Package 'MMLPDEA'

May 2, 2016

Type Package

Title FORTRAN LP interface and DEA-DDEA modeling and bootstrapping

Version 1.02

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Maintainer
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Depends Benchmarking,lpSolveAPI

Description Provides access to FORTRAN LP code and for DEA-DDEA modeling and bootstrapping.

License LGPL-2.1

LazyLoad yes

NeedsCompilation yes

Archs i386, x64

R topics documented:

`MMLPDEA-package` *MMLPDEA*

Description

Uses FORTRAN to bootstrap input/output/DEA/DDEA models.

Also provides an interface to Morris and Miller's open source linear programming Fortran code.

Details

Package:	MMLPDEA
Type:	Package
Version:	1.02
Date:	2016-4-29
License:	LGPL-2.1
LazyLoad:	yes

Author(s)

R-Fortran bootstrapping and random number generation interface/fortran code: Joe Atwood

Correction to Miller's code: Joe Atwood August 2015

The author makes no guarantee nor assumes any liability with repect to the accuracy of the results obtained from the code included in this package.

This material is based upon work partially supported by the National Institute of Food and Agriculture, U.S. Department of Agriculture, Hatch Poject under 1002636 and Hatch/Multi-Sate Project under 1005034.

Alan Miller fortran code obtained from: http://jblevins.org/mirror/amiller/

Site Statement: "This is an archived copy of the Fortran source code repository of Alan Miller previously located at http://users.bigpond.net.au/amiller/. It is hosted by Jason Blevins with permission. The site has been slightly reformatted, but the source code and descriptions below have not been modified. All code written by Alan Miller is released into the public domain."

Fortran linear programming code listing:

"smplx.f90 Linear programming using the simplex algorithm. This is a translation of the Fortran 66 program from the NSWC (Naval Surface Warfare Center) library written by Alfred Morris. There is also a simple test program t_smplx.f90. Needs the module constant.f90 which defines the precision and returns certain machine constants."

Fortran random number generation code listing:

"mt19937.f90 The 'Mersenne Twister' random number generator from Japan with a cycle of length (2^19937 - 1). mt19937a.f90 is a version for compilers which stop when there are integer overflows, as some do when compiler check options are enabled for debugging purposes. .... . mt19937.f90 was revised on 5 February 2002;"

GPL license statement contained in mt19937.f90 code:

! A Fortran-program for MT19937: Real number version

! Code converted using TO_F90 by Alan Miller ! Date: 1999-11-26 Time: 17:09:23 ! Latest revision - 5 February 2002 ! A new seed initialization routine has been added based upon the new ! C version dated 26 January 2002. ! This version assumes that integer overflows do NOT cause crashes. ! This version is compatible with Lahey's ELF90 compiler, ! and should be compatible with most full Fortran 90 or 95 compilers. ! Notice the strange way in which umask is specified for ELF90.

! genrand() generates one pseudorandom real number (double) which is ! uniformly distributed on [0,1]-interval, for each call. ! sgenrand(seed) set initial values to the working area of 624 words. ! Before genrand(), sgenrand(seed) must be called once. (seed is any 32-bit ! integer except for 0). ! Integer generator is obtained by modifying two lines. ! Coded by Takuji Nishimura, considering the suggestions by ! Topher Cooper and Marc Rieffel in July-Aug. 1997.

! This library is free software; you can redistribute it and/or modify it ! under the terms of the GNU Library General Public License as published by ! the Free Software Foundation; either version 2 of the License, or (at your ! option) any later version. This library is distributed in the hope that ! it will be useful, but WITHOUT ANY WARRANTY; without even the implied ! warranty of MERCHANTABILITY or FITNESS FOR A PARTICULAR PURPOSE. ! See the GNU Library General Public License for more details. ! You should have received a copy of the GNU Library General Public License ! along with this library; if not, write to the Free Foundation, Inc., ! 59 Temple Place, Suite 330, Boston, MA 02111-1307 USA

! Copyright (C) 1997 Makoto Matsumoto and Takuji Nishimura. ! When you use this, send an email to: matumoto@math.keio.ac.jp ! with an appropriate reference to your work.

!** ! Fortran translation by Hiroshi Takano. Jan. 13, 1999.

`DDEAboot` *Fortran bootstrapping of DDEA models*

Description

Fortran bootstrapping of DDEA models.

Usage

```
DDEAboot(X,Y,orient='ddea',RTS='crs',nboot=250,bootlist=NULL,dx=NULL,dy=NULL,
DX=NULL,DY=NULL,alpha=0.05,seedval=1001,MMLPV=2,itermax=1000,pullDATA=FALSE)
```

Arguments

`X`	An nDMU x nX matrix of Input observations
`Y`	An nDMU x nY matrix of Output observations
`orient`	Input efficiency "in", output efficiency "out", "inout", or "ddea". Used to create directions if dx,dy,DX,and DY are missing

RTS	Returns to Scale: "vrs","drs","crs", and "irs"
nboot	Number of bootstraps to complete
bootlist	list of nDMUboot DMU's to bootstrap. This is set to 1:nDMU if no entry.
dx	An nDMUboot x nX matrix of Input directions. Set internally if no entry.
dy	An nDMUboot x nY matrix of Output directions. Set internally if no entry.
DX	An nDMU x nX matrix of Input directions. Set internally using orient if no entry.
DY	An nDMU x nY matrix of Output directions. Set internally using orient if no entry.
alpha	Confidence Interval prob
seedval	A positive 32-bit integer
MMLPV	1=Miller's original code, 2=Miller's corrected code (Atwood-2015)
itermax	iteration limit for the LP
pullDATA	compute LPsol,DUAL,and "reduced cost"if TRUE

Value

h	bootstrapping h value
effvals	Vector of Efficiency Scores
effvals.bc	Bias Corrected Vector of Efficiency Scores
bias	estimated bias
var	paramater variances - see Benchmarking package
boot	nDMUboot by nboot matrix of bootstrapped efficiency scores
alpha	alpha level computed
CI	confidence intervals
effstatus	Status of Efficiency Scores indstat = 0 the problem was solved; indstat = 1 the problem has no solution; indstat = 2 itermax iterations were performed-more needed; indstat = 3 sufficient accuracy could not be maintained to solve the problem; indstat = 4 the problem has an unbounded solution; indstat = 5 input error detected; indstat = 6 the solution may have been obtained;
bootstatus	status matrix of bootstrapped efficiency scores
LPsol	matrix of LP solutions for constraint matrix without slack variables.
DUALS	matrix of dual values. INPUT DUALS then OUTPUT DUALS
RC	matrix of "reduced costs"
seedval	seedvalue used in Fortran bootstrapping
iternum	number of first stage LP iterations for each dmu in bootlist
iternumboot	number of bootstrap stage LP iterations

Author(s)

Joe Atwood

References

Peter Bogetoft and Lars Otto; *Benchmarking with DEA, SFA, and R*; Springer 2011.

Cinzia Dario and L. Simar; *Advanced Robust and Nonparametric Methods in Efficiency Analysis*. Methodology and Applications; Springer 2007.

Leopold Simar and Paul .W. Wilson (1998), "Sensitivity analysis of efficiency scores: How to bootstrap in nonparametric frontier models", *Management Science* 44, 49–61.

