# Lab 10

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## 11:59PM May 11, 2020

In the first part of this lab, we will be joining three datasets in an effort to make a design matrix that predicts if a bill will be paid on time. Load up the three files:

```
pacman::p_load(tidyverse, magrittr, data.table, R.utils,ggplot2)
bills = fread("https://github.com/kapelner/QC_Math_390.4_Spring_2020/raw/master/labs/bills_dataset/bill
payments = fread("https://github.com/kapelner/QC_Math_390.4_Spring_2020/raw/master/labs/bills_dataset/p
discounts = fread("https://github.com/kapelner/QC_Math_390.4_Spring_2020/raw/master/labs/bills_dataset/p
```

The unit we care about is the bill. The metric we care about is "paid in full" and it's binary. We would like to build the best design matrix we can and of course generate the y. Warning: this data is highly anonymized and there is likely zero signal! So don't expect to get predictive accuracy. The value of the exercise is in the practice. I think this may be one of the most useful exercises in the entire semester.

I will create the basic steps for you guys. First, join the three datasets in an intelligent way. You will need to examine the datasets beforehand.

```
head(bills)
```

```
##
                 due date invoice date
                                          amount customer_id discount_id
            id
## 1: 15163811 2017-02-12
                            2017-01-13 99490.77
                                                    14290629
                                                                 5693147
## 2: 17244832 2016-03-22
                            2016-02-21 99475.73
                                                    14663516
                                                                 5693147
## 3: 16072776 2016-08-31
                            2016-07-17 99477.03
                                                    14569622
                                                                 7302585
## 4: 15446684 2017-05-29
                            2017-05-29 99478.60
                                                                 5693147
                                                    14488427
## 5: 16257142 2017-06-09
                            2017-05-10 99678.17
                                                    14497172
                                                                 5693147
## 6: 17244880 2017-01-24
                            2017-01-24 99475.04
                                                    14663516
                                                                 5693147
setnames(bills, "amount", "tot_amount")
setnames(payments, "amount", "paid_amount")
head(payments)
```

```
id paid_amount transaction_date bill_id
## 1: 15272980
                  99165.60
                                  2017-01-16 16571185
## 2: 15246935
                  99148.12
                                  2017-01-03 16660000
## 3: 16596393
                  99158.06
                                  2017-06-19 16985407
## 4: 16596651
                  99175.03
                                  2017-06-19 17062491
## 5: 16687702
                  99148.20
                                  2017-02-15 17184583
## 6: 16593510
                  99153.94
                                  2017-06-11 16686215
```

