# Inpainting of Galaxy Redshift Surveys

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#### ABSTRACT

### THE TECNHIQUE

The technique is straightforward to describe and to implement, and we will outline it below. It is the same tecnique outlined Let the map be given by  $a(\Omega)$  and the mask by  $m(\Omega)$  where  $m(\Omega) = 1$  where the underlying galaxies are visible.

(i) Set an initial guess for the underlying map.

$$y_1(\Omega) = \frac{\langle m(\Omega)a(\Omega)\rangle}{\langle m(\Omega)\rangle} \tag{1}$$

(ii) Calculate the residual of the current guess

$$r_t(\Omega) = m(\Omega)a(\Omega) - y_t(\Omega) \tag{2}$$

(iii) Expand the sum of the residuals in the unmasked region and the current guess in spherical harmonics.

$$A_{lm,t} = \int d\Omega Y_{lm}^* \left[ m(\Omega) r_t(\Omega) + y_t(\Omega) \right]$$
 (3)

- (iv) Keep only the components with the largest amplitudes and set the amplitudes smaller than the threshold  $(\lambda_t)$ to zero
  - (v) Calculate the new guess from the largest components

$$y_{t+1}(\Omega) = \sum_{|A_{lm,t}| > \lambda_t} A_{lm,t} Y_{lm}(\Omega). \tag{4}$$

(vi) Decrease the threshold  $\lambda_t$  and repeat from step (ii) until the stopping criterion is reached.

There is of course some art in choosing the size of the underlying basis, the thresholds and the stopping criterion. Here we expand the galaxy map to  $l_{\text{max}} = m_{\text{max}} = 64$ , so there are a total of 2,145 components. The threshold is set to keep a given fraction of the components at each step. The fraction increases from  $10^{-3.5}$  to  $10^{-0.5}$  over 200 iterations, so the initial representations use just a few components and the number of components increases to about 680 at the final iteration, so over two thirds of the spherical harmonic components are set to zero in the final map.

From the iterative procedure above it is apparent that the value of the guess within the masked region (where  $m(\Omega) = 0$ ) does not contribute to the residual and does not influence the solution. However, the spherical harmonics that contribute to the data near the edge of the mask do influence the guess within the masked region.

#### TESTS

### Simulated Maps

To understand the effectiveness of these techniques we simulate galaxy sky maps with the Galactic plane hidden and cross-correlate the restructed galaxy maps with the original simulated map. To make the simulation as realistic as possible we use the angular power spectrum of the observed galaxy map from 2MASS to construct the test maps. These simulated maps by design have the same angular power spectrum as the real 2MASS data including the zone of avoidance but different phases, so they don't exhibit a zone of avoidance and they lack the potential higher order correlations that the data may exhibit. Fig. 1 depicts a particular example of this technique. We used the angular power spectrum of the upper panel to create one hundred independent maps with the same power spectrum; one of these is depicted in the middle panel of the figure. We masked the Galactic plane and used the infilling technique to fill in the region. The lower panel depicts the difference between in the infilled map and the original.

To make statistic sense of the agreement we calculate Pearson's correlation coefficient (r) between the original data and the infilled reproductions within the infilled region for each of the trials and examine its cumulative distribution as depicted in Fig. 2. The distribution of r is wellcharacterized by a normal distribution with mean of 0.267 and a standard deviation of 0.10. For comparision the correlation coefficient of the galaxy map with a bootstrapped realisation of the same map over the test region is typically much higher r = 0.97, so clearly much information is lost in the reconstruction, but the test reveals that the infilling procedure does give a good first-order guess at the hidden structures.

