ID	Expression	Analytical sum
1	$\sum_{n=1}^{\infty} \varepsilon^{-1+n}  ddP[n, 0]$	$\frac{-c w^2 + 3 s^2 \varepsilon}{w^5}$
2	$\sum_{n=1}^{\infty} n  \varepsilon^{-1+n}  ddP[n,  0]$	$\frac{-c w^2 + c (5 s^2 + 2 w^2) \varepsilon^2 - \varepsilon (w^2 + s^2 (-5 - 2 w^2 + 10 \varepsilon^2))}{7}$
3	$\sum_{n=1}^{\infty} n^2  \varepsilon^{-1+n}  ddP[n,  0]$	$-\frac{c}{w^{5}} + \frac{\left(-5+15 s^{2}-2 w^{2}+4 s^{2} w^{2}\right) \varepsilon}{w^{7}} + \frac{c \left(35 s^{2}+5 w^{2}+25 s^{2} w^{2}+w^{4}\right) \varepsilon^{2}}{w^{9}} - \frac{5 \left(-7+7 c^{4}+21 s^{2}-w^{2}+3 s^{2} w^{2}\right) \varepsilon^{3}}{w^{9}} - \frac{5 c \left(7 s^{2}+w^{2}\right) \varepsilon^{4}}{w^{9}} + \frac{35 s^{2} \varepsilon^{5}}{w^{9}}$
		$\frac{w^9}{w^9} - \frac{(-39+c^2)}{w^9} + \frac{33}{w^9}$ $\frac{9 s^2 \varepsilon (1+15 c \varepsilon+18 (-2+c^2) \varepsilon^2+c (-39+c^2) \varepsilon^3-3 (-20+c^2) \varepsilon^4-9 c \varepsilon^5-8 \varepsilon^6)}{w^{11}} +$
4	$\sum_{n=1}^{\infty} n^3 \varepsilon^{-1+n} ddP[n, 0]$	$\frac{1}{w^{9}} \left( -4 c^{4} \varepsilon^{3} + 9 c^{3} \varepsilon^{2} \left( -6 + \varepsilon^{2} \right) - 3 \varepsilon \left( -5 + 13 \varepsilon^{2} + 3 \varepsilon^{4} \right) + 3 c^{2} \varepsilon \left( -10 + 27 \varepsilon^{2} + 6 \varepsilon^{4} \right) + c \left( -1 + 72 \varepsilon^{2} - 66 \varepsilon^{4} + 8 \varepsilon^{6} \right) \right)$
		$-\frac{8 + 4 + (-7 + 4 + 3^{2}) + (-3 + 4 + 2 + 3 + 2 + 4 + 2 + 4 + 2 + 4 + 2 + 4 + 4 + 4$
5	$\sum_{n=1}^{\infty} \frac{\varepsilon^{-1+n} ddP[n,0]}{n}$	$4 w^{3} (1+w-c \varepsilon)^{2}$ $\frac{\varepsilon (5-2 s^{2}+\varepsilon^{2})-2 c (1+2 \varepsilon^{2})}{w^{2} (1+w-c \varepsilon)^{2}}$
		$\frac{2 s^{2} \varepsilon}{w^{2} (1+w-c \varepsilon)^{2}} + \frac{-c+\varepsilon+2 s^{2} \varepsilon}{w (1+w-c \varepsilon)^{2}} +$
6	$\sum_{n=2}^{\infty} \frac{\varepsilon^{-1+n} ddP[n,0]}{-1+n}$	$\frac{c  w - 6  c^2  \varepsilon + \left(4 + \left(-3 + 5  s^2\right)  w\right)  \varepsilon}{\left(1 + w - c  \varepsilon\right)^2}  +  \frac{\varepsilon  \left(s^2 + c  \varepsilon  \left(-1 + c^2  \left(1 - w^3  \left(-3 + \text{Log}\left[2\right]\right)\right)\right)\right)}{w^3  \left(1 + w - c  \varepsilon\right)^2}  + \\$
	211=2 -1+n	$\frac{c\left(-\varepsilon^2 \log[2] - (1+w) \log[4] + c\varepsilon\left(-2+w \log[4] + \log[16]\right)\right)}{\left(1+w-c\varepsilon\right)^2} +$
		$\frac{\text{c} \left(2 (1+\text{w}) - 2 \text{c} (2+\text{w}) \varepsilon - \left(-2+\text{s}^2\right) \varepsilon^2\right) \text{Log}[1+\text{w}-\text{c} \varepsilon]}{\left(1+\text{w}-\text{c} \varepsilon\right)^2}$
7	$\sum_{n=1}^{\infty} \frac{\varepsilon^{-1+n} ddP[n,0]}{1+n}$	$\frac{-C + C \; W + \varepsilon}{S^2 \; W \; \varepsilon^2} \; + \; \frac{-\varepsilon + C \; \varepsilon^2}{W^3 \; \varepsilon^2}$
