

Cryptography

Assignment 2

Dr. Charlie Obimbo

Due: February 11th, 2025

Name: _____

To be done in \LaTeX
Assignment is out of 10

1 One-Time Pad

Recall that in class we demonstrated how using the One-time pad was secure. In effect we showed how, in an effort to try and decrypt the cipher-text:

“ANKYODKYUREPFJBYOJDSPLREYIUNOFDOIUERFPLUYTS”

One cryptanalyst came up with the decryption: “MR MUSTARD WITH THE CANDLESTICK IN THE HALL”; while another: “MISS SCARLET WITH THE KNIFE IN THE LIBRARY.

1. Demonstrate how, using the character as the atomic operand, given the cipher-text:

JACAOYOABLCYOUPOYTBN

One may get:

(a) COMMANDER IN CHIEF

[1 mark]

(b) THE SERGEANT AT ARMS

[1 mark]

2. Joseph sends Aisha a message using a One-time pad. He also sends David another message using the same key. You were able to get both messages, as:

0809 0302 0607 1A17 1A08 1C07 141D and

[2 marks]

0005 1311 1911 1907 0D09 1B08 130B

If the atomic operand is the bit, decrypt both messages and find the potential key.

Consider that one of the phrases may be from the following list:

GORGEOUS SUSAN	SHE ADORES JOHN
NICOTINE IS BAD	MARIJUANAS LEGAL
JUSTINE TRUDEAU	FLOYD MAYWEATHER
ANGELINA JOLIE	EMBEZZLED FUNDS
NANETTE WORKMAN	ELIZABETH MAY
GRANT US PEACE	WE'RE AWESOME

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and extend across the width of the page. There are no margins, text, or other markings on the paper.

2 Number Theory & Hill Cipher

4. Is $2^{82589933} - 1$ prime? [0.5]

Why? [0.5]

5. Use Euclid's Algorithm to find $\gcd(422774, 1009)$. [No Partial Marks] (1 Mark)

6. Find the inverse of $1009 \pmod{422774}$. [No Partial Marks] (1 Mark)

7. Find all solutions (between 1 & 265) to the equation $35x \equiv 15 \pmod{265}$. [1]

8. (Hill-Cipher) Bob sends Alice the following code, in which the Hill-Cipher has been used, modulo 31. The key matrix used is:

$$K = \begin{bmatrix} 5 & 30 & 23 \\ 6 & 30 & 20 \\ 26 & 1 & 9 \end{bmatrix} \quad \text{and The Ciphertext } A \text{ is:}$$

$$\begin{bmatrix} T & 1 & H & I & C & O & Z & F \\ F & W & B & T & S & P & B & J \\ M & R & 2 & A & J & X & K & U \end{bmatrix}$$

If Bob used the following decimal encoding:

Letter	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P
Code	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Letter	Q	R	S	T	U	V	W	X	Y	Z	0	1	2	3	4	
Code	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	

- (a) Compute the inverse of the matrix K (mod 31).

[1]

- (b) Find the plaintext M. (Remember to remove the gibberish & punctuate it correctly.) [1]

9. $-113 \pmod{10} =$ _____

[1]