INDIAN INSTITUTE OF TECHNOLOGY KANPUR



Artificial Intelligence (AI) for Investments





Lesson 2: Introduction to Market Microstructure



Introduction

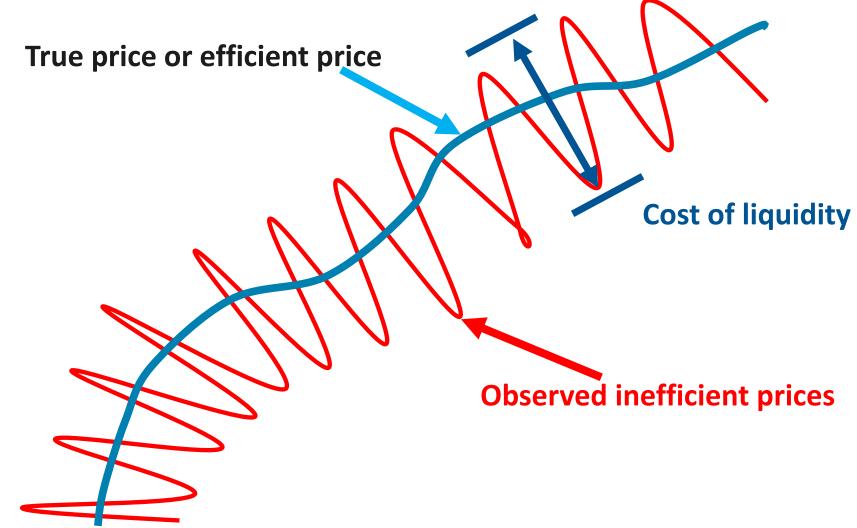
- To channel the savings of an economy towards productive and efficient sectors: Financial Intermediation
- Banks conventionally play this role
- However, financial markets allow investors to directly participate in the process of choosing the best sector for himself
- Thus less bureaucratic hassles or principal-agent problem
- To this end, an economy needs efficient and liquid markets
- What is efficient and liquid?

INDIAN INSTITUTE OF TECHNOLOGY KANPUR



Market Efficiency







The true price or efficient price or fundamental price is called so because it reflects all the "fundamental information" about security

- The information that affects the cash flows of the firm(e.g., macroeconomic information, or information about the firm)
- However, this price is not observed
- What we observe on stock markets is a mix of fundamental prices and noise
- $P_{observed} = P_{true} + e_{noise}$



This noise, though a small component, is at times sufficient for informed traders to conduct arbitrage trading (Speculation?)

- Riskless Arbitrage trading: Same stock is traded in different markets (BSE vs NSE, Cash vs Future)
- If price in one of the markets deviates too much from its true value, informed traders start selling/buying the stock in that market and take opposite position in the other market (buying/selling)
- Since they are not taking any risk, this is called riskless arbitrage (In practical life, no arbitrage is riskless)



However, for arbitrage to take place the price has to move sufficiently to cover the trading costs (costs of liquidity)

- Therefore, the forces of arbitrage only work when the price moves out of the cost of liquidity window
- Then forces of arbitrage kick-in and pull the prices towards the efficient price until it moves back in the liquidity window
- Thus, price keeps oscillating with in the cost of liquidity window
- What is the amplitude of this window?



This amplitude reflects cost of liquidity

- At times prices move-beyond this amplitude and exhibit high fluctuations
- Then we say that prices are volatile
- This happens during some crisis periods or negative news
- A higher volatility means that prices divert away from their true values
- Different markets exhibit different levels of volatility depending upon the level of efficiency



- Weak-form efficiency: When a trader can not make profit using the information contained in past prices, markets are said to be weak-form efficient
- Semi-strong form efficiency: When a trader can not make profit using the information contained in past prices and public
- Strong form efficiency: When a trader can not make profit using the information contained in past prices, public information, as well as private information



- Not efficient at all: Make technical trading strategies, using the information from past price and volume
- Weak-form efficiency: Make profits by collecting public information
- Semi-strong form efficiency: Make profits if one has private information
- Strong form efficiency: Can not beat the market, so follow the market by investing in indices that reflect the broad market movement (Nifty-50)

INDIAN INSTITUTE OF TECHNOLOGY KANPUR



Risk Preference



Risk Preference

Individuals are described by their utility function. These utility functions describe our preferences for different outcomes

- For a given level wealth W, an individual may have wealth as U(W). For all normal things, it is reasonable to assume U'(W) > 0, i.e., more is preferred to less or "non-satiation"
- This means that increase in wealth will always lead to increase in utility, no matter how small
- With this, individuals are classified as (1) Risk neutral; (2) Risk Averse; (3) Risk preferring.



