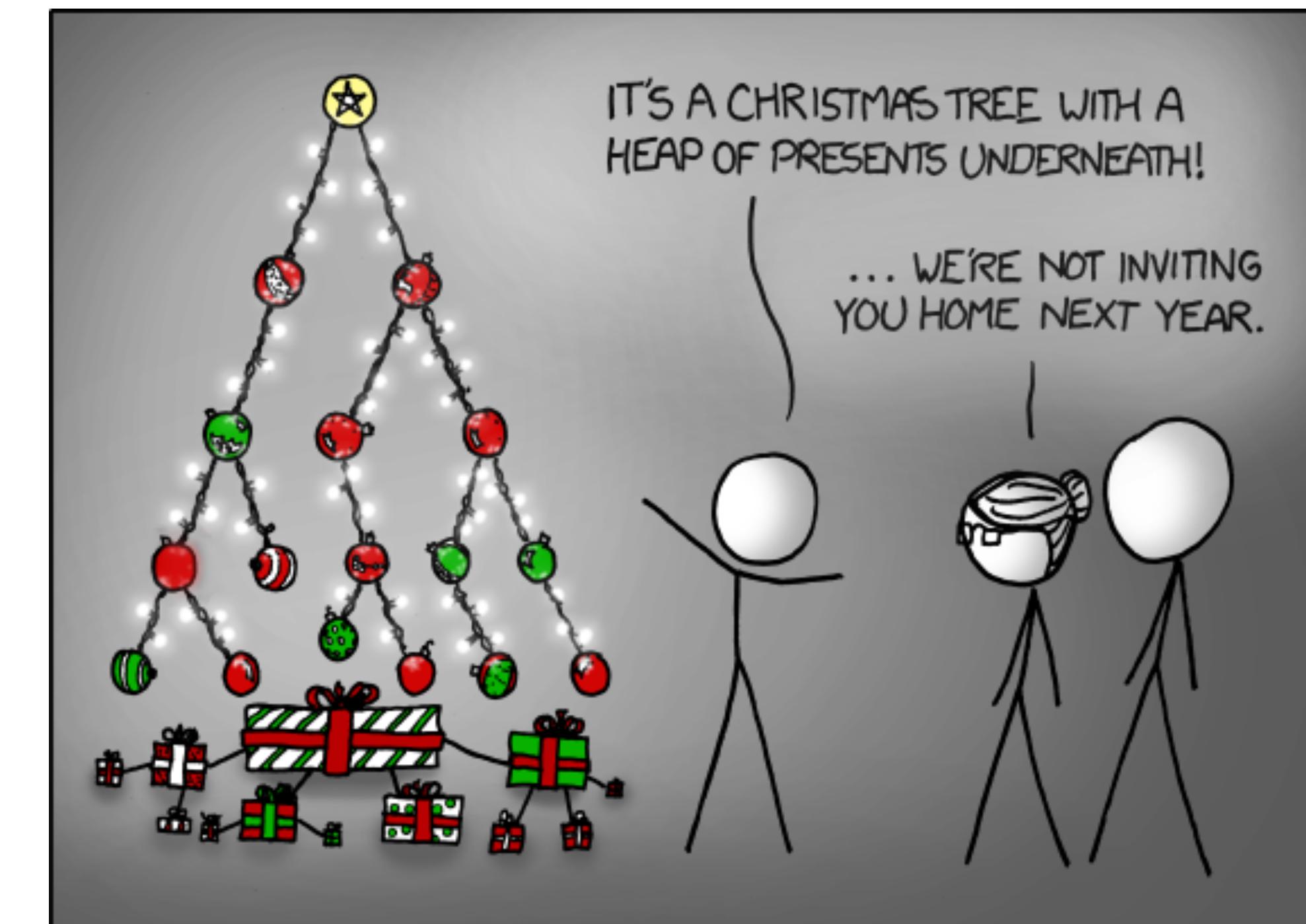


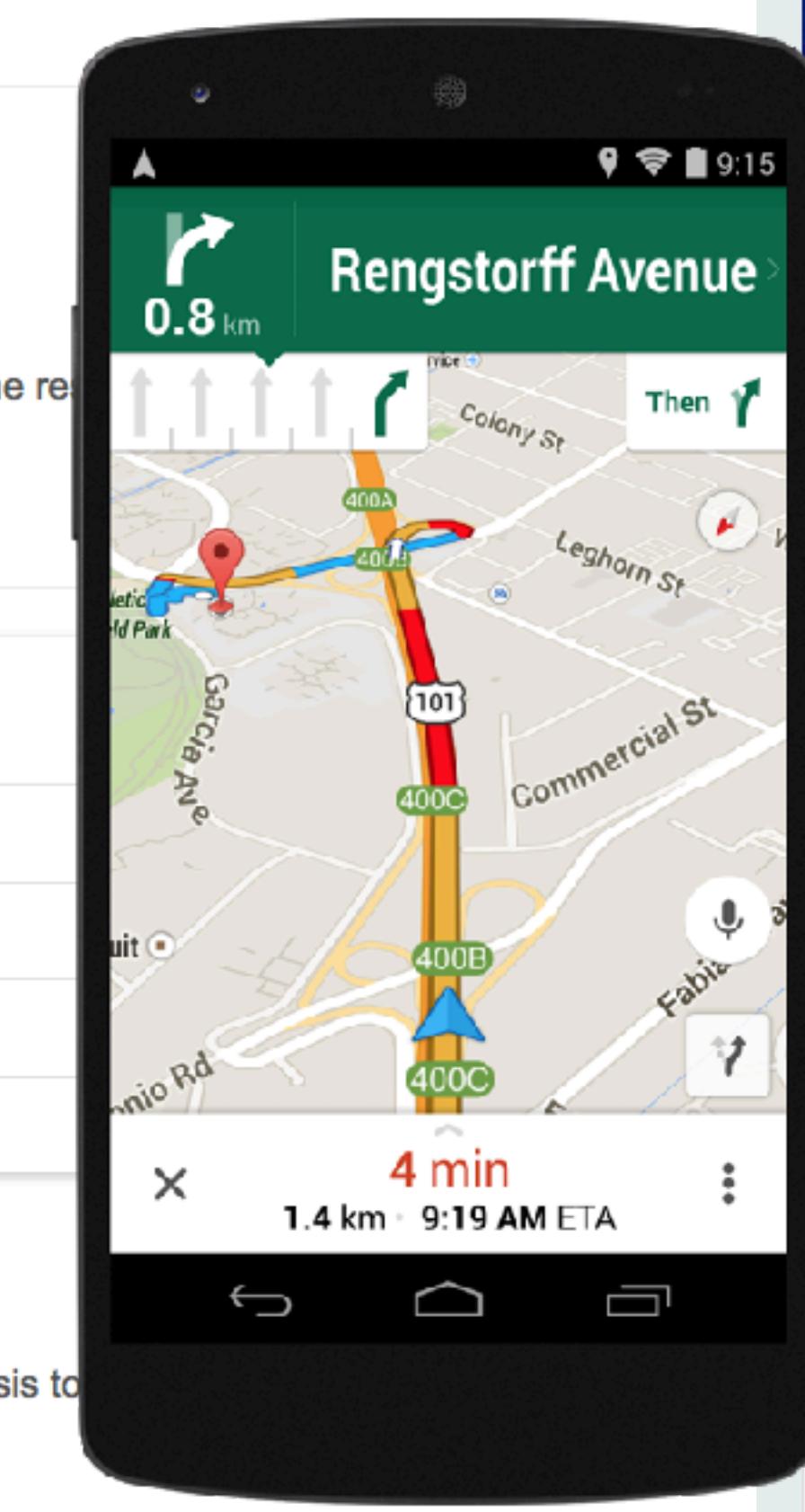
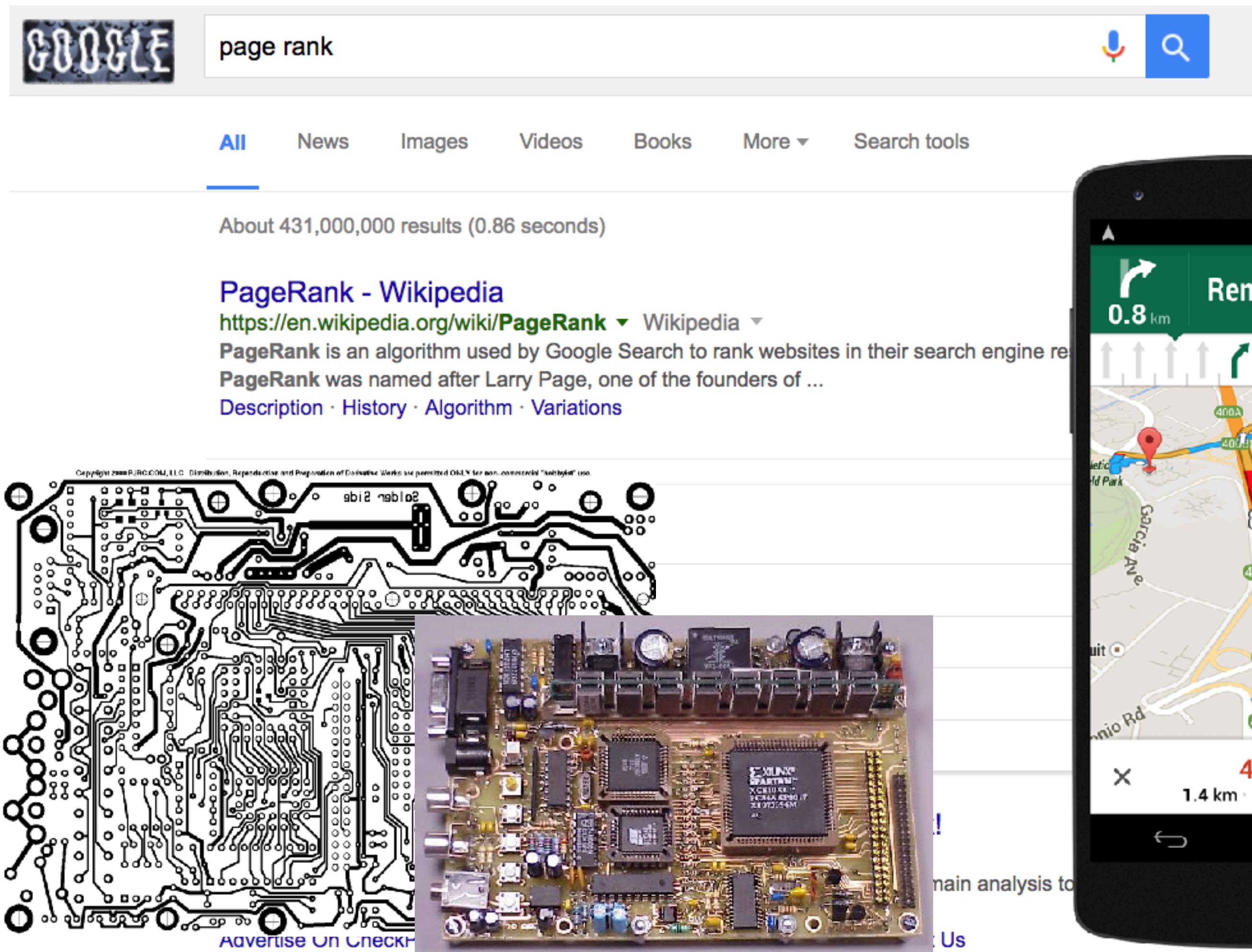
CS-5630 / CS-6630 Visualization Graphs

Alexander Lex
alex@sci.utah.edu



Applications of Graphs

Without graphs, there would be none of these:





facebook

December 2010

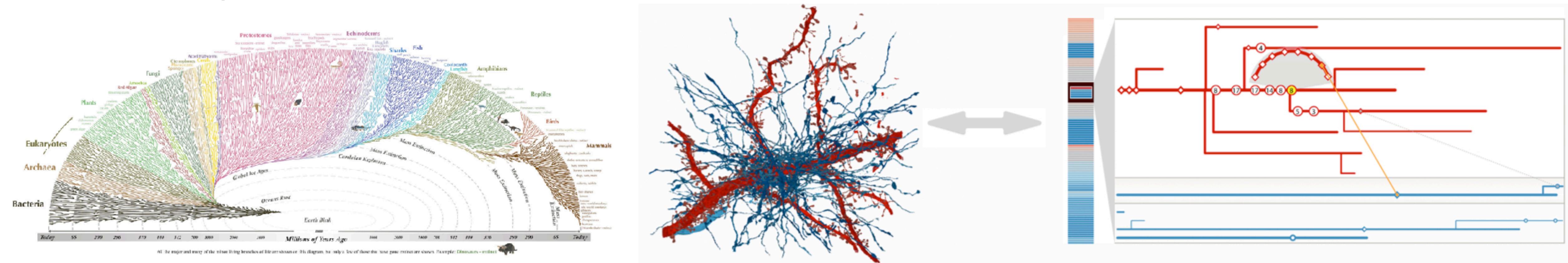
Biological Networks

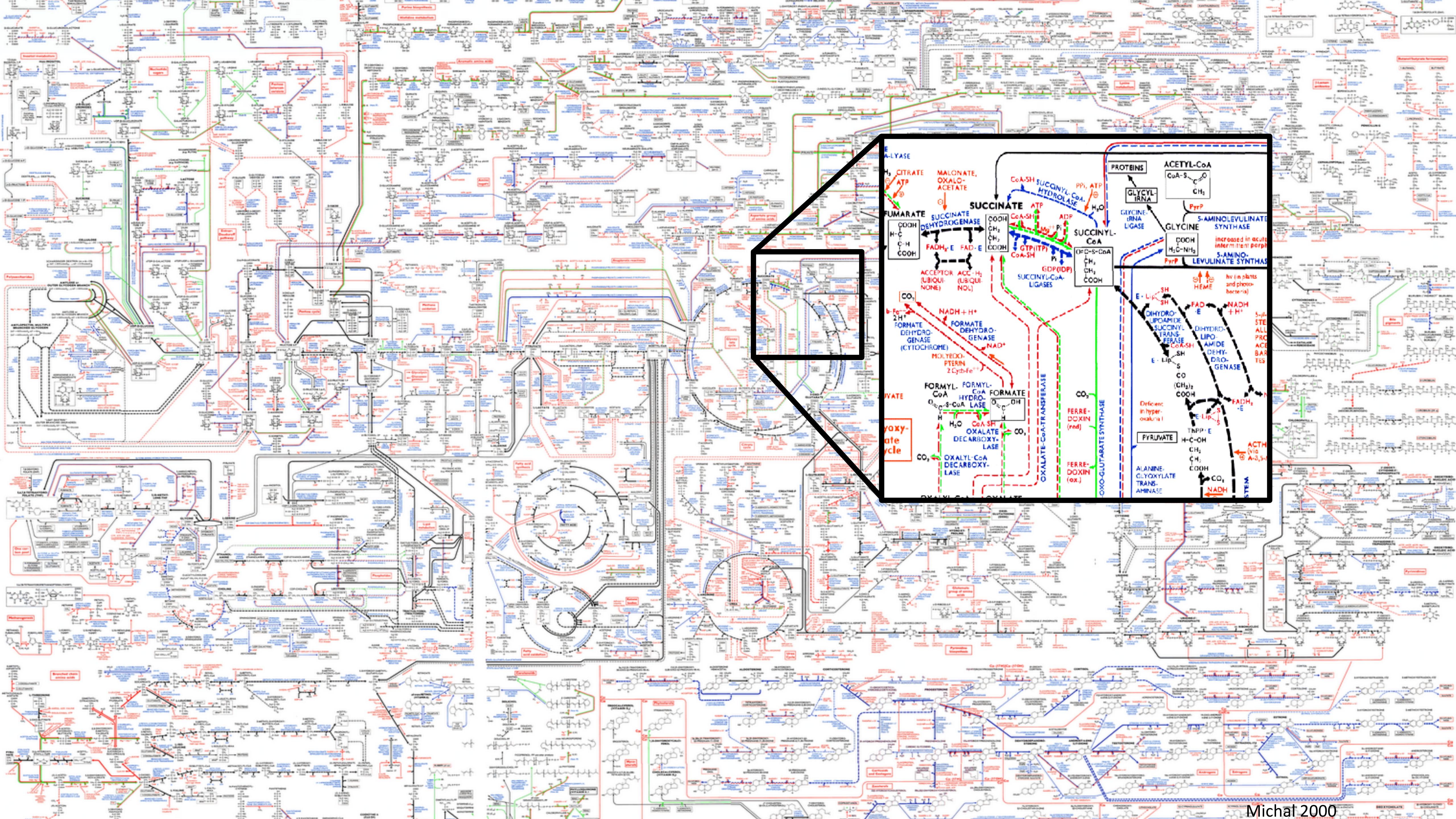
Interaction between genes, proteins and chemical products

The brain: connections between neurons

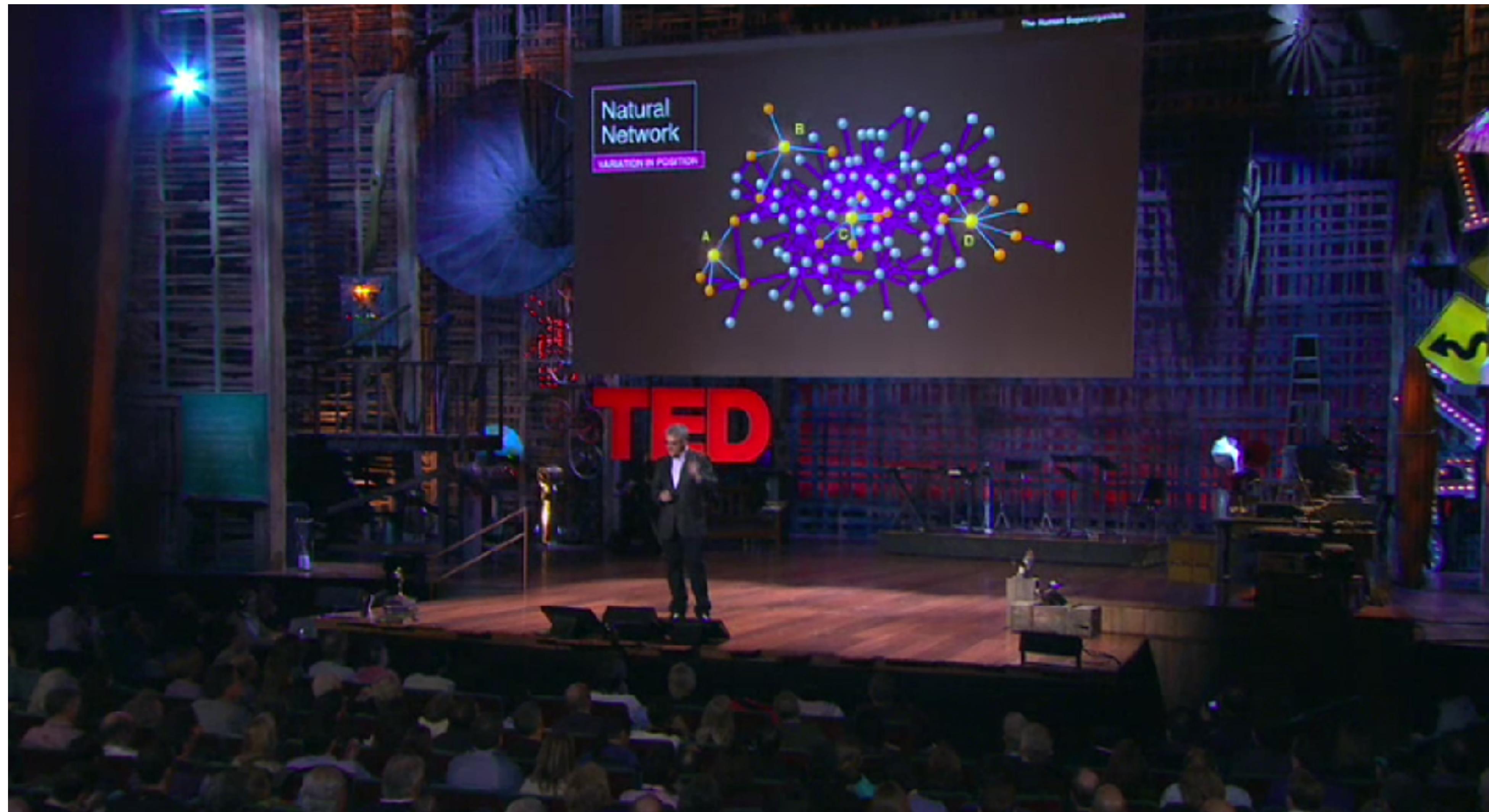
Your ancestry: the relations between you and your family

