**AST** 

# Stack

1. Addition

```
Addition returns Expression:
    Multiplication ({AdditionalExpression.left=current} '+' right=Multiplication)*;

Multiplication returns Expression:
    PrimaryExpression ({MultiplyExpression.left=current} '*' right=PrimaryExpression)*;

PrimaryExpression returns Expression:
    {NumberLiteral} value=INT |
    '(' Addition ')';
```

**AST** 

- 1. Addition
- 2.Multiplication

```
Addition returns Expression:
    Multiplication ({AdditionalExpression.left=current} '+' right=Multiplication)*;

Multiplication returns Expression:
    PrimaryExpression ({MultiplyExpression.left=current} '*' right=PrimaryExpression)*;

PrimaryExpression returns Expression:
    {NumberLiteral} value=INT |
    ('(')Addition ')';
```

**AST** 

- 1. Addition
- 2.Multiplication
- 3. Primary Expression

Text 
$$(1 + 20) * 2$$

**AST** 

- 1. Addition
- 2.Multiplication
- 3. Primary Expression

```
Addition returns Expression:
    Multiplication ({AdditionalExpression.left=current} '+' right=Multiplication)*;

Multiplication returns Expression:
    PrimaryExpression ({MultiplyExpression.left=current} '*' right=PrimaryExpression)*;

PrimaryExpression returns Expression:
    {NumberLiteral} value=INT |
    '('Addition)')';
```

Text 
$$(1 + 20) * 2$$

**AST** 

- 1. Addition
- 2.Multiplication
- 3. Primary Expression

Addition returns Expression:
 (Multiplication) ({AdditionalExpression.left=current} '+' right=Multiplication)\*;

Multiplication returns Expression:
 PrimaryExpression ({MultiplyExpression.left=current} '\*' right=PrimaryExpression)\*;

PrimaryExpression returns Expression:
 {NumberLiteral} value=INT |
 '(' Addition ')';

Text 
$$(1 + 20) * 2$$

**AST** 

- 1. Addition
- 2.Multiplication
- 3. Primary Expression
- 4.Addition

```
Addition returns Expression:
    Multiplication ({AdditionalExpression.left=current} '+' right=Multiplication)*;

Multiplication returns Expression:
    (PrimaryExpression) ({MultiplyExpression.left=current} '*' right=PrimaryExpression)*;

PrimaryExpression returns Expression:
    {NumberLiteral} value=INT |
    '(' Addition ')';
```

Text 
$$(1 + 20) * 2$$

**AST** 

- 1. Addition
- 2.Multiplication
- 3. Primary Expression
- 4. Addition
- 5. Multiplication

```
Addition returns Expression:
    Multiplication ({AdditionalExpression.left=current} '+' right=Multiplication)*;

Multiplication returns Expression:
    PrimaryExpression ({MultiplyExpression.left=current} '*' right=PrimaryExpression)*;

PrimaryExpression returns Expression:
    ({NumberLiteral} value=INT)|
    '(' Addition ')';
```

Text 
$$(1 + 20) * 2$$

**AST** 

- 1. Addition
- 2.Multiplication
- 3. Primary Expression
- 4. Addition
- 5.Multiplication
- 6. Primary Expression

Text 
$$(1 + 20) * 2$$

**AST** 

- 1. Addition
- 2.Multiplication
- 3. Primary Expression
- 4. Addition
- 5.Multiplication
- 6. Primary Expression

Text 
$$(1 + 20) * 2$$

**AST** 

### Stack

- 1. Addition
- 2.Multiplication
- 3. Primary Expression
- 4. Addition
- 5.Multiplication
- 6. Primary Expression

```
Text (1 + 20) * 2
```

**AST** 

### Stack

- 1. Addition
- 2.Multiplication
- 3. Primary Expression
- 4. Addition
- 5.Multiplication
- 6. Primary Expression

```
Addition returns Expression:

Multiplication ({AdditionalExpression.left=current} '+' right=Multiplication)*;
```

Multiplication returns Expression: PrimaryExpression ({MultiplyExpression.left=current} '\*' right=PrimaryExpression)\*

```
PrimaryExpression returns Expression:
    {NumberLiteral} value=INT |
    '(' Addition ')';
```

Text (1 + 20) \* 2

**AST** 

## Reduce!

### Stack

- 1.Addition
- 2.Multiplication
- 3. Primary Expression
- 4. Addition
- 5. Multiplication

```
Addition returns Expression:
    Multiplication ({AdditionalExpression.left=current} '+' right=Multiplication)*;

Multiplication returns Expression:
    PrimaryExpression ({MultiplyExpression.left=current} '*' right=PrimaryExpression)*;

PrimaryExpression returns Expression:
    {NumberLiteral} value=INT |
        '(' Addition ')';
```

Text (1 + 20) \* 2

Reduce!

