### **Supplementary information**

# Closed-loop optimization of fast-charging protocols for batteries with machine learning

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Peter M. Attia, Aditya Grover, Norman Jin, Kristen A. Severson, Todor M. Markov, Yang-Hung Liao, Michael H. Chen, Bryan Cheong, Nicholas Perkins, Zi Yang, Patrick K. Herring, Muratahan Aykol, Stephen J. Harris, Richard D. Braatz<sup>™</sup>, Stefano Ermon <sup>™</sup> & William C. Chueh <sup>™</sup>

### **Supplementary Information for**

### Closed-loop optimization of fast-charging protocols for batteries

Peter M. Attia<sup>1†</sup>, Aditya Grover<sup>2†</sup>, Norman Jin<sup>1</sup>, Kristen A. Severson<sup>3</sup>, Todor M. Markov<sup>2</sup>, Yang-

Hung Liao<sup>1</sup>, Michael H. Chen<sup>1</sup>, Bryan Cheong<sup>1,2</sup>, Nicholas Perkins<sup>1</sup>, Zi Yang<sup>1</sup>,

Patrick K. Herring<sup>4</sup>, Muratahan Aykol<sup>4</sup>, Stephen J. Harris<sup>1,5</sup>, Richard D. Braatz<sup>3\*</sup>,

Stefano Ermon<sup>2\*</sup>, William C. Chueh<sup>1,6\*</sup>

- † These authors contributed equally to this work
- \* Corresponding authors: wchueh@stanford.edu, ermon@cs.stanford.edu, braatz@mit.edu
- 1 Department of Materials Science and Engineering, Stanford University, Stanford, CA, USA
- 2 Department of Computer Science, Stanford University, Stanford, CA, USA
- 3 Department of Chemical Engineering, Massachusetts Institute of Technology, Cambridge, MA,

USA

- 4 Toyota Research Institute, Los Altos, CA, USA
- 5 Materials Science Division, Lawrence Berkeley National Lab, Berkeley, CA, USA
- 6 Applied Energy Division, SLAC National Accelerator Laboratory

### **Supplementary Tables**

**Supplementary Table 1.** Features selected by the elastic net in the early outcome prediction model, along with the feature weights and feature scaling means and standard deviations. See Severson et al.  $^1$  for additional details on feature definitions. Note that this model predicts the  $\log_{10}$  of cycle life, not cycle life itself.

| Feature                                     | Definition                                                 | Weight (×10 <sup>-3</sup> ) | Scaling<br>mean | Scaling<br>standard<br>deviation |
|---------------------------------------------|------------------------------------------------------------|-----------------------------|-----------------|----------------------------------|
| Initial discharge capacity                  | $Q_{ m discharge}$ , cycle 2                               | 21.6                        | 1.0736          | 0.0097                           |
| Max change in discharge capacity            | $\max(Q_{	ext{discharge}}) - Q_{	ext{discharge}},$ cycle 2 | -25.5                       | 0.0054          | 0.0021                           |
| $\min(\Delta Q_{100-10}(V))$                | $\log_{10}( \min(\Delta Q_{100\text{-}10}(V)) )$           | $-21.3\times10^{-3}$        | -1.3537         | 0.1830                           |
| $\operatorname{var}(\Delta Q_{10010}(V))$   | $\log_{10}( \mathrm{var}(\Delta Q_{100-10}(V)) )$          | -145                        | -3.6730         | 0.3758                           |
| $\operatorname{skew}(\Delta Q_{100-10}(V))$ | $\log_{10}( \operatorname{skew}(\Delta Q_{100-10}(V)) )$   | 12.9                        | -0.8553         | 0.4367                           |

**Supplementary Table 2.** Comparison of initial discharge capacities (at cycle 2) of datasets used in Severson et al.<sup>1</sup> and the validation batch. Errors represent 95% confidence intervals. The packing date was 2015-09-26. A linear fit of mean initial discharge capacity vs time (assuming t=0 occurs at the pack date) reveals a slope of -1.2 mAh per 30 days (R<sup>2</sup>=0.91).

| Batch                        | Date started | Mean initial discharge capacity (Ah) | Number of cells |
|------------------------------|--------------|--------------------------------------|-----------------|
| Train/primary test set 1     | 2017-05-12   | $1.078 \pm 0.002$                    | 46              |
| Train/primary test set 2     | 2017-06-30   | $1.071 \pm 0.002$                    | 43              |
| Secondary test set           | 2018-04-12   | $1.064 \pm 0.002$                    | 46              |
| oed_0 (this work)            | 2018-08-28   | $1.055 \pm 0.004$                    | 46              |
| oed_1 (this work)            | 2018-09-02   | $1.061 \pm 0.002$                    | 46              |
| oed_2 (this work)            | 2018-09-06   | $1.061 \pm 0.002$                    | 48              |
| oed_3 (this work)            | 2018-09-10   | $1.055 \pm 0.003$                    | 48              |
| Validation batch (this work) | 2019-01-24   | $1.051 \pm 0.003$                    | 45              |

**Supplementary Table 3.** Charging protocols and their associated CLO-estimated cycle life rankings, cycle lives, and one-sided standard deviations on cycle life at the end of batch 4. Each constant-current step (CC1, CC2, CC3, and CC4) comprises a 20% SOC window, such that CC1 ranges from 0 to 20% SOC, CC2 ranges from 20 to 40% SOC, etc. CC1, CC2, and CC3 are independent parameters, while CC4 is constrained by specifying that all protocols charge in the same total time (10 minutes) from 0% to 80% SOC.