Phylogeny: the evolutionary relationships of life





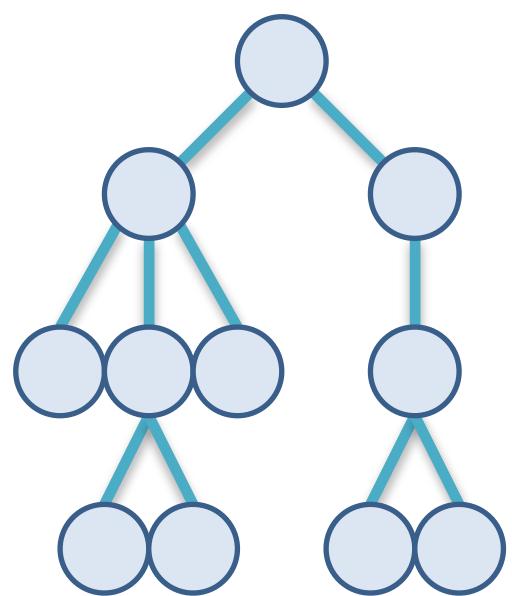
Graph Analysis Case Study



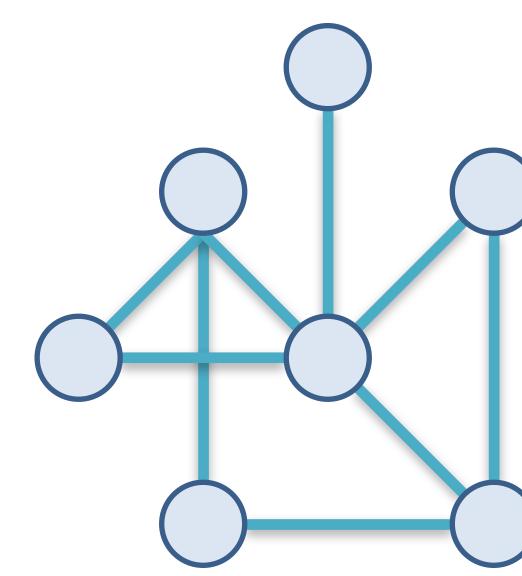
Graph Theory fundamentals

See also “Network Science”, Barabasi
<http://barabasi.com/networksciencebook/chapter/2>

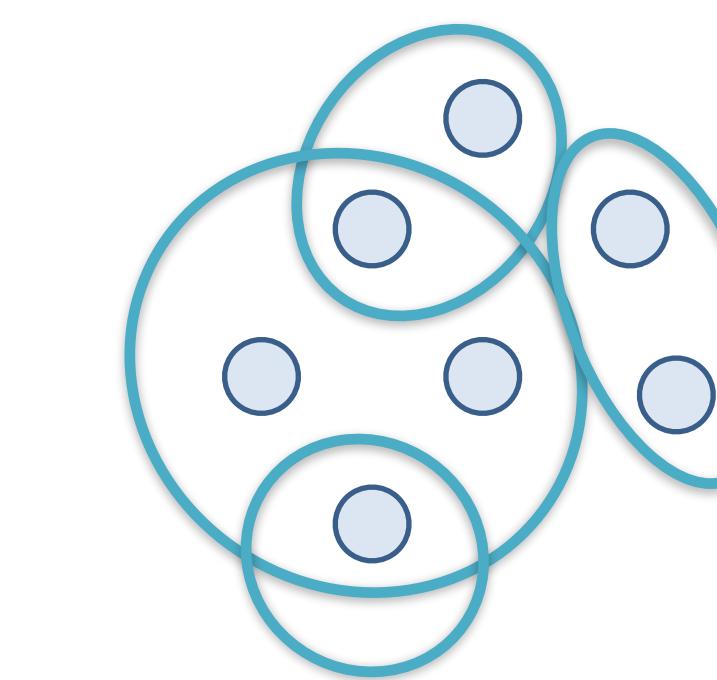
Tree



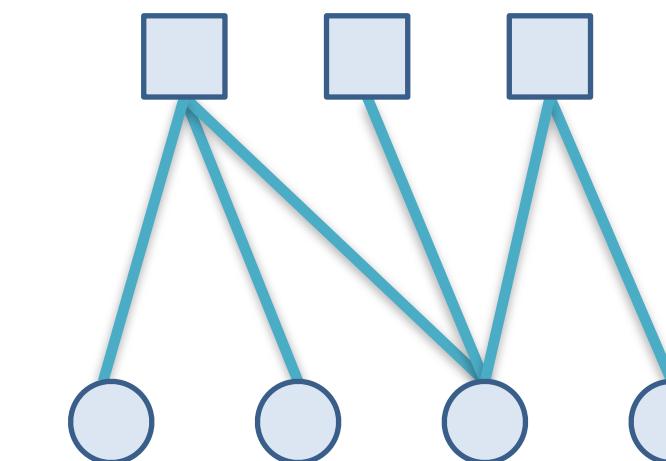
Network



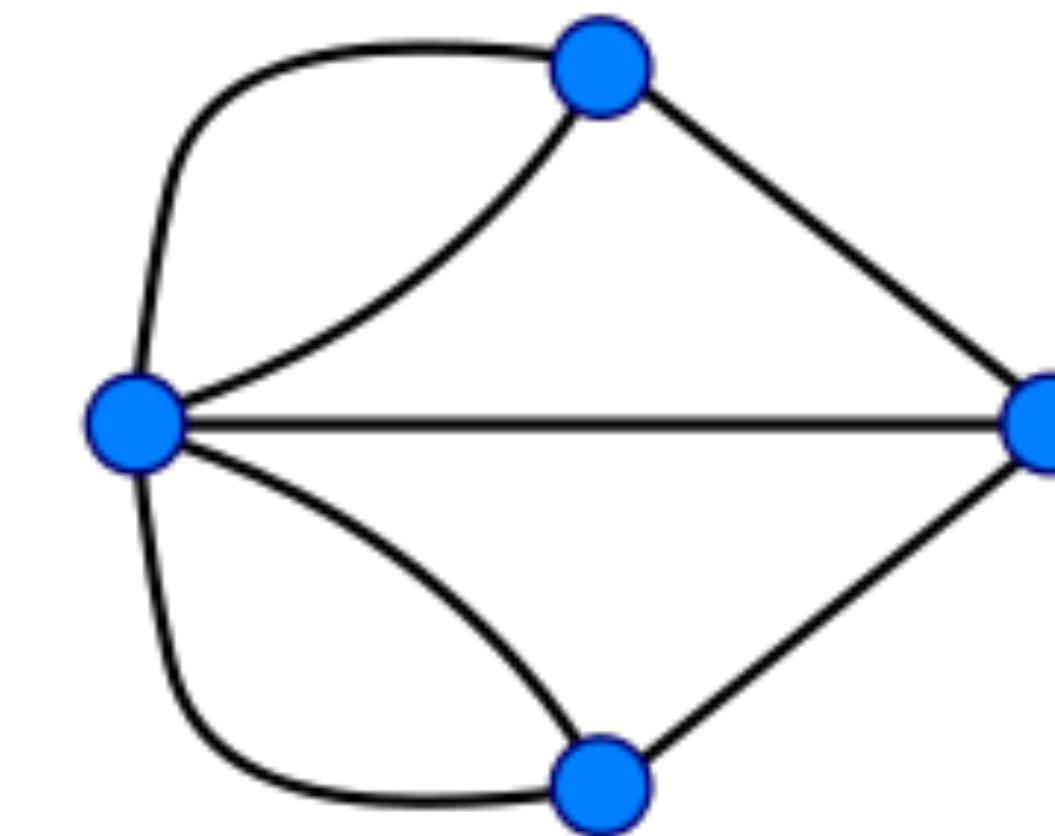
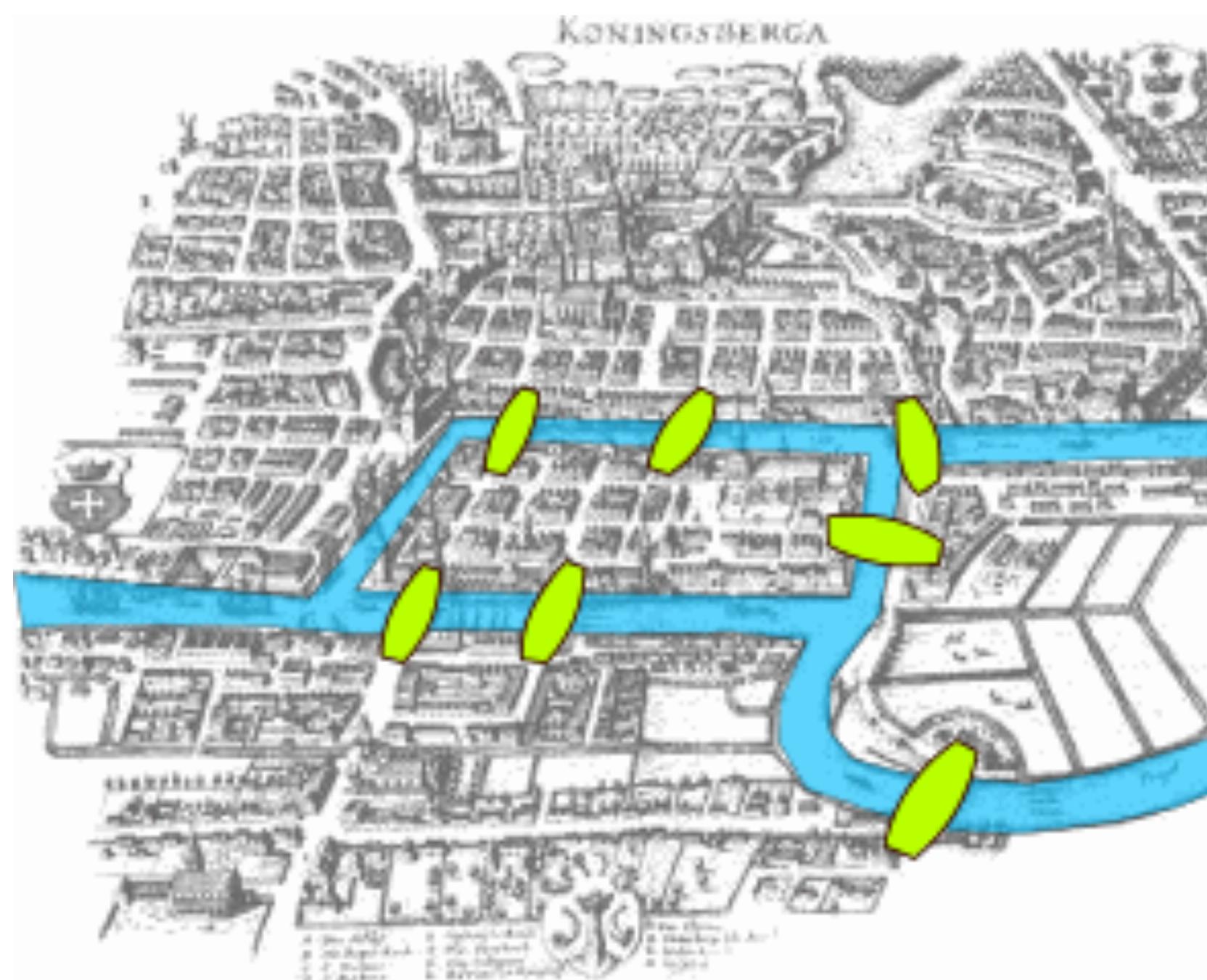
Hypergraph



Bipartite Graph



Königsberg Bridge Problem (1736)

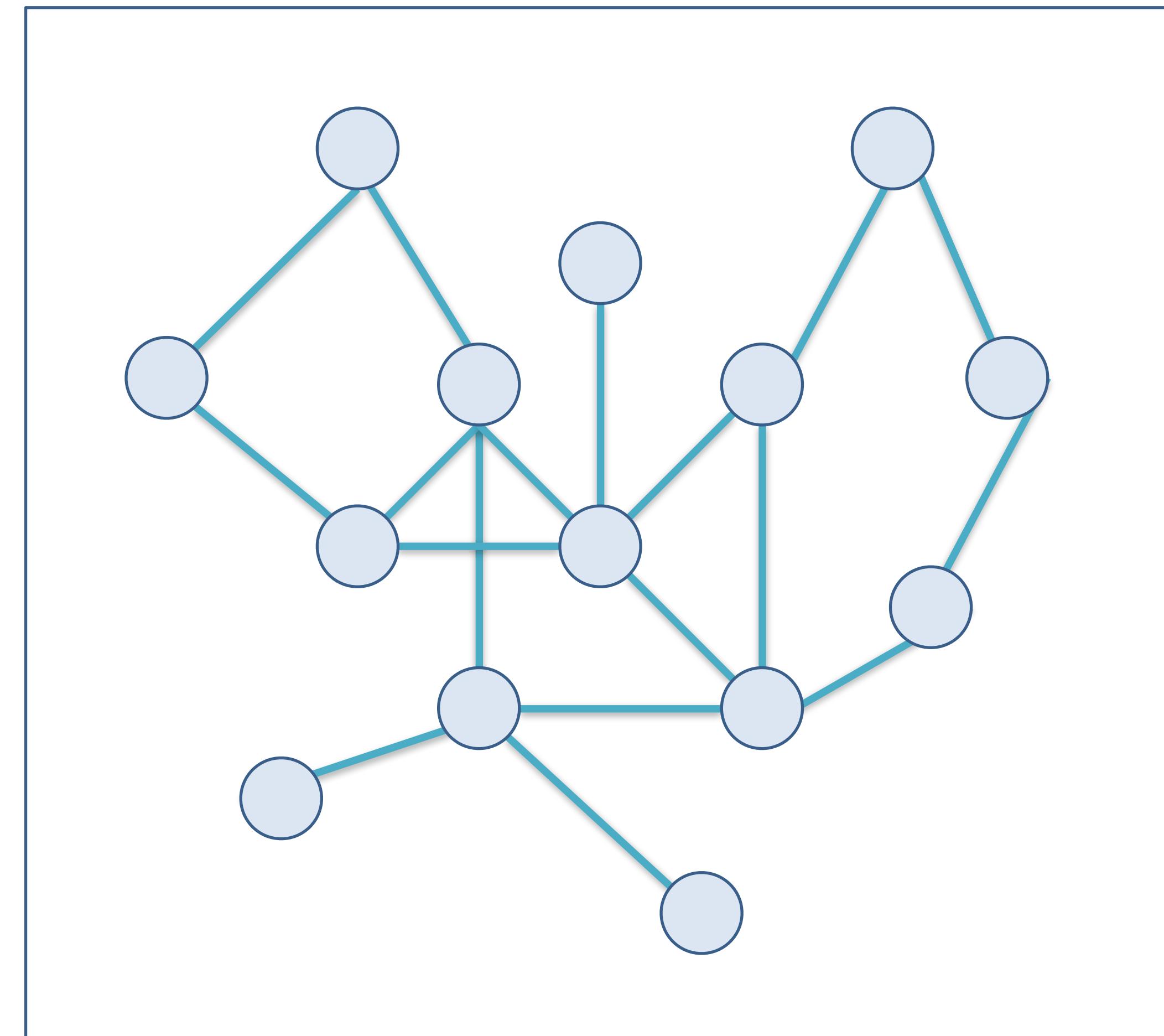


Only possible with a graph with at most two nodes with an odd number of links.
This graph has four nodes with odd number of links.

Graph Terms

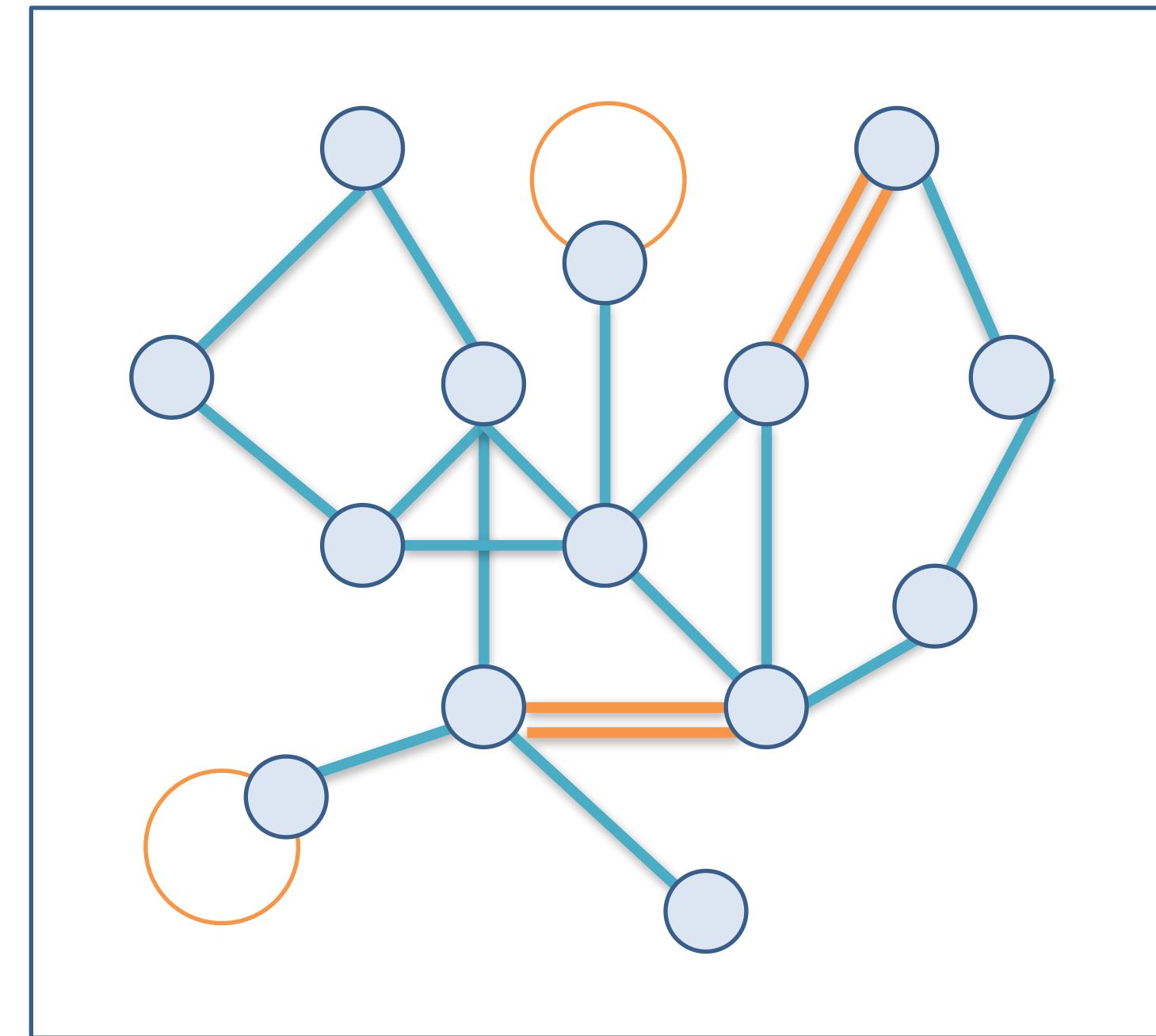
A graph $G(V,E)$ consists of a set of vertices V (also called nodes) and a set of edges E (also called links) connecting these vertices.

