

# Cryptography

## Assignment 2

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Due: February 11th, 2025

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To be done in L<sup>A</sup>T<sub>E</sub>X  
Assignment is out of 10

### 1 One-Time Pad

Recall that in class we demonstrated how using the One-time pad was secure. In effect we showed how, in an effort to try and decrypt the cipher-text:

“ANKYODKYUREPFJBYOJDSPLREYIUNOFDOIUERFPLUYTS”

One cryptanalyst came up with the decryption: “MR MUSTARD WITH THE CANDLESTICK IN THE HALL”; while another: “MISS SCARLET WITH THE KNIFE IN THE LIBRARY.

1. Demonstrate how, using the character as the atomic operand, given the cipher-text:

JACAOYOABLCYOUPOYTBN

One may get:

(a) COMMANDER IN CHIEF

[1 mark]

The first step is to calculate values for the ciphertext and plaintext.

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
J	A	C	A	O	Y	O	A	B	L	C	Y	O	U	P	O	Y	T	B	N
9	0	2	0	14	24	14	0	1	11	2	24	14	20	15	14	24	19	1	13
C	O	M	M	A	N	D	E	R	I	N	C	H	I	E	F				
2	14	12	12	0	13	3	4	17	8	13	2	7	8	4	5				

Since the one-time pad operates on the text like so: PLAINTEXT + PAD = CIPHER-TEXT, we can find the desired plaintext by subtracting the plaintext from the ciphertext: PAD = CIPHERTEXT - PLAINTEXT.

I did the computations in Excel and copied them over to this document. The final result for the pad that gives this ciphertext is is: HMQOOLLWKDPWHMLJ

I ignored spaces, which I’m pretty sure is correct. If I hadn’t, I would have gotten a slightly different result.

9	0	2	0	14	24	14	0	1	11	2	24	14	20	15	14				
M	I	N	U	S															
2	14	12	12	0	13	3	4	17	8	13	2	7	8	4	5				
E	Q	U	A	L	S														
7	-14	-10	-12	14	11	11	#	-16	3	-11	22	7	12	11	9				
M	O	D	2	5															
7	12	16	14	14	11	11	#	10	3	15	22	7	12	11	9				
H	M	Q	O	O	L	L	W	K	D	P	W	H	M	L	J				

(b) THE SERGEANT AT ARMS

[1 mark]

The process for this one is exactly the same:

J	A	C	A	O	Y	O	A	B	L	C	Y	O	U	P	O	Y
9	0	2	0	14	24	14	0	1	11	2	24	14	20	15	14	24
T	H	E	S	E	R	G	E	A	N	T	A	T	A	R	M	S
19	7	4	18	4	17	6	4	0	13	19	0	19	0	17	12	18
9	0	2	0	14	24	14	0	1	11	2	24	14	20	15	14	24
M	I	N	U	S												
19	7	4	18	4	17	6	4	0	13	19	0	19	0	17	12	18
E	Q	U	A	L	S											
##	-7	-2	-18	10	7	8	#	1	-2	-17	24	-5	20	-2	2	6
M	O	D	2	5												
16	19	24	8	10	7	8	#	1	24	9	24	21	20	24	2	6
Q	T	Y	I	K	H	I	W	B	Y	J	Y	V	U	Y	C	G

The final result for the pad that will produce JACAOYOABLCOUPOYTBN from THE SERGEANT AT ARMS is QTYIKHIWBYJYVUYCG

2. Joseph sends Aisha a message using a One-time pad. He also sends David another message using the same key. You were able to get both messages, as:

0809 0302 0607 1A17 1A08 1C07 141D and

[2 marks]

0005 1311 1911 1907 0D09 1B08 130B

If the atomic operand is the bit, decrypt both messages and find the potential key.

Consider that one of the phrases may be from the following list:

GORGEOUS SUSAN	SHE ADORES JOHN
NICOTINE IS BAD	MARIJUANAS LEGAL
JUSTINE TRUDEAU	FLOYD MAYWEATHER
ANGELINA JOLIE	EMBEZZLED FUNDS
NANETTE WORKMAN	ELIZABETH MAY
GRANT US PEACE	WE'RE AWESOME

This image shows a single sheet of white paper with horizontal blue or grey ruling lines. The lines are evenly spaced and run across the width of the page. There are approximately 20 lines visible. The paper has a slight shadow on its right side, suggesting it's resting on a surface.

## 2 Number Theory & Hill Cipher

4. Is  $2^{82589933} - 1$  prime? ..... [0.5]

Why? ..... [0.5]

5. Use Euclid's Algorithm to find  $\gcd(422774, 1009)$ . [No Partial Marks] (1 Mark)

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6. Find the inverse of  $1009 \pmod{422774}$ . [No Partial Marks] (1 Mark)

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7. Find all solutions (between 1 & 265) to the equation  $35x \equiv 15 \pmod{265}$ . [1]

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8. (Hill-Cipher) Bob sends Alice the following code, in which the Hill-Cipher has been used, modulo 31. The key matrix used is:

$$K = \begin{bmatrix} 5 & 30 & 23 \\ 6 & 30 & 20 \\ 26 & 1 & 9 \end{bmatrix} \quad \text{and The Ciphertext } A \text{ is:}$$

$$\begin{bmatrix} T & 1 & H & I & C & O & Z & F \\ F & W & B & T & S & P & B & J \\ M & R & 2 & A & J & X & K & U \end{bmatrix}$$

If Bob used the following decimal encoding:

Letter	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P
Code	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Letter	Q	R	S	T	U	V	W	X	Y	Z	0	1	2	3	4	
Code	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	

- (a) Compute the inverse of the matrix  $K$  (mod 31).

[1]

- (b) Find the plaintext M. (Remember to remove the gibberish & punctuate it correctly.) [1]

9.  $-113 \pmod{10} =$  \_\_\_\_\_

[1]