| Ranking | CC1 | CC2 | CC3 | CC4   | CLO-<br>estimated<br>cycle life<br>( $\mu_{4,i}$ ) | CLO cycle life std. deviation $(\sigma_{4,i})$ |
|---------|-----|-----|-----|-------|----------------------------------------------------|------------------------------------------------|
| 1       | 4.8 | 5.2 | 5.2 | 4.160 | 1185                                               | 78                                             |
| 2       | 5.2 | 5.2 | 4.8 | 4.160 | 1183                                               | 86                                             |
| 3       | 4.4 | 5.6 | 5.2 | 4.252 | 1174                                               | 76                                             |
| 4       | 4.8 | 5.2 | 4.8 | 4.457 | 1174                                               | 93                                             |
| 5       | 4   | 5.6 | 5.6 | 4.421 | 1164                                               | 93                                             |
| 6       | 4   | 5.6 | 5.2 | 4.707 | 1164                                               | 102                                            |
| 7       | 4.4 | 5.2 | 5.2 | 4.516 | 1162                                               | 94                                             |
| 8       | 4.4 | 5.6 | 5.6 | 4.017 | 1162                                               | 83                                             |
| 9       | 5.2 | 5.2 | 4.4 | 4.516 | 1160                                               | 116                                            |
| 10      | 5.2 | 5.2 | 5.2 | 3.900 | 1160                                               | 90                                             |
| 11      | 4.4 | 5.2 | 5.6 | 4.252 | 1159                                               | 88                                             |
| 12      | 4.8 | 5.2 | 5.6 | 3.935 | 1158                                               | 88                                             |
| 13      | 4.8 | 5.6 | 4.8 | 4.200 | 1158                                               | 76                                             |
| 14      | 4.8 | 5.6 | 5.2 | 3.935 | 1156                                               | 76                                             |
| 15      | 4.8 | 4.8 | 5.2 | 4.457 | 1149                                               | 106                                            |
| 16      | 4.4 | 5.6 | 4.8 | 4.563 | 1147                                               | 91                                             |
| 17      | 5.2 | 5.6 | 4.8 | 3.935 | 1144                                               | 84                                             |
| 18      | 4   | 6   | 5.2 | 4.457 | 1142                                               | 89                                             |
| 19      | 4.4 | 6   | 5.2 | 4.047 | 1140                                               | 82                                             |

| 20 | 5.2 | 4.8 | 4.8 | 4.457 | 1140 | 117 |
|----|-----|-----|-----|-------|------|-----|
| 21 | 4   | 5.2 | 5.6 | 4.707 | 1137 | 117 |
| 22 | 5.2 | 4.8 | 5.2 | 4.160 | 1134 | 107 |
| 23 | 4.8 | 4.8 | 5.6 | 4.200 | 1133 | 104 |
| 24 | 4   | 6   | 5.6 | 4.200 | 1133 | 93  |
| 25 | 5.2 | 5.6 | 4.4 | 4.252 | 1130 | 93  |
| 26 | 4.8 | 5.6 | 5.6 | 3.733 | 1121 | 83  |
| 27 | 4.4 | 6   | 4.8 | 4.328 | 1120 | 83  |
| 28 | 4.4 | 6   | 5.6 | 3.834 | 1118 | 94  |
| 29 | 4.8 | 5.6 | 4.4 | 4.563 | 1117 | 98  |
| 30 | 4   | 6   | 4.8 | 4.800 | 1113 | 113 |
| 31 | 4.4 | 4.8 | 5.6 | 4.563 | 1110 | 116 |
| 32 | 5.2 | 5.2 | 5.6 | 3.702 | 1109 | 109 |
| 33 | 5.2 | 5.6 | 5.2 | 3.702 | 1107 | 86  |
| 34 | 5.6 | 5.2 | 4.4 | 4.252 | 1106 | 138 |
| 35 | 5.6 | 5.2 | 4.8 | 3.935 | 1106 | 127 |
| 36 | 4.8 | 6   | 4.8 | 4.000 | 1104 | 83  |
| 37 | 5.2 | 4.8 | 5.6 | 3.935 | 1103 | 131 |
| 38 | 3.6 | 6   | 5.6 | 4.755 | 1103 | 131 |
| 39 | 4.8 | 6   | 5.2 | 3.759 | 1097 | 84  |
| 40 | 5.2 | 5.6 | 4   | 4.707 | 1077 | 147 |
| 41 | 5.2 | 6   | 4.8 | 3.759 | 1071 | 93  |
| 42 | 5.6 | 4.8 | 4.8 | 4.200 | 1071 | 140 |
| 43 | 5.6 | 5.6 | 4.4 | 4.017 | 1070 | 123 |
| 44 | 5.6 | 4.8 | 4.4 | 4.563 | 1069 | 176 |
| 45 | 5.6 | 5.6 | 4.8 | 3.733 | 1068 | 120 |

| 46 | 5.6 | 5.2 | 4   | 4.707 | 1067 | 192 |
|----|-----|-----|-----|-------|------|-----|
| 47 | 4.8 | 6   | 4.4 | 4.328 | 1067 | 94  |
| 48 | 5.6 | 5.2 | 5.2 | 3.702 | 1063 | 146 |
| 49 | 4.4 | 6   | 4.4 | 4.714 | 1062 | 114 |
| 50 | 5.2 | 6   | 4.4 | 4.047 | 1059 | 104 |
| 51 | 4.8 | 6   | 5.6 | 3.574 | 1058 | 97  |
| 52 | 5.6 | 4.8 | 5.2 | 3.935 | 1048 | 156 |
| 53 | 5.2 | 5.6 | 5.6 | 3.523 | 1047 | 100 |
| 54 | 4.8 | 4.4 | 5.6 | 4.563 | 1043 | 160 |
| 55 | 4.8 | 7   | 4.8 | 3.652 | 1039 | 114 |
| 56 | 5.2 | 7   | 4.8 | 3.450 | 1037 | 128 |
| 57 | 5.2 | 6   | 5.2 | 3.545 | 1033 | 93  |
| 58 | 4.8 | 7   | 5.2 | 3.450 | 1032 | 127 |
| 59 | 5.2 | 4.4 | 5.2 | 4.516 | 1032 | 150 |
| 60 | 5.6 | 5.6 | 4   | 4.421 | 1032 | 163 |
| 61 | 4.4 | 7   | 5.2 | 3.691 | 1022 | 143 |
| 62 | 5.2 | 7   | 4.4 | 3.691 | 1017 | 146 |
| 63 | 5.2 | 4.4 | 5.6 | 4.252 | 1017 | 163 |
| 64 | 5.6 | 5.6 | 5.2 | 3.523 | 1016 | 133 |
| 65 | 5.6 | 4.8 | 5.6 | 3.733 | 1016 | 190 |
| 66 | 5.2 | 6   | 4   | 4.457 | 1014 | 152 |
| 67 | 4.8 | 6   | 4   | 4.800 | 1013 | 158 |
| 68 | 5.6 | 5.2 | 5.6 | 3.523 | 1008 | 171 |
| 69 | 5.2 | 7   | 5.2 | 3.269 | 1008 | 148 |
| 70 | 5.6 | 6   | 4.8 | 3.574 | 1005 | 135 |
| 71 | 4.4 | 7   | 4.8 | 3.924 | 1005 | 133 |