Graph and Network are often used interchangeably



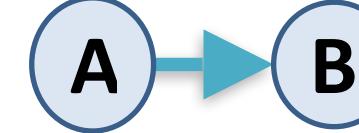
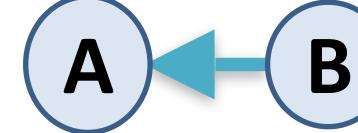
Graph Term: Simple Graph

A simple graph $G(V,E)$ is a graph which contains no multi-edges and no loops



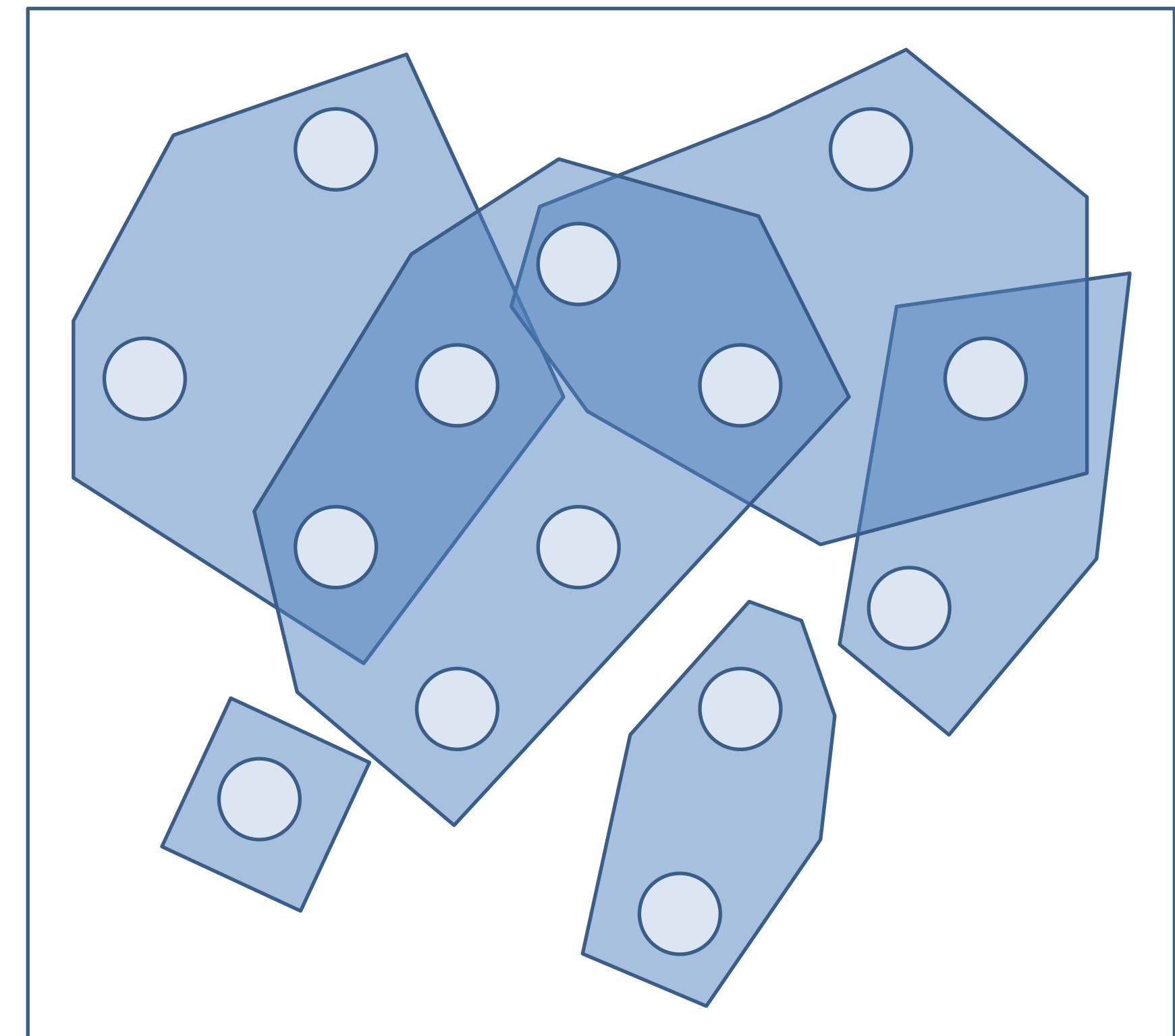
Not a simple graph!
→ A *general graph*

Graph Term: Directed Graph

A directed graph (digraph) is a graph that discerns between the edges  and .

Graph Terms: Hypergraph

A hypergraph is a graph with edges connecting any number of vertices.

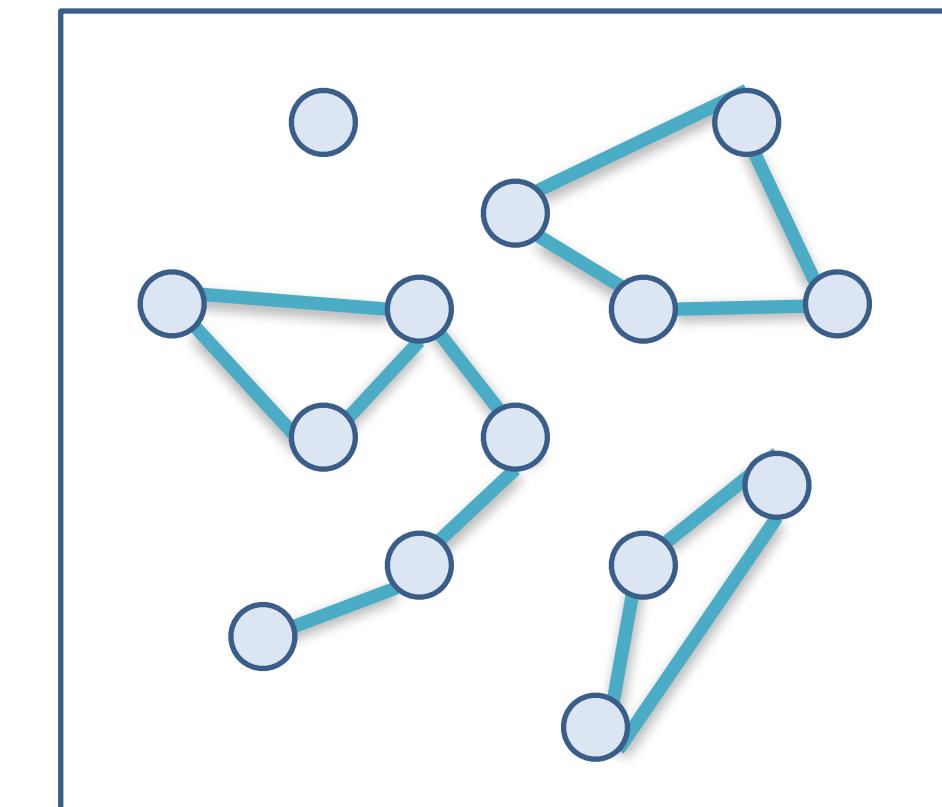


Hypergraph Example

Unconnected Graphs, Articulation Points

Unconnected graph

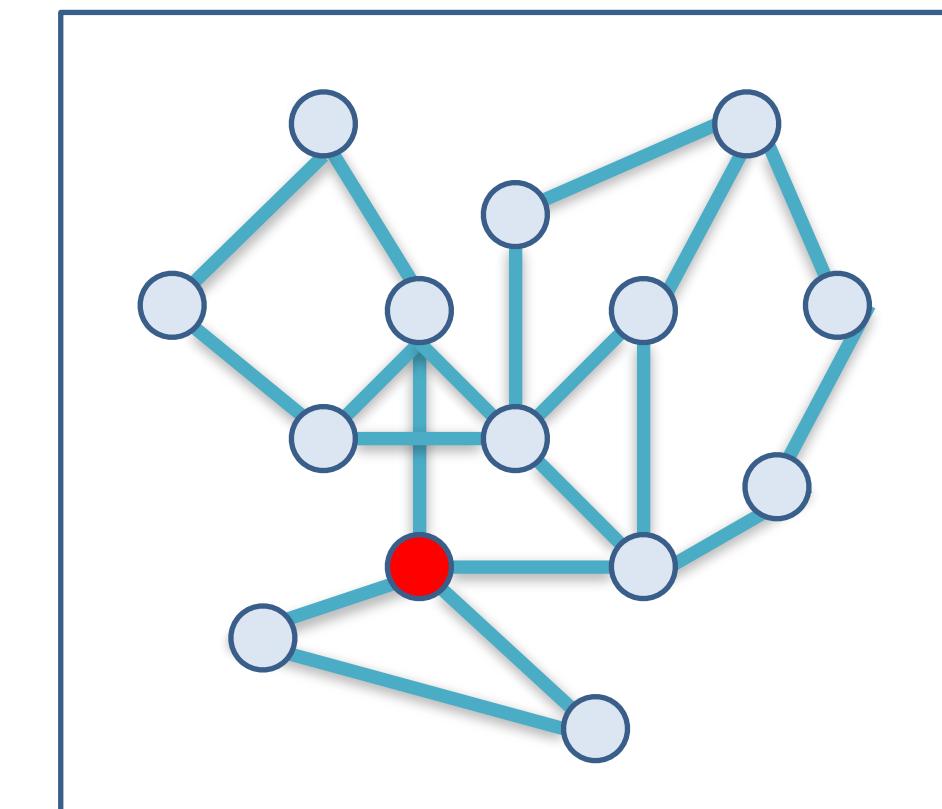
An edge traversal starting from a given vertex cannot reach any other vertex.



Unconnected Graph

Articulation point

Vertices, which if deleted from the graph, would break up the graph in multiple sub-graphs.

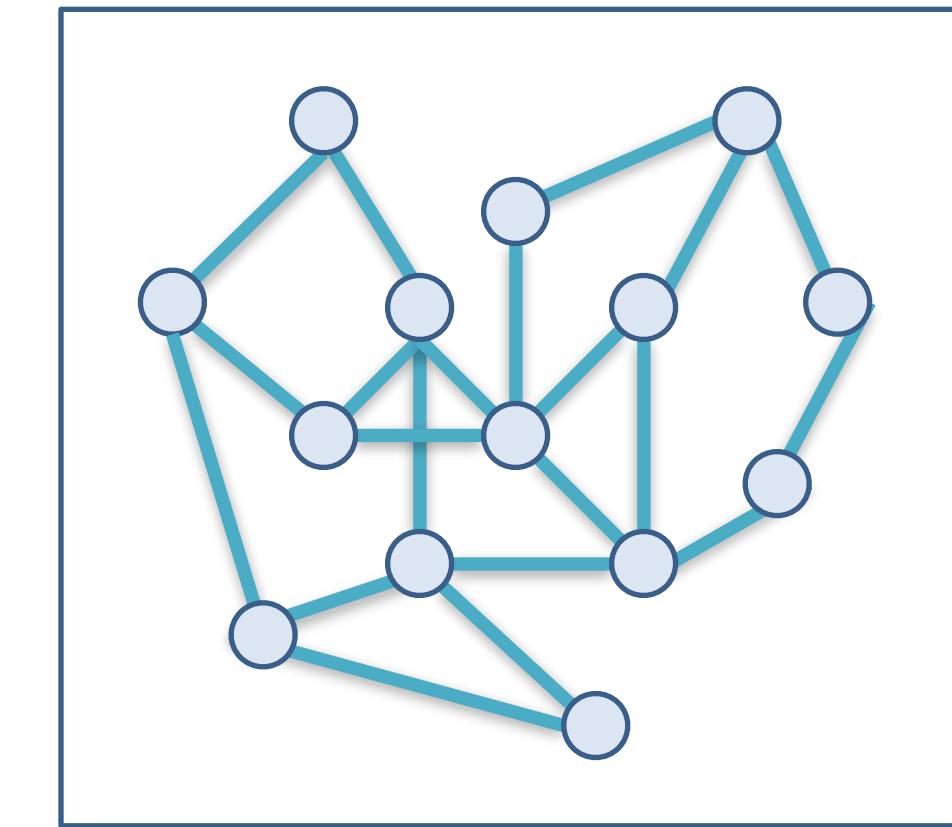


Articulation Point (red)

Biconnected, Bipartite Graphs

Biconnected graph

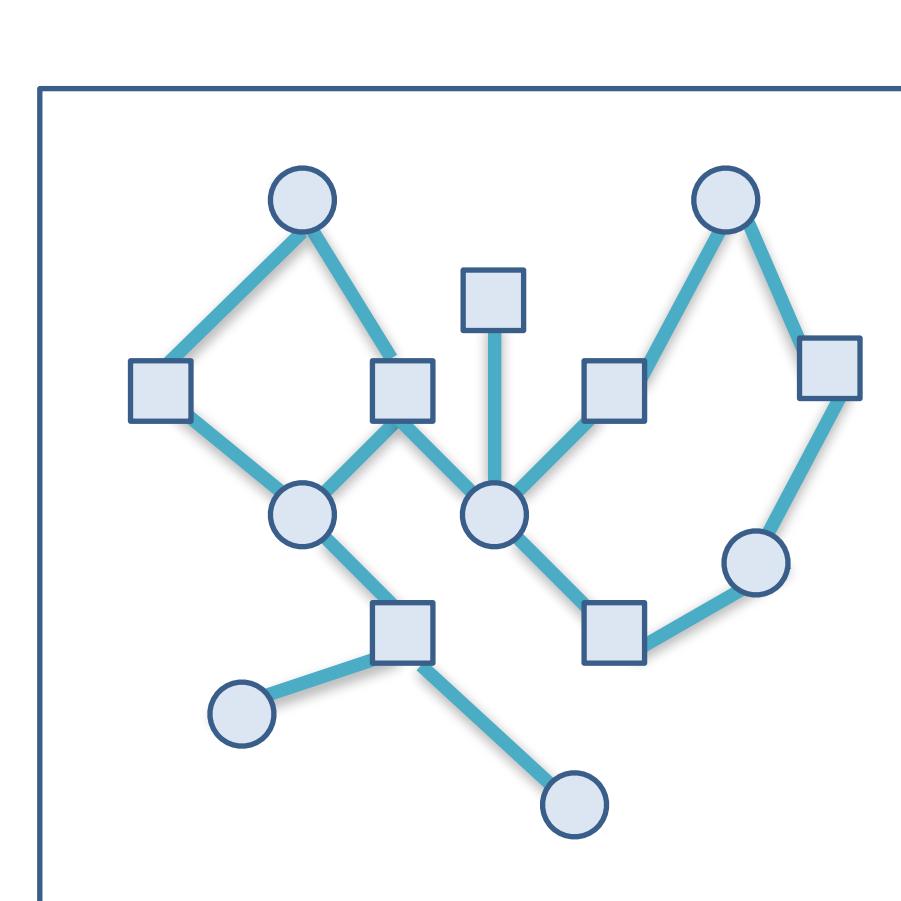
A graph without articulation points.



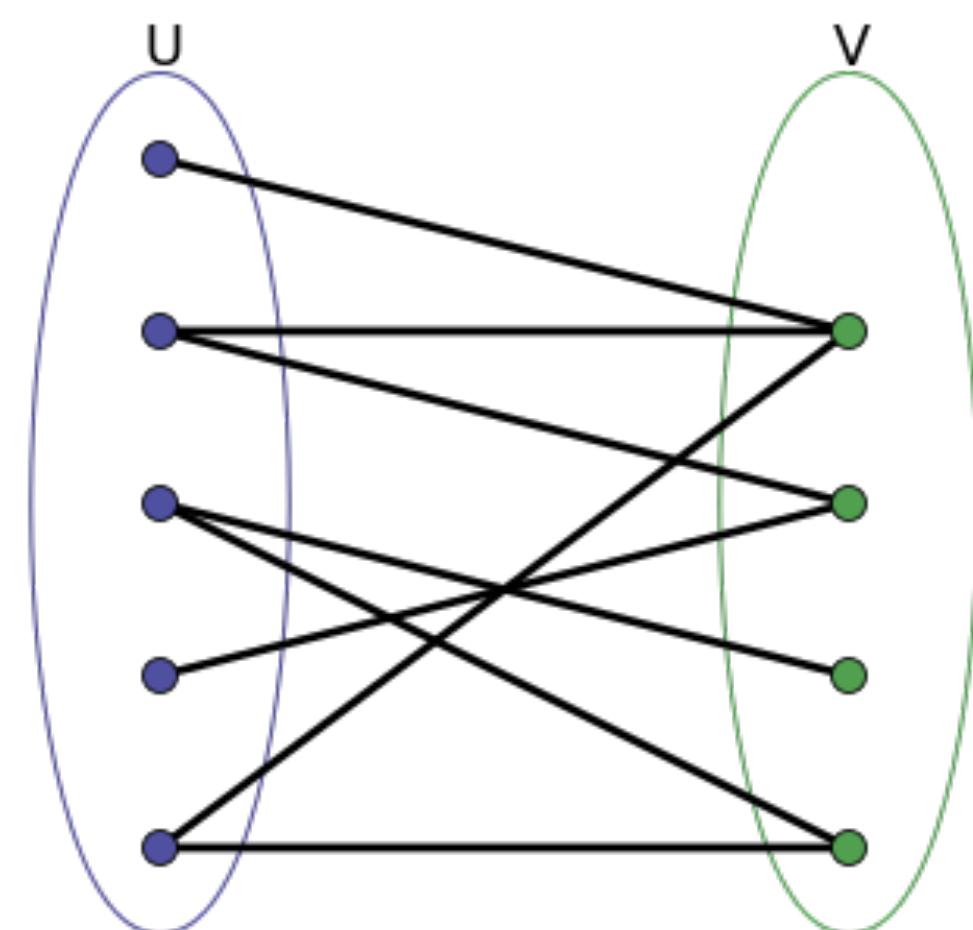
Biconnected Graph

Bipartite graph

The vertices can be partitioned in two independent sets.



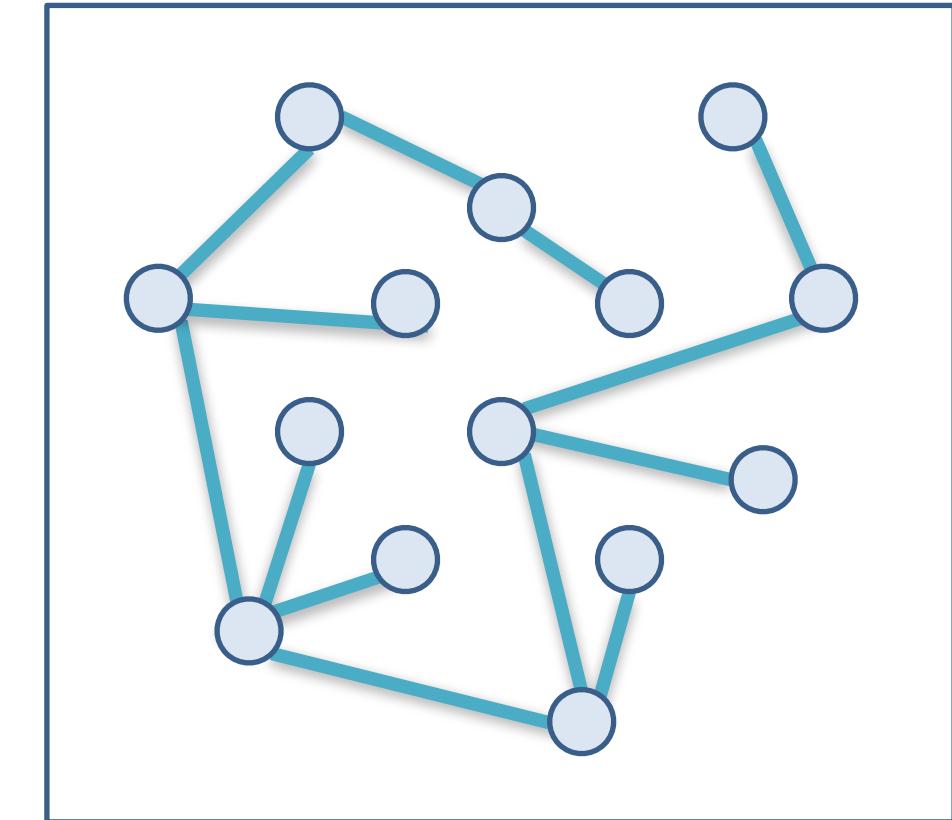
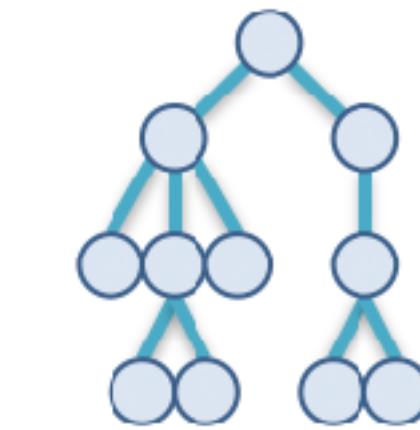
Bipartite Graph



