Part 1: k-Nearest-Neighbour Classifier

| n_neighbors=3   |
|-----------------|
| [0 1 1 1 2 0 2] |
| n_neighbors=7   |
| [0 1 1 2 2 0 2] |

## Part 2: Discriminant Functions

 $b^{t}_{k} = [1, 9, 0, 5, 6, 6]$ 

| x <sup>t</sup> | y <sup>t</sup> |
|----------------|----------------|
| (0, 2)         | (1, 0, 2)      |
| (1, 2)         | (1, 1, 2)      |
| (2, 1)         | (1, 2, 1)      |
| (-3, 1)        | (-1, 3, -1)    |
| (-2, -1)       | (-1, 2, 1)     |
| (-3, -2)       | (-1, 3, 2)     |

|    | a <sup>t</sup>            | <b>y</b> <sup>t</sup> <sub>k</sub> | a <sup>t</sup> y <sub>k</sub> | $a^{t}_{new} = a^{t} + 0.1(b_{k} - a^{t}y_{k}) y^{t}_{k}$ |
|----|---------------------------|------------------------------------|-------------------------------|---|
| 1  | [1, 0, 0]                 | [1, 0, 2]                          | 1                             | [1, 0, 0] + 0.1(1-1) [1, 0, 2] = [1, 0, 0]                |
| 2  | [1, 0, 0]                 | [1, 1, 2]                          | 1                             | [1, 0, 0] + 0.1(9-1) [1, 1, 2] = [1.8, 0.8, 1.6]          |
| 3  | [1.8, 0.8, 1.6]           | [1, 2, 1]                          | 5                             | [1.8, 0.8, 1.6] + 0.1(0-5) [1, 2, 1] = [1.3, -0.2, 1.1]   |
| 4  | [1.3, -0.2, 1.1]          | [-1, 3, -1]                        | -3                            | [1.3, -0.2, 1.1] + 0.1(5+3) [-1, 3, -1] = [0.5, 2.2, 0.3] |
| 5  | [0.5, 2.2, 0.3]           | [-1, 2, 1]                         | 4.2                           | [0.5, 2.2, 0.3]+ 0.1(6-4.2) [-1, 2, 1]                    |
|    |                           |                                    |                               | = [0.32, 2.56, 0.48]                                      |
| 6  | [0.32, 2.56, 0.48]        | [-1, 3, 2]                         | 8.32                          | [0.32, 2.56, 0.48] + 0.1(6-8.32) [-1, 3, 2]               |
|    |                           |                                    |                               | = [0.552, 1.864, 0.016]                                   |
| 7  | [0.552, 1.864, 0.016]     | [1, 0, 2]                          | 0.584                         | [0.552, 1.864, 0.016] + 0.1(1-0.584) [1, 0, 2]            |
|    |                           |                                    |                               | = [0.5936, 1.864, 0.016]                                  |
| 8  | [0.5936, 1.864, 0.016]    | [1, 1, 2]                          | 2.656                         | [0.5936, 1.864, 0.016] + 0.1(9-2.656) [1, 1, 2]           |
|    |                           |                                    |                               | = [1.228, 2.4984, 1.368]                                  |
| 9  | [1.228, 2.4984, 1.368]    | [1, 2, 1]                          | 7.5928                        | [1.228, 2.4984, 1.368] + 0.1(0-7.5928) [1, 2, 1]          |
|    |                           |                                    |                               | = [0.4687, 0.9798, 0.6087]                                |
| 10 | [0.4687, 0.9798, 0.6087]  | [-1, 3, -1]                        | 1.86208                       | [0.4687, 0.9798, 0.6087]+ 0.1(5-1.86208) [-1, 3, -1]      |
|    |                           |                                    |                               | = [0.1549, 1.9212, 0.2949]                                |
| 11 | [0.1549, 1.9212, 0.2949]  | [-1, 2, 1]                         | 3.982432                      | [0.1549, 1.9212, 0.2949] + 0.1(6-3.982432) [-1, 2, 1]     |
|    |                           |                                    |                               | = [-0.0468, 2.3247, 0.4967]                               |
| 12 | [-0.0468, 2.3247, 0.4967] | [-1, 3, 2]                         | 8.014387                      | [0.7764, 2.63368, 0.30696] + 0.1(6-8.014387) [-1, 3, 2]   |
|    |                           |                                    |                               | = [0.1546, 1.7204, 0.0938]                                |