Examples

```
## not run
# ########################################################################
# # NOTE:These examples have been conducted with a dense primal
# # DEA or DDEA problem.  In our experience MMLP is not time competitive
# # with lpSolveAPI or other R lp packages when solving the
# # sparse dual DEA problem with nDMU+1 constraints.
########################################################################
## simulate coverage level for DDEAboot confidence intervals
########################################################################
########################################################################
#require(MMLPDEA)
########################################################################
#set.seed(1001)
########################################################################
##model inputs
########################################################################
#nDMU=1000
#nIN=3
#nOUT=1
#RTS='VRS'
#delta=0.8
#nsims=100
#nboot=2000
#alpha=0.05
#CI=matrix(0,nsims,2)
##directional efficiency score for given DMU1
#eff0=0.50
##DDEA "efficient" input/output values for DMU1
#(xe=rep(10,nIN))
##[1] 10 10 10
#(ye=prod(xe^(1/nIN))^delta)
##[1] 6.309573
########################################################################
## With in-out model dy=y0 and dx=x0
## ye=y0+eff*dy <==> ye=y0+eff*y0  <==> ye=(1+eff)*y0  <==> y0=ye/(1+eff) with 0<=eff
## xe=x0-eff*dx <==> xe=x0-eff*x0  <==> xe=(1-eff)*x0  <==> x0=xe/(1-eff) with 0<=eff<1
########################################################################
## Generate "inefficient point for DMU 1
#(x0=xe/(1-eff0))
##[1] 20 20 20
#(y0=ye/(1+eff0))
##[1] 4.206382
#######################################################
#time1=seconds()
#ns=1
#for(ns in 1:nsims){
```

```
#####################################################
##Generate "efficient points" for population of DMUs
#####################################################
##Generate nDMU points on efficient frontier
# XE=matrix(runif(nDMU*nIN,5,15),nDMU,nIN)
# YE=matrix((apply(XE^(1/nIN),1,prod))^delta,nDMU,1)
#####################################################
##Generate "inefficient points" for population of DMUs
#####################################################
##Generate DEA efficiency scores for population
#####################################################
# eff=rbeta(nDMU,1,5)
# summary(eff)
# eff[eff>0.90]=0.9
# X=XE/(1-eff)
# Y=YE/(1+eff)
##############
##put DMU 0 data in matrices
# (X[1,]=x0)
# (Y[1,]=y0)
# eff[1]=eff0
# DX=X
# DY=Y
#############################################################################
#tmp=DDEAboot(X,Y,orient='ddea',RTS=RTS,DX=DX,DY=DY,nboot=nboot,bootlist=1,alpha=alpha)
# CI[ns,]=tmp$CI
# INCI=ifelse(eff0>=CI[1:ns,1]&eff0<=CI[1:ns,2],1,0)
# (cover=round(mean(INCI),3))
# txt=paste('eff0',eff0,'rep',ns,'of',nsims,'coverest =',cover)
# M=cbind(as.matrix(CI[1:ns,]),eff0)
# matplot(M,type='l',lty=1,col=c(1,1,2),lwd=c(1,1,3),main=txt,ylab='CI')
#############################################################################
#}# end loop for(ns in 1:nsims)
#time2=seconds()
#############################################################################
#(cover=mean(INCI))
##[1] 0.86
#1-alpha
##[1] 0.95
#############################################################################
#time2-time1
##[1] 62.69
#############################################################################
```

DDEAboot_write *Create data file for use with DDEAboot Fortran interface*

Description

Creates/writes data file that can be read by the DDEAboot_MASTER interface available (but commented out) in the package's source code MMLPDEA_subroutines.f90 file To use this data, copy the DDEAboot_Master code from the source file, uncomment the code, and save a copy in an directory. You can then use Simply Fortran, Visual Studio, CodeBlocks, or similar software to compile and step into the fortran code.

Usage

```
DDEAboot_write(X,Y,orient='ddea',RTS='crs',nboot=250,bootlist=NULL,dx=NULL,dy=NULL,
DX=NULL,DY=NULL,alpha=0.05,seedval=1001,MMLPV=2,itermax=1000,pullDATA=FALSE,fname='DDEAboot_dat
```

Arguments

X	An nDMU x nX matrix of Input observations
Y	An nDMU x nY matrix of Output observations
orient	Input efficiency "in", output efficiency "out", "inout", or "ddea". Used to create directions if dx,dy,DX,and DY are missing
RTS	Returns to Scale: "vrs","drs","crs", and "irs"
nboot	Number of bootstraps to complete
bootlist	list of nDMUboot DMU's to bootstrap. This is set to 1:nDMU if no entry.
dx	An nDMUboot x nX matrix of Input directions. Set internally if no entry.
dy	An nDMUboot x nY matrix of Output directions. Set internally if no entry.
DX	An nDMU x nX matrix of Input directions. Set internally using orient if no entry.
DY	An nDMU x nY matrix of Output directions. Set internally using orient if no entry.
alpha	Confidence Interval prob
seedval	A positive 32-bit integer
MMLPV	1=Miller's original code, 2=Miller's corrected code (Atwood-2015)
itermax	iteration limit for the LP
pullDATA	compute LPsol,DUAL,and "reduced cost"if TRUE
fname	file name for fortran data

Author(s)

Joe Atwood

DDEAnCm *Fortran nCm bootstrapping of DDEA models*

Description

Fortran nCm bootstrapping of DDEA models. Uses our modification of Geyer's subsampling bootstrap suggestion to increase computational efficiency.

Note: Although this function allows the user to complete a nCm subsampling process for multiple DMU's at the same time, it is recommended that the user complete this process on one DMU at a time and that the user carefully examine the boxplots of the bootstrapped values . Our endogenous process for determining the subsample sizes in mlist may need to be overridden by the user's exogenously generated mlist when a given DMU's efficiency scores are close to a boundary such as one for the input model or zero for the DDEA model.

Usage

```
DDEAnCm(X,Y,orient='ddea',RTS='crs',nboot=250,bootlist=NULL,DX=NULL,DY=NULL,mlist=NULL,
mcells=10,seedval=1001,replaceum=FALSE,MMLPV=2,alpha=0.05,CILag=1,plotum=FALSE,plottxt='',
itermax=1000,pullDATA=FALSE)
```

Arguments

X	An nDMU x nX matrix of Input observations
Y	An nDMU x nY matrix of Output observations
orient	Input efficiency "in" output efficiency "out"
RTS	Returns to Scale: "vrs","drs","crs", and "irs"
nboot	Number of bootstraps to complete for each sample size m.
bootlist	list of nDMUboot DMU's to bootstrap. Set to 1:nDMU if no entry.
DX	An nDMUboot x nX matrix of Input directions. Set internally if no entry.
DY	An nDMUboot x nY matrix of Output directions. Set internally if no entry.
mlist	list of subsample sizes m. If NA, an mlist will be generated internally
mcells	number of mlevels to use or construct
seedval	A positive 32-bit integer
replaceum	Sample with replacement
MMLPV	1=Miller's original code, 2=Miller's corrected code (Atwood-2015)
alpha	Confidence Interval prob
CILag	Lag for m interval selection process
plotum	plot CI diagnostics use plotum=TRUE to plot
plottxt	text to be included in plot
itermax	iteration limit for LP for each memeber of bootlist
pullDATA	compute LPsol,DUAL,and "reduced cost"if TRUE

Value

effvals	Vector of Efficiency Scores
effvals.bc	Vector of Bias-Corrected Efficiency Scores
bias	Vector of estimated bias levels
mlist	list of sample sizes m
boot	nDMUboot by length(mlist) by nboot array of bootstrapped efficiency scores
mchosen	chosen m interval
alpha	alpha level computed
beta	beta level computed
CI	Confidence Intervals
effstatus	Status of Efficiency Scores indstat = 0 the problem was solved; indstat = 1 the problem has no solution; indstat = 2 itermax iterations were performed-more needed; indstat = 3 sufficient accuracy could not be maintained to solve the problem; indstat = 4 the problem has an unbounded solution; indstat = 5 input error detected; indstat = 6 the solution may have been obtained;
bootstatus	status array of bootstrapped efficiency scores (equal in dimension to boot array)

LPsol	matrix of LP solutions for constraint matrix without slack variables
DUALS	matrix of dual values-INPUT DUALS then OUTPUT DUALS
RC	matrix of "reduced costs"
seedval	seedval used
iternum	number of first stage LP iterations for each dmu in bootlist
iternumboot	number of bootstrap stage LP iterations

Author(s)

Joe Atwood

References

Geyer. C. J. "The Subsampling Bootstrap." http://www.stat.umn.edu/geyer/5601/notes/sub.pdf

Politis, D.N., Romano, J.P., Wolf, M., 1999. "Subsampling". Springer. New York.

Politis, D.N., Romano, J.P., Wolf, M., 2001. "On the asymptotic theory of subsampling." Statistica Sinica 11, 1105-1124.

Simar, L., Wilson, P.W., 2011. "Inference by the m Out of n Bbootstrap in Nonparametric Frontier Models." Journal of Productivity Analysis 36,33-53.

Simar, L. A. Vanhems, P.W. Wilson. 2012 "Statistical Inference for DEA Estimators of Directional Distances." European J. of Operational Research. 220:853-864.

