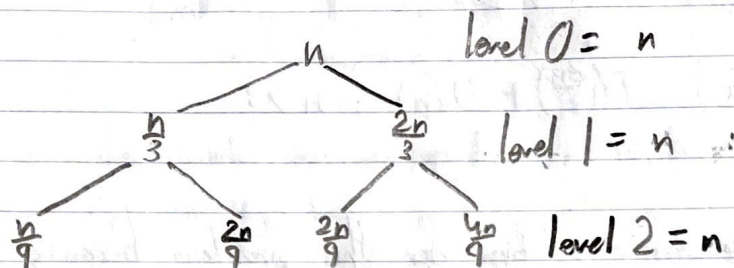


2.)

I will solve my recurrence relation from part 1, by using the tree method.

The tree



Work done per level: n

I will now find k where it will represent the amount of times it will take us to reach the base case:

I will compare $n/3$ and $2n/3$ to see which is value will terminate last:

$$T\left(\frac{n}{3}\right) = \frac{n}{3^{k_1}} \leq 3$$

$$n \leq 3(3^{k_1})$$

$$n \leq 3^{k_1+1}$$

$$\log_3 n \leq \log_3 (3^{k_1+1})$$

$$\log_3 n \leq k_1 + 1$$

$$k_1 > \log_3 n - 1$$

$$T\left(\frac{2n}{3}\right) = \left(\frac{2}{3}\right)^{k_2} n \leq 3$$

$$\left(\frac{2}{3}\right)^{k_2} \leq \frac{3}{n}$$

$$\log_{\frac{2}{3}} \left(\frac{2}{3}\right)^{k_2} \leq \log_{\frac{2}{3}} \frac{3}{n}$$

$$k_2 \leq \log_{\frac{2}{3}} \frac{3}{n}$$

This value will be greater than k_1