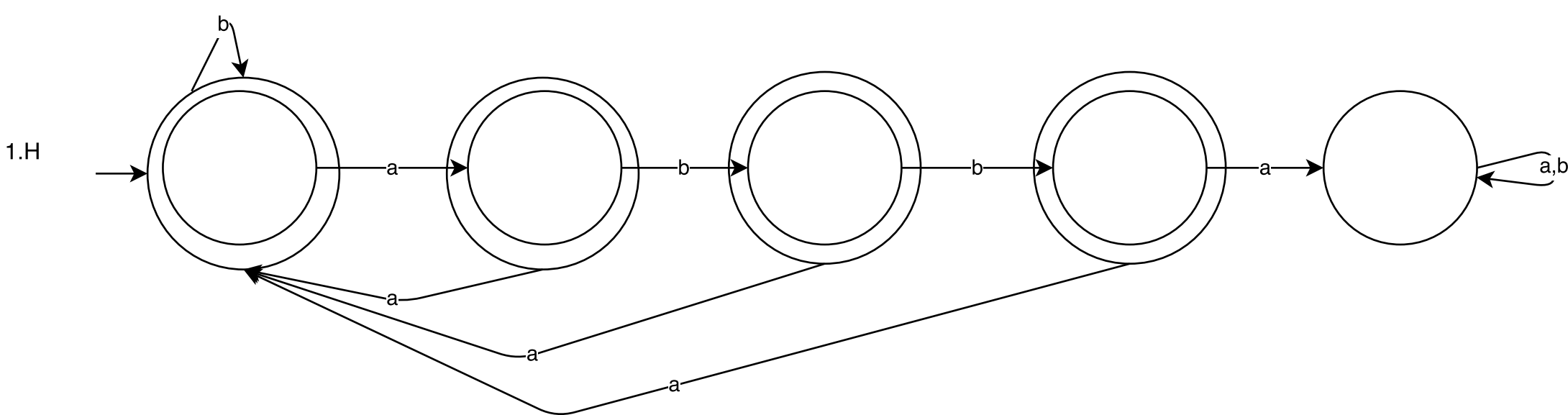
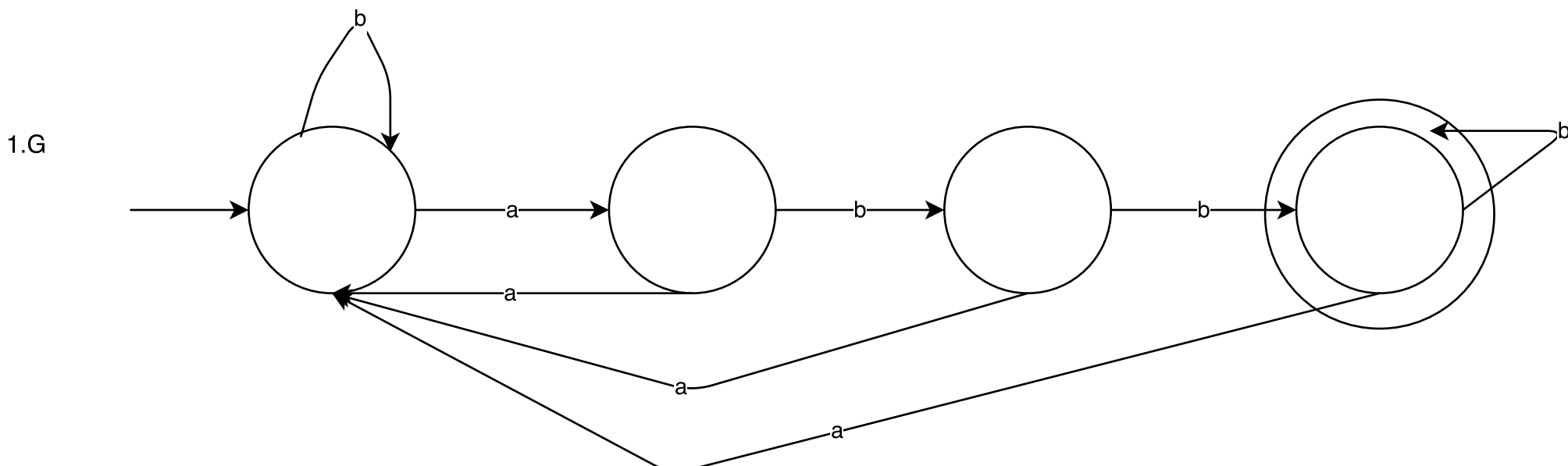
