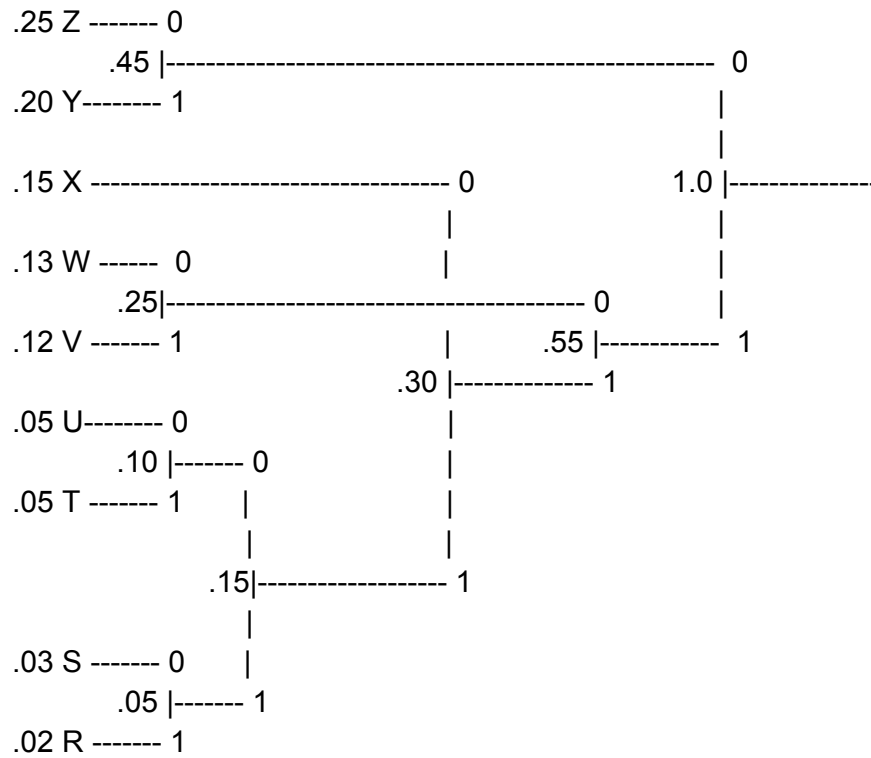
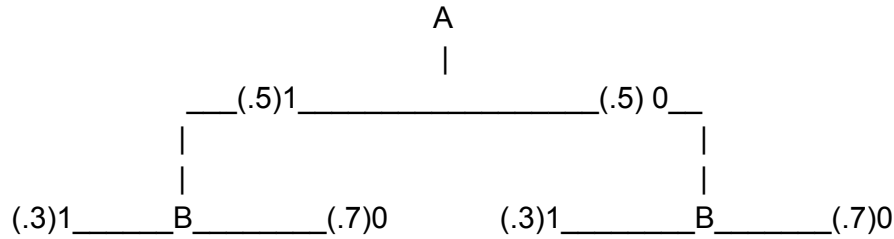


Quiz 2

1. Huffman encoding



2.)



$$.5 \cdot .7 + .5 \cdot .3 = .5$$

I would expect A XOR B to have more entropy than B and the same entropy as A.

$$H(A) = .5 \lg(1/.5) + .5 \lg(1/.5) = 1$$

$$H(B) = .3 \lg(1/.3) + .7 \lg(1/.7) = .881291$$

$$H(A \text{ XOR } B) = .15 \lg(1/.15) + .35 \lg(1/.35) + .15 \lg(1/.15) + .35 \lg(1/.35) = 1.881291$$

Hmm it seems odd that it would equal the sum of the two?

3.)

AAAA BBBB CC DD E F G H

$$A \rightarrow \lg(1/(4/16)) = 2$$

$$B \rightarrow \lg(1/(4/16)) = 2$$

$$C \rightarrow \lg(1/(2/16)) = 3$$

$$D \rightarrow \lg(1/(2/16)) = 3$$

$$E \rightarrow \lg(1/(1/16)) = 4$$

$$F \rightarrow \lg(1/(1/16)) = 4$$

$$G \rightarrow \lg(1/(1/16)) = 4$$

$$H \rightarrow \lg(1/(1/16)) = 4$$

$$4 \cdot 2 + 4 \cdot 2 + 2 \cdot 3 + 2 \cdot 3 + 1 \cdot 4 + 1 \cdot 4 + 1 \cdot 4 + 1 \cdot 4 = 44 \text{ bits of entropy in entire message}$$

$$2 \cdot .25 + 2 \cdot .25 + 3 \cdot (1/8) + 3 \cdot (1/8) + 4 \cdot (1/16) + 4 \cdot (1/16) + 4 \cdot (1/16) + 4 \cdot (1/16) = \text{Avg entropy per symbol} = 2.75$$

Each A has 2 bits of entropy

Each G has 4 bits

Do you have to multiply these values by the probability of A and G?