Inpainting of Galaxy Redshift Surveys

Elisa Antolini[1], Ilaria Caiazzo[2], Jeremy S. Heyl[*2]
[1] *Dipartimento di Fisica e Geologia, Università degli Studi di Perugia, I-06123 Perugia, Italia*
[2] *Department of Physics and Astronomy, University of British Columbia, 6224 Agricultural Road, Vancouver, BC V6T 1Z1, Canada*

ABSTRACT

1 THE TECNHIQUE

The technique is straightforward to describe and to implement, and we will outline it below. Let the map be given by $a(\Omega)$ and the mask by $m(\Omega)$ where $m(\Omega) = 1$ where the underlying galaxies are visible.

(i) Set an initial guess for the underlying map.

$$y_1(\Omega) = \frac{\langle m(\Omega)a(\Omega)\rangle}{\langle m(\Omega)\rangle} \tag{1}$$

(ii) Calculate the residual of the current guess

$$r_t(\Omega) = m(\Omega)a(\Omega) - y_t(\Omega) \tag{2}$$

(iii) Expand the sum of the residuals in the unmasked region and the current guess in spherical harmonics.

$$A_{lm,t} = \int d\Omega Y_{lm}^* [m(\Omega)r_t(\Omega) + y_t(\Omega)] \tag{3}$$

(iv) Keep only the components with the largest amplitudes and set the amplitudes smaller than the threshold (λ_t) to zero.

(v) Calculate the new guess from the largest components

$$y_{t+1}(\Omega) = \sum_{|A_{lm,t}|>\lambda_t} A_{lm,t}Y_{lm}(\Omega). \tag{4}$$

(vi) Decrease the threshold λ_t and repeat from step (ii) until the stopping criterion is reached.

There is of course some art in choosing the size of the underlying basis, the thresholds and the stopping criterion. Here we expand the galaxy map to $l_{\max} = m_{\max} = 64$, so there are a total of 2,145 components. The threshold is set to keep a given fraction of the components at each step. The fraction increases from $10^{-3.5}$ to $10^{-0.5}$ over 200 iterations, so the initial representations use just a few components and the number of components increases to about 680 at the final iteration, so over two thirds of the spherical harmonic components are set to zero in the final map.

From the iterative procedure above it is apparent that the value of the guess within the masked region (where $m(\Omega) = 0$) does not contribute to the residual and does not influence the solution. However, the spherical harmonics that contribute to the data near the edge of the mask do influence the guess within the masked region.

fake test gives R=0.70

2 TESTS

2.1 Simulated Maps

To understand the effectiveness of these techniques we simulate galaxy sky maps with the Galactic plane hidden and cross-correlate the restructed galaxy maps with the original simulated map. For make the simulation as realistic as possible we use the angular power spectrum of the observed galaxy map from 2MASS to construct the test maps. These simulated maps by design have the same angular power spectrum as the real 2MASS data including the zone of avoidance but different phases, so they don't exhibit a zone of avoidance and they lack the potential higher order correlations that the data may exhibit. Fig. **??** depicts a particular example of this technique. We used the angular power spectrum of the upper panel to create one hundred independent maps with the same power spectrum; one of these is depicted in the middle panel of the figure. We masked the Galactic plane and used the infilling techinique to fill in the region. The lower panel depicts the difference between in the infilled map and the original.

To make statistic sense of the agreement we calculate Pearson's correlation coefficient (r) between the original data and the infilled reproductions within the infilled region for each of the trials and examine its cumulative distribution as depicted in Fig. 2. The distribution of r is well-characterized by a normal distribution with mean of 0.267 and a standard deviation of 0.10. For comparision the correlation coefficient of the galaxy map with a bootstrapped realisation of the same map over the test region is typically much higher $r = 0.97$, so clearly much information is lost in the reconstruction, but the test reveals that the infilling procedure does give a good first-order guess at the hidden structures.