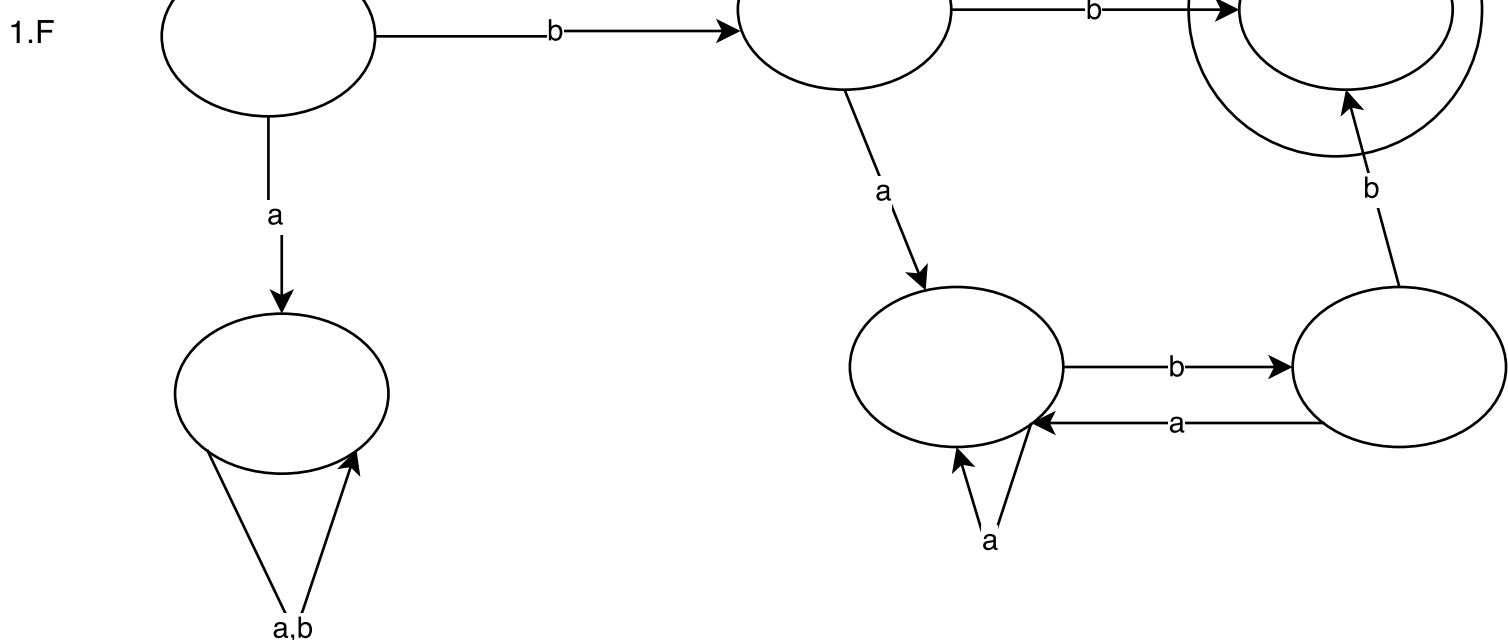