### Observed Maps

Here we will discuss in further detail the tests that we performed in Antolini & Heyl (2016). To summarize we determine the region masked by the Galaxy by finding the region in which the density of galaxies is either less than one tenth of the mean (from the upper panel of Fig. 1) or in which the density of stars (from Fig. 2 Antolini & Heyl 2016) is greater than a threshold that accounts for the masking of the

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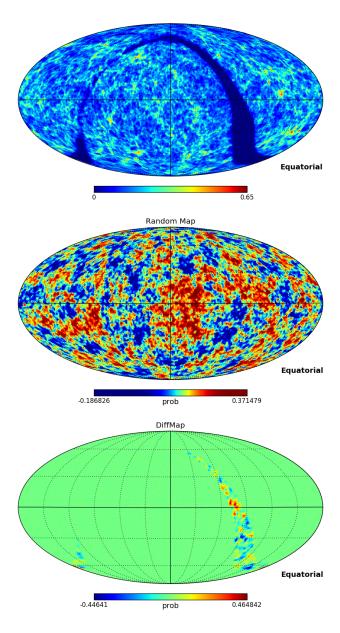


Figure 1. Upper: the relative surface density of galaxies in the 2-MASS Photometric Redshift Survey with photometric redshifts between 0.01 and 0.1, smoothed with a Gaussian of 0.6 degrees (0.01 radian), the input map. Middle: the test map constructed using the angular power spectrum of the map in the upper panel. Lower: we masked the Galactic plane of the middle panel and reconstructed the image using the techinque in § 1. The difference between the middle panel and the reconstructed map is depicted.

background galaxies due to the Large Magellanic Cloud, a feature that is apparent in both figures. Both of these masks are nearly the same, so we combine them.

To demonstrate its efficacy here, we will first apply the procedure to a galaxy map that has an additional mask as depicted in Fig. 3. We have masked both the Galactic plane and the equatorial plane. These equatorial region outside the Galactic plane is our test region where we know the underlying galaxy distribution, and we attempt to reconstruct it from the data outside the masked regions. Most of the struc-

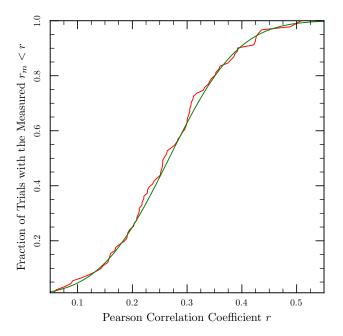


Figure 2. Cumulative distribution of r for 100 trials of the infilling procedure with simulated data in red. The smooth green curve traces the cumulative normal distribution with mean of 0.267 and standard derivation of 0.10.

tures within the equatorial region in the top panel are reproduced in the lower panel. However, to make statistic sense of the agreement we calculate Pearson's correlation coefficient (r) between the original data and the infilled reproduction within the infilled region outside of the Galactic plane. We obtain a value of r=0.25 about the mean from the tests in § 2.1. To estimate the significance of this value, we performed two tests. First, we calculated the angular power spectrum of the original galaxy map and generated 1,000 galaxy maps consistent with this power spectrum. The largest obtained was 0.171, and the distribution was consistent with a normal distribution with  $\sigma=0.066$  and zero mean, so the observed correlation over the test region reaches nearly four-sigma significance.

The second test exploited the fact that the mask that we used was a strip in equatorial coordinates, so if we shift the reconstructed galaxy map relative to the input map in right ascension, we do not expect the two maps to be correlated. This shift test is depicted in the upper panel of Fig. 4. For zero degrees, the maximum correlation of 0.25 is achieved but for shifts greater than a few degrees the correlation appears to be centered about zero. The lower panel gives the cumulative distribution of correlation coefficients. The mean is just slightly less than zero and the standard deviation is 0.04, slightly less than for the first test. Again we see than the observed correlation for the unshifted data of 0.25 is statistically significant. The reconstruction contains much more information about the hidden galaxy distribution that one would expect by chance.