### head(discounts)

##		id	num_days	pct_off	<pre>days_until_discount</pre>
##	1:	5000000	20	NA	NA
##	2:	5693147	NA	2	NA
##	3:	6098612	20	NA	NA
##	4:	6386294	120	NA	NA
##	5:	6609438	NA	1	7

```
bills_with_payments = merge(bills, payments, by.x ="id", by.y = "bill_id", all.x = TRUE)
bills_with_payments[, id.y := NULL]
bills_with_payments
##
                       due_date invoice_date tot_amount customer_id discount_id
##
        1: 5000000 2016-07-31
                                  2016-06-16
                                                99480.18
                                                            12867871
                                                                          7397895
##
        2: 5693147 2017-05-11
                                  2017-04-11
                                                99528.76
                                                                          7397895
                                                            12871311
##
        3: 6098612 2016-01-15
                                  2016-01-04
                                                99477.35
                                                            13135347
                                                                          7397895
        4: 6386294 2016-12-30
##
                                  2016-12-30
                                                99479.31
                                                            12867871
                                                                          7397895
##
            6609438 2017-05-07
                                  2017-04-07
                                                99477.20
                                                            12867871
                                                                          7397895
##
## 279114: 17619324 2017-02-02
                                                99478.67
                                  2017-02-02
                                                            14598456
                                                                          5693147
## 279115: 17619327 2017-05-09
                                  2017-04-09
                                                99688.54
                                                            14475317
                                                                          7708050
## 279116: 17619331 2017-05-05
                                  2017-05-05
                                                99484.81
                                                                          7302585
                                                            14569203
## 279117: 17619334 2017-06-25
                                  2017-05-11
                                                99572.44
                                                            14579003
                                                                          7302585
## 279118: 17619337 2016-10-22
                                  2016-09-22
                                                99475.44
                                                            14755451
                                                                          7302585
           paid_amount transaction_date
##
              99150.43
                              2016-07-01
        1:
##
                              2016-08-08
        2:
              99220.42
##
        3:
              99148.07
                              2016-08-03
##
        4:
              99154.67
                              2016-07-15
##
              99148.07
                              2016-08-03
        5:
## 279114:
                                    <NA>
                    NA
## 279115:
                    NA
                                    <NA>
## 279116:
                    NA
                                    <NA>
## 279117:
                                    <NA>
                    NΔ
## 279118:
              99148.84
                              2017-07-20
bills_payments_discounts = merge(bills_with_payments, discounts, by.x = "discount_id", by.y = "id", all
bills_payments_discounts
##
           discount_id
                              id
                                   due_date invoice_date tot_amount customer_id
##
                        7639057 2017-05-27
                                               2017-04-27
                                                            99475.01
        1:
                    NA
                                                                         13853808
##
        2:
                    NA
                         7708050 2017-02-21
                                               2017-01-22
                                                            99475.01
                                                                         13853808
##
                         7772589 2017-01-28
        3:
                    NΑ
                                               2016-12-29
                                                            99475.01
                                                                         13853808
##
        4:
                    NΑ
                        7833213 2017-08-07
                                               2017-06-08
                                                            99475.01
                                                                         13853808
                        7944439 2016-10-21
##
        5:
                    NA
                                               2016-09-21
                                                            99475.01
                                                                         13853808
##
## 279114:
               9077537 17320780 2016-01-22
                                               2015-12-23
                                                            99476.66
                                                                         15447467
               9077537 17320789 2017-05-07
## 279115:
                                               2017-05-07
                                                            99477.77
                                                                         15447467
## 279116:
               9094345 17313859 2017-01-17
                                               2017-01-17
                                                            99490.42
                                                                         15506929
## 279117:
               9094345 17315622 2016-08-11
                                                            99501.66
                                               2016-07-12
                                                                         15509141
## 279118:
               9094345 17323140 2014-09-03
                                               2014-08-04
                                                            99504.91
                                                                         15506929
##
           paid_amount transaction_date num_days pct_off days_until_discount
##
                    NA
                                    <NA>
                                                NA
                                                        NA
        1:
##
                                    <NA>
                                                NΑ
                                                        NΑ
                                                                             NΑ
        2:
                    NA
##
                                    <NA>
        3:
                    NA
                                                NA
                                                        NA
                                                                             NA
##
        4:
                    NA
                                    <NA>
                                                NA
                                                        NA
                                                                             NΑ
##
        5:
                    NA
                                    <NA>
                                                NA
                                                        NA
                                                                             NA
##
```

NA

## 6: 6791759

## 279114:

## 279115:

NA NA

31

1

45

45

0

0

NA

NA

<NA>

<NA>

```
## 279116:
               99175.09
                                2017-06-26
                                                 365
                                                           NA
                                                                                 NA
## 279117:
               99194.80
                                2017-06-28
                                                 365
                                                           NΑ
                                                                                 NΑ
## 279118:
                     NΑ
                                      <NA>
                                                 365
                                                           NA
                                                                                 NA
```

Now create the response metric "paid\_in\_full" and create the design matrix by ensuring the unit is bill. How should you featurize? Should you create some features? What type(s) should they be?

```
bills_data = bills_payments_discounts %>%
  group_by(id) %>%
  summarise(total_paid_amount = sum(paid_amount), customer_id = first(customer_id), discount_id = first
  mutate(total_paid_amount = ifelse(is.na(total_paid_amount), 0, total_paid_amount), paid_in_full = ife
table(bills_data*paid_in_full, useNA = "always")
```

```
## 0 1 <NA>
## 199061 27373 0
```

Fit a tree to this data. Try to use YARF if you have it. If not, use the package rpart. Below is a guide to installing YARF and ensuring it works.