Examples

```
## not run

# ###########################################################################
# # NOTE:These examples have been conducted with a dense primal
# # DEA or DDEA problem.  In our experience MMLP is not time competitive
# # with lpSolveAPI or other R lp packages when solving the
# # sparse dual DEA problem with nDMU+1 constraints.
###############################################################################
## simulate coverage level for DDEAnCm confidence intervals
###############################################################################
#require(MMLPDEA)
###############################################################################
#set.seed(1001)
###############################################################################
##model inputs
###############################################################################
#nDMU=1000
#nIN=3
#nOUT=1
#RTS='VRS'
#delta=0.8
#nsims=100
#nboot=2000
#alpha=0.05
#CI=matrix(0,nsims,2)
##directional efficiency score for DMU 0
#eff0=0.50
##DDEA "efficient" input/output values for DMU 0
#(xe=rep(10,nIN))
```

```
##[1] 10 10 10
#(ye=prod(xe^(1/nIN))^delta)
##[1] 6.309573
#############################################################################
## With in-out model dy=y0 and dx=x0
## ye=y0+eff*dy <==> ye=y0+eff*y0  <==> ye=(1+eff)*y0  <==> y0=ye/(1+eff) with 0<=eff
## xe=x0-eff*dx <==> xe=x0-eff*x0  <==> xe=(1-eff)*x0  <==> x0=xe/(1-eff) with 0<=eff<1
#############################################################################
## Generate "inefficient point for DMU 0
#(x0=xe/(1-eff0))
##[1] 20 20 20
#(y0=ye/(1+eff0))
##[1] 4.206382
#####################################################
#time1=seconds()
#ns=1
#for(ns in 1:nsims){
#####################################################
##Generate "efficient points" for population of DMUs
#####################################################
##Generate nDMU points on efficient frontier
# XE=matrix(runif(nDMU*nIN,5,15),nDMU,nIN)
# YE=matrix((apply(XE^(1/nIN),1,prod))^delta,nDMU,1)
#####################################################
##Generate "inefficient points" for population of DMUs
#####################################################
##Generate DDEA efficiency scores for population
#####################################################
# eff=rbeta(nDMU,1,5)
# summary(eff)
# eff[eff>0.90]=0.9
# X=XE/(1-eff)
# Y=YE/(1+eff)
##############
##put DMU 0 data in matrices
# (X[1,]=x0)
# (Y[1,]=y0)
# eff[1]=eff0
# DX=X
# DY=Y
#############################################################################
#tmp=DDEAnCm(X,Y,orient='inout',RTS=RTS,nboot=nboot,bootlist=1,alpha=alpha,CILag=2)
# CI[ns,]=tmp$CI
# INCI=ifelse(eff0>=CI[1:ns,1]&eff0<=CI[1:ns,2],1,0)
# (cover=round(mean(INCI),3))
# txt=paste('eff0',eff0,'rep',ns,'of',nsims,'coverest =',cover)
# M=cbind(as.matrix(CI[1:ns,]),eff0)
# matplot(M,type='l',lty=1,col=c(1,1,2),lwd=c(1,1,3),main=txt,ylab='CI')
#############################################################################
#}# end loop for(ns in 1:nsims)
#time2=seconds()
#############################################################################
#(cover=mean(INCI))
##[1] 0.92
#1-alpha
##[1] 0.95
#############################################################################
```

```
#time2-time1
##[1] 26.81
################################################################################
```

DDEAnCm_write *Create data file for use with DDEAnCm Fortran interface*

Description

Creates/writes data file that can be read by the DDEAnCm_MASTER interface available (but commented out) in the package's source code MMLPDEA_subroutines.f90 file To use this data, copy the DDEAnCm_Master code from the source file, uncomment the code, and save a copy in an directory. You can then use Simply Fortran, Visual Studio, CodeBlocks, or similar software to compile and step into the fortran code.

Usage

```
DDEAnCm_write(X,Y,orient='ddea',RTS='crs',nboot=250,bootlist=NULL,DX=NULL,DY=NULL,mlist=NULL,
mcells=10,seedval=1001,replaceum=FALSE,MMLPV=2,alpha=0.05,CILag=1,plotum=FALSE,plottxt='',
itermax=1000,pullDATA=FALSE,fname='DDEAnCm_data.csv')
```

Arguments

X	An nDMU x nX matrix of Input observations
Y	An nDMU x nY matrix of Output observations
orient	Input efficiency "in" output efficiency "out"
RTS	Returns to Scale: "vrs","drs","crs", and "irs"
nboot	Number of bootstraps to complete for each sample size m.
bootlist	list of nDMUboot DMU's to bootstrap. Set to 1:nDMU if no entry.
DX	An nDMUboot x nX matrix of Input directions. Set internally if no entry.
DY	An nDMUboot x nY matrix of Output directions. Set internally if no entry.
mlist	list of subsample sizes m. If NA, an mlist will be generated internally
mcells	number of mlevels to use or construct
seedval	A positive 32-bit integer
replaceum	Sample with replacement
MMLPV	1=Miller's original code, 2=Miller's corrected code (Atwood-2015)
alpha	Confidence Interval prob
CILag	Lag for m interval selection process
plotum	plot CI diagnostics use plotum=TRUE to plot
plottxt	text to be included in plot
itermax	iteration limit for LP for each memeber of bootlist
pullDATA	compute LPsol,DUAL,and "reduced cost"if TRUE
fname	file name for fortran data

Author(s)

Joe Atwood

dea.boot_DEAboot *DEAboot using R*

Description

The function dea.boot_DEAboot is borrowed and modified from the Benchmarking package to give the same answers as those obtained from the fortran code. We thank the authors of the Benchmarking package for allowing us to borrow and edit their code.

This function in included in the DEAboot package primarily to demonstrate that the Fortran code based call DEAboot generates results equivilent to those obtained from the Benchmarking package's function dea.boot if dea.boot is modified to use the same random numbers.

The function DEAboot can be run independently from the function dea.boot_DEAboot.

Usage

```
dea.boot_DEAboot(X, Y, NREP = 200, EFF = NULL, RTS = "vrs", ORIENTATION="in",
         alpha = 0.05, XREF = NULL, YREF = NULL, EREF = NULL,
       DIRECT = NULL, TRANSPOSE = FALSE, LP,printum=FALSE,printmod=5,saveum=FALSE,seedval=1001)
```

Arguments

X	Inputs of firms to be evaluated, a K x m matrix of observations of K firms with m inputs (firm x input)
Y	Outputs of firms to be evaluated, a K x n matrix of observations of K firms with n outputs (firm x input).
NREP	Number of bootstrap replicats
EFF	Efficiencies for (X,Y) relative to the technology generated from (XREF,YREF).
RTS	The returns to scale assumptions as in dea, only works for "vrs", "drs", and "crs"; more to come.
ORIENTATION	Input efficiency "in" (1), output efficiency "out" (2), and graph efficiency "graph" (3).
alpha	One minus the size of the confidence interval for the bias corrected efficiencies
XREF	Inputs of the firms determining the technology, defaults to X.
YREF	Outputs of the firms determining the technology, defaults to Y.
EREF	Efficiencies for the firms in XREF, YREF.
DIRECT	Does not yet work and is therefore not used.
TRANSPOSE	Input and output matrices are K x m and K x n for the default value TRANSPOSE=FALSE; this is standard in R for statistical models. When TRANSPOSE=TRUE data matrices are m x K and n x K.
LP	Only for debugging purposes.
printum	printum==TRUE prints runtime progress reports
printmod	if printum==TRUE, progress reports are printed every printmod'th iteration
saveum	if saveum!=FALSE, returns extra data at end of function call
seedval	A positive 32-bit seed value for the fortran random number generator. This value must equal the value sent to DEAboot to obtain identical answers from this function and the Fortran DEAboot call.

Details

See the Benchmarking package's documentation of the dea.boot function for a complete desription of the arguments returned by the dea.boot function.

Value

The returned values from both functions are as follows:

`eff`	Efficiencies
`eff.bc`	Bias-corrected efficiencies
`bias`	An array of bootstrap bias estimates for the firms in X,Y
`conf.int`	`K x 2` matrix with confidence interval for the estimated efficiencies
`var`	An array of bootstrap variance estimates for the firms in X,Y
`boot`	The replica bootstrap estimates of the Farrell efficiencies, a K times NREP matrix. Note the bootstrap estimates are sorted for each firm.

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Author(s)

The good stuff: Peter Bogetoft and Lars Otto <larsot23@gmail.com>

The bad stuff : Joe Atwood <jatwood@montana.edu>

References

Peter Bogetoft and Lars Otto; *Benchmarking with DEA, SFA, and R*; Springer 2011.