Risk Preference: Risk Neutral Person

If the individual is indifferent in receiving the expected value of gamble

- That means, if you make a bet the expected value of winning the bet is Rs 100. If you are indifferent in directly getting Rs 100 vs taking this bet
- This also means that in this case, expected wealth is important for the investor, not the risk (variance) of the wealth
- Therefore, utility is a linear function of wealth here: U''(W) = 0
- This also means that changing the risk of outcome has no effect on the utility (well-being for a given level of wealth): U[E(W)] = E[U(W)]



Utility function of a risk averse individual is concave, that is U''(W) < 0

- This also means that the individual prefers a certain (ensured) amount over the bet (gamble) with the same expected value: U[E(W)] > E[U(W)]
- This also means that risk averse individuals prefer less risk to more, and they demand additional risk-premia to take the extra-risk



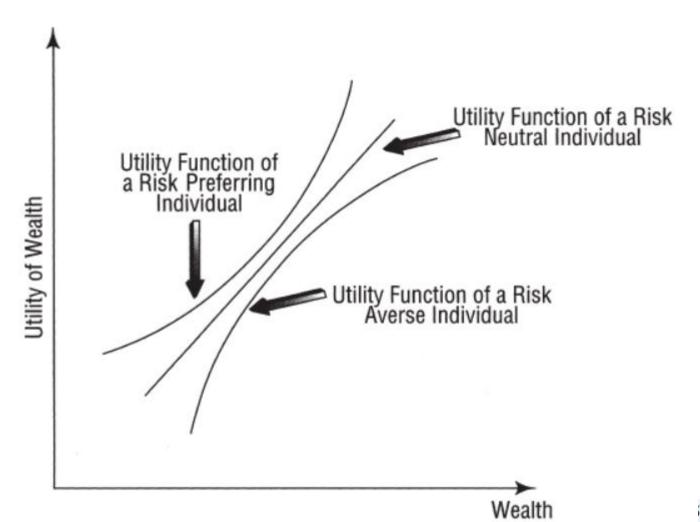
Risk Preference: Risk Preferring Person

A risk preferring individual would prefer the riskier situation

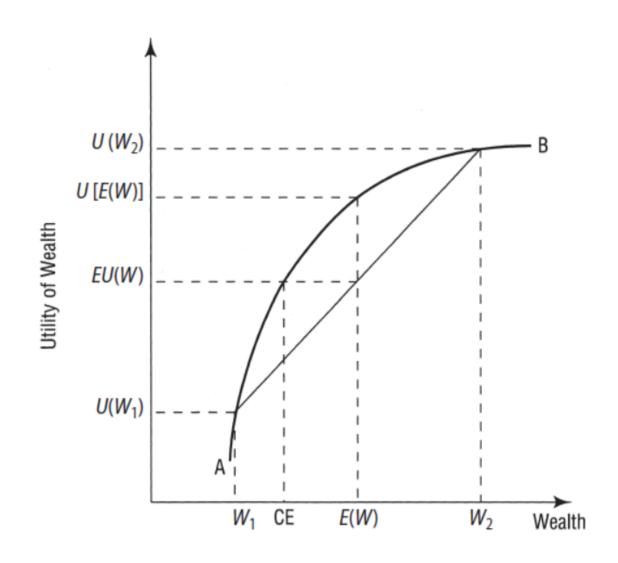
- His utility function would be convex, i.e., U''(W) > 0. This also means that U[E(W)] < E[U(W)]
- However, commonly it is assumed that individuals are risk averse