The reason that we would like an infilled map is that we would like to optimize a survey of the infilled region to find the galaxies within it. The most efficient observing plan would be to follow the observed galaxy distribution as in Antolini & Heyl (2016). This strategy is plotted in

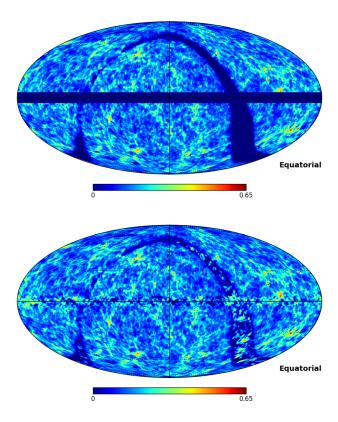


Figure 3. Upper: we masked both the Galactic plane and within five degrees of the celestial equator. Lower: the infilled galaxy distribution both in the Galactic plane and the equatorial plane to compare with the upper panel.

Fig. 5 in green. By surveying 37% of the solid angle, one can find 50% of the galaxies, a 35% increase in efficiency. The red curve depicts the recovery rate by following the reconstructed distribution in the region. By observing 46% of the reconstructed region, one can find 50% of the galaxies, an increase in efficiency of about nine percent relative to an random observing plan. By infilling the map, we can recover about 25% of the efficiency gain that we would have had if we knew the galaxy distribution. In fact the cumulative distribution using the infilled map is well approximated by using 25% of the true galaxy distribution (the green curve) and 75% from the uniform distribution (black line), so in a very concrete sense, the reconstruction recovers about one quarter of the data, approximately the same as the Pearson correlation coefficient.

### 3 RESULTS

After demonstrating the efficacy of the infilling procedure, we now perform the calculation to infill only through the Galactic plane (we did infill the Galactic plane in the tests as well). The upper panel of Fig 6 depicts the mask that we will use to mask the data. For the data we will be using the 2MPZ galaxies with redshifts from 0.01 to 0.02 to compare with the zone of avoidance survey of Staveley-Smith et al. (2016) within the same redshift range. The middle panel gives the initial galaxy map with the masked region filled

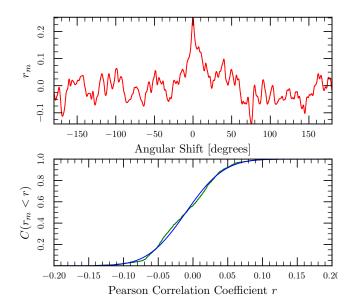


Figure 4. Upper panel: The curve depicts the Pearson's correlation coefficient as a function of the relative shift between in the input map and the reconstuction calculated over the equatorial masked region. Lower panel: The green curve tracks the cumulative distribution of r for shifts greater than 10 degrees. The smooth blue curve traces the cumulative normal distribution with mean of -0.01 and standard derivation of 0.04.

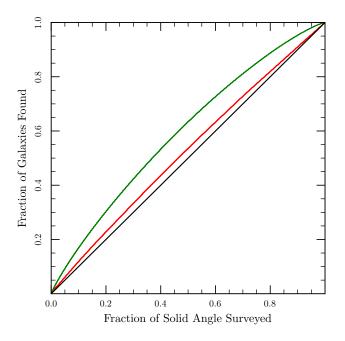


Figure 5. Fraction of galaxies found in the test region using the infilled data to develop the observing plan (red) and the real data (green) as a function of the solid angle surveyed.

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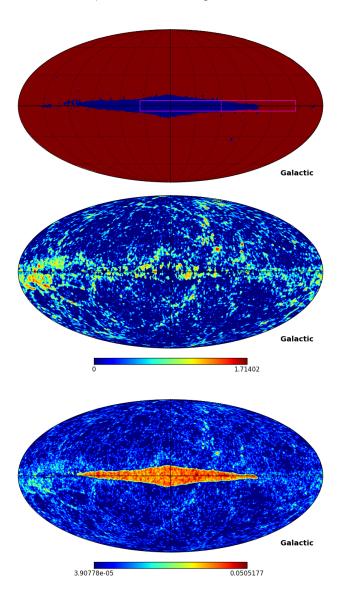