# **AST**

# Stack

- 1. Addition
- 2.Multiplication
- 3. Primary Expression
- 4. Addition

Addition returns Expression:
 Multiplication ({AdditionalExpression.left=current} '+') right=Multiplication)\*;

Multiplication returns Expression:
 PrimaryExpression ({MultiplyExpression.left=current} '\*' right=PrimaryExpression)\*;

PrimaryExpression returns Expression:
 {NumberLiteral} value=INT |
 '(' Addition ')';

```
Text (1 + 20) * 2
```

**AST** 

- 1. Addition
- 2.Multiplication
- 3. Primary Expression
- 4.Addition

Addition returns Expression:

Multiplication ({AdditionalExpression.left=current}) '+' right=Multiplication)\*;

Multiplication returns Expression:

PrimaryExpression ({MultiplyExpression.left=current} '\*' right=PrimaryExpression)\*;

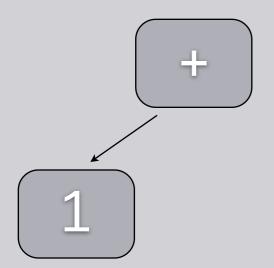
PrimaryExpression returns Expression:

{NumberLiteral} value=INT |

'(' Addition ')';

```
Text (1 + 20) * 2
```

### **AST**

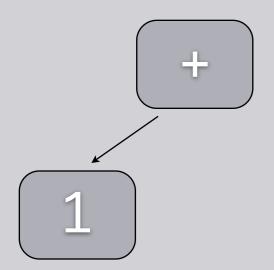


- 1. Addition
- 2.Multiplication
- 3. Primary Expression
- 4.Addition

```
Addition returns Expression:
    Multiplication ({AdditionalExpression.left=current}) '+' right=Multiplication)*;
 Multiplication returns Expression:
    PrimaryExpression ({MultiplyExpression.left=current} '*' right=PrimaryExpression)*;
 PrimaryExpression returns Expression:
       current = ruleMultiplication();
       // {AdditionalExpression.left=current}
       AdditionalExpression temp = new AdditionalExpression();
       temp.setLeft(current);
       current = temp:
                                                2. MULTIPLICATION
                                                3. Primary Expression
                                                4. Addition
```

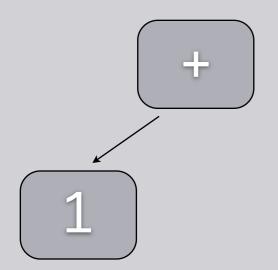
```
Text (1 + 20) * 2
```

## **AST**



- 1. Addition
- 2.Multiplication
- 3. Primary Expression
- 4.Addition

# **AST**



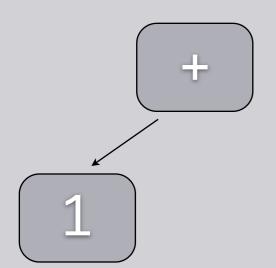
- 1. Addition
- 2.Multiplication
- 3. Primary Expression
- 4.Addition

Addition returns Expression:
 Multiplication ({AdditionalExpression.left=current} '+' right=Multiplication)\*;

Multiplication returns Expression:
 PrimaryExpression ({MultiplyExpression.left=current} '\*' right=PrimaryExpression)\*;

PrimaryExpression returns Expression:
 {NumberLiteral} value=INT |
 '(' Addition ')';

## **AST**



- 1. Addition
- 2.Multiplication
- 3. Primary Expression
- 4.Addition

Addition returns Expression:

Multiplication ({AdditionalExpression.left=current} '+' right=Multiplication)\*;

Multiplication returns Expression:

PrimaryExpression ({MultiplyExpression.left=current} '\*' right=PrimaryExpression)\*;

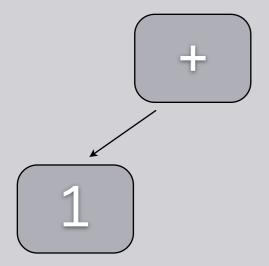
PrimaryExpression returns Expression:

{NumberLiteral} value=INT |

'(' Addition ')';

Text 
$$(1 + 20) \times 2$$

## **AST**



- 1.Addition
- 2.Multiplication
- 3. Primary Expression
- 4. Addition
- 5.Multiplication

Addition returns Expression:

Multiplication ({AdditionalExpression.left=current} '+' right=Multiplication)\*;

Multiplication returns Expression:

PrimaryExpression ({MultiplyExpression.left=current} '\*' right=PrimaryExpression)\*;

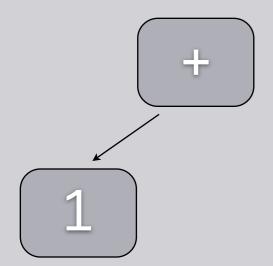
PrimaryExpression returns Expression:

{NumberLiteral} value=INT |

'(' Addition ')';

Text 
$$(1 + 20) \times 2$$

## **AST**



- 1. Addition
- 2.Multiplication
- 3. Primary Expression
- 4. Addition
- 5.Multiplication
- 6. Primary Expression

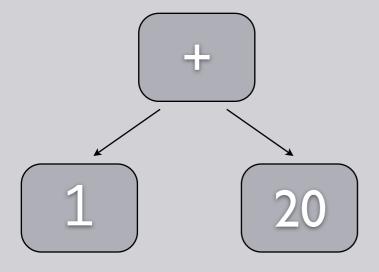
Addition returns Expression:
 Multiplication ({AdditionalExpression.left=current} '+' right=Multiplication)\*;

Multiplication returns Expression:
 PrimaryExpression ({MultiplyExpression.left=current} '\*' right=PrimaryExpression)\*;

PrimaryExpression returns Expression:
 {NumberLiteral} value=INT |
 '(' Addition ')';

Text (1 + 20) \* 2

**AST** 



# Reduce!

- 1. Addition
- 2.Multiplication
- 3. Primary Expression
- 4.Addition

```
Addition returns Expression:

Multiplication ({AdditionalExpression.left=current} '+' right=Multiplication)*;

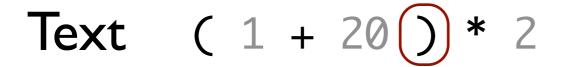
Multiplication returns Expression:

PrimaryExpression ({MultiplyExpression.left=current} '*' right=PrimaryExpression)*;

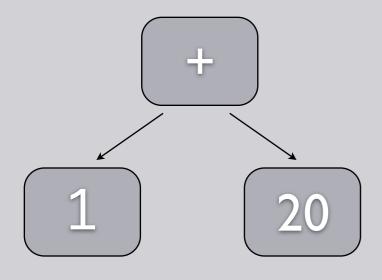
PrimaryExpression returns Expression:

{NumberLiteral} value=INT |

'('(Addition)')';
```



## **AST**



## Reduce!

- 1. Addition
- 2.Multiplication
- 3. Primary Expression

```
Addition returns Expression:

Multiplication ({AdditionalExpression.left=current} '+' right=Multiplication)*;

Multiplication returns Expression:

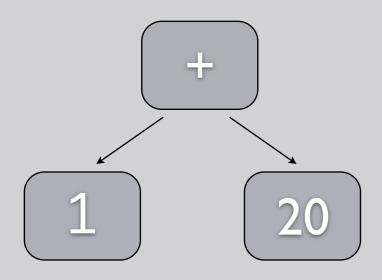
PrimaryExpression ({MultiplyExpression.left=current} '*' right=PrimaryExpression)*;

PrimaryExpression returns Expression:

{NumberLiteral} value=INT |

'(' Addition(')');
```

## **AST**



- 1. Addition
- 2.Multiplication
- 3. Primary Expression

```
Addition returns Expression:

Multiplication ({AdditionalExpression.left=current} '+' right=Multiplication)*;

Multiplication returns Expression:

PrimaryExpression ({MultiplyExpression.left=current} '*' right=PrimaryExpression)*;

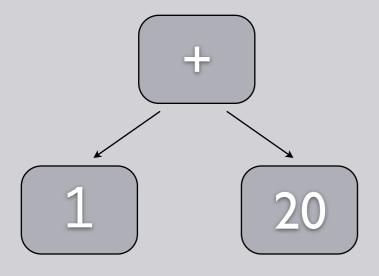
PrimaryExpression returns Expression:

{NumberLiteral} value=INT |

'(' Addition')';
```