Risk Preference: Risk Preferring Person









Assume a gamble with two possible outcomes for wealth W_1 and W_2 , each with 50% probabilities

- Then the expected wealth from this gamble is $E(W)=0.5*W_1+0.5*W_2$
- This will lie midway on the straight-line joining the points W_1 and W_2 on the curve
- Also, if one computes the expected utility wealth E[U(W)], the same will fall midway between $U(W_1)$ and $U(W_2)$
- However, as can be seen from the graph, to generate the same level of utility
 E[U(W)], a lower level of certain (ensured) wealth is required

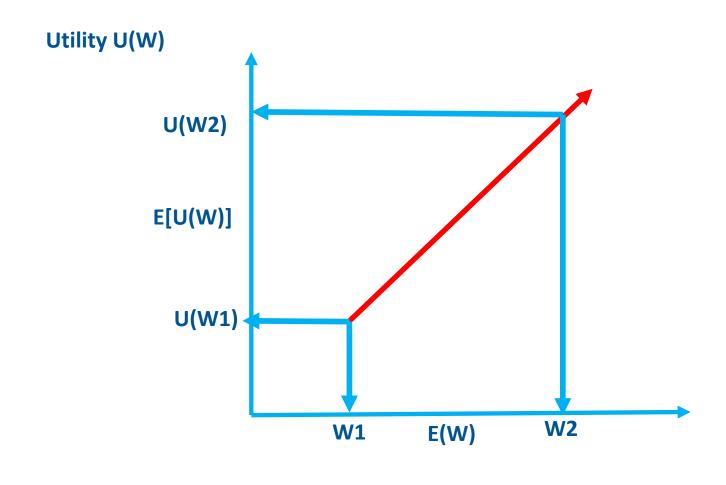


It is very easy to observe here that, for this kind of utility function U[E(W)] > E[U(W)]

- The more concave this function (downward slopping) higher the difference between U[E(W)] and E[U(W)], i.e., the individual will be more risk averse
- A sure payment that makes this individual indifferent between gamble and sure payment is "Certainty Equivalent" (CE)
- As can be seen the certainty equivalent is less than E(W) and this difference represent the risk-premia of this risk-averse individual

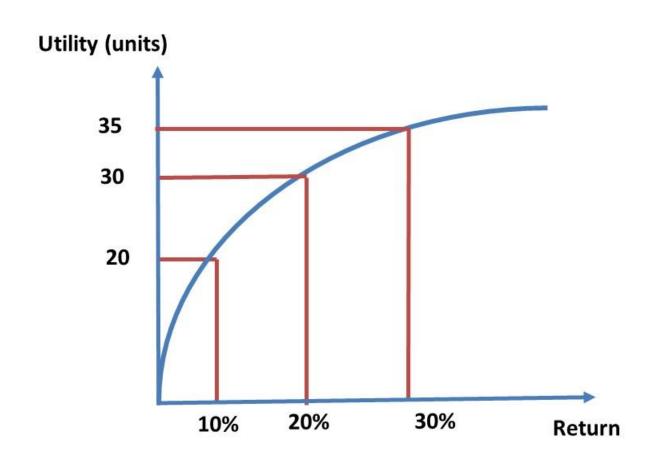


Risk Preference: Risk Neutral Person





Return utility diagram for risk averse person



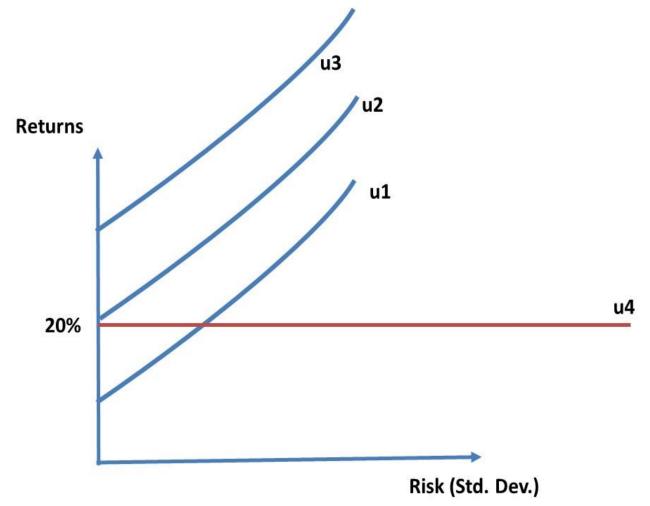


Return vs utility for risk averse person

More return will always have more utility (Non-satiation)

