V_2 and I_2 as the new inputs for another iteration.

Constant drop: $V_D = 0.7 \text{ V}$.

Small Signal:

$$r_d = \frac{V_T}{I_D}$$

Zener Regions:

$$V_Z = V_{Z0} + r_z I_Z$$

Rectifiers:

Ripple voltage:

$$V_r = \frac{V_p}{fCR} = \frac{I_L}{fC}$$