2.2 Observed Maps

Here we will discuss in further detail the tests that we performed in Antolini & Heyl (2016). To summarize we determine the region masked by the Galaxy by finding the region in which the density of galaxies is either less than one tenth of the mean (from the upper panel of Fig. **??**) or in which the density of stars (from Fig. 2 Antolini & Heyl 2016) is greater than a threshold that accounts for the masking of the
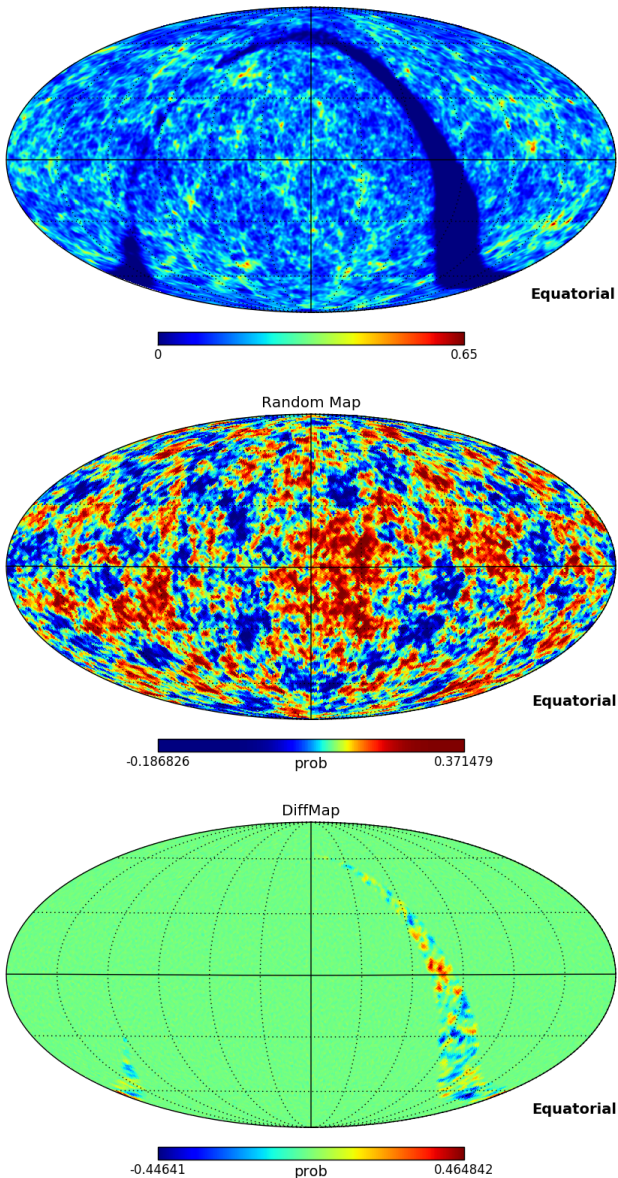
Figure 1. Upper: the relative surface density of galaxies in the 2-MASS Photometric Redshift Survey with photometric redshifts between 0.01 and 0.1, smoothed with a Gaussian of 0.6 degrees (0.01 radian), the input map. Middle: the test map constructed using the angular power spectrum of the map in the upper panel. Lower: we masked the Galactic plane of the middle panel and reconstructed the image using the techinque in § 1. The difference between the middle panel and the reconstructed map is depicted.

background galaxies due to the Large Magellanic Cloud, a feature that is apparent in both figures. Both of these masks are nearly the same, so we combine them.

To demonstrate its efficacy here, we will first apply the procedure to a galaxy map that has an additional mask as depicted in Fig. 3. We have masked both the Galactic plane and the equatorial plane. These equatorial region outside the Galactic plane is our test region where we know the underlying galaxy distribution, and we attempt to reconstruct it from the data outside the masked regions. Most of the struc-
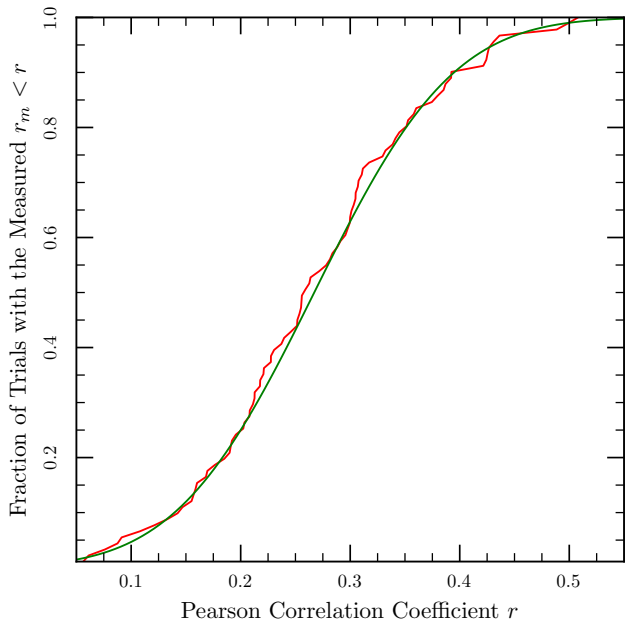

Figure 2. Cumulative distribution of r for 100 trials of the infilling procedure with simulated data in red. The smooth green curve traces the cumulative normal distribution with mean of 0.267 and standard derivation of 0.10.

tures within the equatorial region in the top panel are reproduced in the lower panel. However, to make statistic sense of the agreement we calculate Pearson's correlation coefficient (r) between the original data and the infilled reproduction within the infilled region outside of the Galactic plane. We obtain a value of $r = 0.25$ about the mean from the tests in § 2.1. To estimate the significance of this value, we performed two tests. First, we calculated the angular power spectrum of the original galaxy map and generated 1,000 galaxy maps consistent with this power spectrum. The largest obtained was 0.171, and the distribution was consistent with a normal distribution with $\sigma = 0.066$ and zero mean, so the observed correlation over the test region reaches nearly four-sigma significance.