- However, for a risk-averse investor, the relationship exhibits diminishing marginal utility
- For example, an increase of 10% from 20% to 30% results in 10 unit of additional utility
- However, the next 10% offer only 5 unit of additional utility
- So, the expected returns have to be increased to reach the same amount of additional utility

Indifference curve for risk (SD) and Expected return



Indifference curve for risk (SD) and Expected return

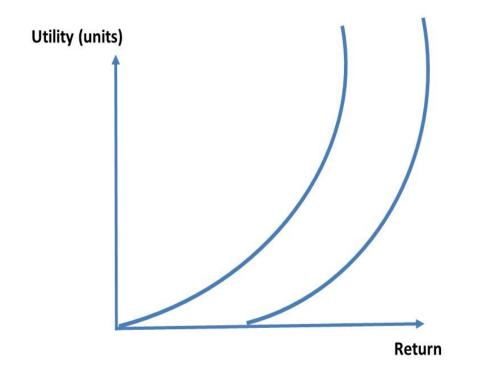
In this graph, u1, u2, u3 are indifference curves for an individual

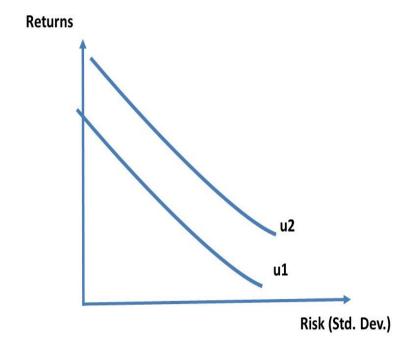
- This means increasing level of expected returns for same risk or same level of returns for lower risk lead to higher utility
- What is the nature of this person?
- However, u4 is horizontal. For this individual, utility remains same despite the increase in risk
- That is the marginal utility does not diminish with increasing risk
- What is the nature of this person?



Return utility graph for increasing marginal utility

For this person, increase in risk results in lower level of return expectations. It means that he enjoys risk (gambler, speculator)





INDIAN INSTITUTE OF TECHNOLOGY KANPUR



Types of Markets



The conventional markets had a very important entity called broker-dealers

- Broker-dealer markets involved designated market makers
- They are called market makers because they provided continuous buy-sell sided quotes also called bid-ask prices
- Incoming buyer can buy at the ask prices and seller can sell at the bid prices
- This is also called liquidity provision



The difference between the bid and ask price is the compensation to the dealer for creating market in that particular security

- These are also called specialists
- Who do I mean when I say "creating market"?
- The dealer role is now performed by large institutional investors
- The difference between these bid and ask prices is also called spread and reflects the liquidity in the market



If there is a very high demand of a security (e.g., Apple, FaceBook) there will be many buyers and sellers

- Thus, the market maker can keep a small spread to generate sufficient profits and cover his costs
- The security will be called a liquid security have a deep market
- In contrast, a security that has a less demand in market will witness very infrequent trading





Price = 150, 500,000 shares



Price = 100????, 10 share



The market maker for that security will have to charge higher spread

- The market maker for that security will have to charge higher spread to cover his costs and make profits
- This security will be called less liquid security and will have a shallow market
- But what are the costs of this dealer for which he is charging money???