Part 3: Neural Networks

(a) Sequential Delta Learning Algorithm,  $w <- w + learning\_rate*(t-y)x^t$  Given -sida=0, w1=-5, w2=6, H(0)=0.5

| x <sup>t</sup> | t | х           |
|----------------|---|-------------|
| (0, 2)         | 1 | (1, 0, 2)   |
| (1, 2)         | 1 | (1, 1, 2)   |
| (2, 1)         | 1 | (1, 2, 1)   |
| (-3, 1)        | 0 | (1, -3, 1)  |
| (-2, -1)       | 0 | (1, -2, -1) |
| (-3, -2)       | 0 | (1, -3, -2) |

 $w_0 = [-sida, w1, w2] = [0, -5, 6]$ 

| index | W          | Х           | y = H(wx)  | t | $w_{new} = w + 1*(t-y)x^t$                |
|-------|------------|-------------|------------|---|---|
| 1     | [0, -5, 6] | [1, 0, 2]   | H(12) = 1  | 1 | [0, -5, 6]                                |
| 2     | [0, -5, 6] | [1, 1, 2]   | H(7) = 1   | 1 | [0, -5, 6]                                |
| 3     | [0, -5, 6] | [1, 2, 1]   | H(-4) = 0  | 1 | [0, -5, 6] + (1-0)*[1, 2, 1] = [1, -3, 7] |
| 4     | [1, -3, 7] | [1, -3, 1]  | H(17) = 1  | 0 | [1, -3, 7] + (0-1)*[1, -3, 1] = [0, 0, 6] |
| 5     | [0, 0, 6]  | [1, -2, -1] | H(-6) = 0  | 0 | [0, 0, 6]                                 |
| 6     | [0, 0, 6]  | [1, -3, -2] | H(-12) = 0 | 0 | [0, 0, 6]                                 |
| 7     | [0, 0, 6]  | [1, 0, 2]   | H(12) = 1  | 1 | [0, 0, 6]                                 |
| 8     | [0, 0, 6]  | [1, 1, 2]   | H(12) = 1  | 1 | [0, 0, 6]                                 |
| 9     | [0, 0, 6]  | [1, 2, 1]   | H(6) = 1   | 1 | [0, 0, 6]                                 |
| 10    | [0, 0, 6]  | [1, -3, 1]  | H(6) = 1   | 0 | [0, 0, 6] + (0-1)*[1, -3, 1] = [-1, 3, 5] |
| 11    | [-1, 3, 5] | [1, -2, -1] | H(-12) = 0 | 0 | [-1, 3, 5]                                |
| 12    | [-1, 3, 5] | [1, -3, -2] | H(-20) = 0 | 0 | [-1, 3, 5]                                |
| 13    | [-1, 3, 5] | [1, 0, 2]   | H(9) = 1   | 1 | [-1, 3, 5]                                |
| 14    | [-1, 3, 5] | [1, 1, 2]   | H(12) = 1  | 1 | [-1, 3, 5]                                |
| 15    | [-1, 3, 5] | [1, 2, 1]   | H(10) = 1  | 1 | [-1, 3, 5]                                |
| 16    | [-1, 3, 5] | [1, -3, 1]  | H(-5) = 0  | 0 | [-1, 3, 5]                                |