1.E Can't be even and odd.

Empty Set

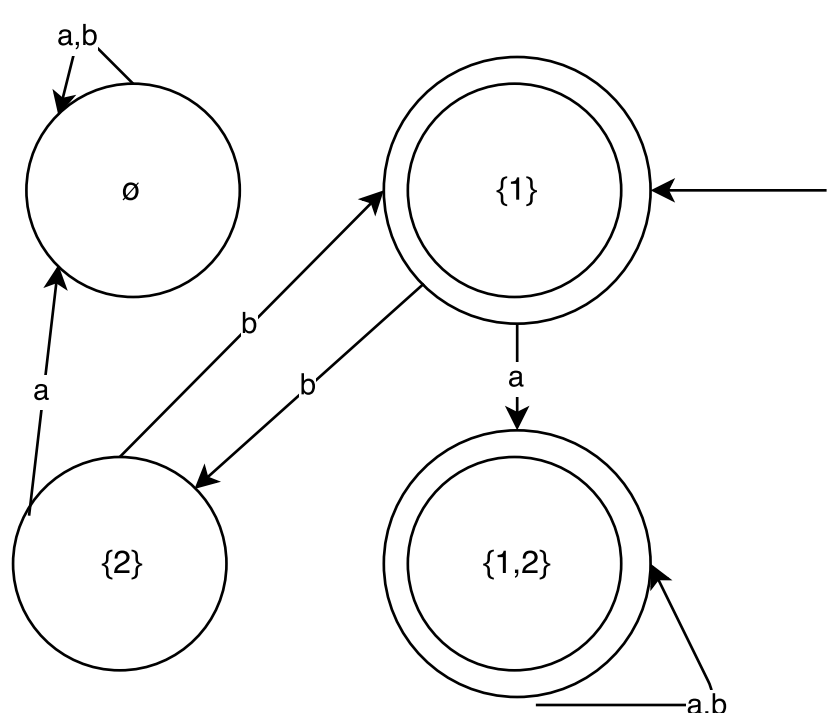


- 2.
- Every state M is a set of states of N.
 - DFA transition function equals the union of all states of the NFA transition function.

2.A

NFA states = {1,2}
DFA states thus = { \emptyset , {1}, {2}, {1,2}}

Next determine start and accept states of DFA.



Start state is E({1}), since there are no empty sets the start state remains the same, as 1.
New Accept states are {{1},{1,2}}, since NFA accept state is {1}.

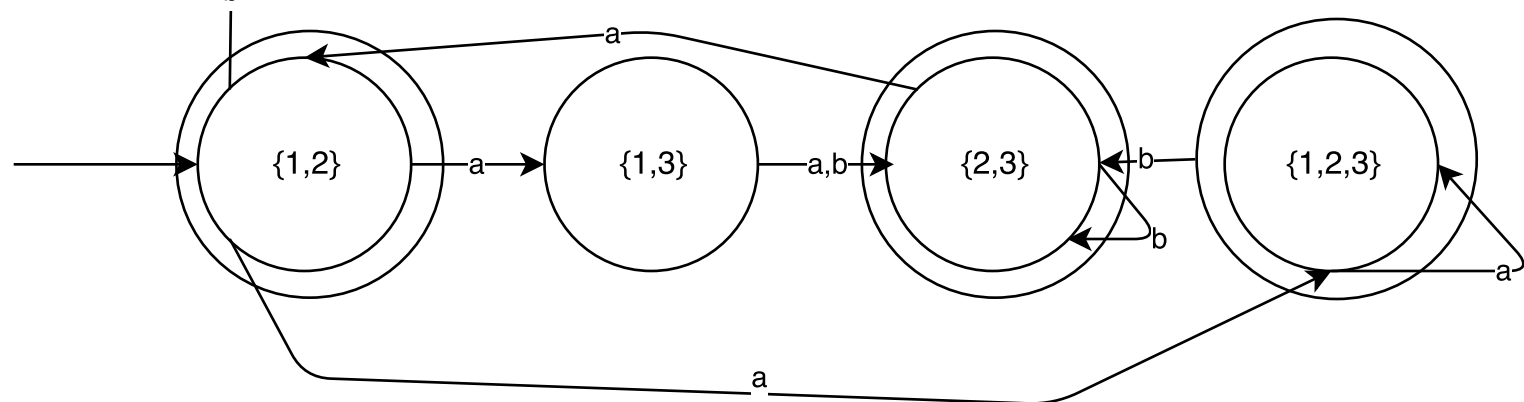
Now we determine transition function for the new DFA.
Each state goes from one place for input a, and one for input b.

Since 2 has no outgoing a it goes to the empty set.
State 2 has an outgoing b that goes to state 1.
both State 1 and 2 have incoming a's and b's thus it goes to itself.
State 1 has an outgoing a to itself and 2 thus it goes to the state {1,2}.
State 1 has an outgoing b to state 2.

