D212 Data Mining II Task 2

AUTHOR

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Part I: Research Question

- **A1.** I want to use principal component analysis (PCA) to successfully identify the principal components in the churn dataset that contribute the most amount of variance.
- **A2.** My goal is to apply PCA to the churn dataset in order to reduce the dimensionality and to understand the variance explained by each principal component.

Part II: Method Justification

- **B1.** PCA analyzes the data by reducing the features into a smaller set of 'principal components' that are ordered by the variance they explain. PCA helps to reduce the dimensionality while maintaining as much variance or patterns as possible while simplifying the dataset (*Lever et al., 2017*). It does this by calculating the covariance between variables before comparing the covariance between different variables in the data.
- **B2.** One of the major assumptions of PCA is that the data is continuous numerical data (*Thaddeus, 2019*). This is because PCA relies on calculating the covariance between variables and categorical variables do not have a numerical distance.

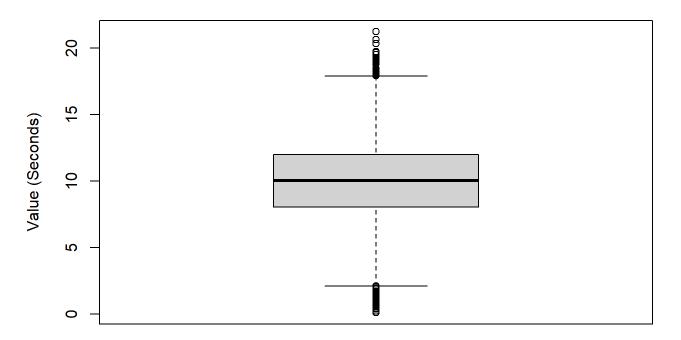
Part III: Data Preparation

C1. The continuous variables I will be using are listed below:

As mentioned above, it is important that the variables are continuous. I've included Age in the variables I'll be using because a person's age is continuous, but here in the dataset it is recorded as a discrete variable.

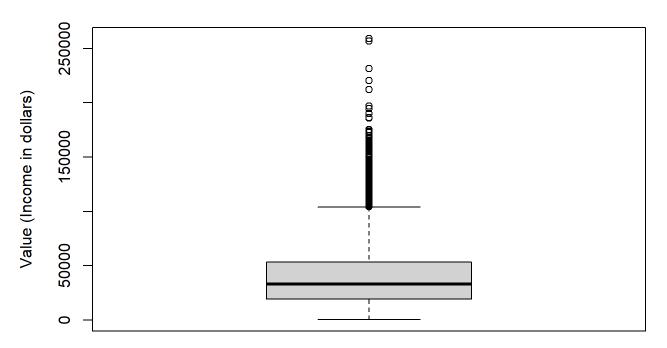
I checked for outliers in all the variables listed above and found outliers in <code>Outage_sec_perweek</code>, and <code>Income.Outage_sec_perweek</code> only had 43 values that were outliers and they did not appear to be so extreme that they needed to be removed and therefore they were retained.

Outage_sec_perweek boxplot with outliers



Income had more 'significant' outliers.

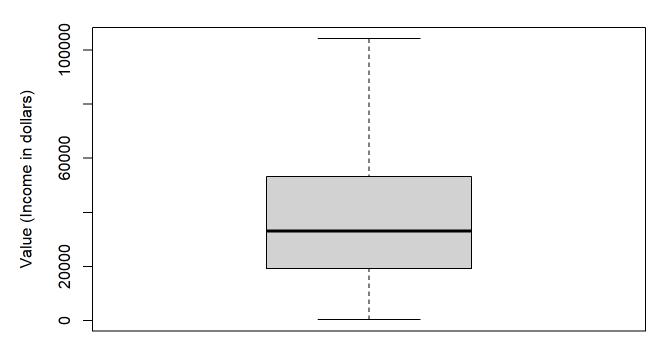
Boxplot of Income with outliers



I chose to cap the income values at the value of the upper whisker using the pmin() function. The mean of income is \$39,806.93 and the Max is \$258,900.70 so imputing the mean would distort the actual incomes so much that this data would not be able to be used accurately in some of the clustering models. Removing the outliers was another option since there were only 336 outliers in the 10,000 row dataset. However, removing these rows excludes the high earning customers from any clustering or regression analysis. Because of this, I chose to just cap the highest earning incomes at the value of the upper whisker, \$104,166.70

Income after using pmin()

Boxplot of Income with outliers capped



C2. The cleaned CSV file will be included in the submission files and will be named 'churn_cleaned_data.csv'. The dataset was scaled and saved as a data frame called 'scaled_churn'.

```
# Standardize the variables into a new dataframe
scaled_churn <- as.data.frame(scale(churn))
head(scaled_churn)</pre>
```

```
Age
                  Income Outage_sec_perweek
                                                Tenure MonthlyCharge
1 0.7208892 -0.40829732
                                 -0.6799436 -1.0486938 -0.003942362
2 -1.2598942 -0.67648638
                                  0.5703026 -1.2619381
                                                         1.630244379
3 -0.1487230 -1.14953527
                                  0.2523344 -0.7099043 -0.295210056
4 -0.2453466 -0.78519548
                                  1.6504233 -0.6594910 -1.226459744
5 1.4455660 0.04195017
                                 -0.6231249 -1.2424891 -0.528059300
6 1.4455660 -0.63911907
                                 -0.5311979 -1.0409231
                                                         0.288355463
  Bandwidth_GB_Year
1
         -1.1384301
2
         -1.1858165
3
         -0.6121071
4
         -0.5618291
5
         -1.4281131
         -1.0767351
```