Cinzia Dario and L. Simar; *Advanced Robust and Nonparametric Methods in Efficiency Analysis*. Methodology and Applications; Springer 2007.

Leopold Simar and Paul .W. Wilson (1998), "Sensitivity analysis of efficiency scores: How to bootstrap in nonparametric frontier models", *Management Science* 44, 49–61.

Examples

```
#not run
```

---

dea.sample_DEAboot *resample efficiency scores in DEAboot*

Description

The function `dea.sample_DEAboot` is borrowed and modified from the Benchmarking package to give the same answers as those obtained from the fortran code. We thank the authors of the Benchmarking package for allowing us to borrow and edit their code for this demonstration.

Usage

```
dea.sample_DEAboot(e,h,K=NULL,seedval)
```

Arguments

e	original DEA eff estimates
h	kernal value
K	Number of bootstrap replicats
seedval	seedvalue for fortran random number generator

Details

See the Benchmarking package's documentation of the dea.sample function for a complete desription of the arguments returned by the dea.sample function.

Value

estar	Resampled Efficiencies
seedval	incremented seed value for fortran random number generator

Author(s)

The good stuff: Peter Bogetoft and Lars Otto <larsot23@gmail.com>

The bad stuff : Joe Atwood <jatwood@montana.edu>

Examples

```
#not run
```

DEAboot *Fortran bootstrapping of input/output DEA models*

Description

Fortran bootstrapping of input/output DEA models

Usage

```
DEAboot(X,Y,orient='in',RTS='crs',nboot=250,bootlist=NULL,alpha=0.05,
seedval=1001,MMLPV=2,itermax=1000,pullDATA=FALSE)
```

Arguments

X	An nDMU x nX matrix of Input observations
Y	An nDMU x nY matrix of Output observations
orient	Input efficiency "in" output efficiency "out"
RTS	Returns to Scale: "vrs","drs","crs", and "irs"
nboot	Number of bootstraps to complete. nboot=0 calculates DEA efficiency scores for each dmu but does not bootstrap the results
bootlist	list of DMU's to bootstrap. Set to 1:nDMU if no entry.
alpha	Desired confidence interval
seedval	A positive 32-bit integer
MMLPV	1=Miller's original code, 2=Miller's corrected code (Atwood-2015)
itermax	iteration limit for the LP
pullDATA	compute LPsol,DUAL,and "reduced cost"if TRUE

Value

h	bootstrapping h value
effvals	Vector of Efficiency Scores
effvals.bc	Bias Corrected Vector of Efficiency Scores
bias	estimated bias
var	paramater variances - see Benchmarking package
boot	nDMUboot by nboot matrix of bootstrapped efficiency scores
alpha	alpha level computed
CI	confidence intervals
effstatus	Status of Efficiency Scores indstat = 0 the problem was solved; indstat = 1 the problem has no solution; indstat = 2 itermax iterations were performed-more needed; indstat = 3 sufficient accuracy could not be maintained to solve the problem; indstat = 4 the problem has an unbounded solution; indstat = 5 input error detected; indstat = 6 the solution may have been obtained;
bootstatus	status matrix of bootstrapped efficiency scores
LPsol	matrix of LP solutions
DUALS	matrix of dual values.INPUT DUALS then OUTPUT DUALS
RC	matrix of "reduced costs" for constraint matrix without slack variables
seedval	seedvalue used in Fortran bootstrapping
iternum	number of first stage LP iterations for each dmu in bootlist
iternumboot	number of bootstrap stage LP iterations

Author(s)

Joe Atwood

References

Peter Bogetoft and Lars Otto; *Benchmarking with DEA, SFA, and R*; Springer 2011.

Cinzia Dario and L. Simar; *Advanced Robust and Nonparametric Methods in Efficiency Analysis*. Methodology and Applications; Springer 2007.

Leopold Simar and Paul .W. Wilson (1998), "Sensitivity analysis of efficiency scores: How to bootstrap in nonparametric frontier models", *Management Science* 44, 49–61.

Examples

```
############################################################
#not run
# ##########################################################
# # NOTE:These examples have been conducted with a dense primal
# # DEA or DDEA problem.  In our experience MMLP is not time competitive
# # with lpSolveAPI or other R lp packages when solving the
# # sparse dual DEA problem with nDMU+1 constraints.#require(MMLPDEA)
#set.seed(2015)
#graphics.off()
############################################################
#orient="out"         # 1=in, 2=out
#RTS="crs"           # 1=vrs, 2=drs, 3=crs, 4=irs
```

```
############################################################
#nDMU=250
#nboot=250
############################################################
## Define Cobb-Douglas technology with CRS
#b1=0.5
#b2=1-b1
############################################################
## Generate "input levels"
#x1=runif(nDMU,5,10)
#x2=runif(nDMU,5,10)
## Generate "frontier" output levels
#y1=x1^b1*x2^(1-b1)
## Generate "inverse output efficiency scores"
#eff0=seq(0.25,1.0,length.out=nDMU)
## Contract output levels away from the efficient frontier
#y1=eff0*y1
## Put input and output quantities into matrices X and Y
#X=as.matrix(cbind(x1,x2))
#Y=as.matrix(y1)
############################################################
#
############################################################
## Call the Fortran based DEAboot function
#time1=seconds() #Note: This function is in the MMLPDEA package.
# tmp1=DEAboot(X,Y,orient=orient,RTS=RTS,nboot=nboot)
#time2=seconds()
############################################################
## Run modified Benchmarking package bootstrapping code
#time3=seconds()
# tmp2=dea.boot_DEAboot(X,Y,NREP=nboot,RTS=RTS,ORIENTATION=orient)
#time4=seconds()
#################
## Run modified Benchmarking package bootstrapping code with
## internal status printing
#time5=seconds()
# tmp3=dea.boot_DEAboot(X,Y,NREP=nboot,RTS=RTS,ORIENTATION=orient,
# printum=TRUE,printmod=25)
##[1] "Range of dist: "
##[1] 1.000000 3.937427
##[1] "25 time = 1.63000000000011"
##[1] "50 time = 3.09999999999991"
##[1] "75 time = 4.63000000000011"
##[1] "100 time = 6.11000000000013"
##[1] "125 time = 7.59000000000015"
##[1] "150 time = 9.11000000000013"
##[1] "175 time = 10.5900000000001"
##[1] "200 time = 12.0700000000002"
##[1] "225 time = 13.5500000000002"
##[1] "250 time = 15.0500000000002"
##[1] "time = 15.1100000000001"
#time6=seconds()
############################################################
## Run Benchmarking package bootstrapping code
#time7=seconds()
#tmp4=dea.boot(X,Y,NREP=nboot,RTS=RTS,ORIENTATION=orient)
#time8=seconds()
```

```
############################################################
## Contrast DEAboot results to Benchmarking results
############################################################
#summary(tmp1$effvals-tmp2$eff)
##      Min.    1st Qu.     Median       Mean    3rd Qu.       Max.
##-4.434e-12 -7.748e-13 -7.139e-14 -1.916e-13  5.462e-13  2.589e-12
#summary(tmp1$effvals.bc-tmp2$eff.bc)
##      Min.    1st Qu.     Median       Mean    3rd Qu.       Max.
##-3.473e-06 -1.960e-10  1.710e-10 -1.190e-08  7.890e-10  3.384e-06
#summary(as.vector(tmp1$boot)-as.vector(tmp2$boot))
##      Min.    1st Qu.     Median       Mean    3rd Qu.       Max.
##-3.092e-04 -7.840e-09 -7.800e-10  1.190e-08  7.020e-09  3.122e-04
#summary(as.vector(tmp1$ci)-as.vector(tmp2$conf.int))
##      Min.    1st Qu.     Median       Mean    3rd Qu.       Max.
##-1.642e-04 -7.660e-09 -7.200e-10 -3.297e-07  4.880e-09  3.594e-08
########################
#(h1=tmp1$h)
##[1] 0.171173
#effhat1=tmp1$effvals
#boot1=tmp1$boot
########################
#(h2=tmp2$h)
##[1] 0.171173
#effhat2=as.vector(tmp2$eff)
#boot2=tmp2$boot
############################################################
#summary(effhat1-effhat2)
##      Min.    1st Qu.     Median       Mean    3rd Qu.       Max.
##-4.434e-12 -7.748e-13 -7.139e-14 -1.916e-13  5.462e-13  2.589e-12
#summary(as.vector(boot1)-as.vector(boot2))
##      Min.    1st Qu.     Median       Mean    3rd Qu.       Max.
##-3.092e-04 -7.840e-09 -7.800e-10  1.190e-08  7.020e-09  3.122e-04
#x11()
#plot(as.vector(boot1),as.vector(boot2))
#abline(0,1,col=2)
############################################################
## DEAboot computation time
#time2-time1
##[1] 0.95
## Benchmarking computation times
#time4-time3
##[1] 15.06
#time6-time5
##[1] 15.14
#time8-time7
##[1] 15.1
############################################################



############################################################################
## simulate coverage level for DEAboot confidence intervals
############################################################################
############################################################################
#set.seed(1001)
############################################################################
##model inputs
```

```
#############################################################################
#nDMU=1000
#nIN=3
#nOUT=1
#orient='in'
#RTS='VRS'
#delta=0.8
#nsims=100
#nboot=2000
#alpha=0.05
#CI=matrix(0,nsims,2)
##input efficiency score for DMU 0
#eff0=0.50
##DEA "efficient" input values for DMU 0
#(xe=rep(10,nIN))
##[1] 10 10 10
#(ye=prod(xe^(1/nIN))^delta)
##[1] 6.309573
#############################################################################
## Generate "inefficient point for DMU 0
#(x0=xe/eff0)
##[1] 20 20 20
#(y0=ye)
##[1] 6.309573
#######################################################
#time1=seconds()
#ns=1
#for(ns in 1:nsims){
#######################################################
##Generate "efficient points" for population of DMUs
#######################################################
##Generate nDMU points on efficient frontier
# XE=matrix(runif(nDMU*nIN,5,15),nDMU,nIN)
# YE=matrix((apply(XE^(1/nIN),1,prod))^delta,nDMU,1)
#######################################################
##Generate "inefficient points" for population of DMUs
#######################################################
##Generate DEA efficiency scores for population
#######################################################
# eff=rbeta(nDMU,5,1)
# summary(eff)
# X=XE/eff
# Y=YE
##############
##put DMU 0 data in matrices
# (X[1,]=x0)
# (Y[1,]=y0)
# eff[1]=eff0
#############################################################################
#tmp=DEAboot(X,Y,orient='in',RTS=RTS,nboot=nboot,bootlist=1,alpha=alpha)
# CI[ns,]=tmp$CI
# INCI=ifelse(eff0>=CI[1:ns,1]&eff0<=CI[1:ns,2],1,0)
# (cover=round(mean(INCI),3))
# txt=paste('eff0',eff0,'rep',ns,'of',nsims,'coverest =',cover)
# M=cbind(as.matrix(CI[1:ns,]),eff0)
# matplot(M,type='l',lty=1,col=c(1,1,2),lwd=c(1,1,3),main=txt,ylab='CI')
#############################################################################
```

```
#}# end loop for(ns in 1:nsims)
#time2=seconds()
################################################################################
#(cover=mean(INCI))
##[1] 0.89
#1-alpha
##[1] 0.95
################################################################################
#time2-time1
##[1] 67.85
################################################################################
```