		$\frac{s(-2+w^2)}{w^5} + \frac{c s(-50+9 w^2) \varepsilon}{w^7} + \frac{5 s(28+w^4-c^2(49+6 w^2)) \varepsilon^2}{w^9} - \frac{1}{w^{11}}$
8	$\sum_{n=1}^{\infty} n^2  \varepsilon^{-1+n}  ddP[n, 1]$	5 s $\varepsilon^3$ $\left(-98 c^4 \varepsilon + 16 c^3 \left(7 + 2 \varepsilon^2\right) + 6 c^2 \varepsilon \left(11 + 3 \varepsilon^2\right) + \right)$
	1.0	$\varepsilon \left(79 + 63 \text{ s}^4 - 45 \varepsilon^2 + 2 \varepsilon^4\right) + c \left(-139 - 34 \varepsilon^2 + 7 \varepsilon^4\right)\right)$ $s \left(35 \text{ s}^2 \varepsilon^2 \left(1 + (c - 2\varepsilon)\varepsilon\right) + w^4 \left(-1 + 2\varepsilon \left(-2 c + \varepsilon\right)\right) + 5 w^2 \varepsilon \left(2\varepsilon + c \left(-3 - 5 c\varepsilon + 6\varepsilon^2\right)\right)\right)$
9	$\sum_{n=1}^{\infty} n  \varepsilon^{-1+n}  ddP[n, 1]$	w <sup>9</sup>
10	$\sum_{n=1}^{\infty} \varepsilon^{-1+n} ddP[n, 1]$	$\frac{15 s^3 \varepsilon^2}{w^7} - \frac{s (w^2 + 9 c \varepsilon)}{w^5}$
11	$\sum_{n=1}^{\infty} \frac{\varepsilon^{-1+n} ddP[n,1]}{n}$	$-\frac{s}{w^3} - \frac{3 s (c-\varepsilon) \varepsilon}{w^5} + \frac{s \varepsilon^2 ((1+w)^2 - c \varepsilon)}{w^3 (1+w-c \varepsilon)^2}$
12	$\sum_{n=1}^{\infty} \frac{\varepsilon^{-1+n}  ddP[n,1]}{1+n}$	$S\left(\frac{1}{w^{3}} - \frac{3(1-c\epsilon)}{w^{5}} + \frac{\frac{1}{w} + \frac{(1+w)^{2}}{1+w-c\epsilon}}{w^{2}(1+w-c\epsilon)}\right)$
13	$\sum_{n=1}^{\infty} \frac{\varepsilon^{-1+n} ddP[n,1]}{n^2}$	$-\frac{s}{w^3} - \frac{1}{sw} + \frac{\left(1+c^2\right) Log\left[\frac{1+c}{c+w-\varepsilon}\right] + 2 c Log\left[\frac{1}{2} (1+w-c\varepsilon)\right]}{s^3 \varepsilon}$
	_	$\frac{12 (1-2 s^{2}) \varepsilon}{w^{5}} + \frac{15 c (2-19 s^{2}) \varepsilon^{2}}{w^{7}} +$
14	$\sum_{n=2}^{\infty} n  \varepsilon^{-1+n}  ddP[n, 2]$	$\frac{15 \left(-35  {s}^2 + 63  {s}^4 + 2  \left(1 - 2  {c}^2\right)  {w}^2\right)  \varepsilon^3}{{w}^9}  +  \frac{105  {s}^2  \varepsilon^4  \left(9  {c}  {s}^2 + 5  {c}  {w}^2 - 9  {s}^2  \varepsilon\right)}{{w}^{11}} \\ \frac{3  \varepsilon  \left(\left(2 - 4  {s}^2\right)  {w}^4 - 25  {c}  {s}^2  {w}^2  \varepsilon + 35  {s}^4  \varepsilon^2\right)}{2  {c}^2}  +  \frac{3  \varepsilon  \left(\left(2 - 4  {s}^2\right)  {w}^4 - 25  {c}  {s}^2  {w}^2  \varepsilon + 35  {s}^4  \varepsilon^2\right)}{2  {c}^2}  +  \frac{3  \varepsilon  \left(\left(2 - 4  {s}^2\right)  {w}^4 - 25  {c}  {s}^2  {w}^2  \varepsilon + 35  {s}^4  \varepsilon^2\right)}{2  {c}^2}  +  \frac{3  \varepsilon  \left(\left(2 - 4  {c}^2\right)  {w}^4 - 25  {c}  {c}^2  {w}^2  \varepsilon + 35  {c}^4  \varepsilon^2\right)}{2  {c}^2}  +  \frac{3  \varepsilon  \left(\left(2 - 4  {c}^2\right)  {w}^4 - 25  {c}  {c}^2  {w}^2  \varepsilon + 35  {c}^4  \varepsilon^2\right)}{2  {c}^2}  +  \frac{3  \varepsilon  \left(\left(2 - 4  {c}^2\right)  {c}^2  {c}^2  {c}^2  {c}^2  \varepsilon^2\right)}{2  {c}^2}  +  \frac{3  \varepsilon  \left(\left(2 - 4  {c}^2\right)  {c}^2  {c}^2  {c}^2  {c}^2  {c}^2  {c}^2  \varepsilon^2\right)}{2  {c}^2}  +  \frac{3  \varepsilon  \left(\left(2 - 4  {c}^2\right)  {c}^2  {c}$