First, ensure you have the Java JDK installed. The JDK is NOT the JRE. The former allows you to compile Java programs and the latter allows you only to run Java programs. Then insure that rJava is installed and working. In other words, the following should work and give the same output from practice lecture 12. If it doesn't, try the code that is commented out to reinstall. Google errors. Frustration in libraries and platforms not working on your computer is unfortunately part of computer science and thus part of data science.

```
options(java.parameters = "-Xmx4000m")
pacman::p_load(rJava)
#if that doesn't work, use:
# install.packages("rJava", type = "source")
# library(rJava)
.jinit() #this initializes the JVM in the background and if this runs with no issues nor output, you pr
java_double = .jnew("java/lang/Double", 3.1415)
java_double
## [1] "Java-Object{3.1415}"
class(java_double)
## [1] "jobjRef"
## attr(,"package")
## [1] "rJava"
.jclass(java_double)
## [1] "java.lang.Double"
#call an instance method
.jcall(java_double, "I", "intValue") #java_double.intValue();
## [1] 3
#call a static method
J("java/lang/String", "valueOf", java_double) #String.valueOf(java_double);
## [1] "3.1415"
#J("java/lang/String", "valueOf", x) #some sort of alphanumeric code for the pointer address
```

It is important to have rJava working on your computer as a fair number of R packages really do make use of it. It's a good thing to have in your toolbox in general.

Now ensure that YARF is installed properly:

```
# pacman::p_install_gh("kapelner/YARF/YARFJARs", ref = "dev")
# pacman::p_install_gh("kapelner/YARF/YARF", ref = "dev")
pacman::p_load(YARF)
```

If that printed out "YARF can now make use of [n] cores", you are in business.

Now create a training-test split and make the tree model and provide oos performance metrics: create a confusion table and compute FDR and FOR.

```
prop test = 0.20
test_indices = sample(1 : 10000, round((prop_test) * 6000))
bills_data_test = bills_data[test_indices, ]
y_test = bills_data_test$paid_in_full
X_test = bills_data_test
bills data test$paid in full = NULL
train_indices = setdiff(1 : 6000, test_indices)
bills_data_train = bills_data[train_indices, ]
y_train = bills_data_train$paid_in_full
X_train = bills_data_train
X_train$paid_in_full = NULL
n_train = nrow(X_train)
tree_model = YARFCART(X_train, y_train)
## YARF initializing with a fixed 1 trees...
## YARF after data preprocessed... 6 total features...
## Beginning YARF regression model construction...done.
## Calculating OOB error...done.
y_hat_train = predict(tree_model, X_train)
y_hat_test = predict(tree_model, X_test)
## Warning in predict.YARF(tree model, X test): Prediction set column names did not match training set
## Attempting to subset to training set columns.
oos_confusion_table = table(y_test, y_hat_test)
oos confusion table
##
         y_hat_test
## y_test
           0
##
       0 1190
                  0
FDR = oos_confusion_table[1,2] / sum(oos_confusion_table[, 2])
FDR
## [1] 0
FOR = oos_confusion_table[2,1] / sum(oos_confusion_table[, 1])
```

## ## [1] 0

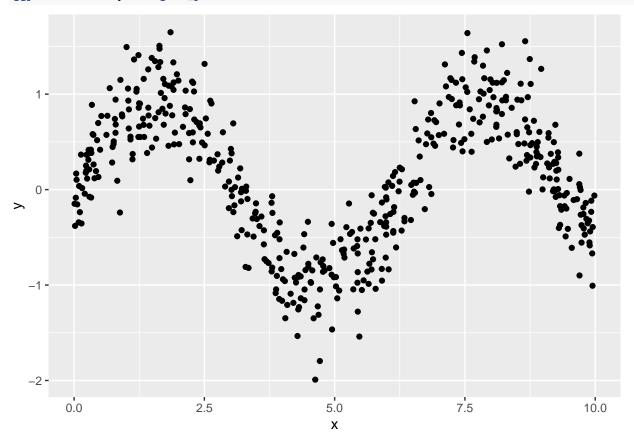
We are done with this unit.

Let's take a look at the simulated sine curve data from practice lecture 12. Below is the code for the data generating process:

```
rm(list = ls())
n = 500
sigma = 0.3
x_min = 0
x_max = 10
x = runif(n, x_min, x_max)
f_x = function(x){sin(x)}
y = f_x(x) + rnorm(n, 0, sigma)
```