(b)

| index | W                               | х                         | у | t | $w_{new} = w + 1*(t-y)x^t$      |
|-------|---------------------------------|---------------------------|---|---|---------------------------------|
| 1     | [0.0, -5.0, 6.0, -6.0, 7.0]     | [1.0, 5.1, 3.5, 1.4, 0.2] | 0 | 1 | [0.1, -4.49, 6.35, -5.86, 7.02] |
| 2     | [0.1, -4.49, 6.35, -5.86, 7.02] | [1.0, 4.9, 3.0, 1.4, 0.2] | 0 | 1 | [0.2, -4.0, 6.65, -5.72, 7.04]  |
| 3     | [0.2, -4.0, 6.65, -5.72, 7.04]  | [1.0, 4.7, 3.2, 1.3, 0.2] | 0 | 1 | [0.3, -3.53, 6.97, -5.59, 7.06] |
| 4     | [0.3, -3.53, 6.97, -5.59, 7.06] | [1.0, 4.6, 3.1, 1.5, 0.2] | 0 | 1 | [0.4, -3.07, 7.28, -5.44, 7.08] |
| 5     | [0.4, -3.07, 7.28, -5.44, 7.08] | [1.0, 5.0, 3.6, 1.4, 0.2] | 1 | 1 | [0.4, -3.07, 7.28, -5.44, 7.08] |
| 6     | [0.4, -3.07, 7.28, -5.44, 7.08] | [1.0, 5.4, 3.9, 1.7, 0.4] | 1 | 1 | [0.4, -3.07, 7.28, -5.44, 7.08] |
| 7     | [0.4, -3.07, 7.28, -5.44, 7.08] | [1.0, 4.6, 3.4, 1.4, 0.3] | 1 | 1 | [0.4, -3.07, 7.28, -5.44, 7.08] |
| 8     | [0.4, -3.07, 7.28, -5.44, 7.08] | [1.0, 5.0, 3.4, 1.5, 0.2] | 1 | 1 | [0.4, -3.07, 7.28, -5.44, 7.08] |
| 9     | [0.4, -3.07, 7.28, -5.44, 7.08] | [1.0, 4.4, 2.9, 1.4, 0.2] | 1 | 1 | [0.4, -3.07, 7.28, -5.44, 7.08] |
| 10    | [0.4, -3.07, 7.28, -5.44, 7.08] | [1.0, 4.9, 3.1, 1.5, 0.1] | 1 | 1 | [0.4, -3.07, 7.28, -5.44, 7.08] |
| 11    | [0.4, -3.07, 7.28, -5.44, 7.08] | [1.0, 5.4, 3.7, 1.5, 0.2] | 1 | 1 | [0.4, -3.07, 7.28, -5.44, 7.08] |
| 12    | [0.4, -3.07, 7.28, -5.44, 7.08] | [1.0, 4.8, 3.4, 1.6, 0.2] | 1 | 1 | [0.4, -3.07, 7.28, -5.44, 7.08] |