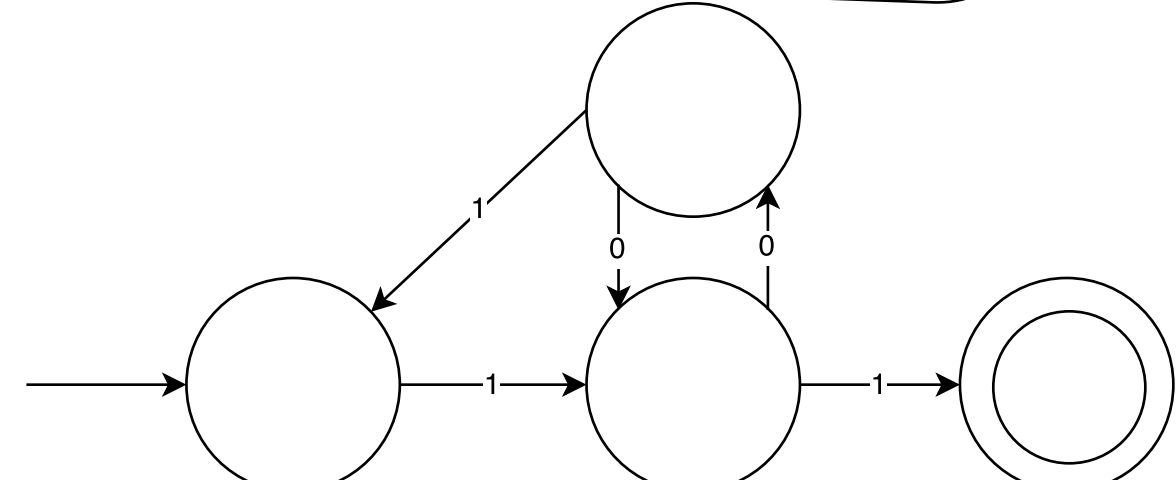
2.B

NFA states = {1,2,3}
DFA states = { \emptyset , {1}, {2}, {3}, {1,2}, {1,3}, {2,3}, {1,2,3}}

Start state for NFA is {1}, but it has an empty set, thus the start state is {1,2}.
Accept state is 2, thus DFA accept states are {{2},{1,2},{2,3},{1,2,3}}.



3.



4. A

The formal definition for a regular language is the following:
The empty language \emptyset , and the empty string $\{e\}$ are regular languages.
For each $a \in \Sigma$, the singleton language $\{a\}$ is a regular language.
If A and B are regular languages, then $A \cup B$, $A \cdot B$ and A^* are regular languages.
- All finite languages are regular.

For any language A, let $A^*R = \{W^*R \mid w \in A\}$. Let $W = s_1 \dots s_n$ and $W^*R = s_n \dots s_1$

If A is regular there exists a DFA M, such that $A(M) = A$.
We can show A^*R is regular by constructing a DFA M' that exemplifies the relationship A and A^*R hold, where A^*R accepts all reversed strings that A accepts.

Let $w^*R = a_0a_1 \dots a_n$ be a string over an alphabet A^*R . The DFA M' accepts the state sequence $r_0r_1 \dots r_n$ if w is a string in DFA A.

1. The start state of M' will be the accept state of M. thus $r_0 = q_n$
2. The transition function of M' will be the transition function of M, except the state and character are reversed. $r'_i + 1 = (r_i, a_{r-1})$ $i = 0, \dots, n-1$ and $r = n-1, n-2, \dots, 0$
3. The accept states of M' is anything that has the start state of M.

Now that A^*R has a DFA M', it is a regular language.

4.B

$B(M) = M$, M is a DFA of B
 $B^*R(M') = B^*R$, M' is a DFA of B^*R

From the prior proof 4.A, we can see that if A is regular, A^*R is regular. Thus, the opposite is true, if A^*R is regular, A is regular.

If B^*R has a DFA M', then it is regular.

In order for M' to be a valid DFA it needs a start state, transition function, and set of accept states.

Using the DFA description of M' in 4.A, we can see that M' will follow the same characteristics.

Now that B^*R has a DFA M', B is a regular language.