| 72 | 4.8 | 7   | 4.4 | 3.924 | 1005 | 127 |
|----|-----|-----|-----|-------|------|-----|
| 73 | 5.6 | 6   | 4.4 | 3.834 | 1003 | 147 |
| 74 | 5.6 | 7   | 4.8 | 3.294 | 998  | 191 |
| 75 | 4.4 | 7   | 5.6 | 3.513 | 996  | 160 |
| 76 | 6   | 5.2 | 4.4 | 4.047 | 994  | 182 |
| 77 | 6   | 4.8 | 4   | 4.800 | 989  | 253 |
| 78 | 6   | 4.8 | 4.4 | 4.328 | 987  | 208 |
| 79 | 5.6 | 4.4 | 4.8 | 4.563 | 987  | 151 |
| 80 | 4.8 | 7   | 5.6 | 3.294 | 987  | 162 |
| 81 | 4   | 7   | 5.2 | 4.030 | 986  | 179 |
| 82 | 6   | 5.2 | 4   | 4.457 | 985  | 213 |
| 83 | 5.6 | 7   | 4.4 | 3.513 | 982  | 188 |
| 84 | 6   | 5.2 | 4.8 | 3.759 | 978  | 188 |
| 85 | 5.2 | 6   | 5.6 | 3.381 | 978  | 116 |
| 86 | 4   | 7   | 5.6 | 3.818 | 977  | 188 |
| 87 | 5.6 | 4.4 | 5.2 | 4.252 | 975  | 150 |
| 88 | 5.2 | 7   | 4   | 4.030 | 971  | 190 |
| 89 | 6   | 4.8 | 4.8 | 4.000 | 971  | 189 |
| 90 | 5.6 | 6   | 4   | 4.200 | 967  | 180 |
| 91 | 4.8 | 7   | 4   | 4.308 | 965  | 168 |
| 92 | 5.6 | 7   | 5.2 | 3.129 | 965  | 197 |
| 93 | 5.6 | 4.4 | 5.6 | 4.017 | 962  | 189 |
| 94 | 4   | 7   | 4.8 | 4.308 | 961  | 166 |
| 95 | 5.6 | 6   | 5.2 | 3.381 | 961  | 140 |
| 96 | 4.4 | 7   | 4.4 | 4.239 | 959  | 133 |
| 97 | 3.6 | 7   | 5.2 | 4.537 | 955  | 236 |

| 98  | 3.6 | 7   | 5.6 | 4.271 | 955 | 242 |
|-----|-----|-----|-----|-------|-----|-----|
| 99  | 6   | 5.6 | 4.4 | 3.834 | 954 | 164 |
| 100 | 5.6 | 5.6 | 5.6 | 3.360 | 954 | 155 |
| 101 | 6   | 4.4 | 4.4 | 4.714 | 953 | 215 |
| 102 | 5.2 | 7   | 5.6 | 3.129 | 953 | 183 |
| 103 | 6   | 5.6 | 4.8 | 3.574 | 947 | 180 |
| 104 | 6   | 4.8 | 5.2 | 3.759 | 944 | 210 |
| 105 | 6   | 7   | 4.8 | 3.170 | 941 | 245 |
| 106 | 6   | 5.6 | 4   | 4.200 | 940 | 186 |
| 107 | 6   | 4.4 | 4.8 | 4.328 | 939 | 165 |
| 108 | 6   | 5.2 | 5.2 | 3.545 | 938 | 212 |
| 109 | 5.6 | 6   | 3.6 | 4.755 | 935 | 240 |
| 110 | 5.2 | 7   | 3.6 | 4.537 | 933 | 245 |
| 111 | 7   | 4.8 | 4   | 4.308 | 933 | 213 |
| 112 | 7   | 4.4 | 4   | 4.690 | 932 | 222 |
| 113 | 5.6 | 7   | 4   | 3.818 | 932 | 195 |
| 114 | 6   | 5.6 | 3.6 | 4.755 | 929 | 244 |
| 115 | 6   | 4   | 4.8 | 4.800 | 927 | 169 |
| 116 | 4.4 | 7   | 4   | 4.690 | 926 | 170 |
| 117 | 6   | 4.4 | 5.2 | 4.047 | 926 | 180 |
| 118 | 6   | 7   | 4.4 | 3.372 | 926 | 225 |
| 119 | 7   | 3.6 | 5.6 | 4.271 | 925 | 271 |
| 120 | 6   | 4.8 | 5.6 | 3.574 | 922 | 242 |
| 121 | 6   | 7   | 5.2 | 3.017 | 918 | 244 |
| 122 | 4   | 7   | 4.4 | 4.690 | 918 | 169 |
| 123 | 6   | 4.4 | 5.6 | 3.834 | 918 | 227 |

| 124 | 5.2 | 4   | 5.6 | 4.707 | 918 | 206 |
|-----|-----|-----|-----|-------|-----|-----|
| 125 | 7   | 3.6 | 5.2 | 4.537 | 916 | 234 |
| 126 | 6   | 4   | 5.2 | 4.457 | 916 | 163 |
| 127 | 5.6 | 7   | 5.6 | 3.000 | 916 | 209 |
| 128 | 6   | 6   | 4.8 | 3.429 | 914 | 199 |
| 129 | 6   | 3.6 | 5.6 | 4.755 | 912 | 247 |
| 130 | 7   | 4   | 5.6 | 3.818 | 911 | 232 |
| 131 | 7   | 4.4 | 4.4 | 4.239 | 911 | 194 |
| 132 | 7   | 4.8 | 4.4 | 3.924 | 909 | 201 |
| 133 | 6   | 6   | 4.4 | 3.667 | 909 | 194 |
| 134 | 5.6 | 4   | 5.2 | 4.707 | 908 | 160 |
| 135 | 6   | 5.6 | 5.2 | 3.381 | 908 | 205 |
| 136 | 6   | 4   | 5.6 | 4.200 | 907 | 211 |
| 137 | 5.6 | 6   | 5.6 | 3.231 | 906 | 168 |
| 138 | 7   | 4   | 5.2 | 4.030 | 905 | 177 |
| 139 | 7   | 5.2 | 3.6 | 4.537 | 904 | 252 |
| 140 | 6   | 5.2 | 5.6 | 3.381 | 901 | 235 |
| 141 | 5.6 | 4   | 5.6 | 4.421 | 899 | 187 |
| 142 | 7   | 4   | 4.4 | 4.690 | 898 | 192 |
| 143 | 7   | 4   | 4.8 | 4.308 | 898 | 167 |
| 144 | 7   | 4.4 | 4.8 | 3.924 | 893 | 172 |
| 145 | 7   | 5.2 | 4   | 4.030 | 892 | 220 |
| 146 | 6   | 7   | 5.6 | 2.897 | 888 | 244 |
| 147 | 5.6 | 7   | 3.6 | 4.271 | 888 | 226 |
| 148 | 6   | 6   | 5.2 | 3.250 | 887 | 213 |
| 149 | 6   | 6   | 4   | 4.000 | 887 | 209 |