Limit order books

Unlike quote-driven markets, order-driven markets (like India) lack designated market makers

- There are two major type of orders Limit orders and Market orders
- The limit order suppliers act as the liquidity suppliers in these markets, and are called de-facto market makers
- Market orders consume liquidity provided by limit orders



Primary vs Secondary Markets

New issue of securities takes place in primary markets

- Securities that are already sold are traded in secondary markets
- Governments through central banks (RBI) auction T-bills and dated securities in primary markets
- Deep and liquid secondary markets are desired to create the appropriate environment for primary issuances



Call Auction vs. Continuous Auction markets

In call markets trading takes place at specific intervals

- Generally global markets use some kind of call-auction at the opening/closing of trading Pre-trade
- Investors can change their orders/place new orders until this specified period of time
- Orders are generally matched as per the price-time priority rules



Example of call auction markets at NSE

Pre-opening session follows call market auction framework

- The session has a duration of 15-minutes from 9:00 AM to 9:15 AM
- The pre-open session is comprised of Order collection period (8 minutes) and order matching period
- During this period orders can be entered, modified and cancelled
- The equilibrium price in this period is obtained at which supply and demand leads to clearing of maximum shares
- The clearing price will be the equilibrium price and also the opening price as well



Example of call auction markets at NSE

	ORDER BOOK DEMAND / SUPPLY SCHEDULE		R BOOK DEMAND / SUPPLY SCHEDULE		
SHARE PRICE	BUY	SELL	DEMAND	SUPPLY	MAXIMUM TRADABLE QUANTITY
103	13500	11500	50500	11500	11500
104	9500	9800	37000	21300	21300
105	12000	15000	27500	36300	27500
106	6500	12000	15500	48300	15500
107	5000	12500	9000	60800	9000
108	4000	8500	4000	69300	4000

INDIAN INSTITUTE OF TECHNOLOGY KANPUR



Theoretical Underpinnings



Types of traders

- Noise traders and Liquidity traders: These traders do not have proper information and their trading activity contributes to noise in prices
- Informed traders: These are large institutional investors that spend considerable amount of resources in information acquisition. Their trading activity increase the pricing efficiency
- Market makers: They provide liquidity to financial markets by offering both buy and sell sided quotes to incoming market participants



There are two key hypothesis that explain various financial market phenomena (e.g., spread)

- Inventory considerations
- These market makers maintain a certain level of inventory
- However, these inventories are affected by adverse price movements
- For example, falling prices of securities may affect the market makers who is making market in that security by maintaining inventory



Information asymmetry

- There is a certain probability that the counterparty against the market maker is more informed
- Market makers incur losses in these trades against informed traders
- Therefore, based on the probability of informed trading, they charge another component of spread

To account of these losses (informed trading and inventory costs) market make, on average, charges a certain extra-component in the form of spread



At times, there is an excess order flow on buy or sell side

- This may lead to order imbalance and disturb the inventory levels
- There can be two causes for this order imbalance
- If this order imbalance is caused by sentiment driven noise trading (what is this?), then market makers temporarily adjust these quotes
- For example, if he observes buy-pressure (Excess of buy orders) then he can adjust his quotes to make sell orders more favorable (How?)



- This quote adjustment would induce more sell orders and subsequently the order flow pressure will be absorbed
- Once the order flow pressure is absorbed, the market maker will revert this quotes back to normal levels
- If this order imbalance is caused by arrival of information, then market maker will make a more permanent quote adjustment
- For example, if there is information of new-discovery by the company, then he will increase both the buy and sell quotes, to reflect the increased value of the security: this quote adjustment is more permanent and durable in nature



- Quote adjustment associated with inventory hypothesis are temporary in nature
- Quote adjustments associated with information asymmetry hypothesis are permanent in nature
- Momentum traders follow this order imbalance measure to make trading strategies
- Order imbalance = $\frac{\text{Buy orders-Sell orders}}{\text{Buy orders+Sell orders}}$
- The orders can be simple share volume, Dollar volume, or number of orders

INDIAN INSTITUTE OF TECHNOLOGY KANPUR



Rise of machines: Limit order books



Unlike quote-driven markets, order-driven markets (like India) lack designated market makers

- There are two major type of orders Limit orders and Market orders
- The limit order suppliers act as the liquidity suppliers in these markets, and are called de-facto market makers
- Market orders consume liquidity provided by limit orders



Market Order: A market order directs the broker (now online brokerage houses) to buy or sell the security at the best available prices. What is best available price