Tree

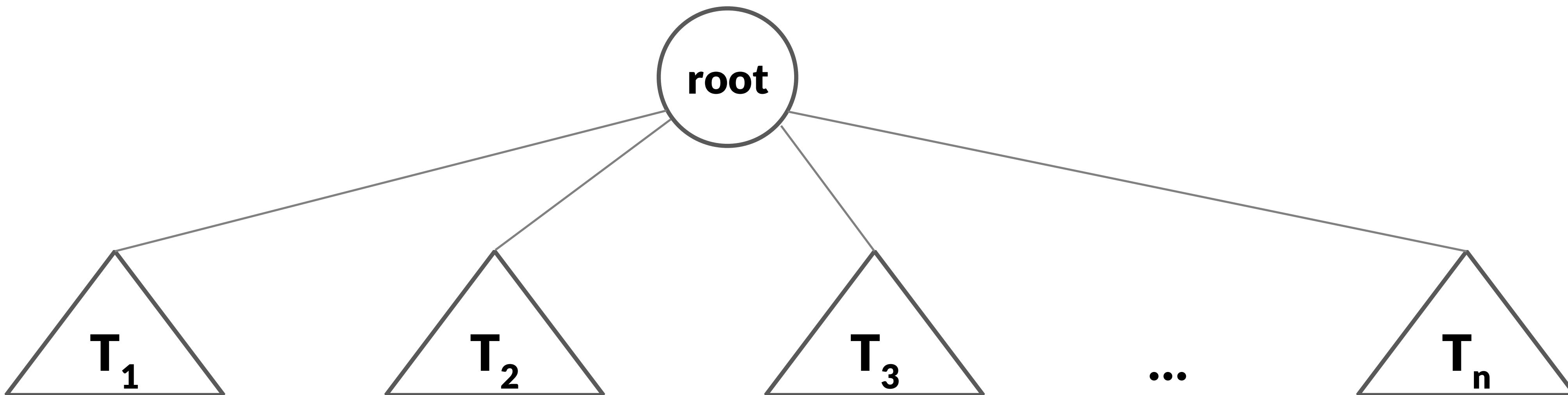
A graph with no cycles - or:

A collection of nodes

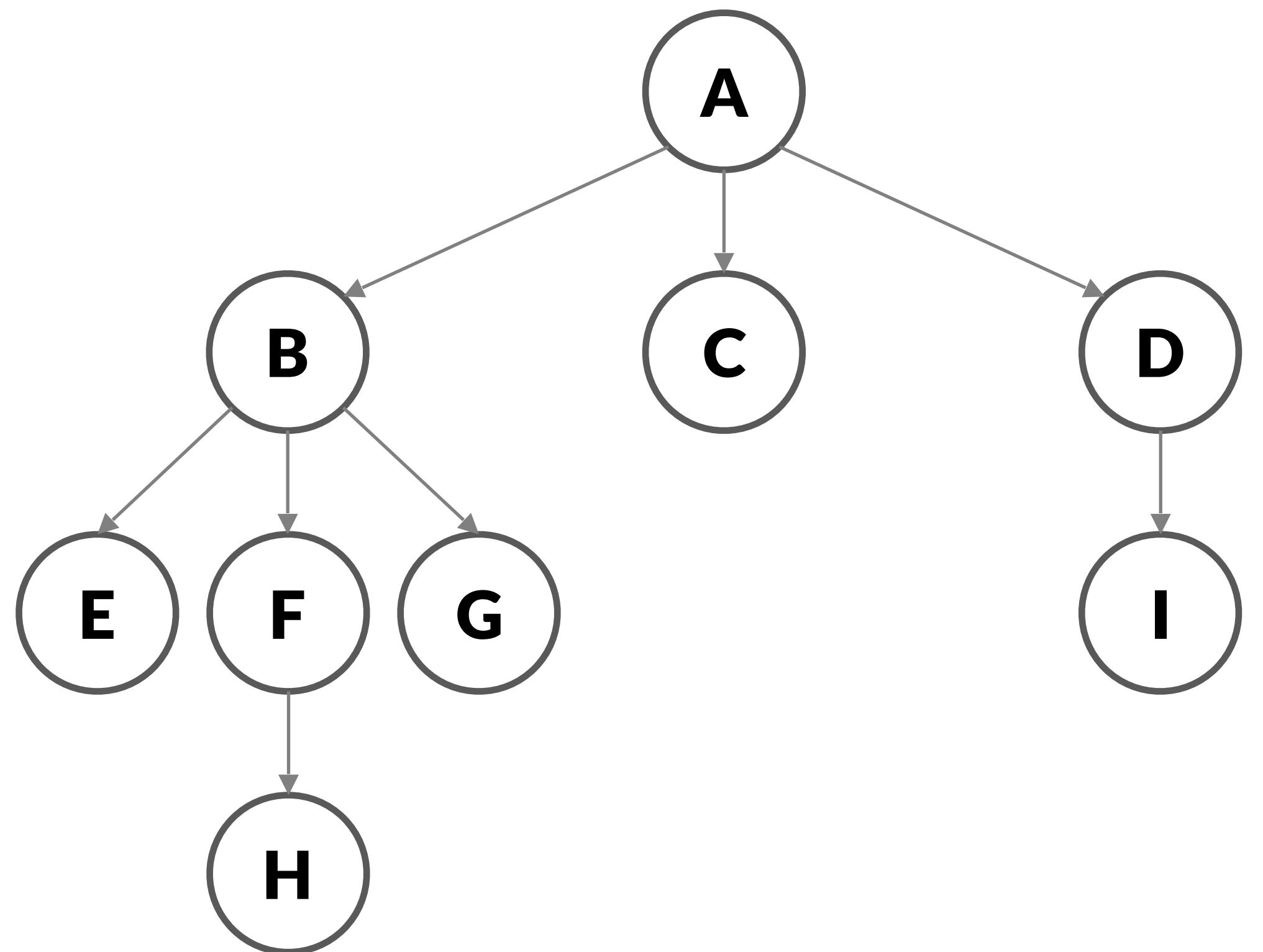


contains a root node and 0-n subtrees

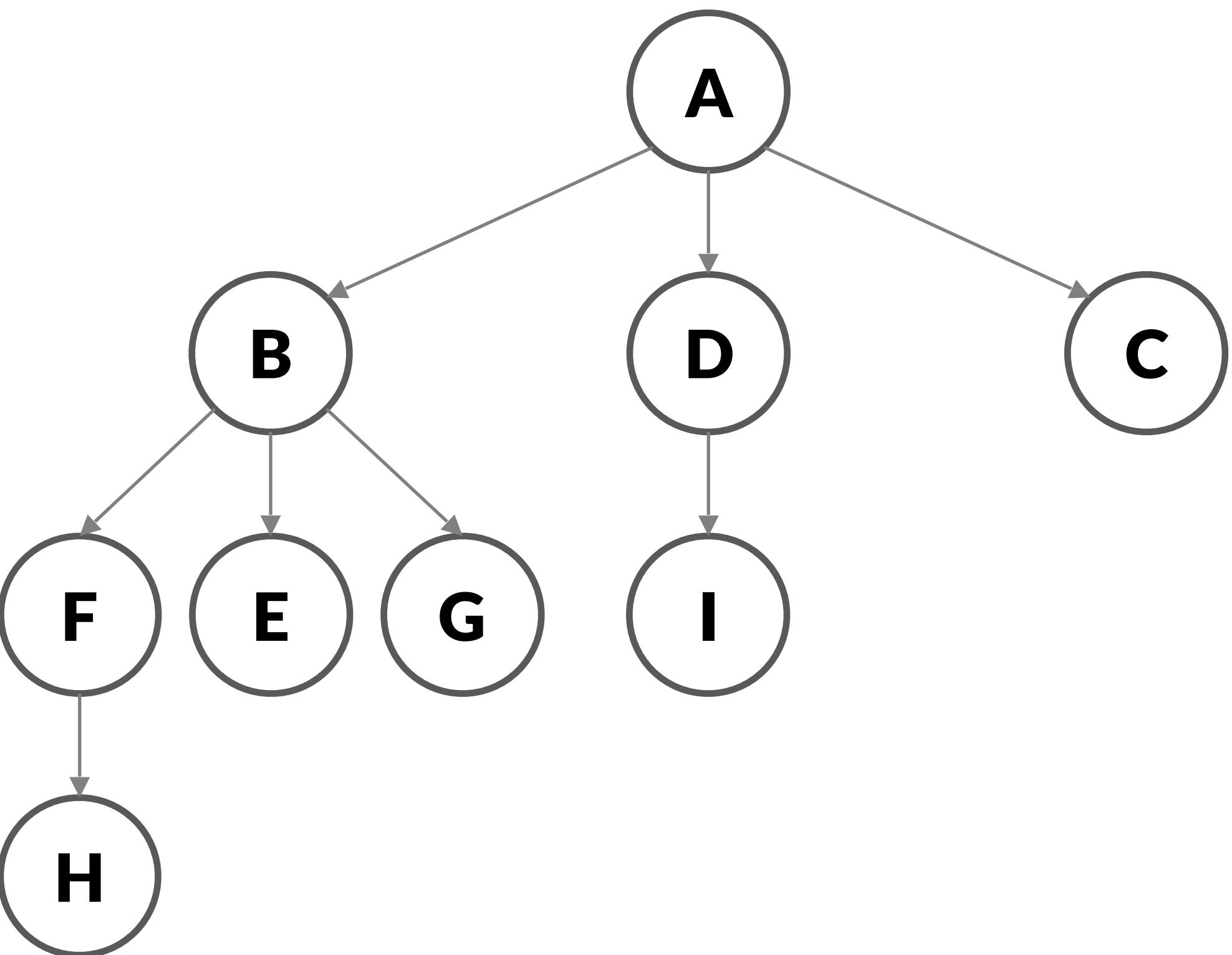
subtrees are connected to root by an edge



Ordered Tree



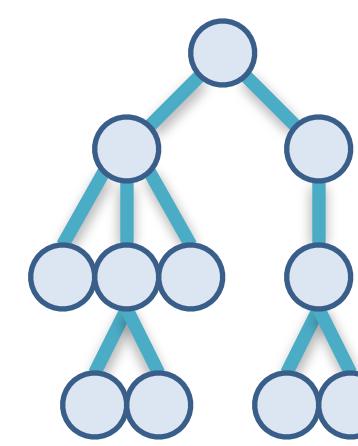
≠



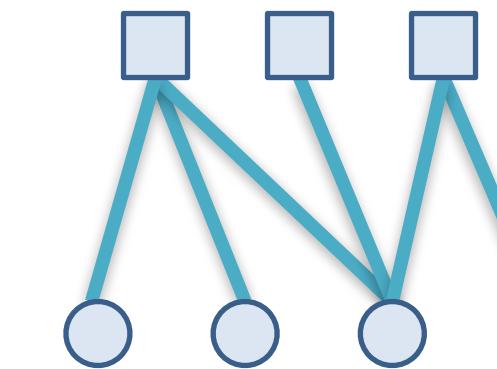
Different Kinds of Graphs

Over 1000 different graph classes

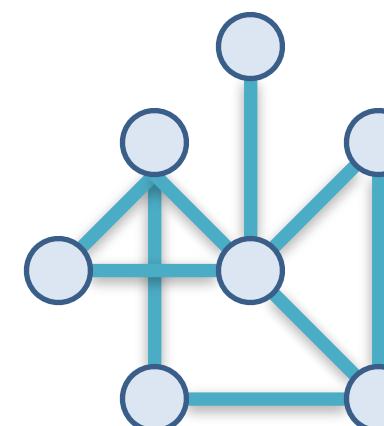
Tree



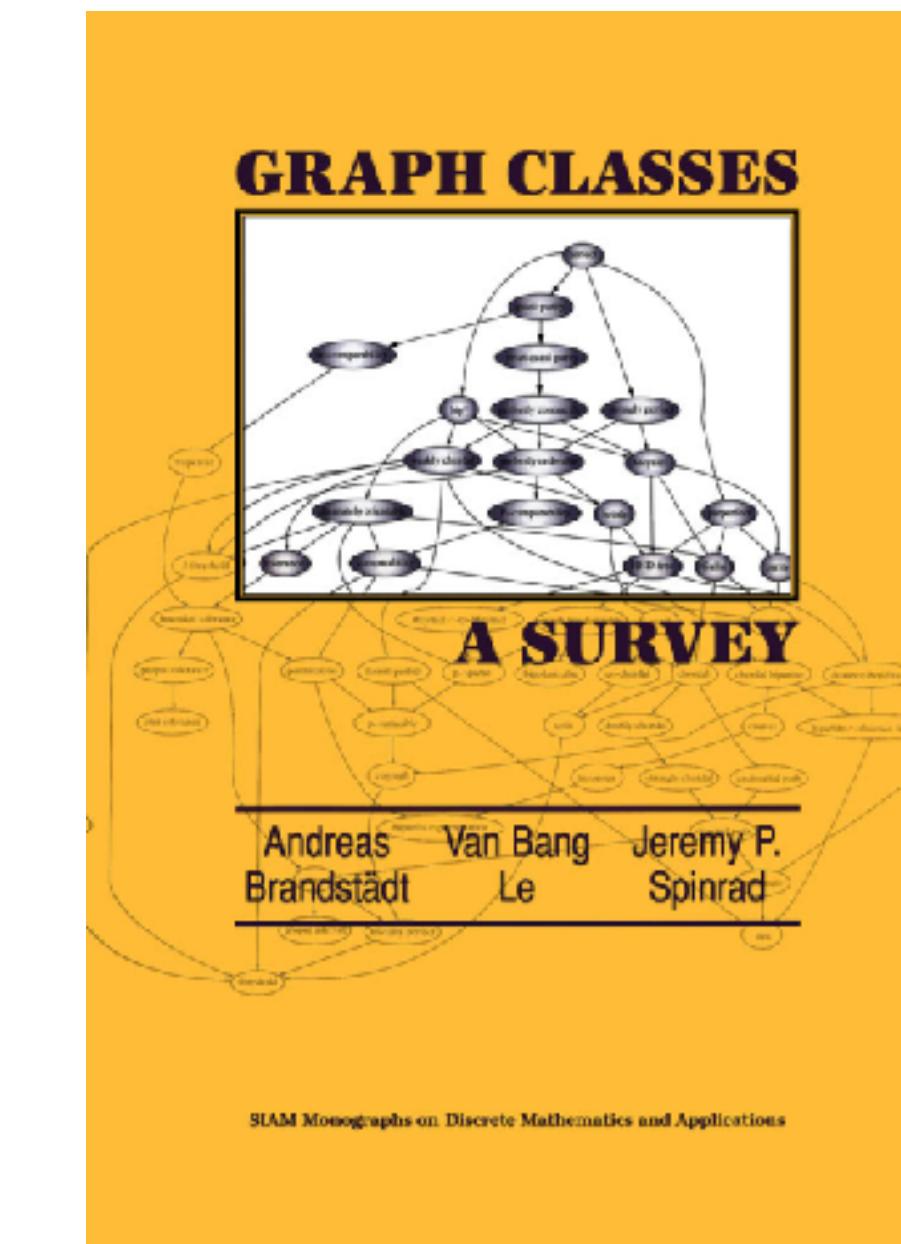
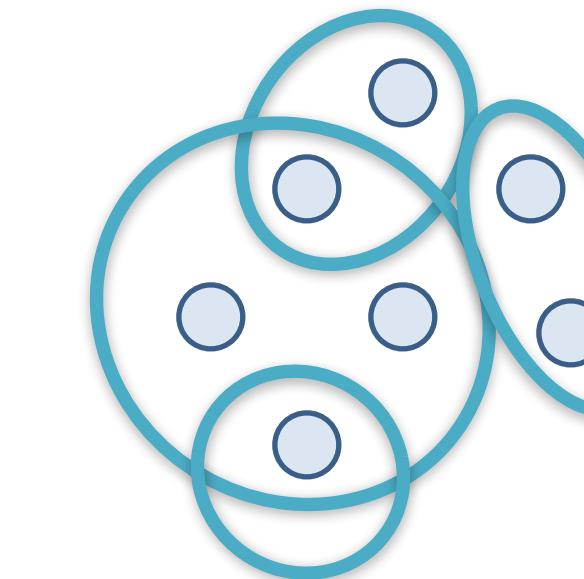
Bipartite Graph



Network



Hypergraph



A. Brandst  dt et al. 1999

Degree

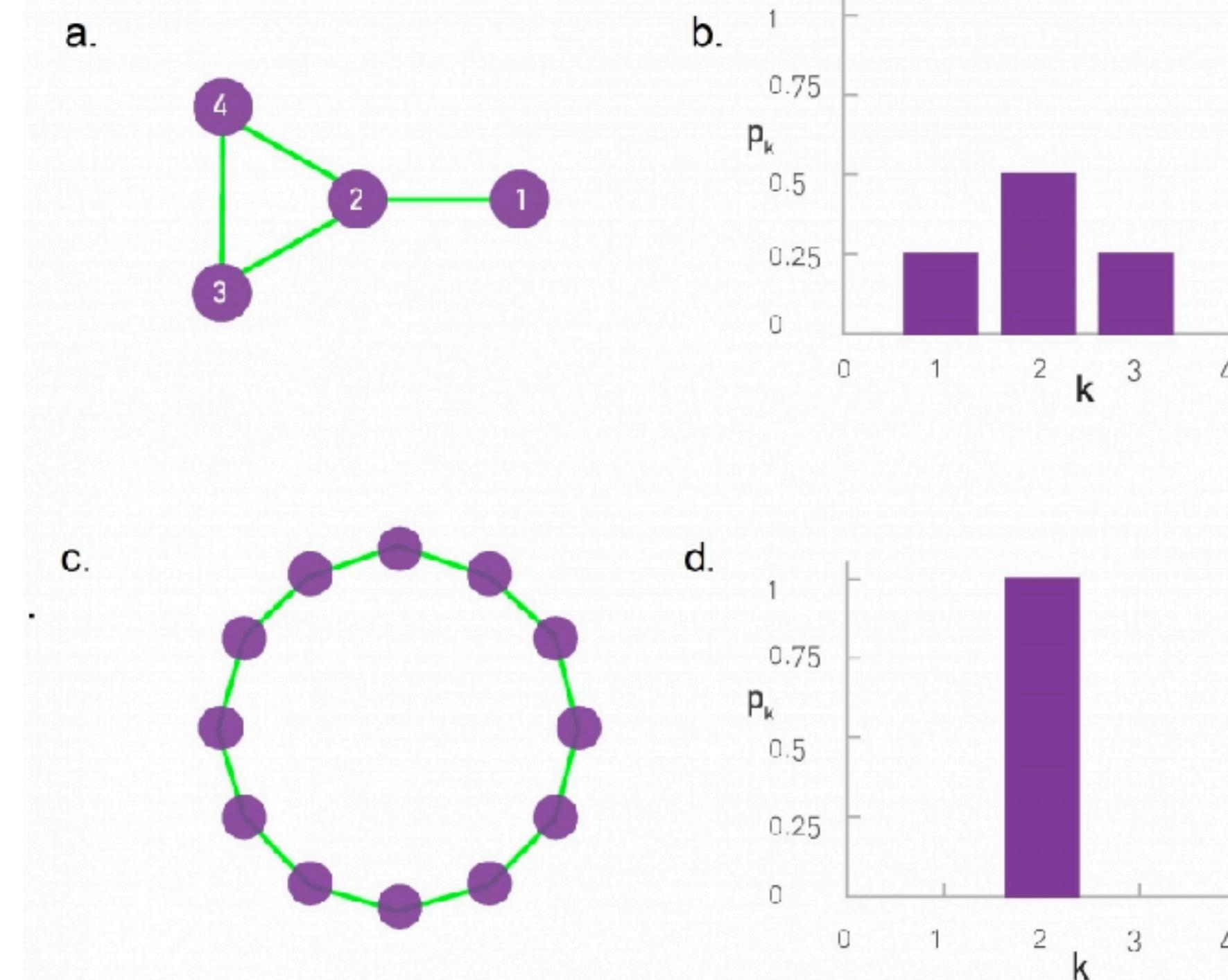
Node degree $\deg(x)$

The number of edges being incident to this node. For directed graphs indeg/outdeg are considered separately.