| 150 | 7 | 4.4 | 5.2 | 3.691 | 881 | 158 |
|-----|---|-----|-----|-------|-----|-----|
| 151 | 6 | 7   | 4   | 3.652 | 880 | 194 |
| 152 | 6 | 6   | 3.6 | 4.500 | 879 | 250 |
| 153 | 7 | 4.4 | 5.6 | 3.513 | 878 | 199 |
| 154 | 7 | 4.8 | 4.8 | 3.652 | 876 | 183 |
| 155 | 7 | 5.2 | 4.4 | 3.691 | 874 | 205 |
| 156 | 6 | 5.6 | 5.6 | 3.231 | 869 | 227 |
| 157 | 8 | 3.6 | 5.6 | 3.969 | 862 | 259 |
| 158 | 6 | 6   | 5.6 | 3.111 | 855 | 237 |
| 159 | 8 | 4   | 4   | 4.800 | 855 | 222 |
| 160 | 8 | 4   | 5.6 | 3.574 | 854 | 264 |
| 161 | 8 | 4.4 | 5.6 | 3.306 | 851 | 262 |
| 162 | 7 | 5.6 | 3.6 | 4.271 | 849 | 233 |
| 163 | 8 | 4.8 | 5.6 | 3.111 | 848 | 250 |
| 164 | 8 | 5.2 | 5.6 | 2.963 | 846 | 265 |
| 165 | 6 | 7   | 3.6 | 4.065 | 845 | 203 |
| 166 | 7 | 4.8 | 5.2 | 3.450 | 845 | 156 |
| 167 | 7 | 5.2 | 4.8 | 3.450 | 844 | 191 |
| 168 | 8 | 3.6 | 5.2 | 4.197 | 837 | 226 |
| 169 | 8 | 5.6 | 5.6 | 2.847 | 837 | 294 |
| 170 | 8 | 4.4 | 4   | 4.328 | 836 | 218 |
| 171 | 8 | 3.6 | 4.8 | 4.500 | 833 | 242 |
| 172 | 7 | 5.6 | 4   | 3.818 | 831 | 214 |
| 173 | 7 | 4.8 | 5.6 | 3.294 | 831 | 174 |
| 174 | 8 | 4   | 4.4 | 4.328 | 829 | 229 |
| 175 | 8 | 5.2 | 5.2 | 3.089 | 828 | 218 |

| 176 | 8 | 4   | 5.2 | 3.759 | 826 | 232 |
|-----|---|-----|-----|-------|-----|-----|
| 177 | 8 | 4.8 | 5.2 | 3.250 | 826 | 203 |
| 178 | 8 | 4.4 | 5.2 | 3.463 | 825 | 228 |
| 179 | 8 | 4.8 | 3.6 | 4.500 | 822 | 251 |
| 180 | 7 | 5.6 | 4.4 | 3.513 | 822 | 207 |
| 181 | 8 | 5.6 | 5.2 | 2.963 | 821 | 266 |
| 182 | 8 | 4.4 | 4.4 | 3.940 | 818 | 212 |
| 183 | 8 | 4   | 4.8 | 4.000 | 817 | 235 |
| 184 | 7 | 7   | 3.6 | 3.706 | 817 | 287 |
| 185 | 8 | 4.4 | 4.8 | 3.667 | 814 | 221 |
| 186 | 7 | 6   | 3.6 | 4.065 | 813 | 217 |
| 187 | 8 | 4.8 | 4.8 | 3.429 | 813 | 186 |
| 188 | 8 | 5.2 | 4.8 | 3.250 | 811 | 189 |
| 189 | 7 | 5.6 | 4.8 | 3.294 | 810 | 215 |
| 190 | 7 | 5.2 | 5.2 | 3.269 | 809 | 181 |
| 191 | 7 | 7   | 4.4 | 3.122 | 809 | 237 |
| 192 | 7 | 7   | 4   | 3.360 | 808 | 270 |
| 193 | 8 | 4.8 | 4   | 4.000 | 805 | 203 |
| 194 | 8 | 4.8 | 4.4 | 3.667 | 805 | 185 |
| 195 | 8 | 5.6 | 4.8 | 3.111 | 802 | 238 |
| 196 | 8 | 6   | 5.6 | 2.754 | 797 | 303 |
| 197 | 7 | 7   | 4.8 | 2.947 | 796 | 195 |
| 198 | 7 | 5.2 | 5.6 | 3.129 | 794 | 191 |
| 199 | 7 | 6   | 4   | 3.652 | 791 | 205 |
| 200 | 7 | 5.6 | 5.2 | 3.129 | 790 | 233 |
| 201 | 7 | 6   | 5.6 | 2.897 | 789 | 284 |

| 202 | 7 | 6   | 4.8 | 3.170 | 789 | 235 |
|-----|---|-----|-----|-------|-----|-----|
| 203 | 7 | 6   | 4.4 | 3.372 | 788 | 208 |
| 204 | 8 | 5.2 | 4.4 | 3.463 | 785 | 175 |
| 205 | 7 | 5.6 | 5.6 | 3.000 | 785 | 248 |
| 206 | 8 | 6   | 5.2 | 2.862 | 784 | 290 |
| 207 | 7 | 6   | 5.2 | 3.017 | 784 | 266 |
| 208 | 8 | 6   | 4.8 | 3.000 | 775 | 273 |
| 209 | 7 | 7   | 5.2 | 2.814 | 774 | 176 |
| 210 | 7 | 7   | 5.6 | 2.710 | 773 | 199 |
| 211 | 8 | 5.2 | 3.6 | 4.197 | 767 | 213 |
| 212 | 8 | 5.6 | 4.4 | 3.306 | 766 | 209 |
| 213 | 8 | 5.2 | 4   | 3.759 | 762 | 173 |
| 214 | 8 | 6   | 4.4 | 3.181 | 745 | 249 |
| 215 | 8 | 7   | 3.6 | 3.476 | 733 | 202 |
| 216 | 8 | 5.6 | 4   | 3.574 | 728 | 178 |
| 217 | 8 | 5.6 | 3.6 | 3.969 | 725 | 193 |
| 218 | 8 | 6   | 3.6 | 3.789 | 712 | 228 |
| 219 | 8 | 6   | 4   | 3.429 | 710 | 224 |
| 220 | 8 | 7   | 4   | 3.170 | 709 | 176 |
| 221 | 8 | 7   | 4.4 | 2.957 | 706 | 173 |
| 222 | 8 | 7   | 4.8 | 2.800 | 684 | 172 |
| 223 | 8 | 7   | 5.6 | 2.585 | 650 | 200 |
| 224 | 8 | 7   | 5.2 | 2.680 | 648 | 174 |
|     |   |     |     |       |     |     |

