#### INDIAN INSTITUTE OF TECHNOLOGY KANPUR

# Artificial Intelligence (AI) for Investments



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# Lesson 3: Making investment decisions



# **Introduction**

In this lesson we will cover the following topics:

- Review of NPV basics
- Alternatives to NPV rule Payback period method
- Alternatives to NPV rule Internal rate of return (IRR) method
- Pitfalls of IRR
- Capital investments with limited resources
- Summary and concluding remarks

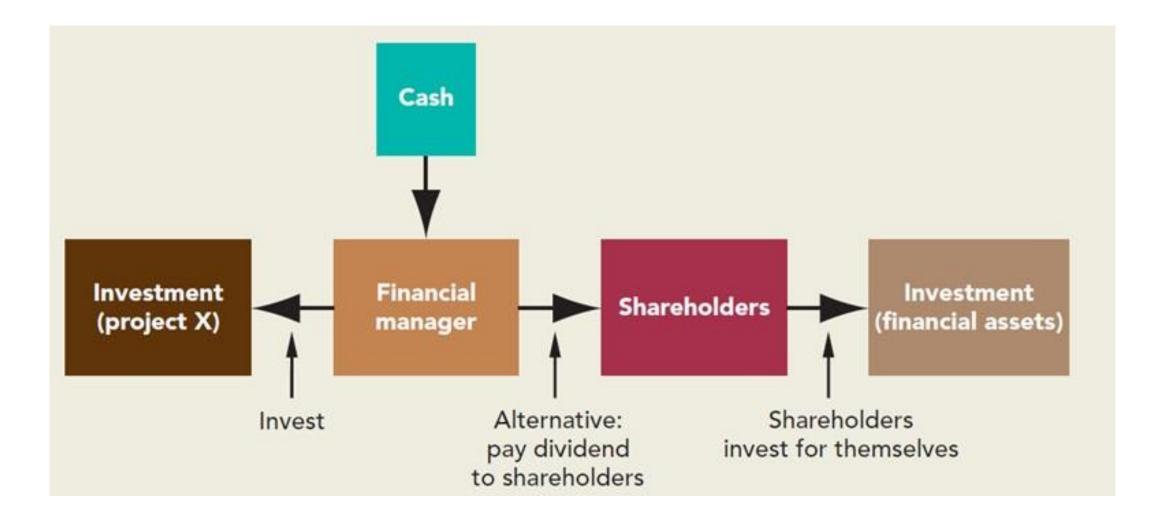


# **Review of NPV basics**

- Consider yourself in a position of a CFO where you are analyzing \$1 million investment in a new venture called project P
- That the current market value of your firm is \$10 million, which includes \$1 million cash that you plan
  to invest min project P
- You find the NPV of this project by discounting the cash flows, adding them up to compute there PV,
   and subtracting the initial investment of \$1 million
- It is easy to understand if PV>9 this project has a positive NPV



### **Review of NPV basics**





### **Review of NPV basics**

- NPV rule recognizes that a dollar today is worth more than a dollar tomorrow
- Any decision rule that is affected by managers' tastes, choice of accounting method, profitability of existing business, or that of other projects will lead to an inefficient decision
- NPV(A+B) = NPV(A) + NPV(B)
- Book incomes are not necessarily the same as cash flows
- Profitability measures such as book rate of returns, heavily depend on the classification of various items as capital investment and their rate of depreciation

# <u>Alternatives to NPV rule – Payback period</u> method



- A project's payback period is simply found by estimating the years it takes for the project cash flows to meet the initial investment
- A washing machine is costing \$800. You spend \$300 a year on washing your clothes. As a thumb rule, if this machine is purchased, it will recover its expenses in 3 years
- The payback rule states that a project should be accepted if its payback period is less than some cutoff period
- Consider a simple example here