- These is a set of ask prices at which the investor can buy the security; of course he will choose the lowest ask
- Similarly these is a set of bid prices at which the investor can sell the security; he will choose the largest bid



Limit orders: These orders specify the worst acceptable terms of trade

- For example, Purchase (Sell) 100 shares of Company A, limit Rs 1000
- So the broker should not pay (receive) anything more (less) than Rs 1000
- Unlike market orders, the execution of limit orders is uncertain
- In the modern order book markets, these kind of orders are inventoried in the order book, till the time they become the best order available and are picked by market or limit orders
- At the closing day, unexecuted limit orders are canceled

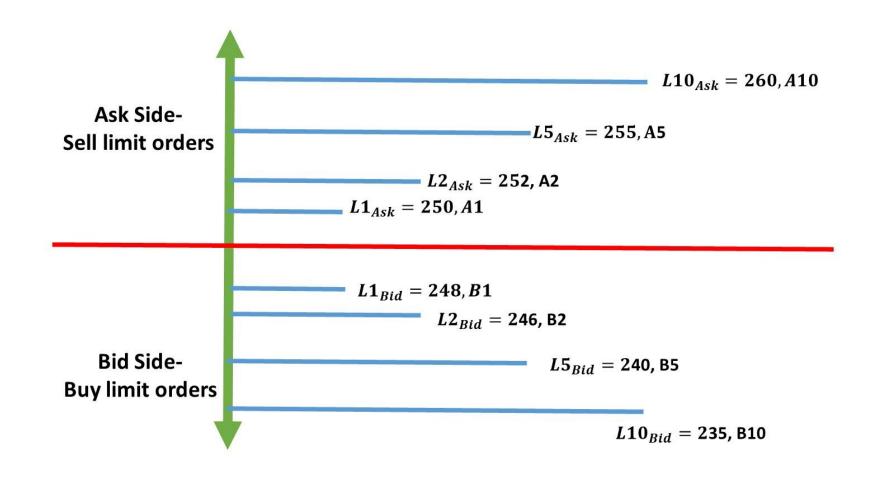


Limit orders are inventoried in order book, in the form of bid and ask orders

- The quantity associated with these bid/ask orders is known as the depth available on the buy and sell side, at the respective level
- The difference between the **best bid (highest buy)** and **best ask (lowest sell)** orders is known as spread, measure of liquidity
- An investor that makes an immediate buy and sell transaction through market order will incur this spread

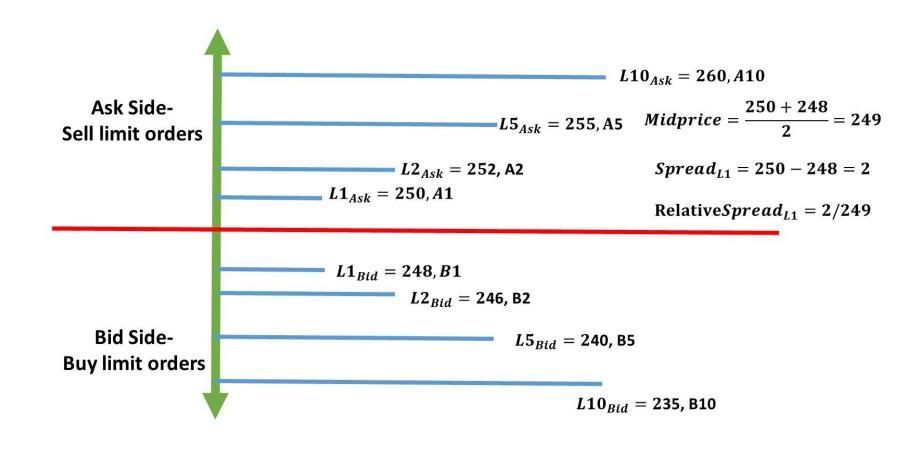


Order book snapshot





Order book snapshot





Driven by algorithmic low latency trading, these markets are extremely fast paced and carry out voluminous trades