**Supplementary Table 4.** Comparison of early outcome predictors. To contextualize the results, we included the fixed-mean baseline, which predicts a constant mean computed on the training set (held-out set is "primary test set" from Severson et al.<sup>1</sup>). See "Related work" section of Supplementary Discussion 2 for more details on the predictors proposed by Domhan et al.<sup>2</sup> and Klein et al.<sup>3</sup>

| Method                                                                                      | Training RMSE (cycles) | Held-out RMSE<br>(cycles) |
|---------------------------------------------------------------------------------------------|------------------------|---------------------------|
| Fixed-mean baseline                                                                         | 327                    | 399                       |
| Domhan et al. <sup>2</sup>                                                                  | 681                    | 756                       |
| Klein et al. <sup>3</sup>                                                                   | 110                    | 190                       |
| "Discharge model" from Severson et al. <sup>1</sup> (similar to ML model used in this work) | 76                     | 86                        |

**Supplementary Table 5.** Hyperparameter values used in the Bayesian optimization algorithm. The "Hyperparameter variable name in code" column refers to the variable name used in the BO code (closed\_loop\_oed.py). The hyperparameters are further detailed in the "Hyperparameter optimization" section of the Methods. The 2018-04-12 batch of Severson et al.¹ is used here because the cycling structure (i.e., rest steps, constant-voltage hold conditions, etc) is similar to that used in this work, although different charging protocols were tested.

| Hyperparameter<br>name             | Hyperparameter variable name in code | Value | Rationale                                                                                                                                                                 |
|------------------------------------|--------------------------------------|-------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Batch size                         | bsize                                | 48    | 48-channel cycler                                                                                                                                                         |
| Budget                             | budget                               | 4     | ~200 cells for optimization (4×48)                                                                                                                                        |
| Standardization mean               | standarization_mean                  | 947   | Mean cycle life of 2018-04-12 batch of Severson et al. <sup>1</sup>                                                                                                       |
| Standardization standard deviation | standarization_std                   | 164   | Standard deviation of 2018-04-12 batch of Severson et al. <sup>1</sup>                                                                                                    |
| Likelihood standard deviation      | likelihood_std                       | 164   | Additive error (square root of the sum of the squares) of the sampling variation (126) and the prediction error (106) in 2018-04-12 batch of Severson et al. <sup>1</sup> |
| γ                                  | gamma                                | 1     | Optimized via<br>simulator                                                                                                                                                |
| $oldsymbol{eta}_0$                 | init_beta                            | 5.0   | Optimized via simulator                                                                                                                                                   |
| ε                                  | epsilon                              | 0.5   | Optimized via<br>simulator                                                                                                                                                |

**Supplementary Table 6.** Temperature dependence of SEI growth at C/10 as estimated from Figure 7 of Smith et al.<sup>4</sup>, as used in the simulator. The data were manually extracted from the figure using WebPlotDigitizer. The slopes and intercepts were determined by linear fits of  $Q_{\rm SEI}$  to  $t^{0.5}$ . The activation energy was determined by fitting the Arrhenius equation, using the slopes as approximations for k. The resulting activation energy is 0.122 eV.

| Temperature (°C) | Slope (mAh g <sup>-1</sup> h <sup>-0.5</sup> ) | Intercept (mAh g <sup>-1</sup> ) |
|------------------|------------------------------------------------|----------------------------------|
| 30               | 1.283                                          | 34.6                             |
| 40               | 1.449                                          | 35.6                             |
| 50               | 1.714                                          | 38.7                             |

### **Supplementary Discussions**

**Supplementary Discussion 1.** Alternate approaches for early outcome prediction and hyperparameter optimization

Early outcome predictor development and BO hyperparameter optimization are two critical components for closed-loop optimization. Both of these tasks require some initial data, which adds to the experimental requirements for the closed loop. Here we discuss our approach, as well as alternative approaches, to address these requirements.

For learning the early outcome predictor, we used a previously collected dataset<sup>1</sup> of 41 batteries cycled to failure as the training set. We note that this dataset contains reach information and can be used for early prediction of relevant outcomes of similar optimization tasks, such as different charging times and SOC windows; if multiple optimization objectives are to be considered for a new problem, we recommend collecting a dataset that spans the conditions of interest. For instance, all batteries in the training set were cycled with three-step or four-step charging protocols, as opposed to six-step. Additionally, while this training set was readily available, accurate predictive performance could likely be achieved with a smaller training set. Finally, previously collected datasets with different chemistries or cycling conditions could be leveraged for other battery optimization tasks using approaches such as transfer learning<sup>5</sup> and hybrid physics-data models.

For tuning hyperparameters of the BO component of our pipeline, we used both the training set for the early predictor and a simple physical simulator (see Methods). This simulator was originally designed for fundamental studies of heat transfer but was adapted to produce cycle life estimates as a function of charging protocol (see Physics-based simulator section of Methods). The

only experimental input is the expected cycle life range. As such, the simulator does not accurately capture degradation during fast charging but provides reasonable estimates for hyperparameter optimization. Given that the simulator does not represent the true parameter space, the selected hyperparameter combination is likely suboptimal; however, we observe that the performance of the BO algorithm is relatively insensitive to the selected hyperparameters (Extended Data Figure 9), meaning that suboptimal hyperparameter combinations can still perform well.

## **Supplementary Discussion 2.** Related work and possible modifications to closed-loop system **Related work review and comparison**

The underlying optimal experimental design problem we seek to address is an instance of multi-fidelity black-box optimization. In black-box optimization, we only have sample access to an underlying function of interest. However, a single evaluation can itself be very expensive (in terms of time or resources), and hence low-fidelity signals that are noisy but easy-to-obtain are often used instead for efficient optimization.

The canonical use case considered in prior work is that of hyperparameter optimization for machine learning algorithms. Here, the goal is to find the optimal configuration of hyperparameters for learning a model on a target dataset. However, training a model with even a single configuration can be compute and time-intensive. To resolve this shortcoming, prominent examples of low-fidelity signals include (a) early prediction of learning curves (e.g., Domhan et al.<sup>2</sup>) and (b) testing a hyperparameter configuration on a subset of the data (e.g., Petrak et al.<sup>6</sup>). Multi-fidelity approaches (e.g., Van den Bosch et al.<sup>7</sup>, Krueger et al.<sup>8</sup>, Sabharwal et al.<sup>9</sup>, and Sparks et al.<sup>10</sup>) use one or more of these low-fidelity signals for dynamically selecting which hyperparameter configuration to test next, e.g., *successive halving* routines<sup>11</sup> such as Hyperband<sup>12</sup>, which periodically removes half of the worst performing configurations. We provide details on methods that predict learning curves, since that form of fidelity signal is similar to the one we consider. We further refer the reader to Hutter et al.<sup>13</sup> (Section 1.4) for an excellent and comprehensive survey on multi-fidelity black box optimization.