Project	C0	C1	C2	C3	Payback Period (years)	<b>NPV at 10%</b>
Α	-2,000	500	500	5,000	3	+2,624
В	-2,000	500	1,800	0	2	-58
С	-2,000	1,800	500	0	2	+50

# <u>Alternatives to NPV rule – Discounted Payback</u> period method



- An improved version of payback period is to employ discounted cash flows
- This discounted payback rule examines that how many years it takes for the discounted cash flows to recover the initial investment, i.e., become NPV positive
- Let us examine our previous example, with the help of discounted cash flows

Project	C0	<b>C1</b>	C2	С3	Discounted Payback Period (years)	NPV at 10%
А	-2,000	$\frac{500}{1.1} = 455$	$\frac{500}{1.1^2} = 413$	$\frac{5,000}{1.1^3} = 3757$	3	+2,624
В	-2,000	$\frac{500}{1.1} = 455$	$\frac{1,800}{1.1^2} = 1488$	-	-	-58
С	-2,000	$\frac{1,800}{1.1} = 1636$	$\frac{500}{1.1^2} = 413$	-	2 INDIAN	+50

# <u>Alternatives to NPV rule – Internal rate of return</u> (IRR) method

IRR rule comes from the simple return measure

• Project return = 
$$\frac{\text{Profit}}{\text{Investment}} = \frac{\text{Payoff}}{\text{Investment}} - 1$$
; or  $-\text{Investment} + \frac{\text{Payoff}}{1 + \text{Project Return}} = 0$ 

IRR is the return or discount rate at which NPV=0

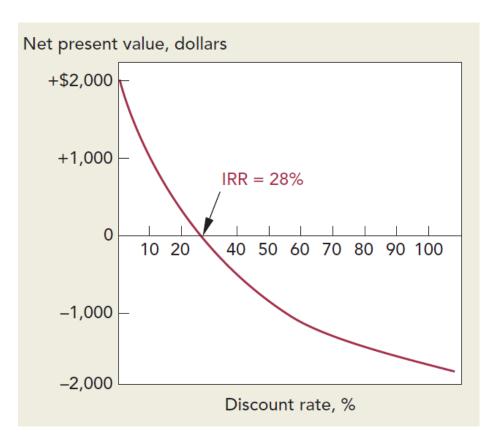
• NPV = 
$$C_0 + \frac{C_1}{(1+IRR)} + \frac{C_2}{(1+IRR)^2} + \dots + \frac{C_T}{(1+IRR)^T} = 0$$

$C_0$	$C_1$	$C_2$
-4000	+2000	+4000

• 
$$NPV = -4000 + \frac{2000}{1 + IRR} + \frac{4000}{(1 + IRR)^2} = 0$$
; solving for this, we get IRR= 28.08%

# <u>Alternatives to NPV rule – Internal rate of return</u> (IRR) method

- If the opportunity cost of capital is less than the 28.08%
   IRR, then the project has a positive NPV
- If opportunity cost of capital is greater than the IRR, the project has a negative NPV
- Please note that IRR is a profitability measure and depends solely on the timing of the project cash flows
- The opportunity cost of capital is the standard of profitability to judge the worth (or NPV) of the project





#### Pitfalls of IRR

- Pitfall 1: Problem of Lending vs borrowing
- Consider the project cash flows from projects A and B as shown here

Projects	Co	$C_1$	IRR	NPV at 10%
А	-1000	+1500	50%	+364
В	1000	-1500	50%	-364

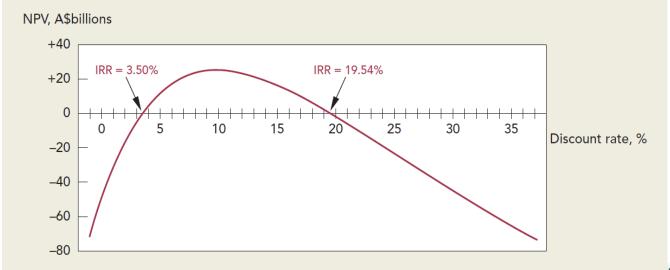
- Both of these projects will give you the same IRR
- In project A, we are paying out \$1000 initally, and getting \$1500 later Case of lending
- While in case of B, we are initially getting \$1000 and paying back \$1500 later- Case of borrowing
- When you lend money, you want a higher return and when you borrow money money you want a
  lower return