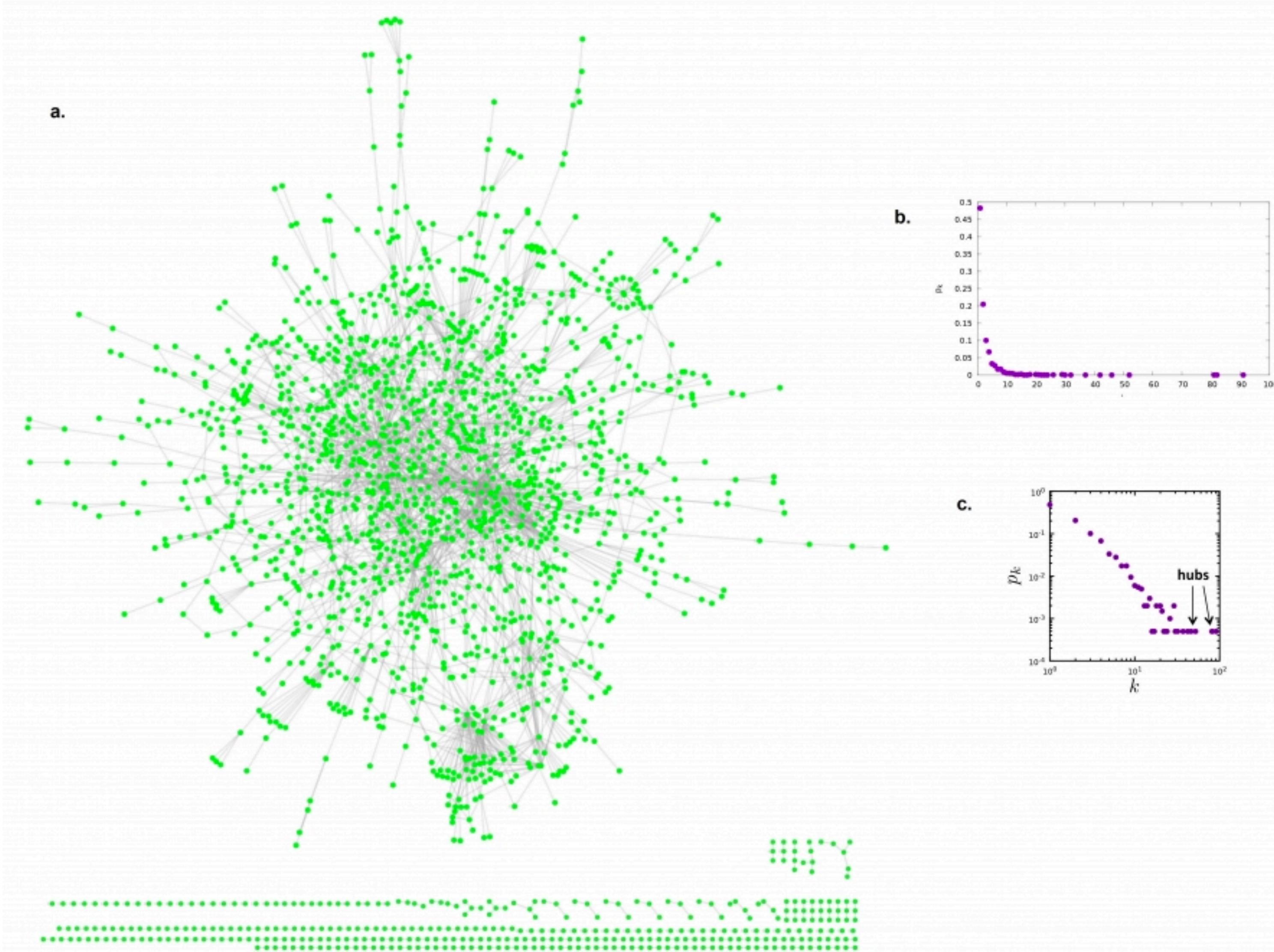
Average degree

$$\langle k \rangle = \frac{1}{N} \sum_{i=1}^N k_i = \frac{2L}{N}$$

Degree distribution

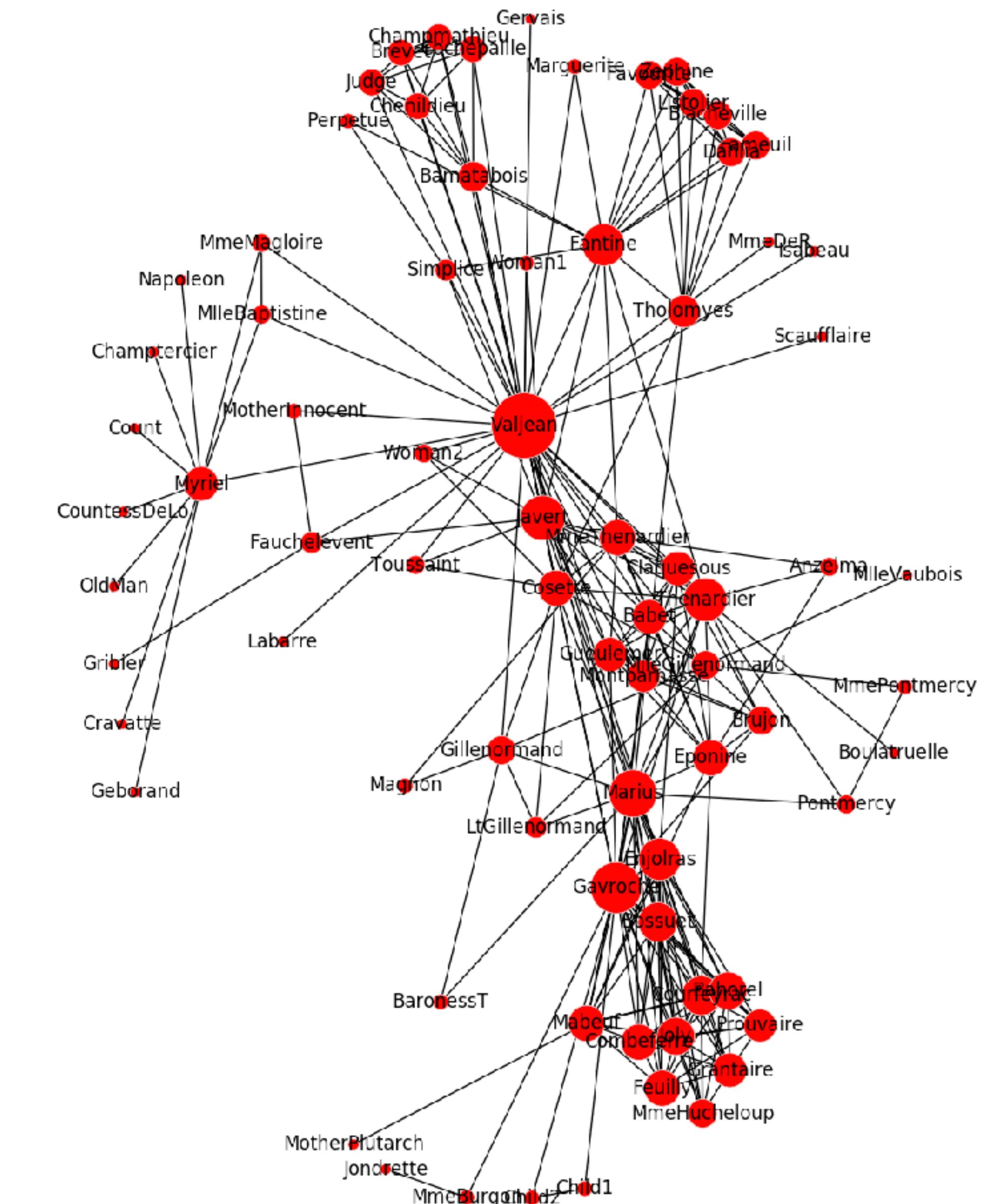


Degree Distribution of a real Network



Degrees

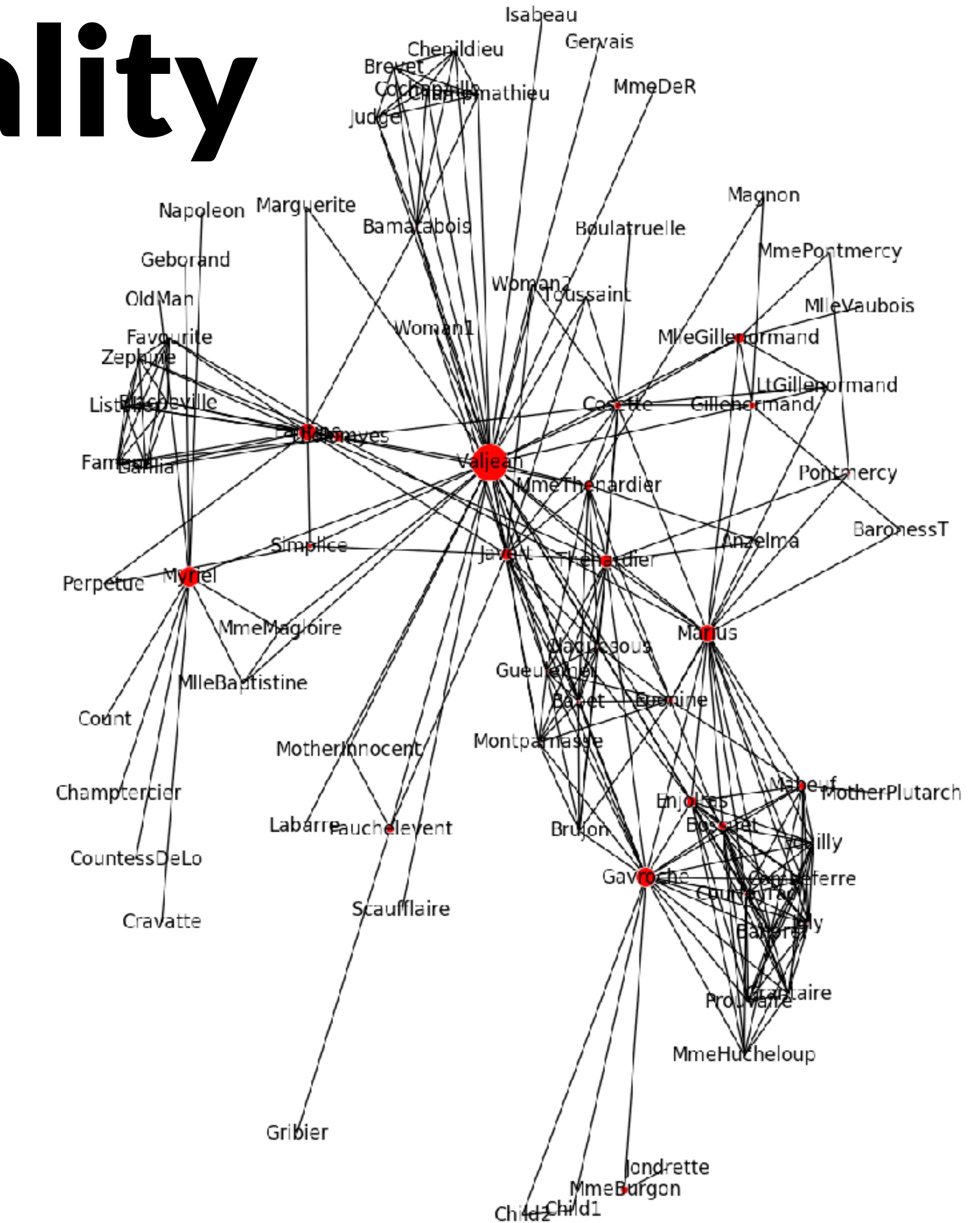
Degree is a measure of local importance



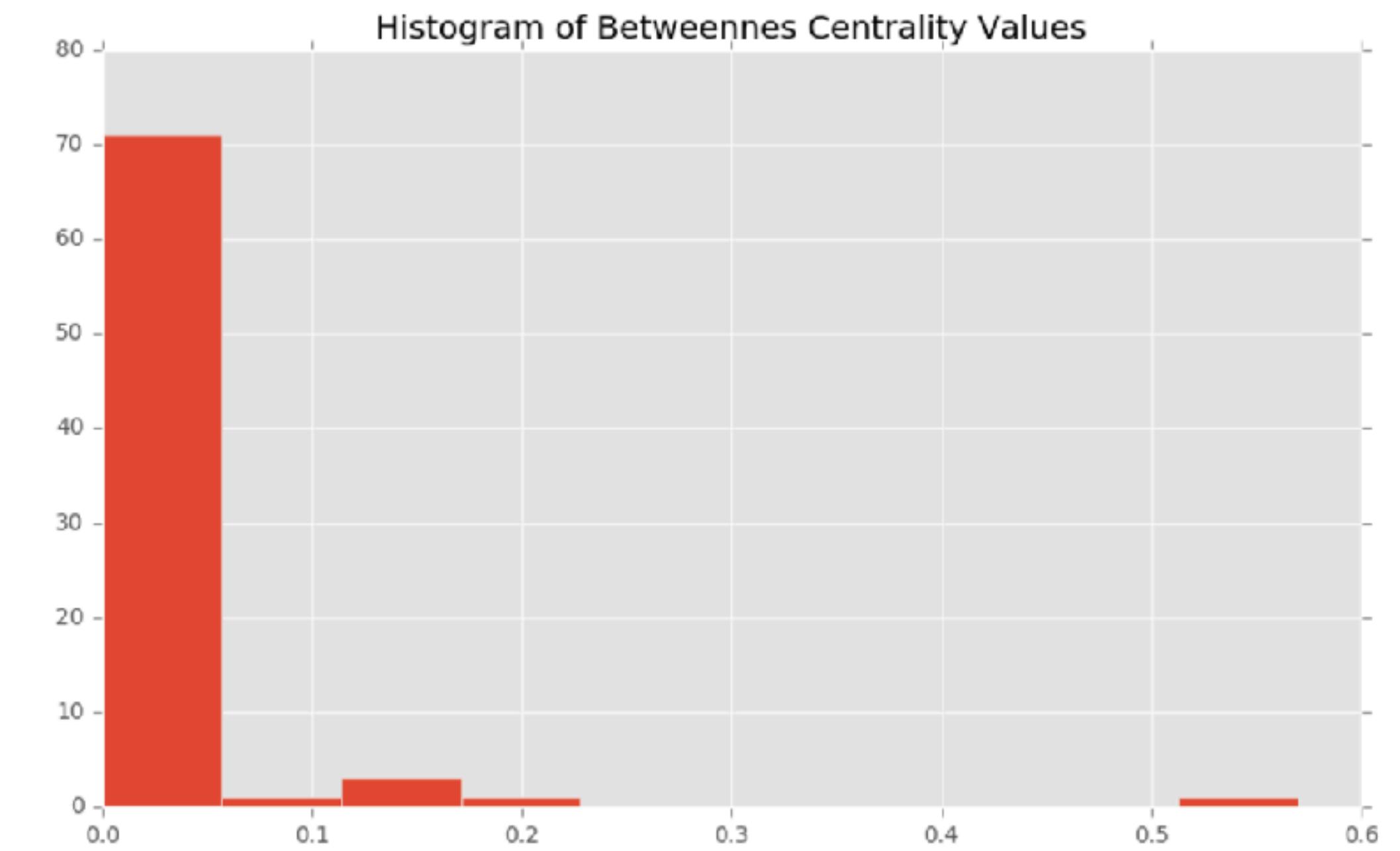
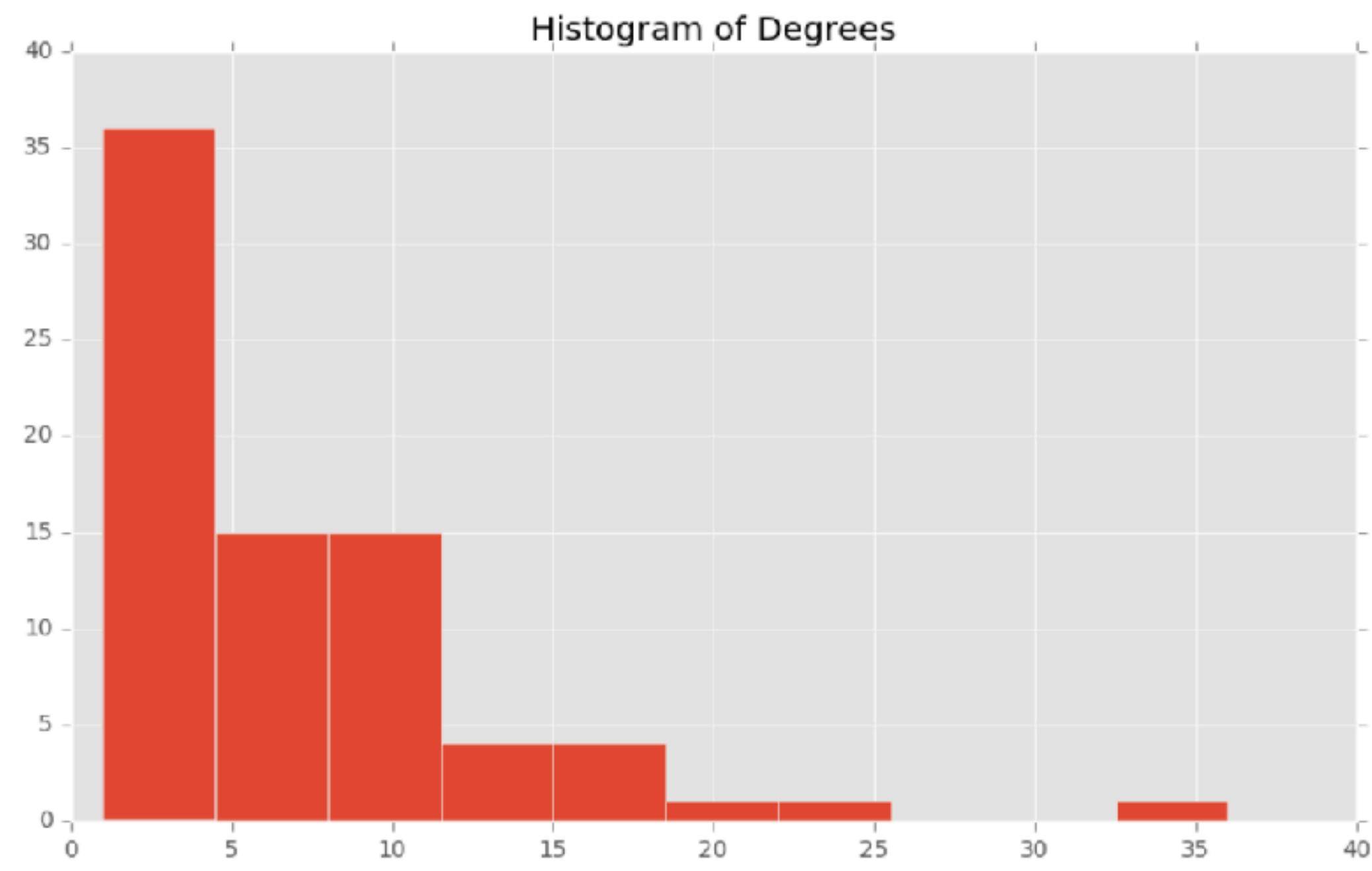
Betweenness Centrality

a measure of how many shortest paths pass through a node

good measure for the overall relevance of a node in a graph



Degree vs BC



Paths & Distances

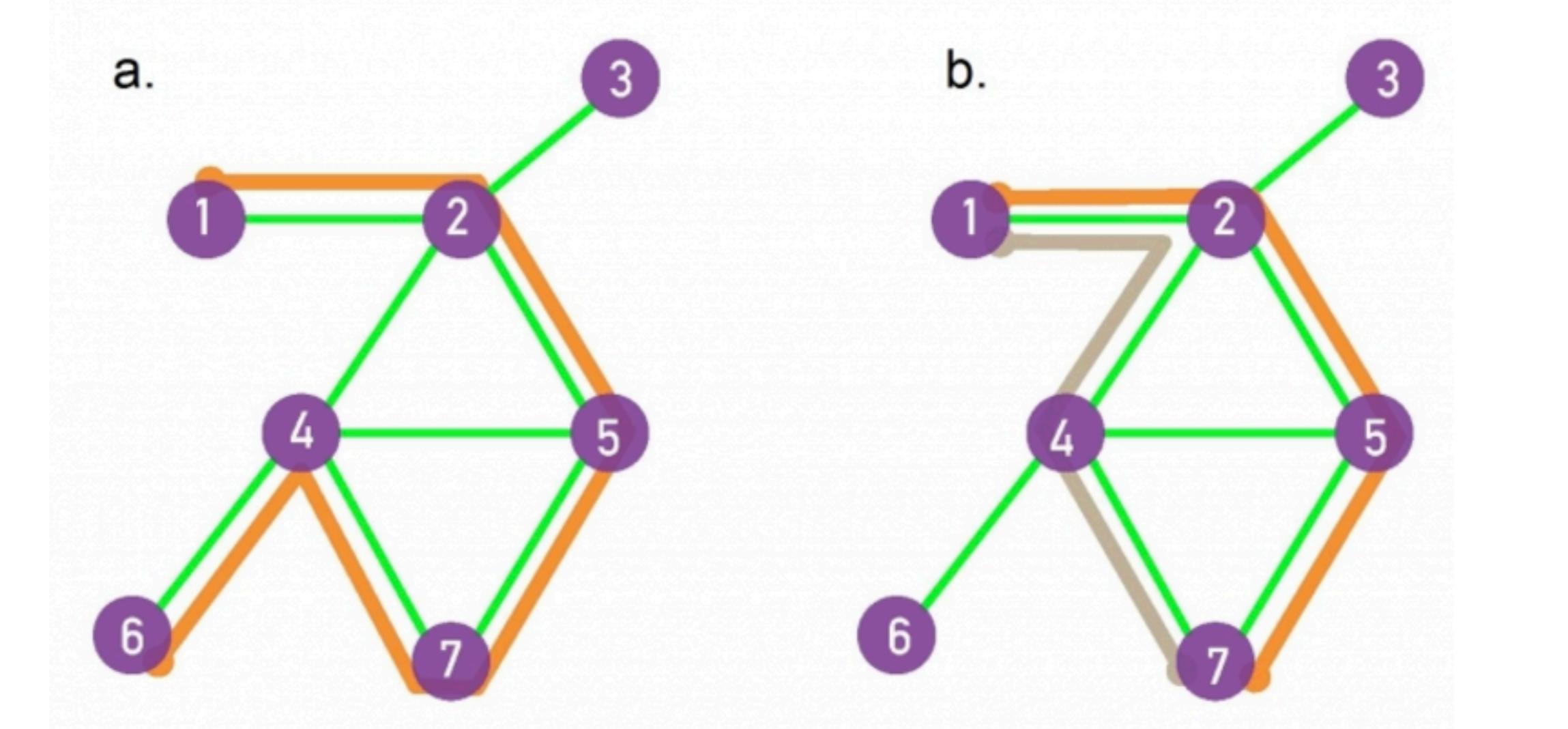
Path is route along links

Path length is the number of links contained

Shortest paths connects nodes i and j with the smallest number of links

Diameter of graph G

The longest shortest path within G.

