# Week 3 CS-312 Homework

October 22, 2020

## 1 Problem 3.1

## 1.1 Question

Give an NFA for the language of RE  $a^*b + b^*a$ 

### 1.2 Answer

### 2 Problem 3.6

### 2.1 Question

Show how to modify an NFA to have a unique accept state with no transition ending at the start state and no transition starting at the accept state.

#### 2.2 Answer

#### 3 Problem 3.7

## 3.1 Question

If M is a DFA accepting language B, then exchanging the accept and reject states gives a new DFA accepting teh complement of B. Does this work for an NFA? Discuss.

#### 3.2 Answer

## 4 Problem 3.9

#### 4.1 Question

For the following NFA, use the subset construction to produce an equivalent DFA.

#### 4.2 Answer

## 5 Problem 3.11

### 5.1 Question

Provide an algorithm to tell if the language is infinite if the input is

#### 5.1.1 An RE

#### 5.1.2 An NFA

#### 6 Problem 4.1

#### 6.1 Question

Show that the set of regular languages is closed under reversal. That is, if L is regular, then so is  $\{x^R : x \in L\}$  where  $x^R$  denotes the reversal of string x.

#### 6.2 Answer

### 7 Problem 4.11

### 7.1 Question

Show taht  $\{x\#x:x\in\{0,1\}^*\}$  is nonregular. (The hash mark/pound sign is a special symbol that should only occur in the middle of the input string.)

#### 7.2 Answer

## 8 Problem 4.13b

#### 8.1 Question

State whether the set of binary nonpalindromes is regular or not. If not, give a proof that it is nonregular.

#### 8.2 Answer

#### 9 Problem 4.14

#### 9.1 Question

Explain what is wrong with the following "proof" that the language L of an RE  $a^*b^*$  is nonregular.

Suppose L were regular. Then it would be accepted by a DFA with, say, k states. Consider the string  $z = 0^k 1^k$ . Split z = uvw with v = 01. Then  $uv^2w$  is not in L. This is a contradiction of the Pumping Lemma, and so our supposition is false.

## 9.2 Answer

# 10 Problem 4.20

## 10.1 Question

Convince your grandmother that there is no FA that accepts the language of binary strings with an equal number of 0's and 1's.

## 10.2 Answer