| 13 | [0.4, -3.07, 7.28, -5.44, 7.08] | [1.0, 4.8, 3.0, 1.4, 0.1] | 1 | 1 | [0.4, -3.07, 7.28, -5.44, 7.08] |
|----|---------------------------------|---------------------------|---|---|---------------------------------|
| 14 | [0.4, -3.07, 7.28, -5.44, 7.08] | [1.0, 4.3, 3.0, 1.1, 0.1] | 1 | 1 | [0.4, -3.07, 7.28, -5.44, 7.08] |
| 15 | [0.4, -3.07, 7.28, -5.44, 7.08] | [1.0, 5.8, 4.0, 1.2, 0.2] | 1 | 1 | [0.4, -3.07, 7.28, -5.44, 7.08] |
| 16 | [0.4, -3.07, 7.28, -5.44, 7.08] | [1.0, 5.7, 4.4, 1.5, 0.4] | 1 | 1 | [0.4, -3.07, 7.28, -5.44, 7.08] |
| 17 | [0.4, -3.07, 7.28, -5.44, 7.08] | [1.0, 5.4, 3.9, 1.3, 0.4] | 1 | 1 | [0.4, -3.07, 7.28, -5.44, 7.08] |
| 18 | [0.4, -3.07, 7.28, -5.44, 7.08] | [1.0, 5.1, 3.5, 1.4, 0.3] | 1 | 1 | [0.4, -3.07, 7.28, -5.44, 7.08] |
| 19 | [0.4, -3.07, 7.28, -5.44, 7.08] | [1.0, 5.7, 3.8, 1.7, 0.3] | 1 | 1 | [0.4, -3.07, 7.28, -5.44, 7.08] |
| 20 | [0.4, -3.07, 7.28, -5.44, 7.08] | [1.0, 5.1, 3.8, 1.5, 0.3] | 1 | 1 | [0.4, -3.07, 7.28, -5.44, 7.08] |
| 21 | [0.4, -3.07, 7.28, -5.44, 7.08] | [1.0, 5.4, 3.4, 1.7, 0.2] | 1 | 1 | [0.4, -3.07, 7.28, -5.44, 7.08] |
| 22 | [0.4, -3.07, 7.28, -5.44, 7.08] | [1.0, 5.1, 3.7, 1.5, 0.4] | 1 | 1 | [0.4, -3.07, 7.28, -5.44, 7.08] |
| 23 | [0.4, -3.07, 7.28, -5.44, 7.08] | [1.0, 4.6, 3.6, 1.0, 0.2] | 1 | 1 | [0.4, -3.07, 7.28, -5.44, 7.08] |
| 24 | [0.4, -3.07, 7.28, -5.44, 7.08] | [1.0, 5.1, 3.3, 1.7, 0.5] | 1 | 1 | [0.4, -3.07, 7.28, -5.44, 7.08] |
| 25 | [0.4, -3.07, 7.28, -5.44, 7.08] | [1.0, 4.8, 3.4, 1.9, 0.2] | 1 | 1 | [0.4, -3.07, 7.28, -5.44, 7.08] |
| 26 | [0.4, -3.07, 7.28, -5.44, 7.08] | [1.0, 5.0, 3.0, 1.6, 0.2] | 0 | 1 | [0.5, -2.57, 7.58, -5.28, 7.1]  |
| 27 | [0.5, -2.57, 7.58, -5.28, 7.1]  | [1.0, 5.0, 3.4, 1.6, 0.4] | 1 | 1 | [0.5, -2.57, 7.58, -5.28, 7.1]  |
| 28 | [0.5, -2.57, 7.58, -5.28, 7.1]  | [1.0, 5.2, 3.5, 1.5, 0.2] | 1 | 1 | [0.5, -2.57, 7.58, -5.28, 7.1]  |
| 29 | [0.5, -2.57, 7.58, -5.28, 7.1]  | [1.0, 5.2, 3.4, 1.4, 0.2] | 1 | 1 | [0.5, -2.57, 7.58, -5.28, 7.1]  |
| 30 | [0.5, -2.57, 7.58, -5.28, 7.1]  | [1.0, 4.7, 3.2, 1.6, 0.2] | 1 | 1 | [0.5, -2.57, 7.58, -5.28, 7.1]  |
| 31 | [0.5, -2.57, 7.58, -5.28, 7.1]  | [1.0, 4.8, 3.1, 1.6, 0.2] | 1 | 1 | [0.5, -2.57, 7.58, -5.28, 7.1]  |
| 32 | [0.5, -2.57, 7.58, -5.28, 7.1]  | [1.0, 5.4, 3.4, 1.5, 0.4] | 1 | 1 | [0.5, -2.57, 7.58, -5.28, 7.1]  |
| 33 | [0.5, -2.57, 7.58, -5.28, 7.1]  | [1.0, 5.2, 4.1, 1.5, 0.1] | 1 | 1 | [0.5, -2.57, 7.58, -5.28, 7.1]  |
| 34 | [0.5, -2.57, 7.58, -5.28, 7.1]  | [1.0, 5.5, 4.2, 1.4, 0.2] | 1 | 1 | [0.5, -2.57, 7.58, -5.28, 7.1]  |
| 35 | [0.5, -2.57, 7.58, -5.28, 7.1]  | [1.0, 4.9, 3.1, 1.5, 0.2] | 1 | 1 | [0.5, -2.57, 7.58, -5.28, 7.1]  |
| 36 | [0.5, -2.57, 7.58, -5.28, 7.1]  | [1.0, 5.0, 3.2, 1.2, 0.2] | 1 | 1 | [0.5, -2.57, 7.58, -5.28, 7.1]  |
| 37 | [0.5, -2.57, 7.58, -5.28, 7.1]  | [1.0, 5.5, 3.5, 1.3, 0.2] | 1 | 1 | [0.5, -2.57, 7.58, -5.28, 7.1]  |
| 38 | [0.5, -2.57, 7.58, -5.28, 7.1]  | [1.0, 4.9, 3.6, 1.4, 0.1] | 1 | 1 | [0.5, -2.57, 7.58, -5.28, 7.1]  |
| 39 | [0.5, -2.57, 7.58, -5.28, 7.1]  | [1.0, 4.4, 3.0, 1.3, 0.2] | 1 | 1 | [0.5, -2.57, 7.58, -5.28, 7.1]  |
| 40 | [0.5, -2.57, 7.58, -5.28, 7.1]  | [1.0, 5.1, 3.4, 1.5, 0.2] | 1 | 1 | [0.5, -2.57, 7.58, -5.28, 7.1]  |
| 41 | [0.5, -2.57, 7.58, -5.28, 7.1]  | [1.0, 5.0, 3.5, 1.3, 0.3] | 1 | 1 | [0.5, -2.57, 7.58, -5.28, 7.1]  |
| 42 | [0.5, -2.57, 7.58, -5.28, 7.1]  | [1.0, 4.5, 2.3, 1.3, 0.3] | 1 | 1 | [0.5, -2.57, 7.58, -5.28, 7.1]  |
| 43 | [0.5, -2.57, 7.58, -5.28, 7.1]  | [1.0, 4.4, 3.2, 1.3, 0.2] | 1 | 1 | [0.5, -2.57, 7.58, -5.28, 7.1]  |
| 44 | [0.5, -2.57, 7.58, -5.28, 7.1]  | [1.0, 5.0, 3.5, 1.6, 0.6] | 1 | 1 | [0.5, -2.57, 7.58, -5.28, 7.1]  |
| 45 | [0.5, -2.57, 7.58, -5.28, 7.1]  | [1.0, 5.1, 3.8, 1.9, 0.4] | 1 | 1 | [0.5, -2.57, 7.58, -5.28, 7.1]  |
| 46 | [0.5, -2.57, 7.58, -5.28, 7.1]  | [1.0, 4.8, 3.0, 1.4, 0.3] | 1 | 1 | [0.5, -2.57, 7.58, -5.28, 7.1]  |
| 47 | [0.5, -2.57, 7.58, -5.28, 7.1]  | [1.0, 5.1, 3.8, 1.6, 0.2] | 1 | 1 | [0.5, -2.57, 7.58, -5.28, 7.1]  |
| 48 | [0.5, -2.57, 7.58, -5.28, 7.1]  | [1.0, 4.6, 3.2, 1.4, 0.2] | 1 | 1 | [0.5, -2.57, 7.58, -5.28, 7.1]  |
| 49 | [0.5, -2.57, 7.58, -5.28, 7.1]  | [1.0, 5.3, 3.7, 1.5, 0.2] | 1 | 1 | [0.5, -2.57, 7.58, -5.28, 7.1]  |
| 50 | [0.5, -2.57, 7.58, -5.28, 7.1]  | [1.0, 5.0, 3.3, 1.4, 0.2] | 1 | 1 | [0.5, -2.57, 7.58, -5.28, 7.1]  |
| 51 | [0.5, -2.57, 7.58, -5.28, 7.1]  | [1.0, 7.0, 3.2, 4.7, 1.4] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1]  |
| 52 | [0.5, -2.57, 7.58, -5.28, 7.1]  | [1.0, 6.4, 3.2, 4.5, 1.5] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1]  |
| 53 | [0.5, -2.57, 7.58, -5.28, 7.1]  | [1.0, 6.9, 3.1, 4.9, 1.5] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1]  |

| 54 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 5.5, 2.3, 4.0, 1.3] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
|----|--------------------------------|---------------------------|---|---|--------------------------------|
| 55 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.5, 2.8, 4.6, 1.5] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 56 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 5.7, 2.8, 4.5, 1.3] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 57 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.3, 3.3, 4.7, 1.6] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 58 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 4.9, 2.4, 3.3, 1.0] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 59 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.6, 2.9, 4.6, 1.3] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 60 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 5.2, 2.7, 3.9, 1.4] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 61 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 5.0, 2.0, 3.5, 1.0] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 62 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 5.9, 3.0, 4.2, 1.5] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 63 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.0, 2.2, 4.0, 1.0] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 64 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.1, 2.9, 4.7, 1.4] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 65 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 5.6, 2.9, 3.6, 1.3] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 66 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.7, 3.1, 4.4, 1.4] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 67 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 5.6, 3.0, 4.5, 1.5] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 68 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 5.8, 2.7, 4.1, 1.0] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 69 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.2, 2.2, 4.5, 1.5] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 70 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 5.6, 2.5, 3.9, 1.1] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 71 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 5.9, 3.2, 4.8, 1.8] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 72 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.1, 2.8, 4.0, 1.3] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 73 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.3, 2.5, 4.9, 1.5] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 74 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.1, 2.8, 4.7, 1.2] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 75 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.4, 2.9, 4.3, 1.3] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 76 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.6, 3.0, 4.4, 1.4] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 77 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.8, 2.8, 4.8, 1.4] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 78 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.7, 3.0, 5.0, 1.7] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 79 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.0, 2.9, 4.5, 1.5] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 80 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 5.7, 2.6, 3.5, 1.0] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 81 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 5.5, 2.4, 3.8, 1.1] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 82 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 5.5, 2.4, 3.7, 1.0] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 83 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 5.8, 2.7, 3.9, 1.2] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 84 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.0, 2.7, 5.1, 1.6] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 85 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 5.4, 3.0, 4.5, 1.5] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 86 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.0, 3.4, 4.5, 1.6] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 87 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.7, 3.1, 4.7, 1.5] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 88 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.3, 2.3, 4.4, 1.3] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 89 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 5.6, 3.0, 4.1, 1.3] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 90 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 5.5, 2.5, 4.0, 1.3] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 91 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 5.5, 2.6, 4.4, 1.2] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 92 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.1, 3.0, 4.6, 1.4] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 93 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 5.8, 2.6, 4.0, 1.2] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 94 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 5.0, 2.3, 3.3, 1.0] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |

| 95  | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 5.6, 2.7, 4.2, 1.3] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
|-----|--------------------------------|---------------------------|---|---|--------------------------------|
| 96  | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 5.7, 3.0, 4.2, 1.2] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 97  | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 5.7, 2.9, 4.2, 1.3] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 98  | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.2, 2.9, 4.3, 1.3] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 99  | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 5.1, 2.5, 3.0, 1.1] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 100 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 5.7, 2.8, 4.1, 1.3] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 101 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.3, 3.3, 6.0, 2.5] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 102 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 5.8, 2.7, 5.1, 1.9] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 103 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 7.1, 3.0, 5.9, 2.1] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 104 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.3, 2.9, 5.6, 1.8] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 105 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.5, 3.0, 5.8, 2.2] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 106 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 7.6, 3.0, 6.6, 2.1] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 107 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 4.9, 2.5, 4.5, 1.7] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 108 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 7.3, 2.9, 6.3, 1.8] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 109 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.7, 2.5, 5.8, 1.8] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 110 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 7.2, 3.6, 6.1, 2.5] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 111 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.5, 3.2, 5.1, 2.0] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 112 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.4, 2.7, 5.3, 1.9] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 113 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.8, 3.0, 5.5, 2.1] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 114 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 5.7, 2.5, 5.0, 2.0] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 115 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 5.8, 2.8, 5.1, 2.4] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 116 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.4, 3.2, 5.3, 2.3] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 117 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.5, 3.0, 5.5, 1.8] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 118 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 7.7, 3.8, 6.7, 2.2] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 119 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 7.7, 2.6, 6.9, 2.3] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 120 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.0, 2.2, 5.0, 1.5] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 121 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.9, 3.2, 5.7, 2.3] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 122 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 5.6, 2.8, 4.9, 2.0] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 123 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 7.7, 2.8, 6.7, 2.0] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 124 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.3, 2.7, 4.9, 1.8] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 125 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.7, 3.3, 5.7, 2.1] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 126 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 7.2, 3.2, 6.0, 1.8] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 127 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.2, 2.8, 4.8, 1.8] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 128 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.1, 3.0, 4.9, 1.8] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 129 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.4, 2.8, 5.6, 2.1] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 130 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 7.2, 3.0, 5.8, 1.6] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 131 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 7.4, 2.8, 6.1, 1.9] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 132 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 7.9, 3.8, 6.4, 2.0] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 133 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.4, 2.8, 5.6, 2.2] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 134 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.3, 2.8, 5.1, 1.5] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 135 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.1, 2.6, 5.6, 1.4] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |

| 136 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 7.7, 3.0, 6.1, 2.3] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
|-----|--------------------------------|---------------------------|---|---|--------------------------------|
| 137 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.3, 3.4, 5.6, 2.4] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 138 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.4, 3.1, 5.5, 1.8] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 139 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.0, 3.0, 4.8, 1.8] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 140 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.9, 3.1, 5.4, 2.1] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 141 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.7, 3.1, 5.6, 2.4] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 142 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.9, 3.1, 5.1, 2.3] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 143 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 5.8, 2.7, 5.1, 1.9] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 144 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.8, 3.2, 5.9, 2.3] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 145 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.7, 3.3, 5.7, 2.5] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 146 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.7, 3.0, 5.2, 2.3] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 147 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.3, 2.5, 5.0, 1.9] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 148 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.5, 3.0, 5.2, 2.0] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 149 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 6.2, 3.4, 5.4, 2.3] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |
| 150 | [0.5, -2.57, 7.58, -5.28, 7.1] | [1.0, 5.9, 3.0, 5.1, 1.8] | 0 | 0 | [0.5, -2.57, 7.58, -5.28, 7.1] |

Get w=[0.5, -2.57, 7.58, -5.28, 7.1]

## (c) test Xtest

Given w=[0.5, -2.57, 7.58, -5.28, 7.1]

| Xtest                                | H(wx)               | у |
|--------------------------------------|---------------------|---|
| [4.43478261, 4.25, 1, 1.25]          | 24.912608695652175  | 1 |
| [7.91304348, 2, 4.33333333, 1.5]     | -16.90652173913044  | 0 |
| [4, 3.25, 5, 1.5]                    | -0.8950000000000014 | 0 |
| [6.17391304, 3.5, 5, 1.75]           | -2.811956521739134  | 0 |
| [6.60869565, 3.5, 5.66666667, 0.25]  | -18.09934782608696  | 0 |
| [6.60869565, 3.75, 1.66666667, 2.25] | 19.115652173913045  | 1 |
| [7.04347826, 2.25, 7, 0]             | -37.50673913043478  | 0 |