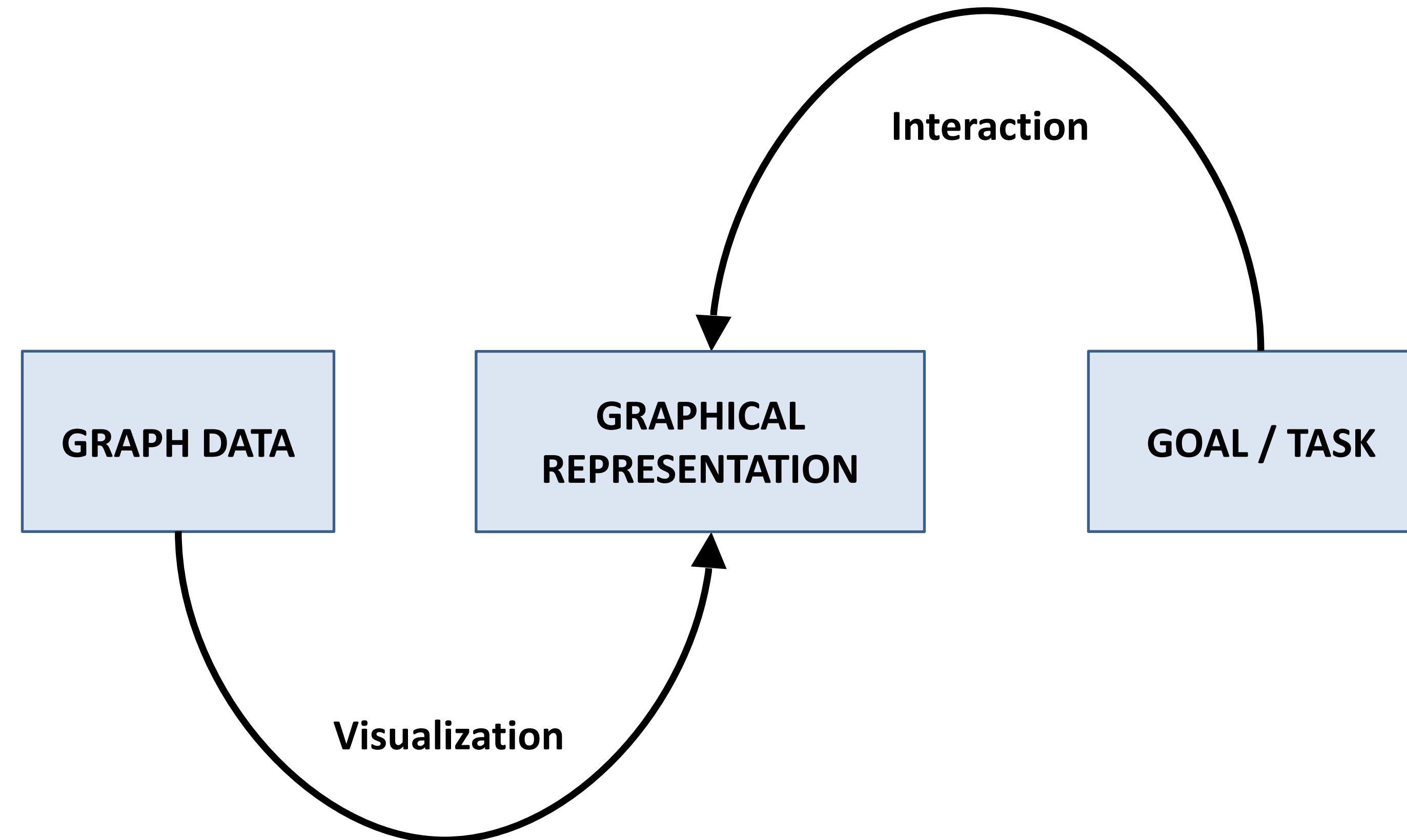


A path from 1 to 6

Shortest paths (two) from 1 to 7.

Graph and Tree Visualization

Setting the Stage



How to decide which **representation** to use for which **type of graph** in order to achieve which kind of **goal**?

Different Kinds of Tasks/Goals

Two principal types of tasks: **attribute-based (ABT)** and **topology-based (TBT)**

Localize – find a single or multiple nodes/edges that fulfill a given property

- ABT: Find the edge(s) with the maximum edge weight.
- TBT: Find all adjacent nodes of a given node.

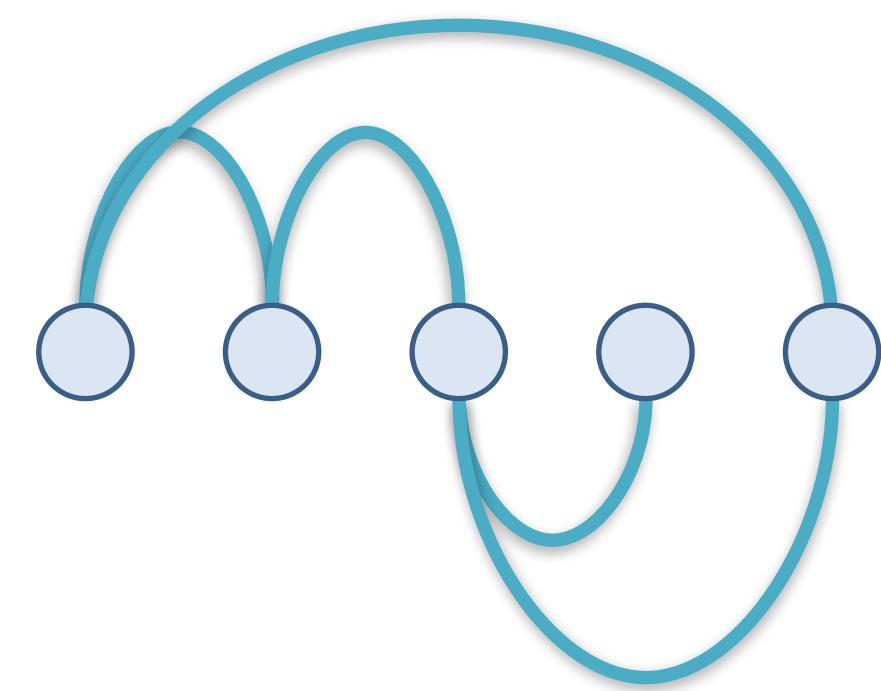
Quantify – count or estimate a numerical property of the graph

- ABT: Give the number of all nodes.
- TBT: Give the indegree (the number of incoming edges) of a node.

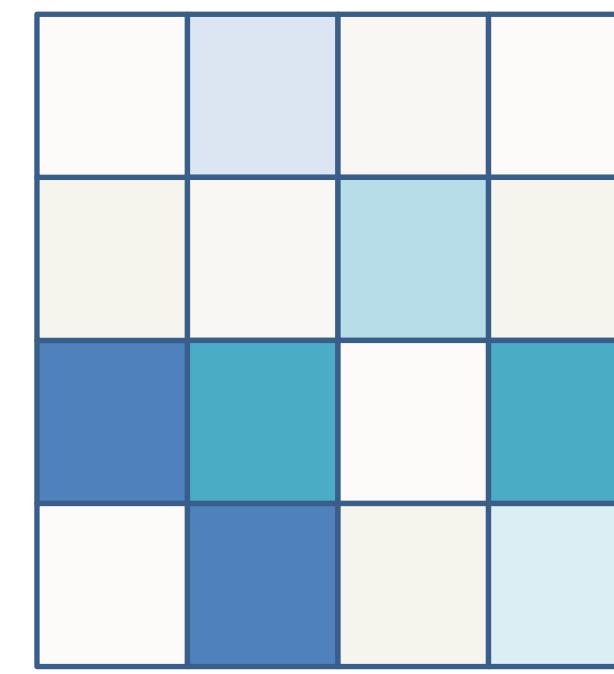
Sort/Order – enumerate the nodes/edges according to a given criterion

- ABT: Sort all edges according to their weight.
- TBT: Traverse the graph starting from a given node.

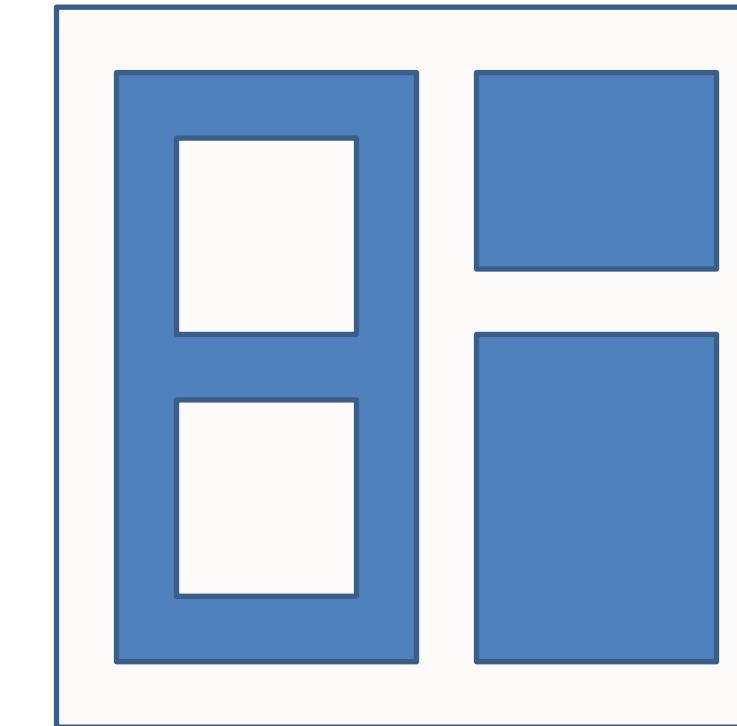
Three Types of Graph Representations



Explicit
(Node-Link)



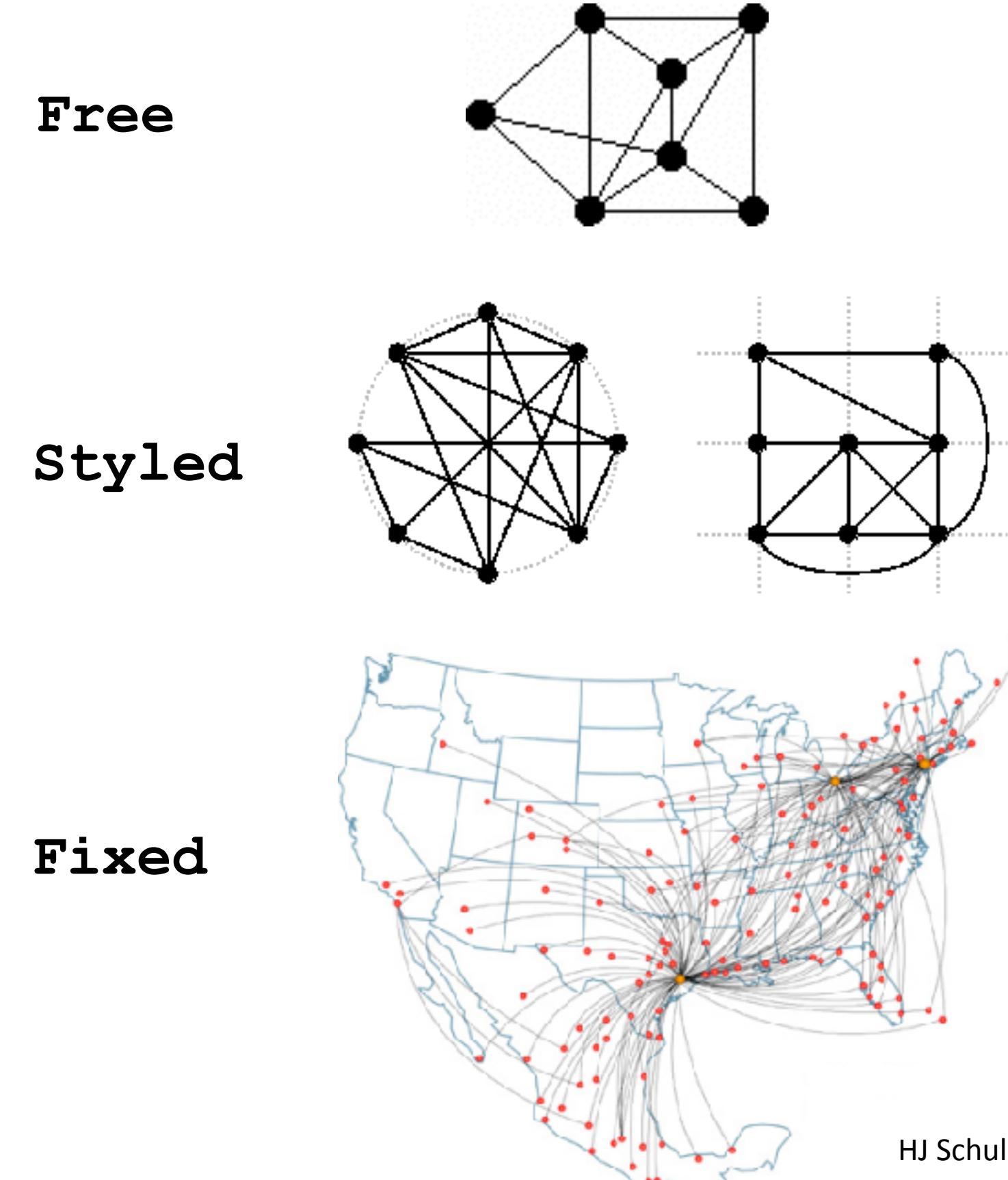
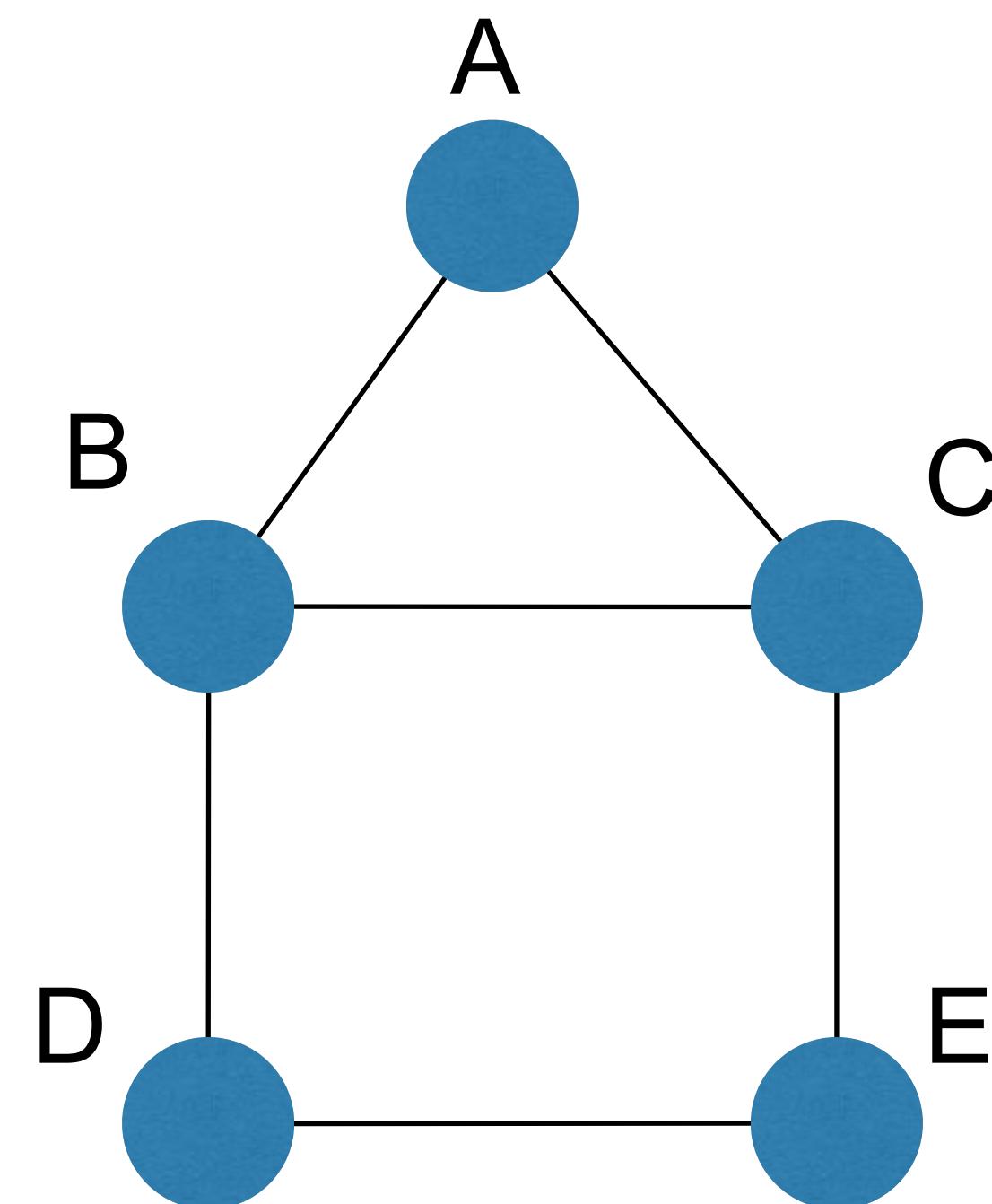
Matrix