DEAboot_write *Create data file for use with DEAboot Fortran interface*

Description

Creates/writes data file that can be read by the DEAboot_MASTER interface available (but commented out) in the package's source code MMLPDEA_subroutines.f90 file To use this data, copy the DEAboot_Master code from the source file, uncomment the code, and save a copy in an directory. You can then use Simply Fortran, Visual Studio, CodeBlocks, or similar software to compile and step into the fortran code.

Usage

```
DEAboot_write(X,Y,orient='in',RTS='crs',nboot=250,bootlist=NULL,alpha=0.05,
seedval=1001,MMLPV=2,itermax=1000,pullDATA=FALSE,fname='DEAboot_data.csv')
```

Arguments

X	An nDMU x nX matrix of Input observations
Y	An nDMU x nY matrix of Output observations
orient	Input efficiency "in" output efficiency "out"
RTS	Returns to Scale: "vrs","drs","crs", and "irs"
nboot	Number of bootstraps to complete. nboot=0 calculates DEA efficiency scores for each dmu but does not bootstrap the results
bootlist	list of DMU's to bootstrap. Set to 1:nDMU if no entry.
alpha	Desired confidence interval
seedval	A positive 32-bit integer
MMLPV	1=Miller's original code, 2=Miller's corrected code (Atwood-2015)
itermax	iteration limit for the LP
pullDATA	compute LPsol,DUAL,and "reduced cost"if TRUE
fname	file name for fortran data

Author(s)

Joe Atwood

lagMat *Generate a non-time series lagged matrix*

Description

lagMat generates a lagged matrix

Usage

```
lagMat(x,lags=2,Lzero='F')
```

Arguments

x	vector of data to be lagged
lags	specifies the lag length(s)
Lzero	include the zero lag vector in matrix

Value

lagMat returns a lagged matrix – See examples below

Author(s)

Joe Atwood

Examples

```
#not run
##########################################
# (x=1:10)
# [1] 1  2  3  4  5  6  7  8  9  10
#lagum(x,1)
# [1] NA  1  2  3  4  5  6  7  8  9
#lagum(x,3)
# [1] NA NA NA  1  2  3  4  5  6  7
#uplag(x)
# [1]  2  3  4  5  6  7  8  9 10 NA
#lagum(x,-1)
# [1]  2  3  4  5  6  7  8  9 10 NA
##########################################
#lagMat(x,2)
#      [,1] [,2]
# [1,]   NA   NA
# [2,]    1   NA
# [3,]    2    1
# [4,]    3    2
# [5,]    4    3
# [6,]    5    4
# [7,]    6    5
# [8,]    7    6
# [9,]    8    7
#[10,]    9    8
#lagMat(x,Lzero='T')
```

```
#      [,1] [,2] [,3]
# [1,]    1   NA   NA
# [2,]    2    1   NA
# [3,]    3    2    1
# [4,]    4    3    2
# [5,]    5    4    3
# [6,]    6    5    4
# [7,]    7    6    5
# [8,]    8    7    6
# [9,]    9    8    7
#[10,]   10    9    8
#lagMat(x,-1:2)
#      [,1] [,2] [,3] [,4]
# [1,]    2    1   NA   NA
# [2,]    3    2    1   NA
# [3,]    4    3    2    1
# [4,]    5    4    3    2
# [5,]    6    5    4    3
# [6,]    7    6    5    4
# [7,]    8    7    6    5
# [8,]    9    8    7    6
# [9,]   10    9    8    7
#[10,]   NA   10    9    8
#lagMat(x,2:-1)
#      [,1] [,2] [,3] [,4]
# [1,]   NA   NA    1    2
# [2,]   NA    1    2    3
# [3,]    1    2    3    4
# [4,]    2    3    4    5
# [5,]    3    4    5    6
# [6,]    4    5    6    7
# [7,]    5    6    7    8
# [8,]    6    7    8    9
# [9,]    7    8    9   10
#[10,]    8    9   10   NA
####################################
```

`lagum` *Generate a non-time series lagged vector*

Description

lagum generates a lagged vector

Usage

```
lagum(x, nlag = 1)
```

Arguments

`x`	vector of data to be lagged
`nlag`	specifies the lag length - can be negative for 'uplag'

Value

lagum returns a vector – See examples below

Author(s)

Joe Atwood

Examples

```
#not run
##########################################
#x=1:10
#lagum(x,1)
# [1] NA  1  2  3  4  5  6  7  8  9
#lagum(x,3)
# [1] NA NA NA  1  2  3  4  5  6  7
#uplag(x)
# [1]  2  3  4  5  6  7  8  9 10 NA
##########################################
```

LP_DF *Example data to demonstrate breakdown in MMLP code.*

Description

Example data to demonstrate breakdown in MMLP code.

Usage

```
data("LP_DF")
```

Format

A data frame with 6 observations on the following 8 variables.

`V1` a numeric vector

`V2` a numeric vector

`V3` a numeric vector

`V4` a numeric vector

`V5` a numeric vector

`V6` a numeric vector

`rest` a character vector

`rhs` a numeric vector

Details

Example data to demonstrate breakdown in MMLP code.