Plot an example dataset of size 500:

```
ggplot(, aes(x,y)) + geom_point()
```



Locate the optimal node size hyperparameter for the regression tree model.

```
Nsim = 10
n_test = .25 * n
n_train = n - n_test
training_gs = list()
all_residuals = matrix(NA, nrow = Nsim, ncol = n_test)
for (nsim in 1 : Nsim){
    x_train = runif(n_train, x_min, x_max)
```

```
delta_train = rnorm(n_train, 0, sigma)
  y_train = sin(x_train) + delta_train
  g_model = YARFCART(data.frame(x = x_train), y_train,
                     bootstrap_indices = 1 : n_train, calculate_oob_error = FALSE)
  training_gs[[nsim]] = g_model
  x_test = runif(n_test, x_min, x_max)
  delta_test = rnorm(n_test, 0, sigma)
  y_test = sin(x_test) + delta_test
  y_hat_test = predict(g_model, data.frame(x = x_test))
  all_residuals[nsim, ] = y_test - y_hat_test
## YARF initializing with a fixed 1 trees...
## YARF after data preprocessed... 1 total features...
## Beginning YARF regression model construction...done.
## YARF initializing with a fixed 1 trees...
## YARF after data preprocessed... 1 total features...
## Beginning YARF regression model construction...done.
## YARF initializing with a fixed 1 trees...
## YARF after data preprocessed... 1 total features...
## Beginning YARF regression model construction...done.
## YARF initializing with a fixed 1 trees...
## YARF after data preprocessed... 1 total features...
## Beginning YARF regression model construction...done.
## YARF initializing with a fixed 1 trees...
## YARF after data preprocessed... 1 total features...
## Beginning YARF regression model construction...done.
## YARF initializing with a fixed 1 trees...
## YARF after data preprocessed... 1 total features...
## Beginning YARF regression model construction...done.
## YARF initializing with a fixed 1 trees...
## YARF after data preprocessed... 1 total features...
## Beginning YARF regression model construction...done.
## YARF initializing with a fixed 1 trees...
## YARF after data preprocessed... 1 total features...
## Beginning YARF regression model construction...done.
## YARF initializing with a fixed 1 trees...
## YARF after data preprocessed... 1 total features...
## Beginning YARF regression model construction...done.
## YARF initializing with a fixed 1 trees...
## YARF after data preprocessed... 1 total features...
## Beginning YARF regression model construction...done.
training_gs
## [[1]]
## YARF v1.0 for regression
## Missing data feature ON.
## 1 trees, training data n = 375 and p = 1
## Model construction completed within 0 minutes.
## Run the 'YARF_update_with_oob_results' function to get out of sample
## performance estimates using the out of bag predictions.
```

```
##
## [[2]]
## YARF v1.0 for regression
## Missing data feature ON.
## 1 trees, training data n = 375 and p = 1
## Model construction completed within 0 minutes.
## Run the 'YARF update with oob results' function to get out of sample
## performance estimates using the out of bag predictions.
##
## [[3]]
## YARF v1.0 for regression
## Missing data feature ON.
## 1 trees, training data n = 375 and p = 1
## Model construction completed within 0 minutes.
## Run the 'YARF_update_with_oob_results' function to get out of sample
## performance estimates using the out of bag predictions.
##
## [[4]]
## YARF v1.0 for regression
## Missing data feature ON.
## 1 trees, training data n = 375 and p = 1
## Model construction completed within 0 minutes.
## Run the 'YARF_update_with_oob_results' function to get out of sample
## performance estimates using the out of bag predictions.
##
## [[5]]
## YARF v1.0 for regression
## Missing data feature ON.
## 1 trees, training data n = 375 and p = 1
## Model construction completed within 0 minutes.
## Run the 'YARF_update_with_oob_results' function to get out of sample
## performance estimates using the out of bag predictions.
##
## [[6]]
## YARF v1.0 for regression
## Missing data feature ON.
## 1 trees, training data n = 375 and p = 1
## Model construction completed within 0 minutes.
## Run the 'YARF_update_with_oob_results' function to get out of sample
## performance estimates using the out of bag predictions.
## [[7]]
## YARF v1.0 for regression
## Missing data feature ON.
## 1 trees, training data n = 375 and p = 1
## Model construction completed within 0 minutes.
## Run the 'YARF_update_with_oob_results' function to get out of sample
## performance estimates using the out of bag predictions.
##
## [[8]]
## YARF v1.0 for regression
## Missing data feature ON.
## 1 trees, training data n = 375 and p = 1
## Model construction completed within 0 minutes.
```

```
## Run the 'YARF_update_with_oob_results' function to get out of sample
## performance estimates using the out of bag predictions.
##
## [[9]]
## YARF v1.0 for regression
## Missing data feature ON.
## 1 trees, training data n = 375 and p = 1
## Model construction completed within 0 minutes.
## Run the 'YARF_update_with_oob_results' function to get out of sample
## performance estimates using the out of bag predictions.
##
## [[10]]
## YARF v1.0 for regression
## Missing data feature ON.
## 1 trees, training data n = 375 and p = 1
## Model construction completed within 0 minutes.
## Run the 'YARF_update_with_oob_results' function to get out of sample
## performance estimates using the out of bag predictions.
```

Plot the regression tree model with the optimal node size.