15	$\sum_{n=2}^{\infty} \varepsilon^{-1+n} ddP[n, 2]$	w <sup>9</sup>
16	$\sum_{n=2}^{\infty} \frac{\varepsilon^{-1+n} ddP[n,2]}{n}$	$\frac{2\left(-2+2w^3\right)}{s^2w^3\varepsilon} + \frac{3c\left(-1+w^2+c\varepsilon\right)}{w^5} + \frac{2c\left(1+2w^2+c\varepsilon\right)}{s^2w^3} + \\ \frac{3s^2\varepsilon\left(-3+\varepsilon\left(c+2\varepsilon\right)\right)}{w^7} + \frac{6c\left(\varepsilon+c\left(-2+2w+c\varepsilon\right)\right)}{s^4w\varepsilon}$
		$\frac{9 c + 4 c^{3} - c^{5}}{s^{4}} + \frac{5 c \varepsilon^{2} \left(-11 + c^{2} + 10 c \varepsilon - 30 \varepsilon^{2}\right)}{w^{7}} +$
17	$\sum_{n=2}^{\infty} \frac{\varepsilon^{-1+n} ddP[n,2]}{-1+n}$	$\frac{(c-\varepsilon) (1+2\varepsilon (c+6\varepsilon))}{w^5} - \frac{2 (c-\varepsilon) (-1+\varepsilon^2 (-25+6c\varepsilon-4\varepsilon^2))}{s^2 w^5} +$
		$\frac{12 \; \left(\text{c-}\varepsilon\right) \; \left(-1\text{-}\varepsilon^2 \; \left(6\text{+}\varepsilon^2\right)\text{+4 c} \; \left(\varepsilon\text{+}\varepsilon^3\right)\right)}{\text{s}^4 \; \text{w}^5} \; - \; \frac{5 \; \varepsilon \; \left(3\text{+}\text{c}^4\text{+20 c}^2 \; \varepsilon^2 \; \left(2\text{+}\varepsilon^2\right)\text{-4 c} \; \varepsilon \; \left(5\text{+10 } \varepsilon^2\text{+}\varepsilon^4\right)\right)}{\text{s}^2 \; \text{w}^7}$
		$-\frac{7 c (31+5 c^{4}-26 s^{2})}{s^{4} w^{7}}+\frac{2 c (5+c^{2}) (-1+w^{7})}{s^{4} w^{7} \varepsilon^{2}}+\frac{14 (5+c^{4}-5 s^{2})}{s^{4} w^{7} \varepsilon}+$
18	$\sum_{n=2}^{\infty} \frac{\varepsilon^{-1+n} ddP[n,2]}{1+n}$	$\frac{\left(181+200 \ c^{4}+39 \ c^{6}-183 \ s^{2}\right) \ \varepsilon}{s^{4} \ w^{7}} \ - \ \frac{c \ \left(3 \ \left(99+40 \ c^{4}+c^{6}\right)-241 \ s^{2}\right) \ \varepsilon^{2}}{s^{4} \ w^{7}} \ +$
		$\frac{\left(103+155\;c^{4}-6\;c^{6}-86\;s^{2}\right)\;\epsilon^{3}}{s^{4}\;w^{7}}\;+\;\frac{4\;\left(-3+2\;s^{2}\right)\;\left(7\;c-\epsilon\right)\;\epsilon^{4}}{s^{4}\;w^{7}}$
10	$\sum_{n=2}^{\infty} \frac{\varepsilon^{-1+n} ddP[n,2]}{n^2}$	$-\frac{3 s^{2} \varepsilon}{w^{5}} + \frac{-2 - c^{2} + 2 w + c^{2} w - 3 c \varepsilon}{s^{2} w \varepsilon} - \frac{w^{2} - w^{3} + \varepsilon^{2}}{w^{3} \varepsilon} - \frac{12 c^{2} Log[2]}{s^{4} \varepsilon} -$
13	∠n=2	$\frac{\text{Log[16]}}{\text{s}^2 \ \varepsilon} \ + \ \frac{2 \ \text{c} \ \left(5 + \text{c}^2\right) \ \text{Log}\left[-\frac{\text{c} + \text{w} + \varepsilon}{\text{-}1 + \text{c}}\right]}{\text{s}^4 \ \varepsilon} \ + \ \frac{4 \ \left(1 + 2 \ \text{c}^2\right) \ \text{Log[1 + w - c} \ \varepsilon]}{\text{s}^4 \ \varepsilon}$