Examples

```
#not run
#data(LP_DF)
#require(lpSolve)
#(obj2=as.vector(t(LP_DF[6,1:6])))
#(A2=as.matrix(LP_DF[1:5,1:6]))
#(rest2=as.vector(LP_DF$rest[1:5]))
#(rhs2=as.vector(LP_DF$rhs[1:5]))
#MMLP(objtype='min',obj=obj2,A=A2,rest=rest2,rhs=rhs2,MMLPV=1)$objval
#lp("min",obj2,A2,rest2,rhs2)
#MMLP(objtype='min',obj=obj2,A=A2,rest=rest2,rhs=rhs2,MMLPV=2)$objval
```

MMLP *Morris-Miller Fortran LP code interface*

Description

Morris-Miller Fortran LP code interface

Usage

```
MMLP(objtype='max',obj,A,rest,rhs,itermax=1000,nsims=1,MMLPV=2)
```

Arguments

objtype	character string 'max' or 'min'
obj	vector of objective coefficients
A	matrix of constraint coefficients
rest	character vector of constraint signs '<=','>=', or'='
rhs	vector of RHS values
itermax	maximal number of LP iterations
nsims	number of repititions before returning results
MMLPV	1=Miller's original code, 2=Miller's corrected code (Atwood-2015)

Value

objval	objective value
xvals	If indstat = 0 or 6, xvals returns the solution, the slack, and the surplus variable levels
duals	dual values
rc	"reduced costs"
indstat	indstat = 0 the problem was solved; indstat = 1 the problem has no solution; indstat = 2 itermax iterations were performed-more needed; indstat = 3 sufficient accuracy could not be maintained to solve the problem; indstat = 4 the problem has an unbounded solution; indstat = 5 input error detected; indstat = 6 the solution may have been obtained;
iternum	number of iterations

Author(s)

R and Fortran interface, duals calculations: Joe Atwood

MMLP code:

WRITTEN BY ALFRED H. MORRIS JR.

NAVAL SURFACE WEAPONS CENTER

DAHLGREN, VIRGINIA

———————

INITIAL VERSION DEC 1977

LAST UPDATE OCT 1990

———————-

Converted using F90 intrinsics by

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Latest revision - 5 February 1997

obtained from: http://jblevins.org/mirror/amiller/

Site Statement: "This is an archived copy of the Fortran source code repository of Alan Miller previously located at http://users.bigpond.net.au/amiller/. It is hosted by Jason Blevins with permission. The site has been slightly reformatted, but the source code and descriptions below have not been modified. All code written by Alan Miller is released into the public domain."

Fortran linear programming code listing:

"smplx.f90 Linear programming using the simplex algorithm. This is a translation of the Fortran 66 program from the NSWC (Naval Surface Warfare Center) library written by Alfred Morris. There is also a simple test program t_smplx.f90. Needs the module constant.f90 which defines the precision and returns certain machine constants."

NOTE: Atwood modified Miller's code in August 2015 to correct solution error. See example below:

Examples

```
# not run
################################################################################
#Example 1
################################################################################
#Demonstrate potential error in original MM LP code
################################################################################
#data(LP_DF)
#require(lpSolve)
#(obj2=as.vector(t(LP_DF[6,1:6])))
#(A2=as.matrix(LP_DF[1:5,1:6]))
#(rest2=as.vector(LP_DF$rest[1:5]))
#(rhs2=as.vector(LP_DF$rhs[1:5]))
#MMLP(objtype='min',obj=obj2,A=A2,rest=rest2,rhs=rhs2,MMLPV=1)$objval
#lp("min",obj2,A2,rest2,rhs2)
#MMLP(objtype='min',obj=obj2,A=A2,rest=rest2,rhs=rhs2,MMLPV=2)$objval
################################################################################
#
#
```

```
# ##############################################################################
# Example 2
# ##############################################################################
# # Determine computation times required to solve the Wyndor example 100,000
# # times using loops with lpSolveAPI and MMLP and constrasting the
# # results to solving the Wyndor problem 100,000 times within the MMLP fortran code
# ##############################################################################
# rm(list=ls())
# ##############################################################################
# require(MMLPDEA)
# require(lpSolve)
# require(lpSolveAPI)
# ##############################################################################
# nsims=100000
# ##############################################################################
# #construct problem
# nr=3
# nc=2
# objtype='max'
# objmax=1
# obj=c(3,5)
# A=matrix(c(
#   c(1,0),
#   c(0,2),
#   c(3,2)
#  ),3,2,byrow=T)
# b=c(4,12,18)
# rest=c('<=','<=','<=')
# ##############################################################################
#
#
# ##############################################################################
# #set up lpSolveAPI object
# LP_API=make.lp(nrow=nr,ncol=nc)
#
# lp.control(LP_API,sense=objtype)
#
# set.objfn(LP_API,obj)
# for(i in 1:nr){
#  set.row(LP_API,i,A[i,])
# }
# set.constr.type(LP_API,rest)
# set.rhs(LP_API,b)
# ##################################################################
#
# ##################################################################
# #solve with lpSolve
# tmp=lp(objtype,obj,A,rest,b,compute.sens=TRUE)
# tmp$objval;tmp$solution;tmp$duals[1:nr]
# #[1] 36
# #[1] 2 6
# #[1] 0.0 1.5 1.0
# ##################################################################
# #solve with lpSolveAPI
# (status=solve(LP_API))
# #[1] 0
# get.objective(LP_API);get.variables(LP_API);get.dual.solution(LP_API)[2:(nr+1)]
```

```
# #[1] 36
# #[1] 2 6
# #[1] 0.0 1.5 1.0
# ###################################################################
# #solve with MMLP
# tmp2=MMLP(objtype=objtype,obj=obj,A=A,rest=rest,rhs=b)
# tmp2$objval;tmp2$xvals[1:nc];tmp2$duals
# #[1] 36
# #[1] 2 6
# #[1] 0.0 1.5 1.0
# ###################################################################
#
#
# ###################################################################
# # time to obtain nsims solutions
# ###################################################################
# time0=seconds()
# ############################
# # lpSolveAPI with loops
# obj1=0
# for(j1 in 1:nsims){
#   set.objfn(LP_API,obj)
#   for(i in 1:nr){
#    set.row(LP_API,i,A[i,])
#   }
#   set.constr.type(LP_API,rest)
#   set.rhs(LP_API,b)
#   (status=solve(LP_API))
#   obj1[j1]=get.objective(LP_API)
# }# end loop
# ############################
# time1=seconds()
# ############################
# #remove lpSolveAPI object
# delete.lp(LP_API)
# ############################
# time2=seconds()
# ############################
# # MMLP with loops
# obj2=0
# for(j2 in 1:nsims){
#  tmp=MMLP(objtype=objtype,obj=obj,A=A,rest=rest,rhs=b)
#  obj2[j2]=tmp$objval
# }
# ############################
# time3=seconds()
# ############################
# # MMLP with internal loops
# tmp=MMLP(objtype=objtype,obj=obj,A=A,rest=rest,rhs=b,nsims=nsims)
# ############################
# time4=seconds()
# ##########################################################
#
# ##########################################################
# time1-time0 # lpSolveAPI loop time
# #[1] 17.89
# time3-time2 # MMLP loop time
```

```
# #[1] 14.36
# time4-time3 # MMLP internal loop time
# #[1] 0.09
# ##########################################################
#

# ##########################################################
#
#
#
#
# ############################################################
# # Example 3: A more realistic example
# ############################################################
# # A DEA example that computes the efficiency score for each
# # of 10000 DMUs. The example uses traditional looping
# # with both lpSolve and MMLP and constrasts the "R" loop
# # times to the results of using fortran loops within DEAboot
# # (without running the bootstraps i.e. by setting nloop = 0)
# # to obtain the efficiency score estimates for each DMU.
# ############################################################
# require(MMLPDEA)
# require(lpSolveAPI)
# ############################################################
# set.seed(2015)
# ############################################################
# nDMU=10000
# ############################################################
# # Define Cobb-Douglas technology with CRS
# b1=0.5
# b2=1-b1
# ############################################################
# # Generate "input levels"
# x1=runif(nDMU,5,10)
# x2=runif(nDMU,5,10)
# # Generate "frontier" output levels
# y1=x1^b1*x2^(1-b1)
# # Generate "inverse output efficiency scores"
# inv_eff0=seq(0.25,1.0,length.out=nDMU)
# # Contract output levels away from the efficient frontier
# y1=inv_eff0*y1
# eff0=1/inv_eff0
# # Put input and output quantities into matrices X and Y
# X=as.matrix(cbind(x1,x2))
# Y=as.matrix(y1)
# ############################################################
# # set up output orientation model for DMU 1 and VRS
# objtype='max'
# obj=c(rep(0,nDMU),1)
#
# A=matrix(0,4,nDMU+1)
# A[1,1:nDMU]=t(Y); A[1,(nDMU+1)]=-Y[1,1]
# A[2:3,1:nDMU]=t(X)
# A[4,1:nDMU]=1
#
# b=c(0,X[1,],1)
# rest=c('>=','<=','<=','=')
```

```
# ############################################################
# #set up lpSolveAPI object
# LP_API=make.lp(nrow=nrow(A),ncol=ncol(A))
# lp.control(LP_API,sense=objtype)
# set.objfn(LP_API,obj)
# for(i in 1:nrow(A)){
# set.row(LP_API,i,A[i,])
# }
# set.constr.type(LP_API,rest)
# set.rhs(LP_API,b)
# ############################################################
# #solve with lpSolveAPI
# (status=solve(LP_API))
# #[1] 0
# get.objective(LP_API)
# #[1] 3.976337
# ############################################################
# #solve with MMLP
# tmp2=MMLP(objtype=objtype,obj=obj,A=A,rest=rest,rhs=b)
# tmp2$objval
# #[1] 3.976337
# ################################################################
#
# ################################################################
# # solve efficiency scores for all DMU's
# time_API=0;time_MMLP=0
# effhat_API=0;effhat_MMLP=0
#
# i=1
# for(i in 1:nDMU){
#  A[1,ncol(A)]=-Y[i,1]
#  b=c(0,X[i,],1)
#  time0=seconds()
#  set.mat(LP_API,1,ncol(A),-Y[i,1])
#  set.rhs(LP_API,b)
#  status=solve(LP_API)
#  (effhat_API[i]=get.objective(LP_API))
#  time1=seconds()
#  time_API=time_API+(time1-time0)
#
#  time0=seconds()
#  tmp2=MMLP(objtype=objtype,obj=obj,A=A,rest=rest,rhs=b)
#  (effhat_MMLP[i]=tmp2$objval)
#  time1=seconds()
#  time_MMLP=time_MMLP+(time1-time0)
#
#  if(i%%100==0) plot(i,nDMU,main=paste('dmu, nDMU',i,nDMU))
#
# } # end loop "for(i in 1:nDMU)"
# ############################################################
# # Compute eff scores using DEAboot with nboot=0
# time0=seconds()
#  tmp=DEAboot(X,Y,orient='out',RTS='vrs',nboot=0)
# time1=seconds()
# time_DEAboot=time1-time0
# ############################################################
# summary(effhat_API-effhat_MMLP)
```

```
# #      Min.    1st Qu.     Median       Mean    3rd Qu.       Max.
# #-1.028e-09 -6.000e-13  0.000e+00  1.841e-10  7.000e-13  4.352e-07
# summary(effhat_MMLP-tmp$effvals)
#   Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
#      0       0       0       0       0       0
# time_API;time_MMLP;time_DEAboot
# #[1] 33.3     # R looping time lpSolveAPI    (no bootstrapping)
# #[1] 12.22    # R looping time MMLP          (no bootstrapping)
# #[1] 6.63     # Fortran looping time DEAboot (no bootstrapping)
##############################################################
#
# ###################################################################
# # NOTE:These examples have been conducted with a dense primal
# # DEA or DDEA problem.  In our experience MMLP is not time competitive
# # with lpSolveAPI or other R lp packages when solving the
# # sparse dual DEA problem with nDMU+1 constraints.
# ###################################################################
```