#### #T0-D0

Provide the bias-variance decomposition of this DGP fit with this model. It is a lot of code, but it is in the practice lectures.

```
#TO-DO
```

Load the boston housing data. Leave 25% of the observations oos for honest validation.

```
library(MASS)
```

##

```
##
## Attaching package: 'MASS'
## The following object is masked from 'package:dplyr':
##
## select
data(Boston)
Boston = Boston[sample(1:nrow(Boston)), ]
Boston_train = Boston[1 : 380, ]
Boston_test = Boston[381 : nrow(Boston), ]
```

Fit a linear model with all first-order interactions and provide std err of residuals in the test set.

```
mod = lm(medv ~ .*., Boston_train)
mod

##
## Call:
## lm(formula = medv ~ . * ., data = Boston_train)
```

```
## Coefficients:
##
     (Intercept)
                          crim
                                                       indus
                                                                      chas
                                           zn
     -1.570e+02
                  -2.738e+01
                                  -1.290e-01
                                                 -2.630e+00
                                                                 1.658e+01
##
                                                        dis
##
                           rm
                                          age
                                                                       rad
            nox
                                                                 1.833e+00
                     2.596e+01
##
      4.038e+01
                                  1.191e+00
                                                 -4.082e+00
                       ptratio
##
            tax
                                       black
                                                      lstat
                                                                   crim:zn
```

```
##
       3.611e-02
                       4.154e+00
                                       5.130e-02
                                                        1.279e+00
                                                                        3.615e-01
##
      crim:indus
                       crim:chas
                                         crim:nox
                                                          crim:rm
                                                                         crim:age
                                                        1.718e-01
##
      -1.306e-01
                       3.568e+00
                                      -1.744e+00
                                                                       -3.226e-03
##
                        crim:rad
                                                    crim:ptratio
                                                                       crim:black
        crim:dis
                                        crim:tax
##
      -1.033e-01
                      -8.672e-01
                                       4.861e-02
                                                        8.981e-01
                                                                       -4.023e-04
##
      crim:lstat
                        zn:indus
                                          zn:chas
                                                           zn:nox
                                                                            zn:rm
##
       2.979e-02
                                                                       -4.597e-03
                      -1.885e-03
                                      -8.192e-02
                                                        3.372e-01
##
          zn:age
                          zn:dis
                                           zn:rad
                                                           zn:tax
                                                                       zn:ptratio
##
       3.420e-05
                       4.831e-03
                                      -1.925e-03
                                                        4.458e-04
                                                                       -7.027e-03
##
        zn:black
                        zn:1stat
                                      indus:chas
                                                        indus:nox
                                                                         indus:rm
##
       1.661e-04
                      -1.340e-02
                                      -4.501e-01
                                                        3.134e+00
                                                                        3.852e-01
##
                                       indus:rad
                                                                   indus:ptratio
       indus:age
                       indus:dis
                                                        indus:tax
##
      -1.870e-03
                      -8.920e-02
                                      -1.011e-02
                                                        6.415e-04
                                                                       -7.946e-02
##
     indus:black
                     indus:1stat
                                         chas:nox
                                                          chas:rm
                                                                         chas:age
                       5.470e-03
##
       9.587e-04
                                      -2.231e+01
                                                       -5.412e+00
                                                                        2.786e-02
##
        chas:dis
                                         chas:tax
                                                     chas:ptratio
                                                                       chas:black
                        chas:rad
##
       2.518e+00
                      -8.986e-01
                                       4.659e-02
                                                       -7.194e-01
                                                                        7.492e-02
##
      chas:1stat
                                                          nox:dis
                          nox:rm
                                          nox:age
                                                                          nox:rad
##
      -2.674e-01
                       8.732e+00
                                      -1.054e+00
                                                        1.361e+00
                                                                       -3.728e-01
##
         nox:tax
                     nox:ptratio
                                       nox:black
                                                        nox:1stat
                                                                           rm:age
##
       1.081e-02
                      -4.372e+00
                                      -4.293e-02
                                                        1.769e+00
                                                                       -3.900e-02
##
          rm:dis
                          rm:rad
                                           rm:tax
                                                       rm:ptratio
                                                                         rm:black
##
       5.990e-01
                                                       -6.662e-01
                                                                       -9.890e-03
                      -1.441e-01
                                      -2.097e-02
##
        rm:lstat
                         age:dis
                                          age:rad
                                                          age:tax
                                                                      age:ptratio
##
      -2.614e-01
                      -2.948e-02
                                       1.916e-02
                                                       -4.690e-04
                                                                       -5.595e-03
##
       age:black
                       age:1stat
                                         dis:rad
                                                          dis:tax
                                                                      dis:ptratio
##
      -4.230e-04
                      -4.240e-03
                                      -8.042e-03
                                                       -3.818e-03
                                                                       -4.446e-02
##
       dis:black
                       dis:1stat
                                          rad:tax
                                                     rad:ptratio
                                                                        rad:black
##
       1.481e-03
                       2.045e-01
                                      -6.523e-05
                                                      -6.302e-02
                                                                        5.952e-04
##
       rad:1stat
                     tax:ptratio
                                       tax:black
                                                        tax:1stat
                                                                   ptratio:black
##
      -3.440e-02
                       6.086e-03
                                       4.874e-06
                                                       -1.224e-03
                                                                        3.392e-03
##
   ptratio:lstat
                     black:1stat
##
      -1.581e-02
                      -9.859e-04
yhat = predict(mod, Boston_test)
sd(Boston_test$medv - yhat)
```