### Pitfalls of IRR

- Pitfall 2: Multiple rates of return
- Consider another project that involves an initial investment of \$3 Billion and then produce a cash flow \$1
   Billion per year, for next nine years
- At the end of the project, the company will incur \$6.5 billion of cleanup costs

$C_0$	$c_1$	$C_2$	$\mathcal{C}_3$	C <sub>4</sub>
-3	1	1	1	1
<i>C</i> <sub>5</sub>	<i>C</i> <sub>6</sub>	<i>C</i> <sub>7</sub>	<i>C</i> <sub>8</sub>	<b>C</b> 9
1	1	1	1	1





### Pitfalls of IRR

- Pitfall 3: Mutually exclusive projects
- Firms often have to choose from mutually exclusive projects, since it may not be feasible to take all of them
- In the project cash flows shown here, it seems IRR and NPV are contradicting each other

Projects	$C_0$	$C_1$	IRR (%)	NPV at 10%	
D	-10000	+20000	100	8182	
Е	20000	+35000	75	11818	

In such cases, IRR can still be salvaged by examining incremental cash flows as shown here

Projects	$C_0$	$\mathcal{C}_1$	IRR (%)	NPV at 10%
E-D	-10000	+15000	50	3636



#### **IRR** in Conclusion

- Many things can go wrong with IRR, but it is still a very useful benchmark
- To see its utility, have a look at the project cash flows, NPV, and IRR estimates for two projects X and Y as shown here (\$, thousands)

Projects	$C_{0}$	$C_1$	$C_2$	$C_3$	NPV at 8%	IRR (%)
X	-9.0	2.9	4.0	5.4	1.4	15.58
Υ	-9000	2560	3540	4530	1.4	8.01

- Both of these projects offer the same positive NPV of \$1400
- As rational individuals you would select X over Y (Why?)
- The higher IRR associated with X (15.58%) reflects the low risk and efforts involved as compared with Y



# Capital investments with limited resources

- Capital is a scarce resource, thus it is not possible to select all the positive NPV projects
- Thus, firms would like to select those projects that offer highest NPV per dollar of investment

• Profitability index (PI) = 
$$\frac{NPV}{Initial Investment}$$

Cash Flows (\$ Mn)							
Project	C0	C1	C2	NPV at 10%	PI		
А	-10	+30	+5	21	2.1		
В	-5	+5	+20	16	3.2		
С	-5	+5	+15	12	2.4		



# Capital investments with limited resources

Let us add another project D, which needs \$40 Mn investment in second year

Project	C0	C1	C2	<b>NPV at 10%</b>	PI
А	-10	+30	+5	21	2.1
В	-5	+5	+20	16	3.2
С	-5	+5	+15	12	2.4
D	0	-40	+60	13	0.4

- The firm can only raise \$10 Mn in the second year: additional constraint of capital rationing
- The simple way of ranking projects as per PI may not work here
- This particular problem is rather simple, as A and D combined offer a higher NPV than B and C combined
- However, more complex problems are solved with linear programming (LP) techniques of technology KANPU

# Summary and concluding remarks



- In addition to NPV, other rules are also employed to examine alternate investments
- These include book rate of return, payback period, and IRR method
- Book rate of return is simply computed as book income divided by book value of investment
- Payback method examines the project cash flows against a certain specific cut-off period
- Only those projects with payback period is less than cut-off period, are considered
- Lastly, IRR is the discount rate at which the firm NPV is zero
- As per the IRR rule, firms should accept those projects that have an IRR greater than opportunity cost of capital



# Thanks!