The second test exploited the fact that the mask that we used was a strip in equatorial coordinates, so if we shift the reconstructed galaxy map relative to the input map in right ascension, we do not expect the two maps to be correlated. This shift test is depicted in the upper panel of Fig. 4. For zero degrees, the maximum correlation of 0.25 is achieved but for shifts greater than a few degrees the correlation appears to be centered about zero. The lower panel gives the cumulative distribution of correlation coefficients. The mean is just slightly less than zero and the standard deviation is 0.04, slightly less than for the first test. Again we see than the observed correlation for the unshifted data of 0.25 is statistically significant. The reconstruction contains much more information about the hidden galaxy distribution that one would expect by chance.
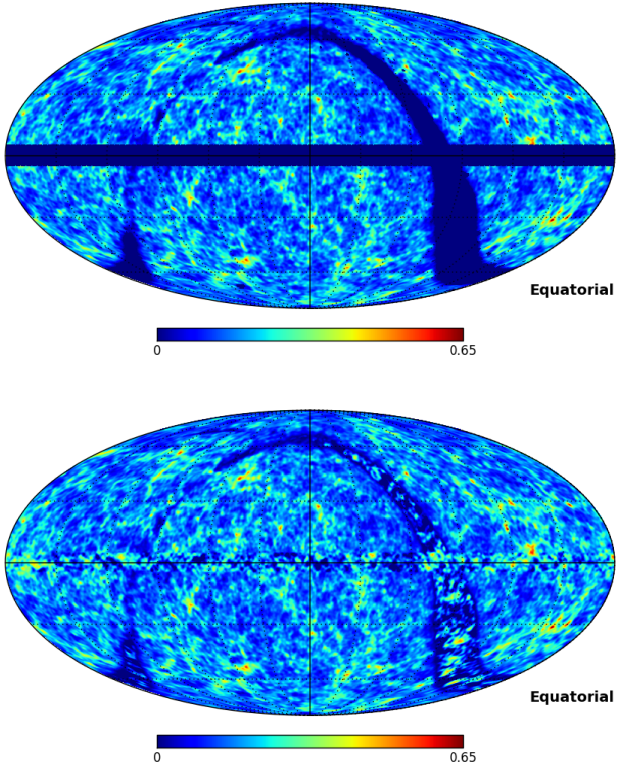
Figure 3. Upper: we masked both the Galactic plane and within five degrees of the celestial equator. Lower: the infilled galaxy distribution both in the Galactic plane and the equatorial plane to compare with the upper panel.
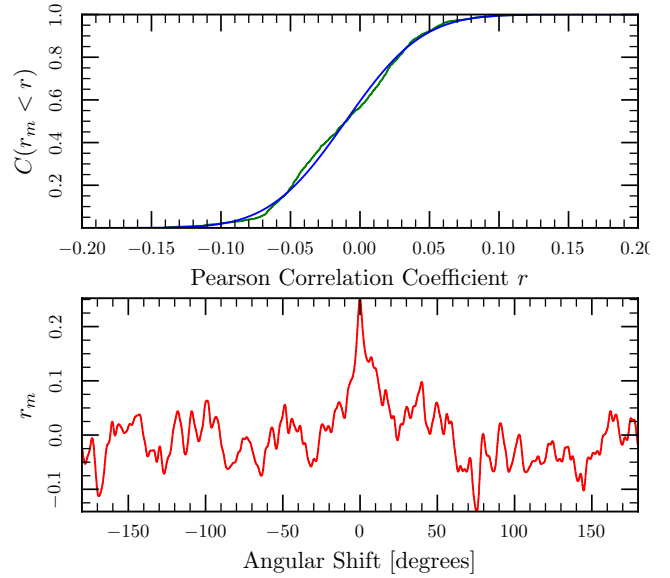

Figure 4. Upper panel: Pearson's correlation coefficient as a function of the relative shift between in the input map and the reconstuction calculated over the equatorial masked region. Lower panel: Cumulative distribution of r for shifts greater than 10 degrees. The smooth green curve traces the cumulative normal distribution with mean of -0.01 and standard derivation of 0.04.

3   RESULTS

After demonstrating the efficacy of the infilling procedure, we now perform the calculation to infill only through the Galactic plane (we did infill the Galactic plane in the tests as well). The upper panel of Fig **??** depicts the mask that we will use to mask the data in Fig. **??**, and the middle panel gives the initial galaxy map with the masked region filled in. There are several structures within masked region that connect with the structures on either side of the Galactic plane. Finally, we can estimate the signal-to-noise of the infilled map by calculate a series of galaxy density maps by resampling the 2MPZ to obtain new catalogues, new maps and new infilled maps. The lower panel of Fig. **??** depicts the signal-to-noise ratio of the map. Outside of the Galactic plane the signal-to-noise almost everywhere exceeds four. In the infilled region most of the overdense structures correspond to high signal-to-noise regions and therefore may provide a reliable estimate of the regions in the zone of avoidance where P(Position) is large.

4   DISCUSSION

REFERENCES

Antolini, E. & Heyl, J. S. 2016, Mon. Not. Roy. Ast. Soc., submitted (7 pages)