Text 
$$(1 + 20)$$
\* 2

## **AST**



- 1. Addition
- 2.Multiplication
- 3. Primary Expression

Addition returns Expression:

Multiplication ({AdditionalExpression.left=current} '+' right=Multiplication)\*;

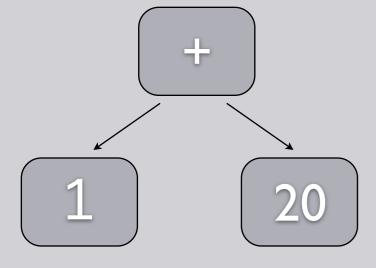
Multiplication returns Expression:

PrimaryExpression ({MultiplyExpression.left=current} '\*' right=PrimaryExpression)\*

PrimaryExpression returns Expression:
 {NumberLiteral} value=INT |
 '(' Addition ')';

Text (1 + 20)\* 2

**AST** 



# Reduce!

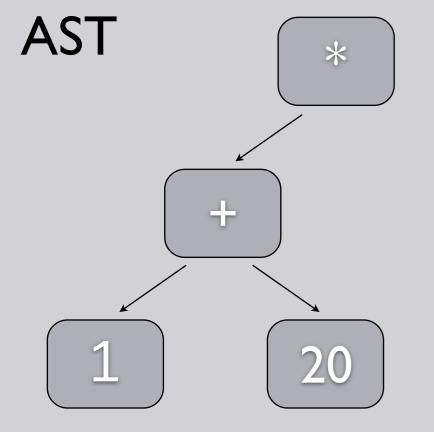
- 1. Addition
- 2.Multiplication

```
Addition returns Expression:
Multiplication ({AdditionalExpression.left=current} '+' right=Multiplication)*;
```

Multiplication returns Expression:
PrimaryExpression ({MultiplyExpression.left=current}) '\*' right=PrimaryExpression)\*;

PrimaryExpression returns Expression:
 {NumberLiteral} value=INT |
 '(' Addition ')';

Text 
$$(1 + 20)$$
\* 2



- 1. Addition
- 2.Multiplication

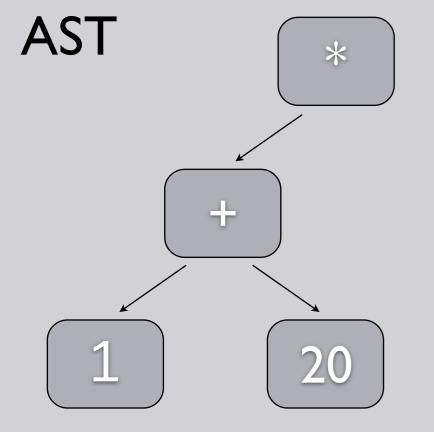
```
Addition returns Expression:

Multiplication ({AdditionalExpression.left=current} '+' right=Multiplication)*;
```

Multiplication returns Expression:
 PrimaryExpression ({MultiplyExpression.left=current} ('\*') right=PrimaryExpression)\*;

```
PrimaryExpression returns Expression:
    {NumberLiteral} value=INT |
    '(' Addition ')';
```

Text 
$$(1 + 20)$$
\* 2



- 1. Addition
- 2.Multiplication

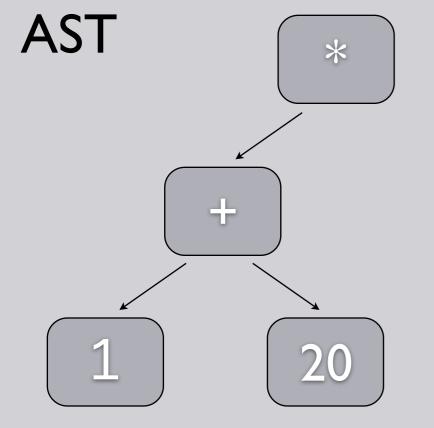
```
Addition returns Expression:

Multiplication ({AdditionalExpression.left=current} '+' right=Multiplication)*;
```

Multiplication returns Expression:
 PrimaryExpression ({MultiplyExpression.left=current} ('\*') right=PrimaryExpression)\*;

```
PrimaryExpression returns Expression:
    {NumberLiteral} value=INT |
    '(' Addition ')';
```