A learning curve tracks the performance of a machine learning algorithm (as measured via a suitable metric such as classification accuracy on a validation dataset) as a function of training time (as measured via number of iterations, gradient updates, etc.). These curves are typically

increasing functions, and the performance metric saturates over time. Since observing the asymptote of a learning curve for any single hyperparameter configuration can be expensive, Domhan et al.<sup>2</sup> proposed to *predict* a learning curve after training the model only for a small number of iterations. The goal is to terminate the training procedure early if the asymptotic performance on a validation set is unlikely to beat the validation performance of the best known hyperparameter configuration so far. The predictor is parameterized using a mixture of functional forms (e.g., Weibull, vapor pressure, etc.) that have similar characteristics as learning curves (i.e., increasing and saturating with respect to the performance metric). Using standard Bayesian inference over the unknown parameters, the probability that the performance of the algorithm at a future iteration will exceed the best known performance so far can be estimated. Such estimates are then used within a downstream black-box optimization routine such as SMAC<sup>14,15</sup> or Tree Parzen Estimator<sup>16</sup> for the purpose of deciding whether to terminate training of a given hyperparameter configuration and utilize the remaining budget for testing other candidate hyperparameter configurations. Klein et al.<sup>3</sup> extend this approach via Bayesian neural networks to utilize additional data from past runs of related hyperparameter configurations. This permits learning more accurate predictors without having to observe a substantial portion of the learning curve.

To draw an analogy with the current work, we are interested in predicting the cycle life at which the capacity of a charging protocol drops to a predefined value (80% of initial capacity, or 0.88 Ah). In contrast to typical shapes of learning curves, (a) the capacity is decreasing as a function of cycle life and (b) the cycle life saturates with respect to the capacity (y-axis). That is, the capacity decreases slowly in the beginning until it hits a transition point. Beyond the transition point, the capacity quickly drops to 0.88 Ah. This transition point is unknown and occurs close to

the final cycle life. As a result, predicting the final cycle life is challenging without having substantially cycled the battery to observe the transition point. To overcome this challenge, our early predictor<sup>1</sup> uses both information from prior capacity curves as well as additional features at every timestep (e.g., voltage and capacity). This method allows for highly accurate predictions only after the first 100 cycles and generalization to protocols outside our training dataset.

Empirically, we perform comparisons with the approaches of Domhan et al.<sup>2</sup> and Klein et al.<sup>3</sup> for early prediction of cycle lives based on capacity curves. Due to the aforementioned differences between the shapes of learning curves and capacity curves, naively plugging in capacity curve data within these approaches gives extremely poor estimates. Instead, we modified the problem by switching the x- and y-axes of a capacity curve: that is, the "rotated capacity curve" plots the cycle life on the y-axis against the capacity on the x-axis. Further, to match the monotonically increasing behavior of a learning curve, we consider an invertible transformation  $x \to 1.1-x$  (since the nominal initial capacity is 1.1 Ah) for these curves. The empirical results post these transformations still lag our approach (Supplementary Table 4). We believe these results are largely because both Domhan et al.<sup>2</sup> and Klein et al.<sup>3</sup> do not use additional features (e.g., voltage) recorded *during* cycling of a battery, unlike our approach.

### Further improvements to optimization approach

Our closed-loop system demonstrates both high efficiency and high accuracy on this parameter space given the specified budget. However, additional untested modifications could further improve the performance of the closed loop in some settings. We discuss some possible modifications to consider in future work here. Many of these are active areas of research within the broader research community working on black-box optimization.

Requiring fewer cycles for early outcome prediction. In this work, we use a single model that predicts the final cycle life after 100 cycles, similar to that developed by Severson et al.<sup>1</sup> Predictive models that achieve similar accuracy but require fewer cycles could further reduce the time per experiment.

Incorporating adaptive early outcome predictions (multi-fidelity optimization). In this work, all predictions are generated after a specified number of cycles has been generated (i.e., 100). An alternative approach, detailed in Grover et al., would dynamically incorporate predictions made at various cycle numbers. In general, the accuracy of early outcome predictions increases with additional cycling data. If a prediction at an early cycle number has low expected lifetime with sufficiently high confidence, the experiment could be terminated early, and a new experiment could be run in its place. In practice, however, "batching" experiments as we have done may have practical advantages. For example, because the early outcome predictions are quite sensitive to temperature, we sought to minimize the number of times that we opened the environmental testing chamber; given our single temperature chamber for all channels, continuous cell switching would lead to frequent temperature disruptions. Furthermore, the practical cell switching frequency is around once or twice per day; "continuous" cell switching would be enabled by robotic cell switching technologies.

An alternative multi-fidelity approach is multi-phase closed-loop optimization. For instance, we could consider two phases of closed-loop testing. The first would perform preliminary classification of charging protocols into low-cycle-life or high-cycle-life classes; Severson et al.<sup>1</sup> demonstrated high classification accuracy using only the first 5 cycles. After this initial rapid screening phase, the second phase would proceed on the high-cycle-life protocols using a regression model for cycle life prediction.

Incorporating more fine-grained uncertainties in early predictions. In our system, all predictions are treated as scalar values; prediction intervals are computed for each prediction but are only used to flag anomalous high-uncertainty predictions. However, we expect the magnitude of the prediction intervals to vary for different cells (due to differences in manufacturing) and as a function of charging protocol (since some protocols will induce more cycle life variation than others). In future work, we could update the distribution of CLO-estimated cycle lives using confidence intervals specific to an early outcome predictor as opposed to a uniform upper bound. This modification would account for the nonuniform confidence in each prediction.

Incorporating better batching strategies. We disallowed repeated runs of the same charging protocol within a given round for inducing more exploration. This does not exclude the possibility that the top-48 protocols in a batch are highly similar. In principle, we want to select protocols which score well on the explore-exploit frontier and are diverse to ensure more efficient coverage. Methods based on slice sampling (to filter out a good subset of protocols) followed by clustering techniques (to group similar protocols together) can be applied for a more diverse selection of charging protocols to test. On the other extreme, an even more advanced batching strategy for BO would also permit repeated testing of promising charging protocols even within the same round for protocols for faster reduction of uncertainty.