Implicit

Explicit Graph Representations

Node-link diagrams: vertex = point, edge = line/arc



Criteria for Good Node-Link Layout

Minimized **edge crossings**

Minimized **distance** of neighboring nodes

Minimized **drawing area**

Uniform edge **length**

Minimized edge **bends**

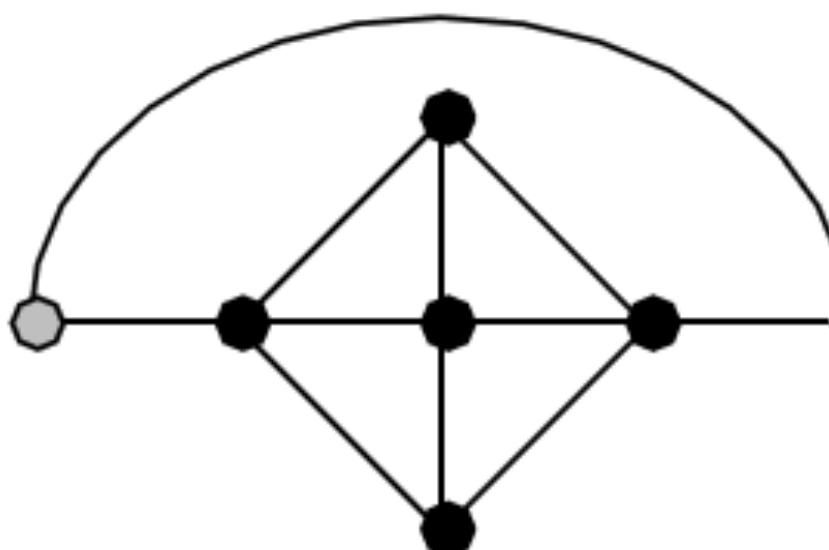
Maximized **angular distance** between different edges

Aspect ratio about 1 (not too long and not too wide)

Symmetry: similar graph structures should look similar

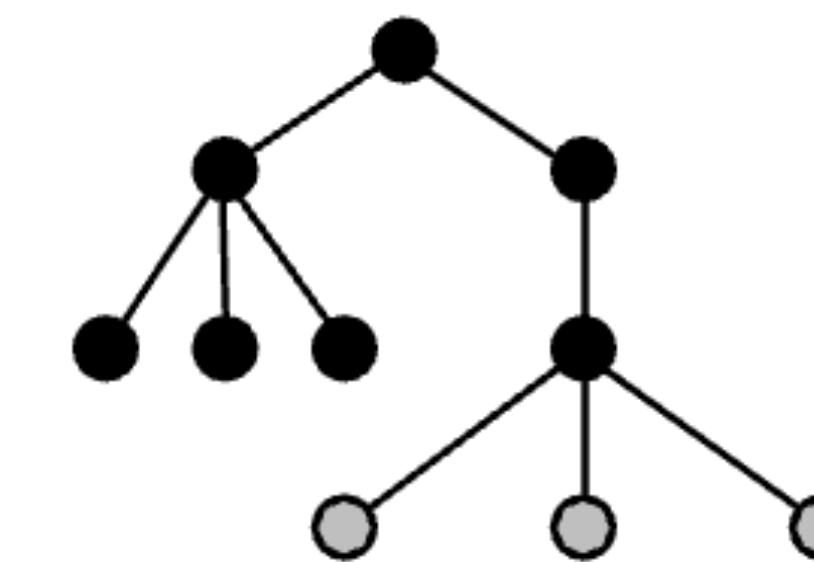
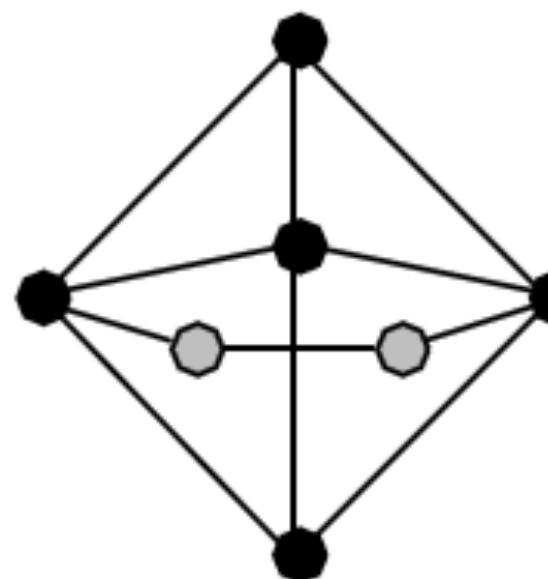
Conflicting Criteria

Minimum number
of edge crossings



vs.

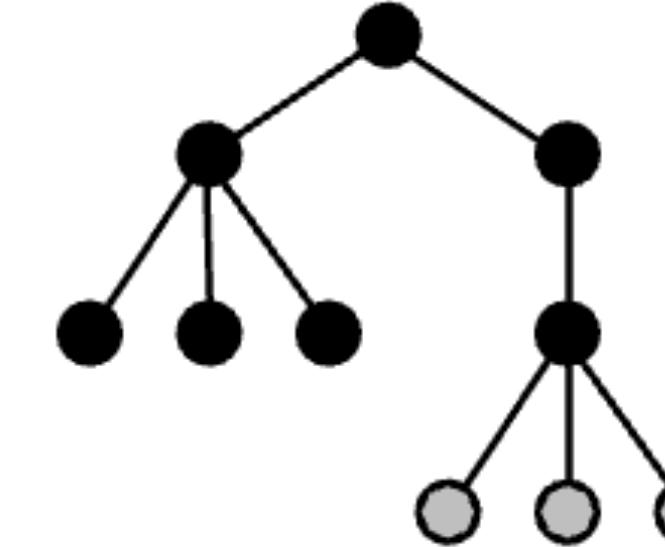
Uniform edge
length



Space utilization

vs.

Symmetry



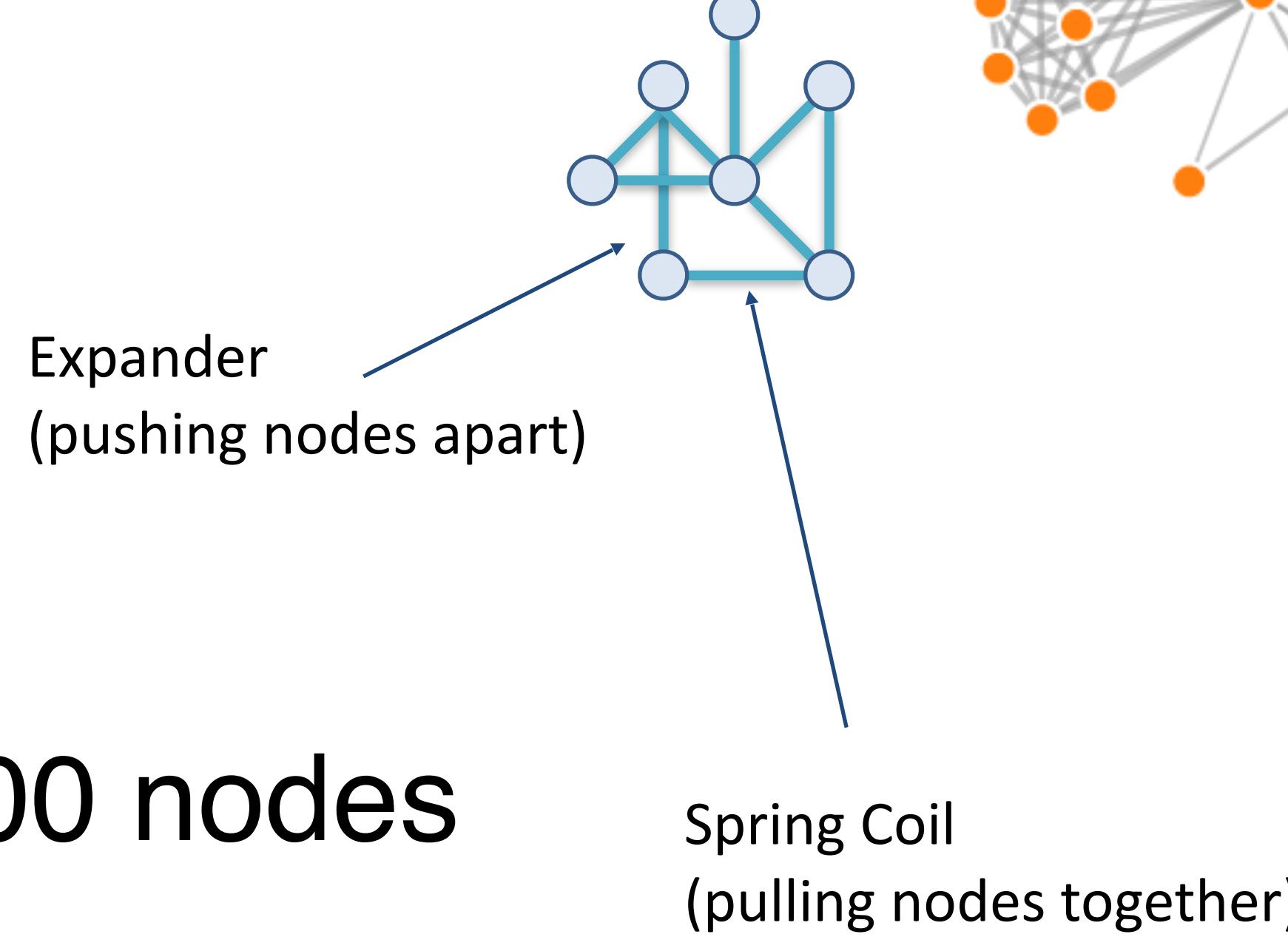
Force Directed Layouts

Physics model:
edges = springs,
vertices = repulsive magnets

in practice: damping,
center of gravity

Computationally
expensive: $O(n^3)$

Limit (interactive): ~1000 nodes





Giant Hairball

Explicit Representations

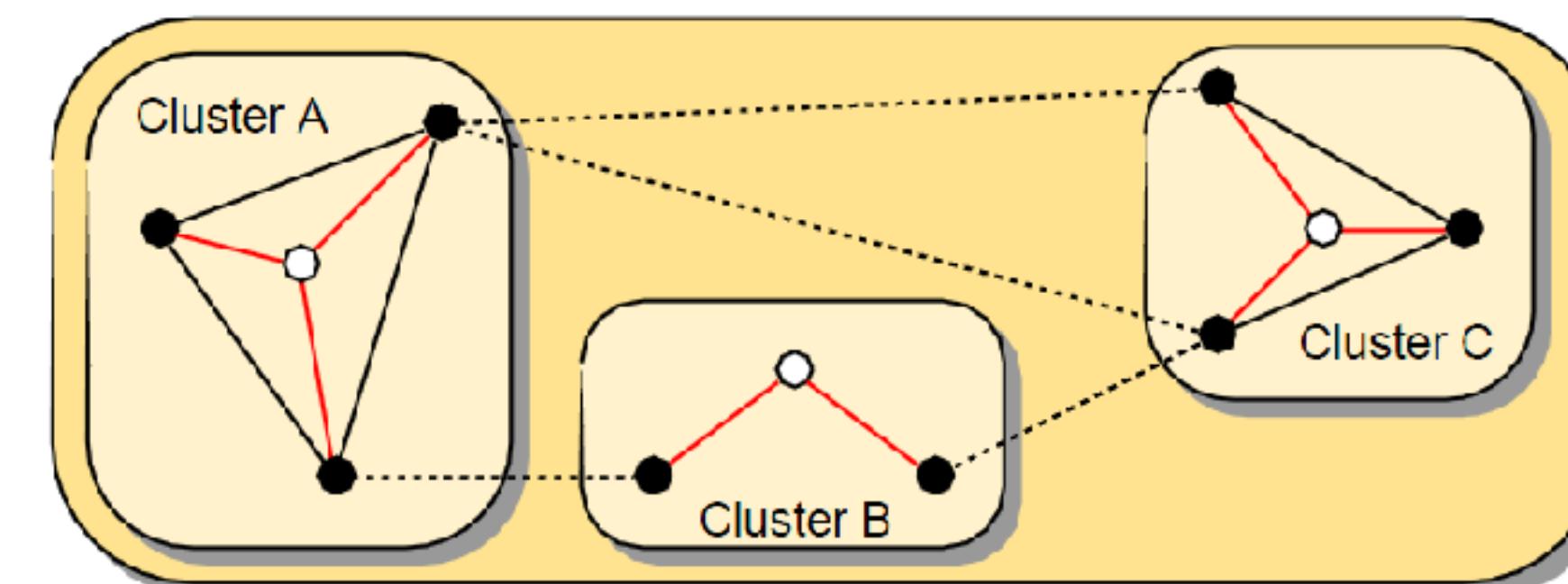
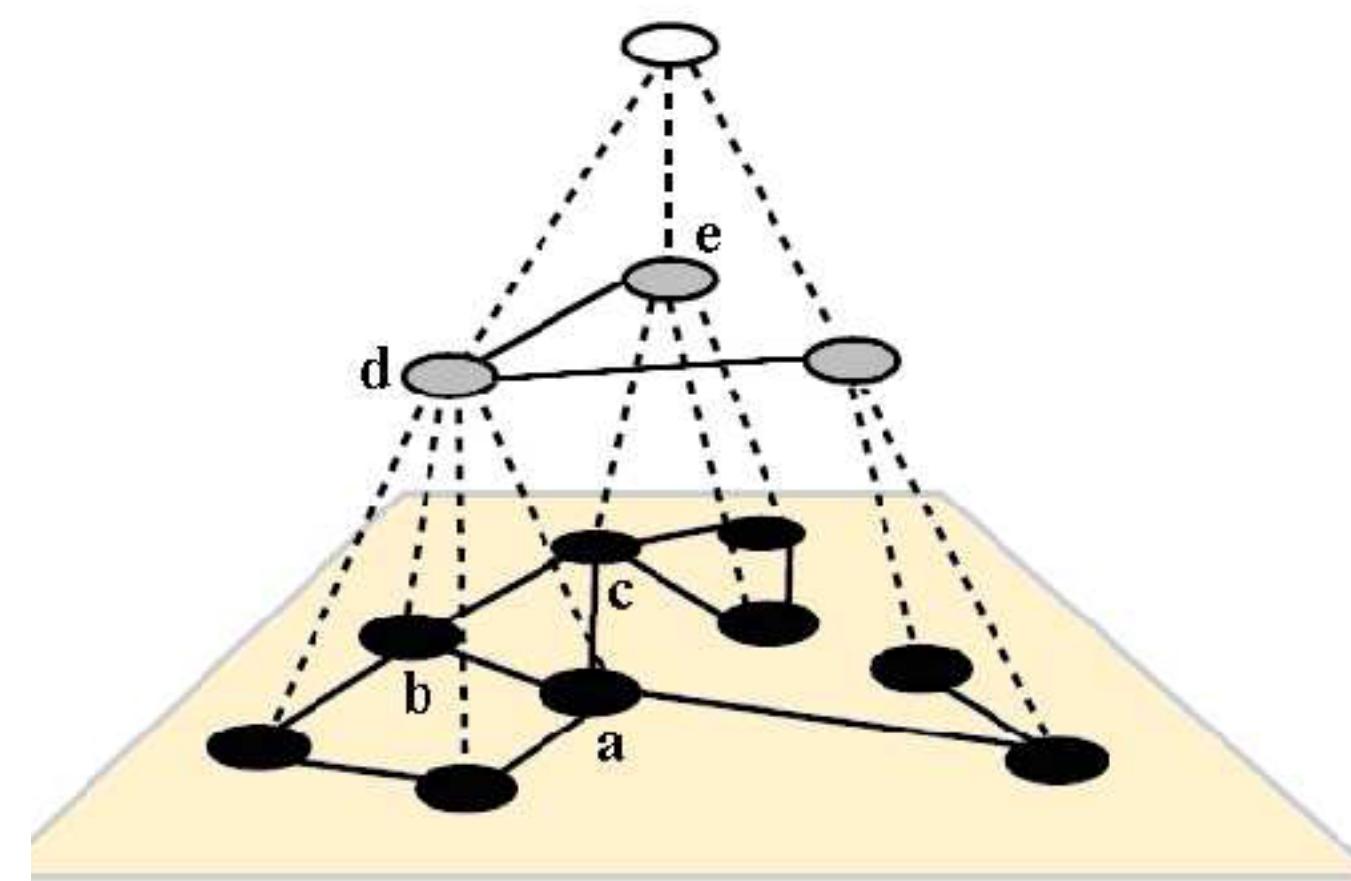
Problem #1: computing an optimal layout lies in NP

Solution approach: formulate the layout problem as an optimization problem

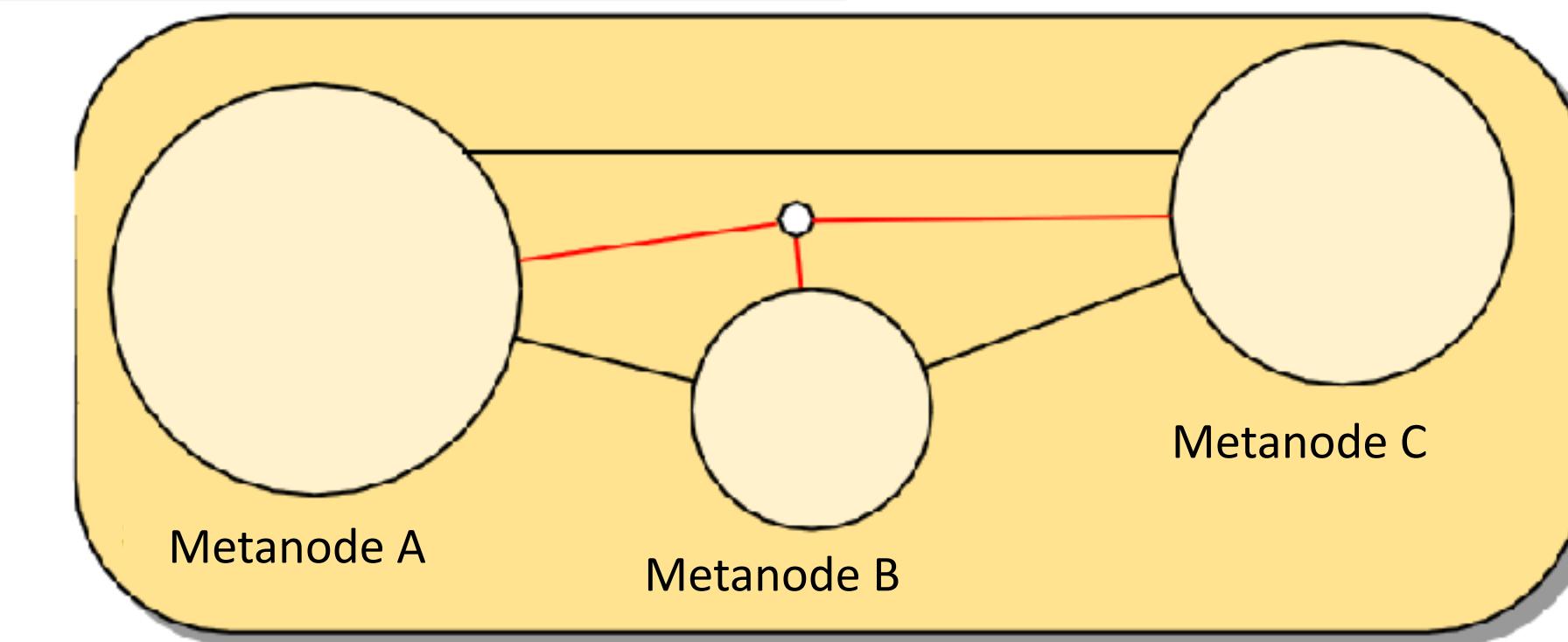
BUT: naïve runtime complexity is still $O(n^2)$!

in each optimization step, all vertices have to be checked against all other vertices