Text 
$$(1 + 20) * (2)$$



- 1. Addition
- 2.Multiplication

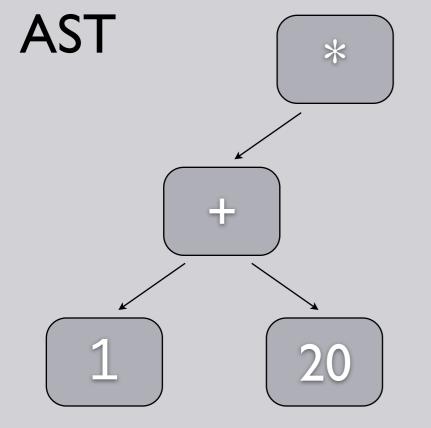
```
Addition returns Expression:

Multiplication ({AdditionalExpression.left=current} '+' right=Multiplication)*;
```

Multiplication returns Expression: PrimaryExpression ({MultiplyExpression.left=current} '\*' (right=PrimaryExpression)\*
PrimaryExpression returns Expression:

{NumberLiteral} value=INT |
'(' Addition ')';

Text 
$$(1 + 20) * (2)$$



- 1. Addition
- 2.Multiplication

```
Addition returns Expression:

Multiplication ({AdditionalExpression.left=current} '+' right=Multiplication)*;

Multiplication returns Expression:

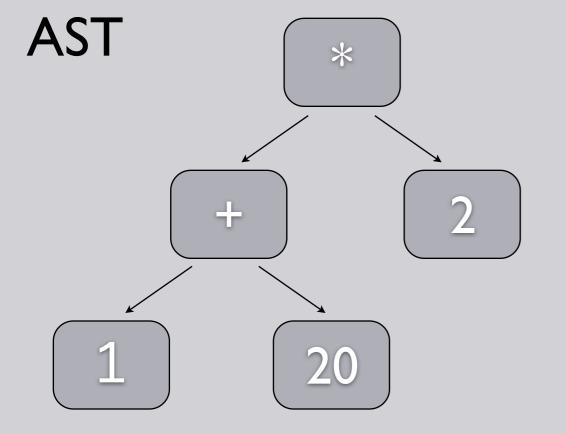
PrimaryExpression ({MultiplyExpression.left=current} '*' right=PrimaryExpression)*

PrimaryExpression returns Expression:

({NumberLiteral} value=INT)|
```



(' Addition ')';



- 1. Addition
- 2.Multiplication
- 3. Primary Expression

```
Addition returns Expression:

Multiplication ({AdditionalExpression.left=current} '+' right=Multiplication)*;

Multiplication returns Expression:

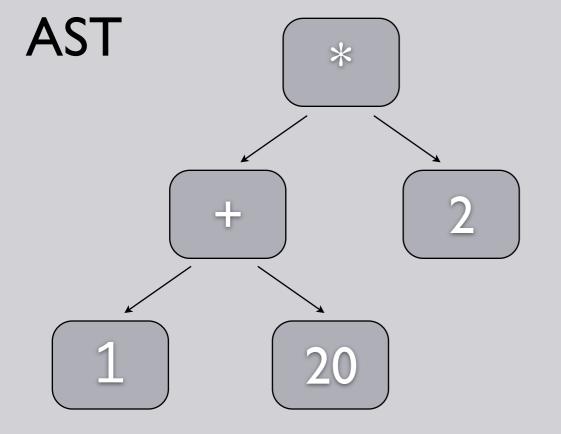
PrimaryExpression ({MultiplyExpression.left=current} '*' right=PrimaryExpression)*

PrimaryExpression returns Expression:

{NumberLiteral} value=INT |

'(' Addition ')';
```





- 1. Addition
- 2.Multiplication
- 3. Primary Expression

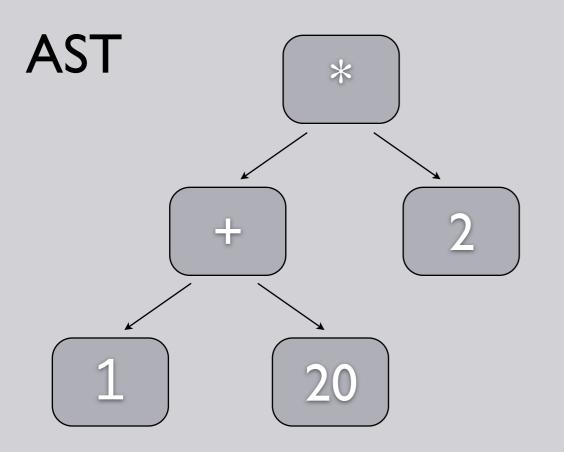
```
Addition returns Expression:

Multiplication ({AdditionalExpression.left=current} '+' right=Multiplication)*;
```