- Low latency algorithms exploit any inefficiency in prices within 10^{-6} second
- Thus, prices are pulled within the window of efficiency in no-time
- This has also led to a debate of "Man vs Machine"
- That is, is it even fair now for humans to trade manually, as they can not compete with algos
- Different algorithms are available to exploit different kind of inefficiencies



Trading terminologies- Order flows

Time	Price (Rs)	Numbers	
Sellers (Ask/ Offer)			
12:10:00	100	400	Worst
12:10:30	99	320	
12:10:20	98	290	
12:11:00	95	200	
12:10:40	95	220	Best
Buyers (Bid)			
12:10:56	98	200	Best
12:10:57	95	420	
12:10:55	94	95	
12:10:40	93	250	
12:10:50	93	200	
12:10:10	92	535	
12:10:00	90	600	Worst



Time	Price (Rs)	Numbers	
Sellers (A	sk/ Offer)		
12:10:40	95	220	
12:11:00	95	200	
12:10:20	98	290	
12:10:30	99	320	
12:10:00	100 400		
Buyer			
12:10:55	94	95	
12:10:40	93	250	
12:10:50	93	200	
12:10:10	92	535	
12:10:00	90	600	



Spread and Impact cost

- Best Ask= 95; Best bid=94
- Absolute spread = 95-94=1
- Relative spread = Absolute spread / Relative price = 1/ (95+94)/2=1.06%
- Impact cost as per NSE: % change in prices on account of Rs 1 lakh trade (either side: buy side and sell side)
- (Wt. Average Buy or Sell price/Mid Price)-1
- This takes place continuously and called of continuous auction trading



Time	Price (Rs)	Numbers
Sellers (A	sk/ Offer)	
12:10:40	95	220
12:11:00	95	200
12:10:20	98	290
12:10:30	99	320
12:10:00	100	400
Buyers		
12:10:55	94	95
12:10:40	93	250
12:10:50	93	200
12:10:10	92	535
12:10:00	90	600



Time	Price (Rs)	Numbers	Order Size (Rs)
Sellers (A	sk/ Offer)		
12:10:40	95	220	20,900
12:11:00	95	200	19,000
12:10:20	98	290	28,420
12:10:30	99	320	31,680
12:10:00	100	400	40,000
Buyers (Bid)			
12:10:55	94	95	8,930
12:10:40	93	250	23,250
12:10:50	93	200	18,600
12:10:10	92	535	49,220
12:10:00	12:10:00 90		54,000



Time	Price (Rs)	Numbers Order Size (Rs)		Cumulative Orders
Sellers (A	\sk/ Offer)			
12:10:40	95	220	20,900	20,900
12:11:00	95	200	19,000	39,900
12:10:20	98	290	28,420	68,320
12:10:30	99	320	31,680	1,00,000
12:10:00	100	400 40,000		1,40,000
Buyer	Buyers (Bid)			
12:10:55	12:10:55 94		8,930	8,930
12:10:40	93	93 250		32,180
12:10:50	93	200	18,600	50,780
12:10:10	92	535	49,220	1,00,000
12:10:00	90	600	54,000	1,54,000



Time	Price (Rs)	Numbers	Order Size (Rs)	Cumulative Orders	Av. Price	Impact Cost
Sellers (Ask/ Offer)						
12:10:40	95	220	20,900	20,900	Best	
12:11:00	95	200	19,000	39,900		
12:10:20	98	290	28,420	68,320		
12:10:30	99	320	31,680	1,00,000	97.08738	2.74%
12:10:00	100	400	40,000	1,40,000	Worst	For Buyers
Buyer	Buyers (Bid)					
12:10:55	94	95	8,930	8,930	Best	
12:10:40	93	250	23,250	32,180		
12:10:50	93	200	18,600	50,780		
12:10:10	92	535	49,220	1,00,000	92.59259	-2.02%
12:10:00	90	600	54,000	1,54,000	Worst	For Sellers



Other key terms

Stop loss buy/sell orders: These orders are activated when price of the security reaches some pre-defined limit

- For example, a stop-loss sell order at Rs 40 would become a market order to sell if the price trades at Rs 40 or below
- Vice-versa for buy order
- These orders are used to lock a gain or limit a loss



Thanks!