Studying a wider variety of acquisition functions. Our acquisition function to trade-off exploration-exploitation was based on the Upper Confidence Bound (UCB) criteria, which enjoys strong regret guarantees in many scenarios and is highly popular in the literature on multi-armed bandits. In future work, we would like to study the effect of other acquisition functions used in Bayesian optimization, such as expected improvement and Thompson sampling.

Specifying criteria for early termination of the closed loop. As illustrated in Figure 3 and Extended Data Figures 3a–c, CLO converges relatively quickly on the high-cycle life region of the parameter space. If the time and/or cells are at a premium, formal early-stopping criteria could be used to determine when acceptable cycle life estimates have been obtained in the fixed-budget setting, even before the specified budget is exhausted. In other words, the closed loop could be terminated early (i.e., before the specified budget is exhausted) if a performance objective was reached with sufficient confidence. For example, a threshold for the "change in cycle life" metric presented in Extended Data Figures 3a–c could be used, i.e., stop when the change in CLO-estimated cycle life with increasing rounds falls below some threshold. Confidence-based stopping criteria could also be used, i.e., stop when the bounds on the top protocol(s) fall below some threshold. Finally, the closed loop can be operated in the fixed-confidence setting (i.e., continue testing until confidence in the best protocol exceeds some threshold), as opposed to the fixed-budget setting used in this work (arguably more practical).

Continuous parameter space. In line with the prior algorithms that we extend in this work, <sup>17,18</sup> we optimized over a discretized parameter space of charging protocols. Using alternate algorithms based on continuous parameter spaces could lead to performance improvements, as the search space for continuous optimization approaches can subsume the protocols in the discretized space. However, for relatively smooth parameter spaces such as the one considered in this work, discrete optimization can perform well with sufficiently fine discretization.

*Multi-objective closed-loop optimization.* Fast-charging protocols need to balance two competing objectives: fast charging time and high cycle life. In this work, we fixed charging time and optimized for cycle life, since any choice of a multi-objective function would be arbitrary. However, instead of optimizing for cycle life with fixed charging time, we could optimize over a

function that balanced both objectives. Ideally, multi-objective functions would be carefully developed with input from business units, consumers, and other stakeholders.

### Supplementary Discussion 3. Degradation mechanism

Our results revealed that fast-charging protocols with nearly constant-current current profiles generally exhibited the highest lifetimes, while protocols with monotonically decreasing currents performed relatively poorly. The optimized charging protocols revealed in this work are unexpected since we expect lithium plating to be the dominant form of degradation during fast charging, and plating would be minimized by monotonically decreasing currents to avoid large negative overpotentials. <sup>19–21</sup> In general, this result highlights the need for data-driven approaches to this problem, as first-principles approaches fail to capture the dominant degradation modes. While work is ongoing to precisely determine the dominant degradation modes, we hypothesize that solid-electrolyte interphase (SEI) growth, exacerbated by high temperatures, is the dominant degradation mode during these extreme operating conditions:

- While lithium plating is generally expected at high charging rates, the high environmental temperature (30°C) is a temperature regime in which lithium plating is unfavorable.<sup>22</sup> The rate of heat generation during fast charging surpasses the convective cooling in the chamber, so the cell temperature increase during cycling is significant (Extended Data Figure 2). In general, side reaction rates increase exponentially with the inverse temperature from the Arrhenius relation.
- Resistive (Ohmic) heat generation is governed by  $I^2R$  (Çengel & Boles<sup>23</sup>). In Extended Data Figures 1e–f, we determined that the resistance is both Ohmic (linear overpotential vs. current relationship) and largely independent of SOC, particularly for minimally-cycled cells. For a constant R,  $I^2$  is minimized via constant-current charging, which is consistent with our observation that the highest-lifetime protocols as identified by CLO are similar to

constant-current charging. This hypothesis is also loosely supported by Extended Data Figure 3e, in which a simple relationship between the sum of squared currents,  $sum(I^2)$  and the OED-estimated lifetimes yields a correlation coefficient of -0.84. We recognize, however, that temperature has a complex effect on battery degradation.

Previous reports<sup>24–29</sup> have observed SEI growth leading to loss of active material via electrochemistry and microscopy on similar or identical LFP/graphite cylindrical cells.
 Loss of active graphite material is responsible for the rapid decrease in capacity observed in these cells during fast charging.<sup>1,27</sup> Thus, SEI growth is consistent with known degradation modes in these cells.

### Supplementary Discussion 4. Bias in early outcome prediction

Figure 4c and Extended Data Figure 7 reveal a non-trivial bias in early outcome prediction for the validation protocols, in which nearly all final lifetimes fall well below their predictions. The mean predicted cycle lives exceed the mean final cycle lives by 145 cycles. If this bias is corrected for in the predictions, the root-mean-square error decreases from 173 cycles to 96 cycles, while the mean absolute percent error decreases from 20.1% to 9.46%, in line with the errors reported in Severson et al.<sup>1</sup> Importantly, the rankings of validation protocols are relatively unaffected (Extended Data Figure 7), implying a relatively consistent offset.

We attribute the source of this systematic bias to additional calendar aging, which lowers the initial discharge capacities and thus leads to larger predictions. A similar effect was presented in Supplementary Figures 6 and 7 and Supplementary Note 2 of Severson et al.<sup>1</sup> Calendar aging results in additional SEI growth, which consumes lithium inventory and reduces the capacity.<sup>30,31</sup> Supplementary Table 2 displays the mean initial discharge capacities of various datasets using the same cells. Although all cells have the same pack date (2015-09-26), the time between tests varies significantly (nearly 20 months between train/primary test set 1 and the validation batch), and thus so does the mean initial capacity. Given the feature weights and scalings in Supplementary Table 1, a change of 10 mAh in the initial discharge capacity leads to an additional 234 cycles predicted, which more than compensates for the bias observed here. Because the training set has uniform calendar life, this calendar life aging effect is not accounted for in the predictive model, and thus the cycle lives of the validation batch are overestimated.