Figure 6. Upper: the mask used for the infilling procedure obtained by determining the regions where the galaxy density is less than one tenth of the mean or the star density lies above a given threshold (see text for details). The box shows the region surveyed by (Staveley-Smith et al. 2016). The region to the left of the dashed vertical line is our test region. Middle: the infilled galaxy distribution. Lower: The standard deviation of the infilled map obtained by bootstrapping the galaxy catalogue.

in. There are several structures within masked region that connect with the structures on either side of the Galactic plane. Finally, we can estimate the dispersion of the infilled map by calculate a series of galaxy density maps by resampling the 2MPZ to obtain new catalogues, new maps and new infilled maps. The lower panel of Fig. 6 depicts the dispersion ratio of the map. Outside of the Galactic plane the signal-to-noise almost everywhere exceeds four. In the infilled region most of the overdense structures correspond to high signal-to-noise regions.

We can compare these results with the discovery of galaxies within the zone of avoidance. We will focus on the recent HI Survey of Staveley-Smith et al. (2016) within five

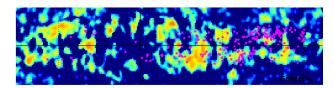


Figure 7. Detail from the Galactic Plane in Fig. 6 with the 232 galaxies with redshifts from 0.01 to 0.02 from the survey survey of Staveley-Smith et al. (2016)

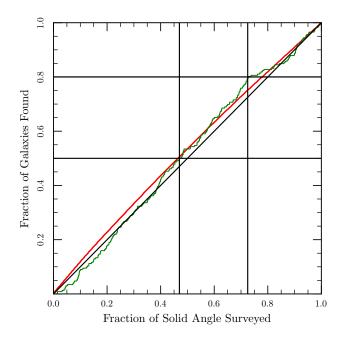
degrees of the Galactic plane. We restrict our analysis to those galaxies with  $l < 36^{\circ}$  and  $l > 300^{\circ}$ , that lie within the masked region in Fig. 6. Fig. 7 plots the 232 galaxies found in the zone of avoidance in the redshift range of 0.01 to 0.02 on top of the infilled map from Fig. 6. The correspondence between the overdensities in the infilled map and the observed galaxies is striking. To quantify this correspondence we use the infilled galaxy map to generate an observing plan as in Antolini & Heyl (2016) and to determine what fraction of the area must be surveyed to find a given fraction of the galaxies. Fig. 8 shows the fraction of the HZOA survev region that would have to be observed to find a given fraction of the HZOA galaxies (the green curve) if we use the infilled galaxy map as a guide. To recover half of the galaxies in the survey would require observing just 47% of the survey region, a 6% gain in efficiency. To recover 80% of the galaxies requires surveying 72.5% of the region, a 10% gain. There are a few important points to keep in mind. We have used the approximate photometric redshifts from the 2-MASS Photometric Redshift Survey to estimate the density of galaxies in the redshift range of 0.01 to 0.02 well outside the HZOA survey region. Next we extend this map into a region with no information using the data outside to achieve a 10% increase in the survey efficiency to find the bulk of the galaxies in the set redshift range. We have also plotted the results from the test in which we masked a region of sky, reconstructed and compared it back to the data. The red curve shows the efficiency of finding the galaxies in that reconstruction, and we see that it is similar to results

How to quantify this in a better way? If we pick 365 points at random they will not do as well as corresponding to our map as the real galaxies. But what we want is to ask if we use our map to find galaxies in the region, how well do we get the observed galaxies? Perhaps we should focus on telescope fields. How many random fields to observe to get half of the galaxies vs how many fields to observe following the obsplan?

## 4 DISCUSSION

## REFERENCES

Antolini, E. & Heyl, J. S. 2016, Mon. Not. Roy. Ast. Soc.,



**Figure 8.** Fraction of galaxies found in the HZOA survey (green) as a function of the solid surveyed. The red curve is the same as the red curve in Fig. 5.

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