---

nCm *pulls nCm samples*

Description

pulls nCm samples giving same results as in the Fortran DDEAnCm bootstrap code

Usage

```
nCm(nvals=1:10,m=5,replaceum=FALSE,seedval=1001)
```

Arguments

nvals	values to sample from
m	number of values to sample
replaceum	sample with TRUE or without FALSE replacement
seedval	seed value

Value

vector of m sampled values

Author(s)

Joe Atwood

Examples

```
#not run
###################################
# nCm(1:100,10)
###################################
```

newseed *newseed*

Description

generates new 32 bit seed value from seedval u=ugen(1,seedval) newseed=floor(u[1]*2147483645) if(newseed==0,newseed=1)

Usage

```
newseed(seedval)
```

Arguments

seedval	seed value for fortran random number generator

Value

newseed	new 32 bit seed value for fortran random number generator

Author(s)

Joe Atwood <jatwood@montana.edu>

Examples

```
newseed(1001)
```

normgen *generates normal random variates using uniform variates geenrated from Fortran code: mt19937.f90*

Description

generates normal random variates using the uniform twister algorithym in Fortran code: mt19937.f90

Usage

```
normgen(n,seedval)
```

Arguments

n	number of random numbers to simulate
seedval	a positive 32 bit integer seedvalue

Value

Returns a vector of normal variates

Author(s)

R and Fortran interface to mt19937.f90 code: Joe Atwood

Alan Miller fortran code obtained from: http://jblevins.org/mirror/amiller/

Site Statement: "This is an archived copy of the Fortran source code repository of Alan Miller previously located at http://users.bigpond.net.au/amiller/. It is hosted by Jason Blevins with permission. The site has been slightly reformatted, but the source code and descriptions below have not been modified. All code written by Alan Miller is released into the public domain."

Fortran random number generation code listing:

"mt19937.f90 The 'Mersenne Twister' random number generator from Japan with a cycle of length (2^19937 - 1). mt19937a.f90 is a version for compilers which stop when there are integer overflows, as some do when compiler check options are enabled for debugging purposes. .... . mt19937.f90 was revised on 5 February 2002;"

GPL license statement contained in mt19937.f90 code:

! A Fortran-program for MT19937: Real number version

! Code converted using TO_F90 by Alan Miller ! Date: 1999-11-26 Time: 17:09:23 ! Latest revision - 5 February 2002 ! A new seed initialization routine has been added based upon the new ! C version dated 26 January 2002. ! This version assumes that integer overflows do NOT cause crashes. ! This version is compatible with Lahey's ELF90 compiler, ! and should be compatible with most full Fortran 90 or 95 compilers. ! Notice the strange way in which umask is specified for ELF90.

! genrand() generates one pseudorandom real number (double) which is ! uniformly distributed on [0,1]-interval, for each call. ! sgenrand(seed) set initial values to the working area of 624 words. ! Before genrand(), sgenrand(seed) must be called once. (seed is any 32-bit ! integer except for 0). ! Integer generator is obtained by modifying two lines. ! Coded by Takuji Nishimura, considering the suggestions by ! Topher Cooper and Marc Rieffel in July-Aug. 1997.

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! Copyright (C) 1997 Makoto Matsumoto and Takuji Nishimura. ! When you use this, send an email to: matumoto@math.keio.ac.jp ! with an appropriate reference to your work.

!***! Fortran translation by Hiroshi Takano. Jan. 13, 1999.

Examples

```
##########################################
 x=normgen(100,seedval=2014)
```

RDDEAnCm *R nCm bootstrapping of DDEA models*

Description

R nCm bootstrapping of DDEA models. Uses our modification of Geyer's subsampling bootstrap suggestion to increase computational efficiency.