Multiplication returns Expression: PrimaryExpression ({MultiplyExpression.left=current} '\*' (right=PrimaryExpression)\*; PrimaryExpression returns Expression:

```
{NumberLiteral} value=INT |
'(' Addition ')';
```





### Reduce!

- 1. Addition
- 2.Multiplication

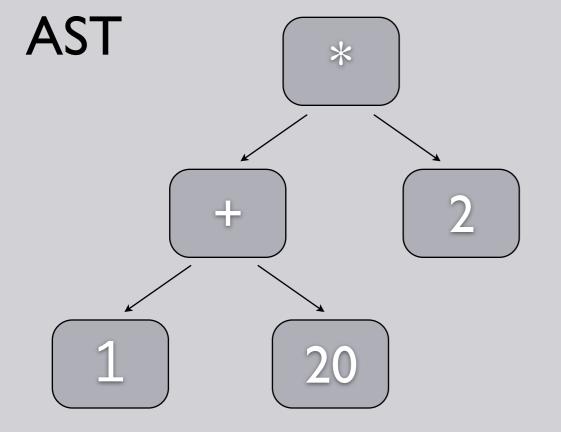
```
Addition returns Expression:

Multiplication ({AdditionalExpression.left=current} '+' right=Multiplication)*;
```

Multiplication returns Expression: PrimaryExpression ({MultiplyExpression.left=current} '\*' (right=PrimaryExpression)\*; PrimaryExpression returns Expression:

```
{NumberLiteral} value=INT |
'(' Addition ')';
```

Text 
$$(1 + 20) * 2 EOF$$

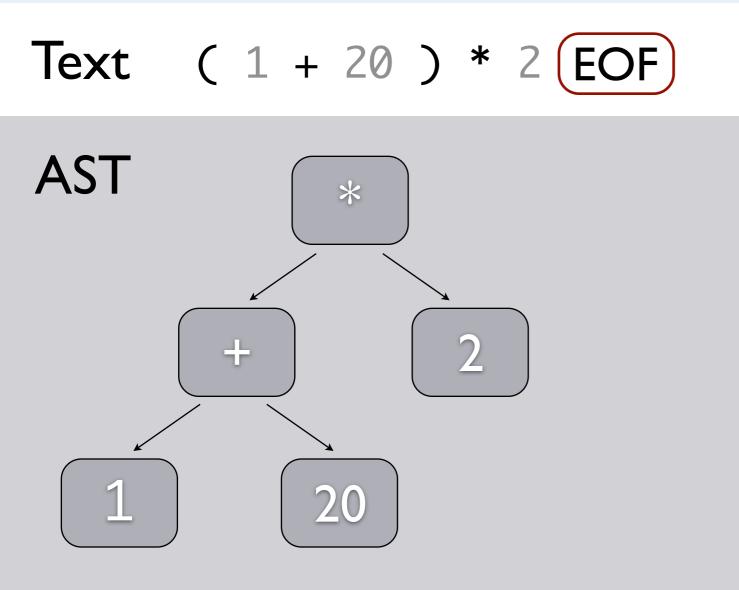


- 1. Addition
- 2.Multiplication

Addition returns Expression:
 Multiplication ({AdditionalExpression.left=current} '+' right=Multiplication)\*;

Multiplication returns Expression:
 PrimaryExpression ({MultiplyExpression.left=current} '\*' right=PrimaryExpression)\*;

PrimaryExpression returns Expression:
 {NumberLiteral} value=INT |
 '(' Addition ')';



### Reduce!

### Stack

1. Addition

```
Addition returns Expression:
    Multiplication ({AdditionalExpression.left=current} '+' right=Multiplication)*;

Multiplication returns Expression:
    PrimaryExpression ({MultiplyExpression.left=current} '*' right=PrimaryExpression)*;

PrimaryExpression returns Expression:
    {NumberLiteral} value=INT |
    '(' Addition ')';
```