#### **Supplementary References**

- 1. Severson, K. A. *et al.* Data-driven prediction of battery cycle life before capacity degradation. *Nature Energy* **4**, 383–391 (2019).
- Domhan, T., Springenberg, J. T. & Hutter, F. Speeding Up Automatic Hyperparameter Optimization of Deep Neural Networks by Extrapolation of Learning Curves. in *Proceedings of the 24th International Conference on Artificial Intelligence* 3460–3468 (AAAI Press, 2015).
- 3. Klein, A., Falkner, S., Springenberg, J. T. & Hutter, F. Learning curve prediction with Bayesian neural networks. in *Proceedings of the 2017 International Conference on Learning Representations* 1–16 (2017).
- 4. Smith, A. J., Burns, J. C., Zhao, X., Xiong, D. & Dahn, J. R. A High Precision Coulometry Study of the SEI Growth in Li/Graphite Cells. *J. Electrochem. Soc.* **158**, A447–A452 (2011).
- 5. Hutchinson, M. L. *et al.* Overcoming data scarcity with transfer learning. *arXiv:1711.05099 [cond-mat, stat]* (2017).
- 6. Petrak, J. Fast Subsampling Performance Estimates for Classification Algorithm Selection. 3–14 http://citeseerx.ist.psu.edu/viewdoc/download?doi=10.1.1.28.3305&rep=rep1&type=pdf (2000).
- 7. Bosch, A. van den. Wrapped progressive sampling search for optimizing learning algorithm parameters. in *Proceedings of the Belgium-Netherlands Conference on Artificial Intelligence* 219–226 (2004).
- 8. Krueger, T., Panknin, D. & Braun, M. Fast Cross-validation via Sequential Testing. *J. Mach. Learn.*Res. 16, 1103–1155 (2015).
- 9. Sabharwal, A., Samulowitz, H. & Tesauro, G. Selecting Near-Optimal Learners via Incremental Data Allocation. in *Proceedings of the Thirtieth AAAI Conference on Artificial Intelligence (AAAI-16)* 2007–2015 (2016).
- 10. Sparks, E. R. *et al.* Automating Model Search for Large Scale Machine Learning. in *Proceedings* of the Sixth ACM Symposium on Cloud Computing 368–380 (ACM, 2015).

- 11. Karnin, Z., Koren, T. & Somekh, O. Almost Optimal Exploration in Multi-armed Bandits. in Proceedings of the 30th International Conference on International Conference on Machine Learning - Volume 28 III–1238–III–1246 (JMLR.org, 2013).
- 12. Li, L., Jamieson, K., DeSalvo, G., Rostamizadeh, A. & Talwalkar, A. Hyperband: A Novel Bandit-Based Approach to Hyperparameter Optimization. *Journal of Machine Learning Research* 18, 1–52 (2018).
- 13. Automated Machine Learning: Methods, Systems, Challenges. (Springer International Publishing, 2019).
- 14. Hutter, F., Hoos, H. H. & Leyton-Brown, K. Sequential Model-based Optimization for General Algorithm Configuration. in *Proceedings of the 5th International Conference on Learning and Intelligent Optimization* 507–523 (Springer-Verlag, 2011). doi:10.1007/978-3-642-25566-3\_40.
- 15. Hutter, F., Xu, L., Hoos, H. H. & Leyton-Brown, K. Algorithm Runtime Prediction: Methods & Evaluation. in *Proceedings of the 24th International Conference on Artificial Intelligence* 4197–4201 (AAAI Press, 2015).
- 16. Bergstra, J. S., Bardenet, R., Bengio, Y. & Kégl, B. Algorithms for Hyper-Parameter Optimization. in *Advances in Neural Information Processing Systems 24* (eds. Shawe-Taylor, J., Zemel, R. S., Bartlett, P. L., Pereira, F. & Weinberger, K. Q.) 2546–2554 (Curran Associates, Inc., 2011).
- 17. Grover, A. et al. Best arm identification in multi-armed bandits with delayed feedback. in Proceedings of the 21st International Conference on Artificial Intelligence and Statistics (AISTATS) vol. 84 833–842 (2018).
- 18. Hoffman, M. W., Shahriari, B. & de Freitas, N. On correlation and budget constraints in model-based bandit optimization with application to automatic machine learning. in *Proceedings of the 17th International Conference on Artificial Intelligence and Statistics (AISTATS)* vol. 33 365–374 (2014).
- 19. Keil, P. & Jossen, A. Charging protocols for lithium-ion batteries and their impact on cycle life—

- An experimental study with different 18650 high-power cells. *Journal of Energy Storage* **6**, 125–141 (2016).
- 20. Ahmed, S. *et al.* Enabling fast charging A battery technology gap assessment. *Journal of Power Sources* **367**, 250–262 (2017).
- 21. Schindler, S., Bauer, M., Cheetamun, H. & Danzer, M. A. Fast charging of lithium-ion cells: Identification of aging-minimal current profiles using a design of experiment approach and a mechanistic degradation analysis. *Journal of Energy Storage* 19, 364–378 (2018).
- 22. Waldmann, T., Wilka, M., Kasper, M., Fleischhammer, M. & Wohlfahrt-Mehrens, M.
  Temperature dependent ageing mechanisms in Lithium-ion batteries A Post-Mortem study. *Journal of Power Sources* 262, 129–135 (2014).
- 23. Çengel, Y. A. & Boles, M. A. *Thermodynamics: An Engineering Approach*. (McGraw-Hill Education, 2015).
- 24. Liu, P. *et al.* Aging Mechanisms of LiFePO<sub>4</sub> Batteries Deduced by Electrochemical and Structural Analyses. *J. Electrochem. Soc.* **157**, A499–A507 (2010).
- 25. Safari, M. & Delacourt, C. Aging of a Commercial Graphite/LiFePO<sub>4</sub> Cell. *J. Electrochem. Soc.* **158**, A1123–A1135 (2011).
- Sarasketa-Zabala, E. et al. Understanding Lithium Inventory Loss and Sudden Performance Fade in Cylindrical Cells during Cycling with Deep-Discharge Steps. J. Phys. Chem. C 119, 896–906 (2015).
- 27. Anseán, D. *et al.* Fast charging technique for high power LiFePO<sub>4</sub> batteries: A mechanistic analysis of aging. *Journal of Power Sources* **321**, 201–209 (2016).
- 28. Lewerenz, M., Marongiu, A., Warnecke, A. & Sauer, D. U. Differential voltage analysis as a tool for analyzing inhomogeneous aging: A case study for LiFePO<sub>4</sub>|Graphite cylindrical cells. *Journal of Power Sources* **368**, 57–67 (2017).
- 29. Lewerenz, M., Warnecke, A. & Sauer, D. U. Post-mortem analysis on LiFePO<sub>4</sub>|Graphite cells describing the evolution & composition of covering layer on anode and their impact on cell

performance. Journal of Power Sources 369, 122-132 (2017).

- 30. Broussely, M. *et al.* Aging mechanism in Li ion cells and calendar life predictions. *Journal of Power Sources* **97–98**, 13–21 (2001).
- 31. Keil, P. *et al.* Calendar Aging of Lithium-Ion Batteries I. Impact of the Graphite Anode on Capacity Fade. *J. Electrochem. Soc.* **163**, A1872–A1880 (2016).