Comparison of R to Fortran nCm results and times Replicates Fortran procedures in R to facilitate user understanding of Fortran DDEAnCm process

Usage

```
RDDEAnCm(X,Y,orient='ddea',RTS='crs',nboot=250,bootlist=NULL,DX=NULL,DY=NULL,mlist=NULL,
mcells=10,seedval=1001,replaceum=FALSE,alpha=0.05,CILag=1,plotum=FALSE,plottxt='')
```

Arguments

X	An nDMU x nX matrix of Input observations
Y	An nDMU x nY matrix of Output observations
orient	Input efficiency "in" output efficiency "out"
RTS	Returns to Scale: "vrs","drs","crs", and "irs"
nboot	Number of bootstraps to complete for each sample size m.
bootlist	list of nDMUboot DMU's to bootstrap. Set to 1:nDMU if no entry.
DX	An nDMUboot x nX matrix of Input observations. Set internally if no entry.
DY	An nDMUboot x nY matrix of Output observations. Set internally if no entry.
mlist	list of subsample sizes m. If NA, an mlist will be generated internally
mcells	number of mlevels to use or construct
seedval	A positive 32-bit integer
replaceum	Sample with replacement
alpha	Confidence Interval prob
CILag	Lag for m interval selection process
plotum	plot CI diagnostics use plotum=TRUE to plot
plottxt	text to be included in plot

Value

effvals	Vector of Efficiency Scores
effvals.bc	Vector of Bias-Corrected Efficiency Scores
bias	Vector of estimated bias levels
mlist	list of sample sizes m
boot	nDMUboot by length(mlist) by nboot array of bootstrapped efficiency scores
mchosen	chosen m interval
alpha	alpha level computed
beta	beta level computed

CI	Confidence Intervals
effstatus	Status of Efficiency Scores indstat = 0 the problem was solved; indstat = 1 the problem has no solution; indstat = 2 itermax iterations were performed-more needed; indstat = 3 sufficient accuracy could not be maintained to solve the problem; indstat = 4 the problem has an unbounded solution; indstat = 5 input error detected; indstat = 6 the solution may have been obtained;
bootstatus	status array of bootstrapped efficiency scores (equal in dimension to boot array)
seedval	seedval used

Author(s)

Joe Atwood

References

Geyer. C. J. "The Subsampling Bootstrap." http://www.stat.umn.edu/geyer/5601/notes/sub.pdf

Politis, D.N., Romano, J.P., Wolf, M., 1999. "Subsampling". Springer. New York.

Politis, D.N., Romano, J.P., Wolf, M., 2001. "On the asymptotic theory of subsampling." Statistica Sinica 11, 1105-1124.

Simar, L., Wilson, P.W., 2011. "Inference by the m Out of n Bbootstrap in Nonparametric Frontier Models." Journal of Productivity Analysis 36,33-53.

Simar, L. A. Vanhems, P.W. Wilson. 2012 "Statistical Inference for DEA Estimators of Directional Distances." European J. of Operational Research. 220:853-864.

Examples

```
# not run
##############################################################################
## contrast and time R versus Fortran nCm bootstrap results
##############################################################################
#require(MMLPDEA)
#graphics.off()
##############################################################################
#set.seed(101)
##############################################################################
## model inputs
#nDMU=1000
#nIN=3
#nOUT=1
#delta=1
## directional efficiency score for given DMU1
#eff0=0.50
## DDEA "efficient" input/output values for DMU1
#(xe=rep(10,nIN))
##[1] 10 10 10
#(ye=prod(xe^(1/nIN))^delta)
##[1] 10
##############################################################################
## With in-out model dy=y0 and dx=x0
## ye=y0+eff*dy with eff>0 <=ye=y0+eff*y0 <=ye=(1+eff)*y0 <=y0=ye/(1+eff) with eff>0
## xe=x0-eff*dx <=xe=x0-eff*x0 <=xe=(1-eff)*x0 <=x0=xe/(1-eff) with 0<=eff<1
##############################################################################
##Generate "inefficient" point for DMU 1
```

```
#(x0=xe/(1-eff0))
##[1] 20 20 20
#(y0=ye/(1+eff0))
##[1] 6.666667
#######################################################
##Generate "efficient points" for population of DMUs
#######################################################
##Generate nDMU points on efficient frontier
# XE=matrix(runif(nDMU*nIN,5,15),nDMU,nIN)
# YE=matrix((apply(XE^(1/nIN),1,prod))^delta,nDMU,1)
#######################################################
##Generate "inefficient points" for population of DMUs
#######################################################
##Generate DEA efficiency scores for population
# eff=rbeta(nDMU,1,5)
# summary(eff)
##     Min.   1st Qu.    Median      Mean   3rd Qu.      Max.
##0.0002952 0.0554500 0.1266000 0.1654000 0.2321000 0.7771000
#
# eff[eff>0.90]=0.9
#
# X=XE/(1-eff)
# Y=YE/(1+eff)
#############
##put DMU 0 data in matrices
# (X[1,]=x0)
##[1] 20 20 20
# (Y[1,]=y0)
##[1] 6.666667
# eff[1]=eff0
#######################################################
##estimate eff scores for all DMU's
# time1=seconds()
# tmp1=RDDEAnCm(X,Y,orient='inout',RTS='CRS',nboot=0,bootlist=1:nDMU)
# time2=seconds()
# tmp2=DDEAnCm(X,Y,orient='inout',RTS='CRS',nboot=0,bootlist=1:nDMU)
# time3=seconds()
# summary(tmp1$effvals-tmp2$effvals)
##      Min.    1st Qu.     Median       Mean    3rd Qu.
##-6.051e-13 -5.762e-14  5.153e-14  4.751e-14  1.561e-13
##      Max.
## 5.463e-13
# plot(eff,tmp2$effvals)
# time2-time1
##[1] 1.7
# time3-time2
##[1] 0.13
# (time2-time1)/(time3-time2)
##[1] 13.07692
#######################################################
##conduct,time, and contrast R versus Fortran nCm bootstraps
# time4=seconds()
# tmp3=RDDEAnCm(X,Y,orient='inout',RTS='CRS',nboot=2000,bootlist=1)
# time5=seconds()
# tmp4=DDEAnCm(X,Y,orient='inout',RTS='CRS',nboot=2000,bootlist=1)
# time6=seconds()
# summary(as.vector(tmp3$boot-tmp4$boot))
```

```
##     Min.   1st Qu.    Median      Mean   3rd Qu.      Max.
##0.000e+00 0.000e+00 0.000e+00 2.252e-09 0.000e+00 6.987e-06
# time5-time4
##[1] 43.57
# time6-time5
##[1] 0.45
# (time5-time4)/(time6-time5)
##[1] 96.82222
################################################################################
```

`sampleum` *Samples with replacement using Fortran generated random numbers.*

Description

Samples with replacement using Fortran generated random numbers.

Usage

```
sampleum(nobs,x,seedval)
```

Arguments

`nobs`	sample size
`x`	values to sample from
`seedval`	seed value for fortran random number generator

Value

`xsample`	nobs values resampled from x

Author(s)

Joe Atwood <jatwood@montana.edu>

Examples

```
sampleum(10,1:5)
```

seconds *Pulls seconds from system clock*

Description

Pulls seconds from system clock.

Usage

```
seconds()
```

Arguments

none

Value

seconds from system clock

Author(s)

Joe Atwood <jatwood@montana.edu>

Examples

```
seconds()
```

ugen *obtains uniform random variates using Fortran code: mt19937.f90*

Description

generates uniform random variates using the twister algorithym in Fortran code: mt19937.f90

Usage

```
ugen(n,seedval)
```

Arguments

n	number of random numbers to simulate
seedval	a positive 32 bit integer seedvalue

Value

Returns a vector of uniform variates

Author(s)

R and Fortran interface to mt19937.f90 code: Joe Atwood

Alan Miller fortran code obtained from: http://jblevins.org/mirror/amiller/

Site Statement: "This is an archived copy of the Fortran source code repository of Alan Miller previously located at http://users.bigpond.net.au/amiller/. It is hosted by Jason Blevins with permission. The site has been slightly reformatted, but the source code and descriptions below have not been modified. All code written by Alan Miller is released into the public domain."

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GPL license statement contained in mt19937.f90 code:

! A Fortran-program for MT19937: Real number version

! Code converted using TO_F90 by Alan Miller ! Date: 1999-11-26 Time: 17:09:23 ! Latest revision - 5 February 2002 ! A new seed initialization routine has been added based upon the new ! C version dated 26 January 2002. ! This version assumes that integer overflows do NOT cause crashes. ! This version is compatible with Lahey's ELF90 compiler, ! and should be compatible with most full Fortran 90 or 95 compilers. ! Notice the strange way in which umask is specified for ELF90.

! genrand() generates one pseudorandom real number (double) which is ! uniformly distributed on [0,1]-interval, for each call. ! sgenrand(seed) set initial values to the working area of 624 words. ! Before genrand(), sgenrand(seed) must be called once. (seed is any 32-bit ! integer except for 0). ! Integer generator is obtained by modifying two lines. ! Coded by Takuji Nishimura, considering the suggestions by ! Topher Cooper and Marc Rieffel in July-Aug. 1997.

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!***! Fortran translation by Hiroshi Takano. Jan. 13, 1999.

Examples

```
x=ugen(100,seedval=2014)
```

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