D1. In PC1 the greatest contributors are Tenure and Bandwidth_GB_Year. PC2's greatest contributors are Outage_sec_perweek and MonthlyCharge. PC3's single greatest contributor is Age. The first two principal components explain 50.31% of variance and 67.08 for the first three components.

```
#Loading Matrix
print(pca$rotation)
```

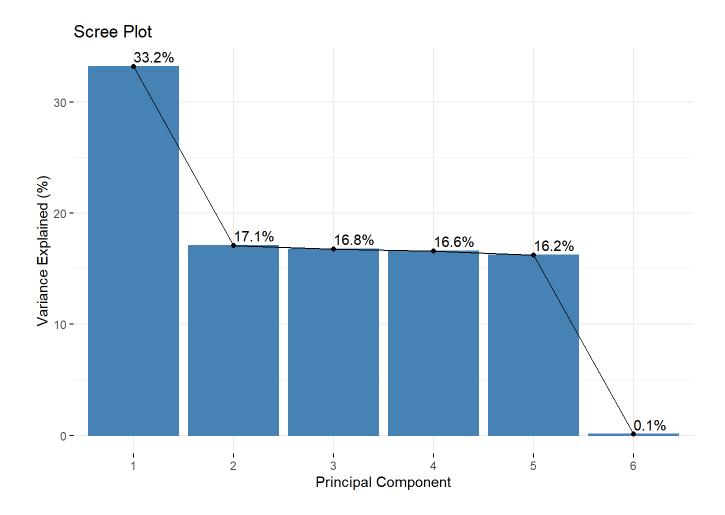
```
PC1
                              PC2
                                        PC3
                                                   PC4
              -0.001973296 -0.090901771 0.899913648
                                            0.0046938480
Age
Income
              Outage_sec_perweek -0.005870177 -0.641660666 -0.374029108 0.1536067997
Tenure
              MonthlyCharge
              -0.040773650 -0.643846956 0.219981478 0.4096718024
Bandwidth_GB_Year
              PC5
                              PC6
               0.42583671 -0.0230101507
Age
Income
               0.16318990 0.0012460947
Outage_sec_perweek   0.65172407 -0.0002254553
Tenure
               0.04044808 0.7055413805
MonthlyCharge
              -0.60456450 0.0455799257
Bandwidth GB Year
              -0.01239395 -0.7068258344
```

```
# Summary and loadings
summary(pca)
```

Importance of components:

```
PC1 PC2 PC3 PC4 PC5 PC6 Standard deviation 1.4118 1.0127 1.0032 0.9978 0.9866 0.07701 Proportion of Variance 0.3322 0.1709 0.1677 0.1659 0.1622 0.00099 Cumulative Proportion 0.3322 0.5031 0.6708 0.8368 0.9990 1.00000
```

D2. Initially I opted to use the elbow method with a scree plot. The elbow below shows that the cutoff should be at 2 principal components accounting for 50.31% of the variance.



The kaiser method suggested that the first three Principal Components are kept due to the these having an eigenvalue above 1 (*Statistics Easily 2023*). Retaining the first three principal components results in a model that accounts for 67.08% of the variance. Therefore I will be using the kaiser method for the remainder of this analysis.

Scree Plot (Kaiser Method) 2.0 - 2 1.5 - 1.0 - 1.5 - 1.0 - 1.5 - 1.0 - 1.5 - 1.0 - 1.5 - 1.0 - 1.5 - 1.0 - 1.5 - 1.0 - 1.5 - 1.0 - 1.5 - 1.0 - 1.5 - 1.0 - 1.5 - 1.0 - 1.5 - 1.0 - 1.5 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 - 1.0 -

Eigenvalues: 1.993176 1.025507 1.006355 0.9956913 0.9733402 0.005930071

3

Principal Component

5

Number of components to keep: 3

0.0 -

 PC1
 PC2
 PC3

 Age
 -0.001973296
 -0.090901771
 0.899913648

 Income
 -0.001212034
 0.404812205
 -0.040989021

 Outage_sec_perweek
 -0.005870177
 -0.641660666
 -0.374029108

 Tenure
 -0.705863063
 0.039898143
 0.001524399

 MonthlyCharge
 -0.040773650
 -0.643846956
 0.219981478

 Bandwidth_GB_Year
 -0.707145688
 0.002184496
 -0.013541712

2

D3. PC1 explains 33.22% of variance. PC2 explains 17.09% of variance. And PC3 explains 16.77% of variance.

[1] 0.3321961 0.1709179 0.1677258

D4. The first three principal components, recomended by the kaiser method, capture a total explained variance (*cumulative proportion*) of 67.08% or 0.6708397.

PC1 PC2 PC3
Standard deviation 1.411799 1.012673 1.003172
Proportion of Variance 0.332200 0.170920 0.167730
Cumulative Proportion 0.332200 0.503110 0.670840

5. This PCA analysis reduced the original six principal components to three components while maintaining 67.08% of the original variance. PC1 is mainly influenced by Tenure and Bandwidth_GB_Year, PC2 by Outage_sec_perweek and MonthlyCharge, and PC3 by Age. While the elbow method suggested keeping two components, accounting for 50.31% of variance, the Kaiser method recommended three components with eigenvalues above 1. Therefore the Kaiser method was chosen for its high explained variance and better representation of the data.

Part V: Attachments

E-F. Sources:

Lever, J., Krzywinski, M., & Altman, N. (2017). *Principal component analysis*. *Nature Methods, 14*(7), 641-642. https://www.nature.com/articles/nmeth.4346

Statistics Easily. (2023). What is Kaiser criterion? Detailed explanation. https://statisticseasily.com/glossario/what-is-kaiser-criterion-detailed-explanation/

Thaddeus. (2019, August 31). When to use principal component analysis. Crunching the Data. https://www.crunchingnumbers.live/2019/08/31/when-to-use-principal-component-analysis/