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- MODULE FastPaxos
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This is a simplified specification of $Leslie\ Lamport$'s Fast Paxos protocol. The following papers, Fast Paxos by $Leslie\ Lamport$ and Fast Paxos Made Easy: Theory and Implementation by $Zhao\ Wenbing$ was referenced in writing this specification.

This simplified specification was written by Lim Ngian Xin Terry & Gaurav Gandhi.

The following assumptions are made in this simplified specification.

- 1. There is a unique coordinator in the system. Therefore, Phase 1a and 1b can be omitted.
- 2. All agents in the system can communicate with one another.
- 3. Agents must have some stable storage that survives failure and restarts. An agent restores its state from stable storage when it restarts, so the failure of an agent is indistinguishable from its simply pausing. There is thus no need to model failures explicitly.

EXTENDS Paxos

CONSTANTS FastQuorums, FastBallots

VARIABLES cValue Value chosen by coordinator.

 $ClassicBallots \triangleq Ballots \setminus FastBallots$ The set of ballots of classic rounds.

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FastAssume \triangleq
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Assume $PaxosAssume \land FastAssume$

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IsMajorityValue(M, v) \stackrel{\triangle}{=} Cardinality(M) \div 2 < Cardinality(\{m \in M : m.value = v\})
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Phase 2a (Fast):
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The coordinator starts a fast round by sending a P2a "Any" message, if no other values has been proposed before.

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FastAny \triangleq
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Phase 2b (Fast):

Acceptors can reply to a P2a "Any" message with a P2b message containing their proposed value.

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FastPropose \triangleq
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\land UNCHANGED \langle decision, cValue \rangle
\land \exists a \in Replicas, m \in p2aMessages, v \in Values :
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A value is chosen if a fast quorum of acceptors proposed that value in a fast round.

Because the quorum size of a fast round and classic round is different, we assume that the acceptor distinguishes a fast round and classic round based on the P2a message it receives. If the P2a message contains the special value "any", it is a fast round. Else it is a classic round.

$FastDecide \triangleq$

Phase 2a (Classic)

If more than one value has been proposed, the collision is resolved using the following rules:

- 1. If the proposals contain different values, a value must be selected if the majority of acceptors in the fast quorum have casted a vote for that value.
- 2. Otherwise, the coordinator is free to select any value.

$ClassicAccept \triangleq$

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\land SendMessage([type \mapsto "P2a",
                                             ballot \mapsto b,
                                             value \mapsto v)
  Phase 2b (Classic)
  Same as in Paxos.
ClassicAccepted \triangleq
     \land UNCHANGED \langle cValue \rangle
     \land PaxosAccepted
  Consensus is achieved when a majority of acceptors accept the same ballot number.
  Functionally similar to PaxosDecide in Paxos.tla, but we also have to ensure that it can only
  occur in classic rounds and not fast rounds.
ClassicDecide \triangleq
     \land UNCHANGED \langle messages, maxBallot, maxVBallot, maxValue, cValue\rangle
     \land \exists b \in ClassicBallots, q \in Quorums:
          LET M \triangleq \{m \in p2bMessages : m.ballot = b \land m.acceptor \in q\}
          IN \land \forall a \in q : \exists m \in M : m.acceptor = a
                 \land \exists m \in M : decision' = m.value
FastTypeOK \stackrel{\triangle}{=} \land PaxosTypeOK
                        \land cValue \in Values \cup \{none\}
FastInit \stackrel{\triangle}{=} \land PaxosInit
                   \land cValue = none
FastNext \triangleq \lor FastAny
                   \vee FastPropose
                   \vee FastDecide
                   \lor ClassicAccept
                   \lor ClassicAccepted
                   \lor ClassicDecide
FastSpec \triangleq \land FastInit
                   \land \ \Box[\mathit{FastNext}]_{\langle \mathit{messages}, \ \mathit{decision}, \ \mathit{maxBallot}, \ \mathit{maxVBallot}, \ \mathit{maxValue}, \ \mathit{cValue}\rangle}
                   \land SF<sub>(messages, decision, maxBallot, maxVBallot, maxValue, cValue)</sub>(FastDecide)
                   \land \mathit{SF}_{\langle \mathit{messages}, \; \mathit{decision}, \; \mathit{maxBallot}, \; \mathit{maxVBallot}, \; \mathit{maxValue}, \; \mathit{cValue} \rangle}(\mathit{ClassicDecide})
 Non-triviality safety property: Only proposed values can be learnt.
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 $\lor \exists m \in p2bMessages : m.value = decision \land m.ballot \in FastBallots$

 $FastNontriviality \stackrel{\Delta}{=} \lor decision = none$