## ## [1] 3.338034

Bag this algorithm with M=1000 and provide std err of residuals in the test set.

```
colnames (Boston) # last we need set as the y
                                                dont encud
                   "zn"
                             "indus"
                                       "chas"
                                                            "rm"
                                                                       "age"
##
    [1] "crim"
                                                  "nox"
##
    [8] "dis"
                   "rad"
                             "tax"
                                       "ptratio" "black"
                                                            "lstat"
                                                                       "medv"
X = Boston_train
X$medv = NULL
y = Boston_train$medv
X_test = Boston_test
X_test$medv = NULL
M = 10 #I changed this because it talking way too long and keps on crashing on my computer
training gs = list()
for (m in 1:M) {
  bag_model = YARFBAG(X,y)
  y_hat_oos = predict(bag_model, Boston_test)
```

```
training_gs[[m]] = bag_model
}
## YARF initializing with a fixed 500 trees...
## YARF after data preprocessed... 13 total features...
## Beginning YARF regression model construction...done.
## Calculating OOB error...done.
## Warning in predict.YARF(bag_model, Boston_test): Prediction set column names did not match training
## Attempting to subset to training set columns.
## YARF initializing with a fixed 500 trees...
## YARF after data preprocessed... 13 total features...
## Beginning YARF regression model construction...done.
## Calculating OOB error...done.
## Warning in predict.YARF(bag_model, Boston_test): Prediction set column names did not match training
## Attempting to subset to training set columns.
## YARF initializing with a fixed 500 trees...
## YARF after data preprocessed... 13 total features...
## Beginning YARF regression model construction...done.
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## Calculating OOB error...done.
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## YARF after data preprocessed... 13 total features...
## Beginning YARF regression model construction...done.
## Calculating OOB error...done.
## Warning in predict.YARF(bag_model, Boston_test): Prediction set column names did not match training
## Attempting to subset to training set columns.
## YARF initializing with a fixed 500 trees...
## YARF after data preprocessed... 13 total features...
## Beginning YARF regression model construction...done.
## Calculating OOB error...done.
## Warning in predict.YARF(bag_model, Boston_test): Prediction set column names did not match training
## Attempting to subset to training set columns.
## YARF initializing with a fixed 500 trees...
## YARF after data preprocessed... 13 total features...
## Beginning YARF regression model construction...done.
## Calculating OOB error...done.
## Warning in predict.YARF(bag_model, Boston_test): Prediction set column names did not match training
## Attempting to subset to training set columns.
## YARF initializing with a fixed 500 trees...
## YARF after data preprocessed... 13 total features...
```

```
## Beginning YARF regression model construction...done.
## Calculating OOB error...done.
## Warning in predict.YARF(bag_model, Boston_test): Prediction set column names did not match training
## Attempting to subset to training set columns.
## YARF initializing with a fixed 500 trees...
## YARF after data preprocessed... 13 total features...
## Beginning YARF regression model construction...done.
## Calculating OOB error...done.
## Warning in predict.YARF(bag_model, Boston_test): Prediction set column names did not match training
## Attempting to subset to training set columns.
## YARF initializing with a fixed 500 trees...
## YARF after data preprocessed... 13 total features...
## Beginning YARF regression model construction...done.
## Calculating OOB error...done.
## Warning in predict.YARF(bag_model, Boston_test): Prediction set column names did not match training
## Attempting to subset to training set columns.
training_gs
## [[1]]
## YARF v1.0 for regression
## Missing data feature ON.
## 500 trees, training data n = 380 and p = 13
## Model construction completed within 0.2 minutes.
## 00B results on all observations:
##
    R^2: 0.86806
##
    RMSE: 3.438
##
    MAE: 2.337
##
    L2: 4490.83
##
    L1: 887.91
##
## [[2]]
## YARF v1.0 for regression
## Missing data feature ON.
## 500 trees, training data n = 380 and p = 13
## Model construction completed within 0.19 minutes.
## 00B results on all observations:
    R^2: 0.8713
    RMSE: 3.395
##
##
    MAE: 2.299
    L2: 4380.42
##
##
    L1: 873.59
##
## [[3]]
## YARF v1.0 for regression
## Missing data feature ON.
## 500 trees, training data n = 380 and p = 13
## Model construction completed within 0.19 minutes.
## 00B results on all observations:
    R^2: 0.87144
##
##
    RMSE: 3.393
    MAE: 2.323
##
```

```
L2: 4375.79
##
    L1: 882.88
##
##
## [[4]]
## YARF v1.0 for regression
## Missing data feature ON.
## 500 trees, training data n = 380 and p = 13
## Model construction completed within 0.19 minutes.
## 00B results on all observations:
    R^2: 0.8683
##
##
     RMSE: 3.435
##
    MAE: 2.334
    L2: 4482.49
##
##
    L1: 886.88
##
## [[5]]
## YARF v1.0 for regression
## Missing data feature ON.
## 500 trees, training data n = 380 and p = 13
## Model construction completed within 0.19 minutes.
## 00B results on all observations:
##
    R^2: 0.87155
##
    RMSE: 3.392
##
    MAE: 2.324
##
   L2: 4371.79
##
    L1: 883.08
##
## [[6]]
## YARF v1.0 for regression
## Missing data feature ON.
## 500 trees, training data n = 380 and p = 13
## Model construction completed within 0.19 minutes.
## 00B results on all observations:
    R^2: 0.87027
##
    RMSE: 3.409
##
    MAE: 2.325
##
   L2: 4415.53
##
##
    L1: 883.55
##
## [[7]]
## YARF v1.0 for regression
## Missing data feature ON.
## 500 trees, training data n = 380 and p = 13
## Model construction completed within 0.2 minutes.
## 00B results on all observations:
    R^2: 0.86523
##
##
    RMSE: 3.474
##
    MAE: 2.362
    L2: 4587.13
##
##
    L1: 897.6
##
## [[8]]
## YARF v1.0 for regression
## Missing data feature ON.
```

```
## 500 trees, training data n = 380 and p = 13
## Model construction completed within 0.19 minutes.
## 00B results on all observations:
##
     R^2: 0.86971
##
     RMSE: 3.416
##
    MAE: 2.342
    L2: 4434.56
     L1: 890
##
##
## [[9]]
## YARF v1.0 for regression
## Missing data feature ON.
## 500 trees, training data n = 380 and p = 13
## Model construction completed within 0.19 minutes.
## 00B results on all observations:
##
     R^2: 0.87424
##
     RMSE: 3.356
##
     MAE: 2.298
##
    L2: 4280.33
##
    L1: 873.31
##
## [[10]]
## YARF v1.0 for regression
## Missing data feature ON.
## 500 trees, training data n = 380 and p = 13
## Model construction completed within 0.21 minutes.
## 00B results on all observations:
##
     R^2: 0.86772
     RMSE: 3.442
##
    MAE: 2.35
##
     L2: 4502.42
##
##
     L1: 893.11
```

What is your gain over the unbagged model? Why is there a gain?

The gain come from reducing the variance. The gain comes from randomly sampling the data into pieces and then training on each. There is also free validation that is provided. The model return a  $R^2$  of 86% and a RSME of 3.394