CSCI 3104 Fall 2022 Instructors: Prof. Grochow and Chandra Kanth Nagesh

Quiz 3 S7

Due Date	Thursday Sep 29, 2022 8pm MT
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Quiz Code (enter in Canvas to get access to the LaTeX template)	\dots FWERT
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Instructions

- You may either type your work using this template, or you may handwrite your work and embed it as an image in this template. If you choose to handwrite your work, the image must be legible, and oriented so that we do not have to rotate our screens to grade your work. We have included some helpful LaTeX commands for including and rotating images commented out near the end of the LaTeX template.
- You should submit your work through the **class Gradescope page** only. Please submit one PDF file, compiled using this LATEX template.
- You may not need a full page for your solutions; pagebreaks are there to help Gradescope automatically find where each problem is. Even if you do not attempt every problem, please submit this document with no fewer pages than the blank template (or Gradescope has issues with it).
- You may not collaborate with other students. Copying from any source is an Honor Code violation. Furthermore, all submissions must be in your own words and reflect your understanding of the material. If there is any confusion about this policy, it is your responsibility to clarify before the due date.
- Posting to any service including, but not limited to Chegg, Discord, Reddit, StackExchange, etc., for help on an assignment is a violation of the Honor Code.
- You **must** virtually sign the Honor Code (see Section). Failure to do so will result in your assignment not being graded.

Honor Code (Make Sure to Virtually Sign)

Problem HC. • My submission is in my own words and reflects my understanding of the material.

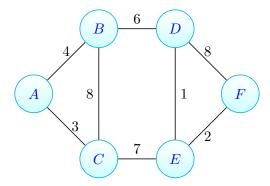
- Any collaborations and external sources have been clearly cited in this document.
- I have not posted to external services including, but not limited to Chegg, Reddit, StackExchange, etc.
- I have neither copied nor provided others solutions they can copy.

agree to the above, Tyler Huynh.	
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7 Standard 7: Kruskal's Min Spanning Tree Algorithm

Problem 7. Consider the following graph G(V, E, w). You should:

- Clearly indicate the order in which **Kruskal's algorithm** adds the edges to the minimum-weight spanning tree.
- You may simply list the order of the edges; it is not necessary to exhibit the state of the algorithm (i.e., the disjoint-set data structure) at each iteration.
- If any edge is considered by the algorithm but not added to the MST, state this clearly and explain why (briefly just a few words should do)



Answer. A priority queue sorted from the smallest edge weight to the largest edge weight, by definition of Kruskal's algorithm:

Vertices:	{D, E}	{E, F}	$\{A, C\}$	{A, B}	{B, D}	{C, E}	{B, C}	$\{D, F\}$
Edge Weights:	1	2	3	4	6	7	8	8

This is the order in which Kruskal's algorithm chooses the edges to add to the Minimum Weight Spanning Tree of G:

$$\{D,\,E\},\,\{E,\,F\},\,\{A,\,C\},\,\{A,\,B\},\,\{B,\,D\}$$

For the edges of {C, E}, {B, C}, {D, F} the algorithm does not add these edges because it will create cycles.

The Minimum Weight Spanning Tree of G:

