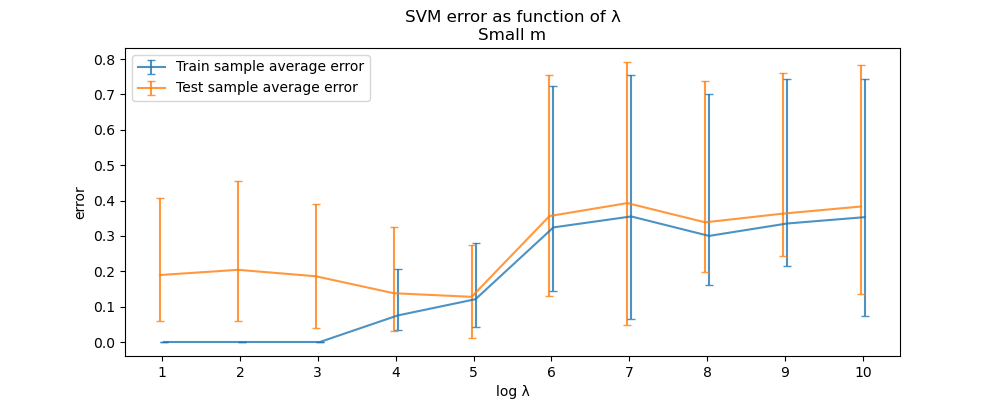
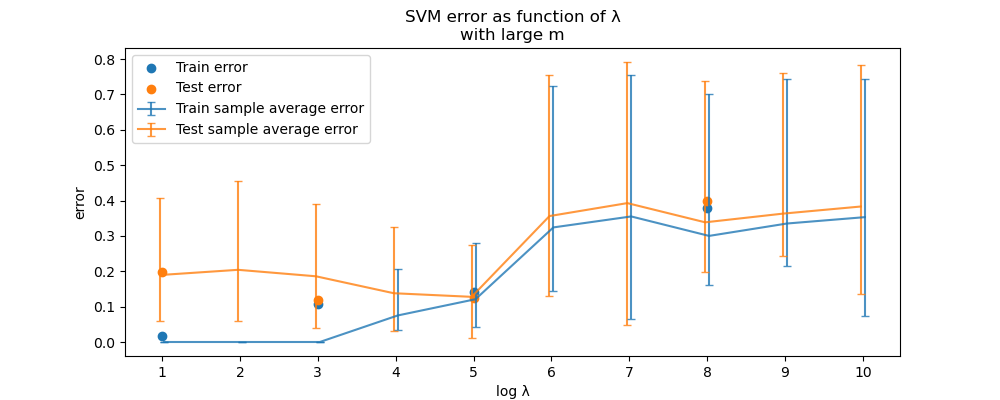
2.

(a)

(b)

(c)

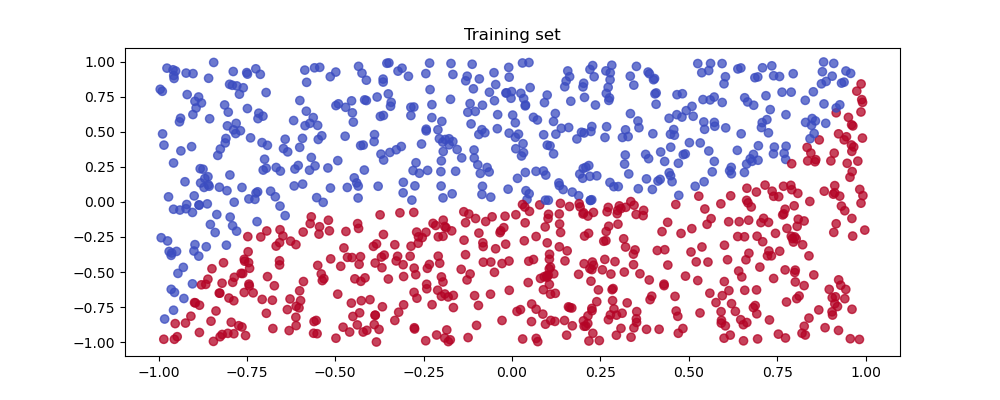
TODO

*Which sample size should get a smaller training error? What about test error? Do the results match your expectations?*

*What should be the trend in the training error as a function of λ (decreasing/increasing/other)? Why? Do the results (for the small sample size) match your expectations?*

*What should be the trend in the test error as a function of λ (decreasing/increasing/other)? Why? Do the results (for the small sample size) match your expectations?*

4.

(a)

(b)

polynomial kernel errors by :

|  |  |
| --- | --- |
|  | Error |
| (1.0, 8.0) | 0.051000000000000004 |
| (1.0, 5.0) | 0.059 |
| (10.0, 8.0) | 0.059 |
| (100.0, 8.0) | 0.061 |
| (10.0, 5.0) | 0.064 |
| (100.0, 5.0) | 0.064 |
| (1.0, 2.0) | 0.069 |
| (100.0, 2.0) | 0.069 |

linear soft-SVM errors by :

|  |  |
| --- | --- |
|  | Error |
| 1.0 | 0.063 |
| 10.0 | 0.063 |
| 100.0 | 0.063 |

We can see the best results are for the polynomial kernel achieved by ,

And for the linear soft-SVM the results are the same for all three values of

When using these parameters on the entire training set we got the following errors:

For polynomial kernel soft-SVM: 0.005

For linear soft-SVM: 0.04

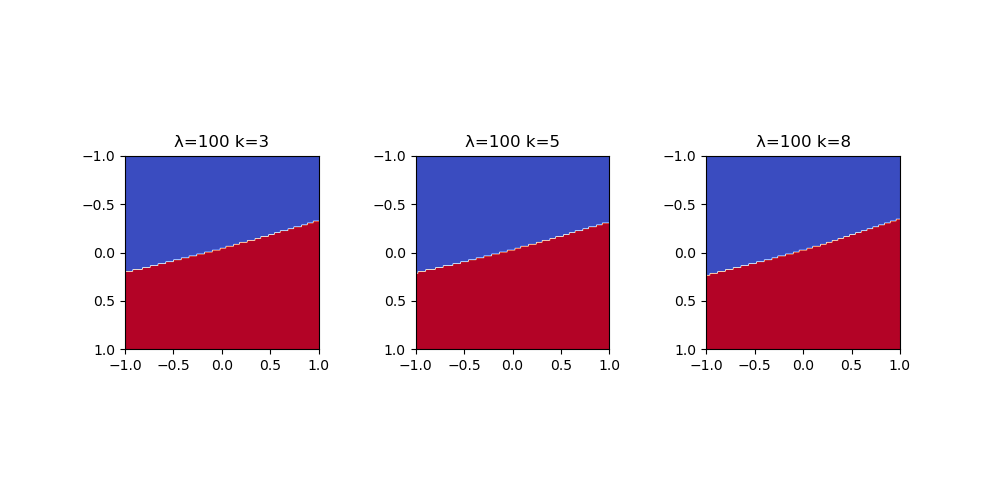
(c)

The polynomial kernel got better results as expected, since as can be seen by the plot in section (a), any linear separator will get large error on these samples.

With the polynomial kernel we get polynomial separator, which can curve according to the training set and thus get better results.

(d)

TODO

(e)

(f)

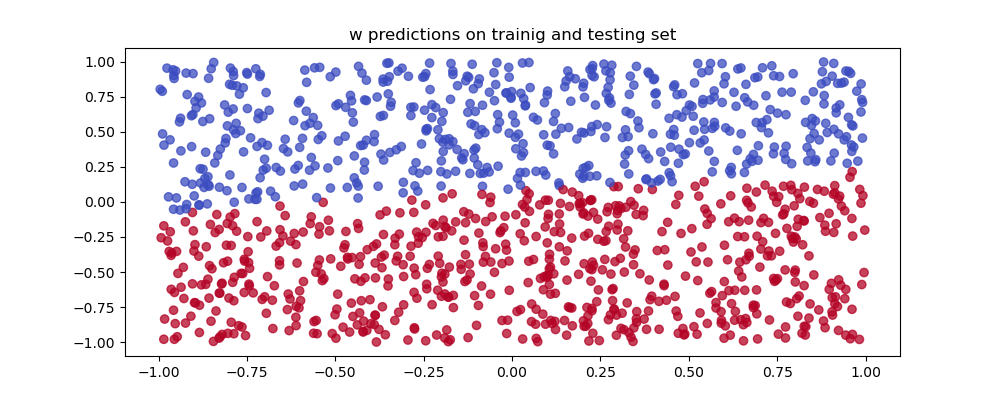
As seen in the table in section (b), for we will choose .

where are the coefficients form the solution to the quadratic formula and using

such that:

W=

iii.

iv.

5.

Let be the set of all undirected graphs over n vertices numbered 1,…,n with degree at most 7.

as the described function

(a)

We cannot know how D is defined,

We’ll show an example of D which is not realizable:

Example: for every graph ,

So D is a distribution over . Also, the label of a graph x is deterministic function of ,

Also, there’s no such that will get error 0 on D.

Let - graph with n vertices such that every vertex in is degree 4

Let - graph with n vertices such that every vertex in is degree 4 except vertex 1 which is degree 7

So:

we’ll get and we get an error on

If well get and we get an error on

For the described D there’s no such which we get an .

And thus we get only the agnostic PAC bound for which we know we get dependence on

(b)

Let us calculate the size of the hypothesis class:

Any labeled undirected graph size n can have different edges as the way to pick 2 vertices

and for any graph we can choose between assign a specific edge or not

thus we got labeled graphs with n vertices, also we should leave the graph with no edges because .

In conclusion

As we showed in class the PAC-learning upper bound for the sample complexity of learning H is:

We’ll describe the upper bound for both Pac cases (if D is Realizable by H and if D is not Realizable by H), for unknown D we can use only the agnostic case

For the realizable case:

For the agnostic case:

(c)

For any such that

There are 2 cases:

we can only label :

there’s no such such that or

we can only label but there’s no such that and thus we cannot shutter any group size 2 for that case,

Thus the VC dimension of H is 1

As we showed in class the better upper bound for the sample complexity of learning H depends on the VC dimension of H is:

We’ll describe the upper bound for both Pac cases (if D is Realizable by H and if D is not Realizable by H), for unknown D we can use only the agnostic case

For the realizable case:

For the agnostic case:

6.

For

We showed in class the Preceptron performs at most updates.

Thus we should find of the Sample S.

We also showed in class Hard-SVM algorithm with input S return which is a maximal-margin separator.

Now we can describe the algorithm who returns an upper bound on Preceptron number of updates:

**Input**: a labeled sample S of labeled examples from X × Y

**Output**: an upper bound on the number of updates that the Perceptron algorithm would require if it was run on this sample.

1. runs Hard-SVM on sample S
   1. if Hard-SVM gets an error while running then the algorithm returns -1
   2. else w Hard-SVM output
      1. R sample with max norm between all samples
      2. Dxmin
      4. Return

**complexity:**

Hard-SVM has polynomial runtime complexity,

For b.i we need to find the maximal norm in , calculating norm is and finding max is so this section is

b.ii takes because inner product of two vectors in is and get min of m items is

b.iii calculating norm of w:

b.iv

in conclusion, we get **polynomial runtime complexity**

7. (a)

In order to express the problem

in terms of

,

we will define variable and rewrite the problem as

,

(b)

since we only need sum of squares of , we don’t need to use , we can compile it into :

8. (a)

Claim:

Proof: assume in contradiction that exists such function, Let be that function.

So

Let

We assumed , therefore

But for ) we get

And .

we assumed such existed and found 2 vectors which the assumption doesn’t hold for them, thus no such existed.

Therefore, the representer theorem does not hold for the objective given in the question.

(b)

The representer theorem guarantees that if we can represent objective in a specific form there’s a solution of a form .

Since we can’t represent the given objective in that form, we can only know there **might be** a solution in the form above, but we can’t **know** that such solution exists or doesn’t exist.

Hence, we can’t really infer anything based on the fact that the representer theorem does not hold for the given subjective.

9.(a)

To prove that cannot be a kernel function for any feature mapping, we need to show such that .

from inner products property: . Hence:

even though for we get that

which means for some , in contradiction to inner product properties. Hence, no such exists.

(b)

Assume in contradiction that

Thus, for

for we get .

we assumed that such that and got contradiction, hence no such exists and cant be a kernel function.

(c)

let

we found some that satisfy , hence can be a kernel function.