Address Computational Scalability: Multilevel Approaches

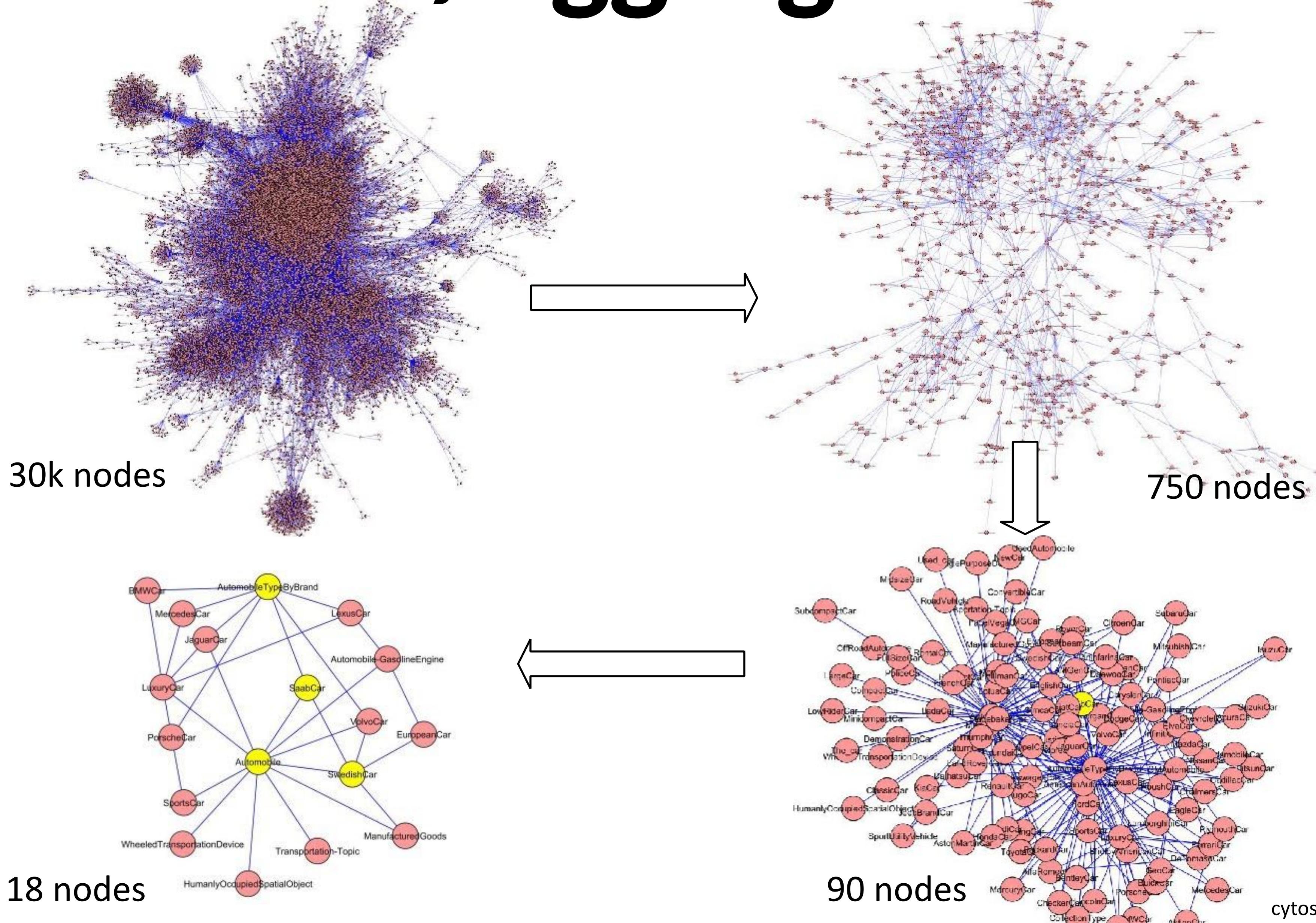


- real vertex
- virtual vertex
- internal spring
- virtual spring
- - - external spring



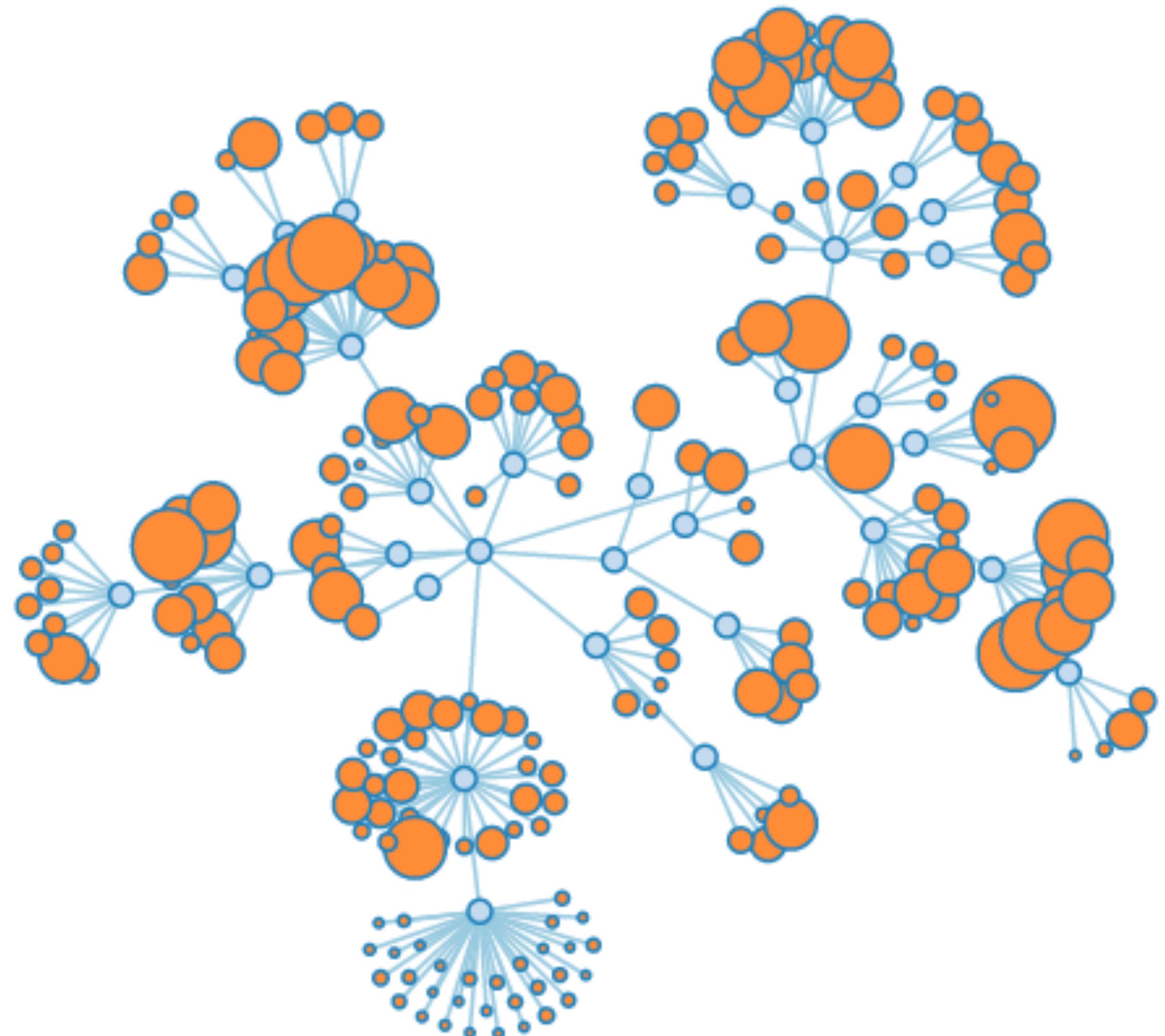
[Schulz 2004]

Abstraction/Aggregation



Collapsible Force Layout

Supernodes: aggregate of nodes
manual or algorithmic clustering

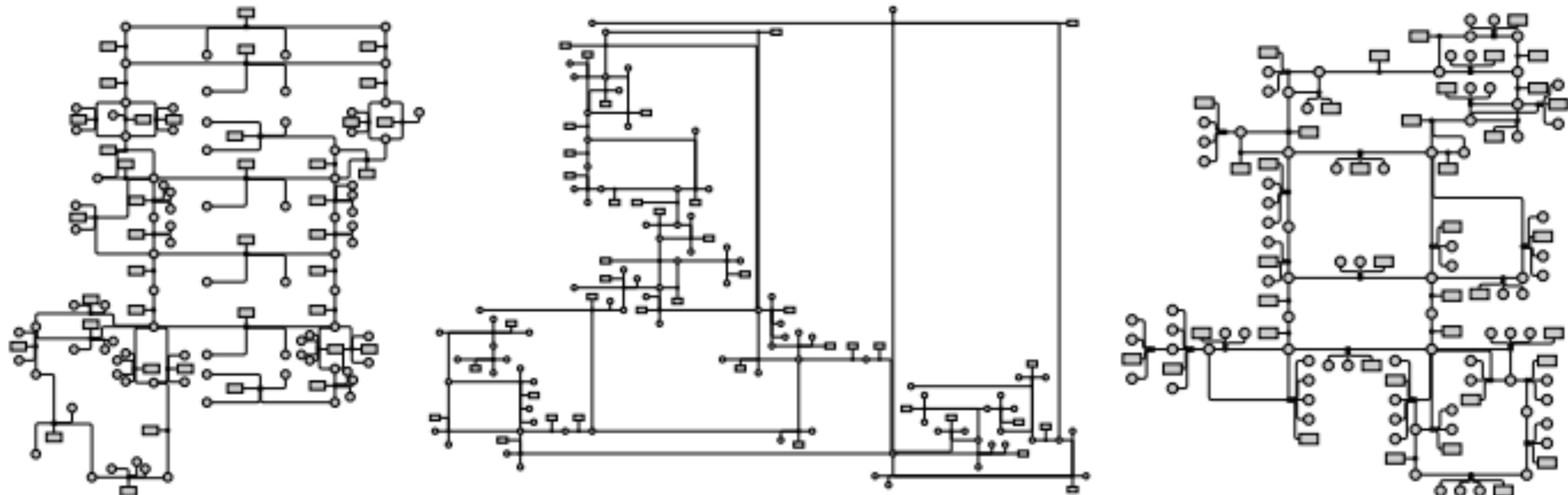


HOLA: Human-like Orthogonal Layout

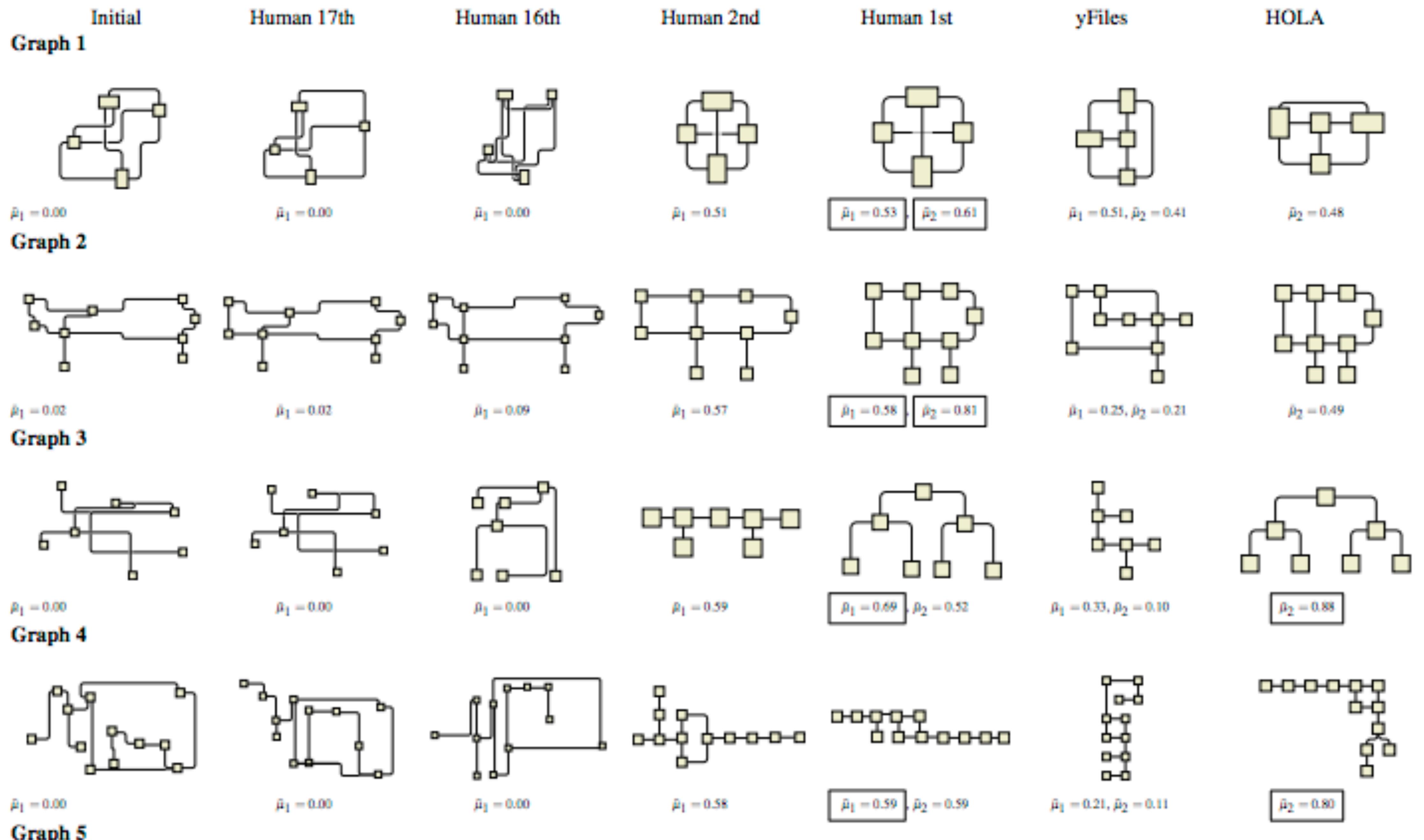
Study how humans lay-out a graph

Try to emulate layout

Left: human, middle: conventional algo, right new algo



[Kieffer et al, InfoVis 2015]

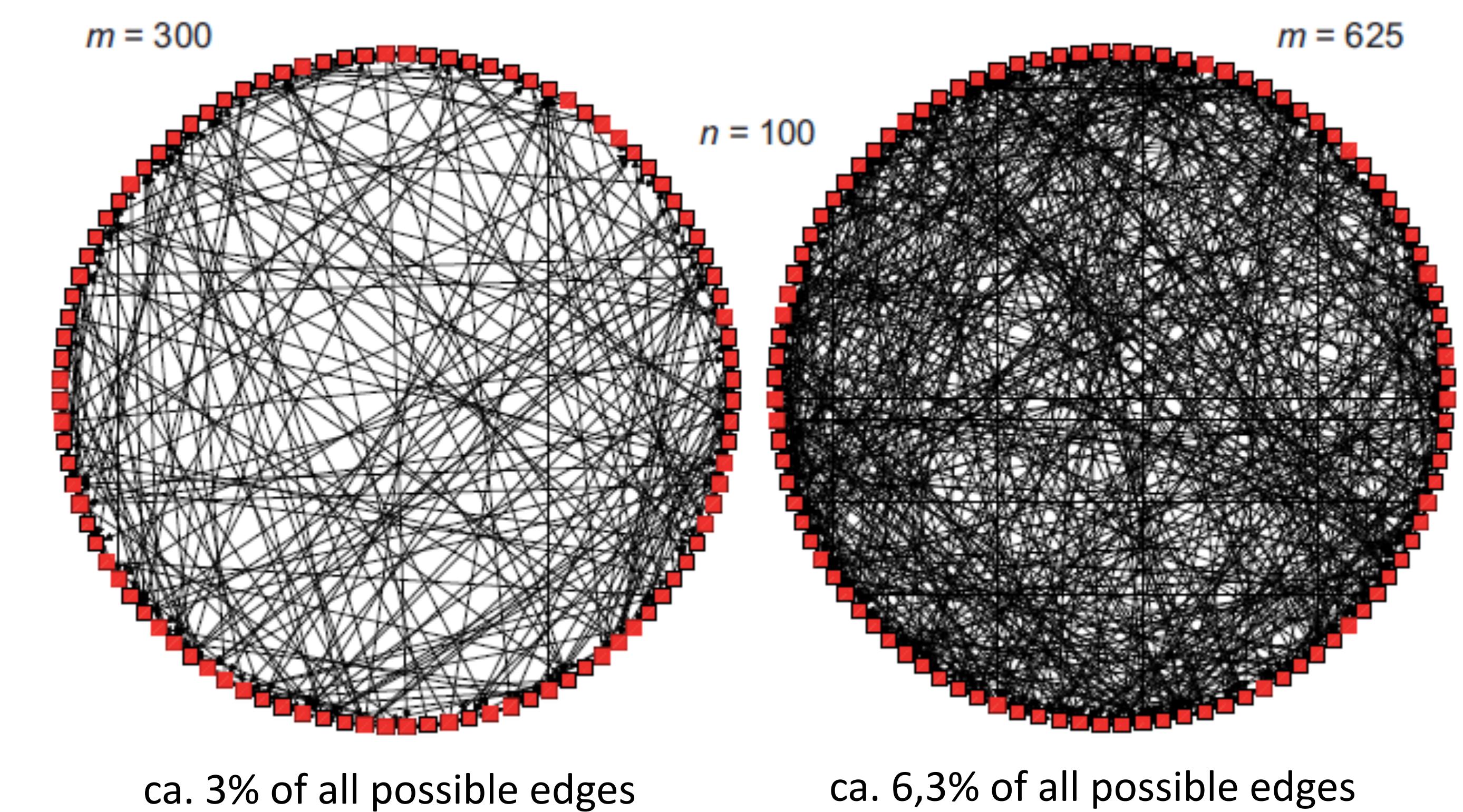


Styled / Restricted Layouts

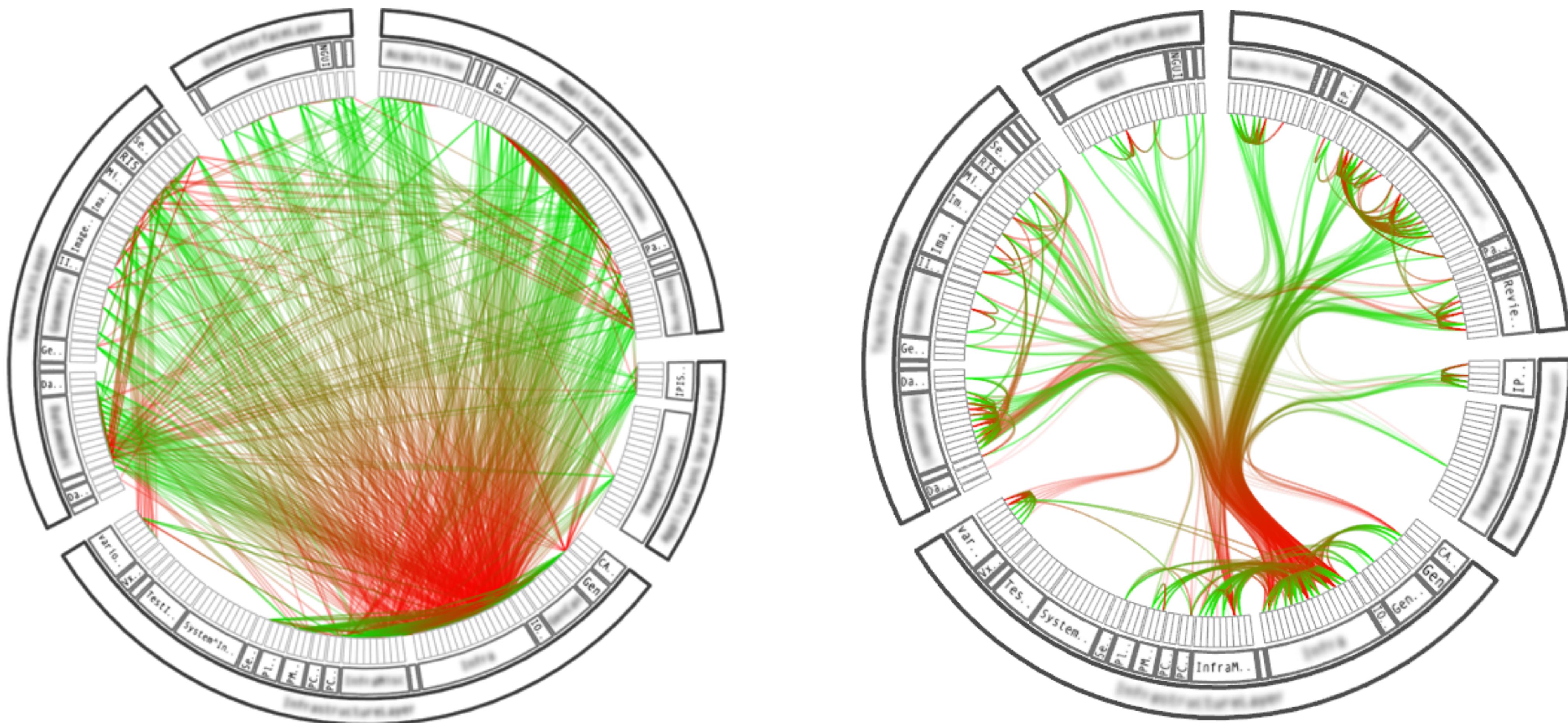
Circular Layout

Node ordering

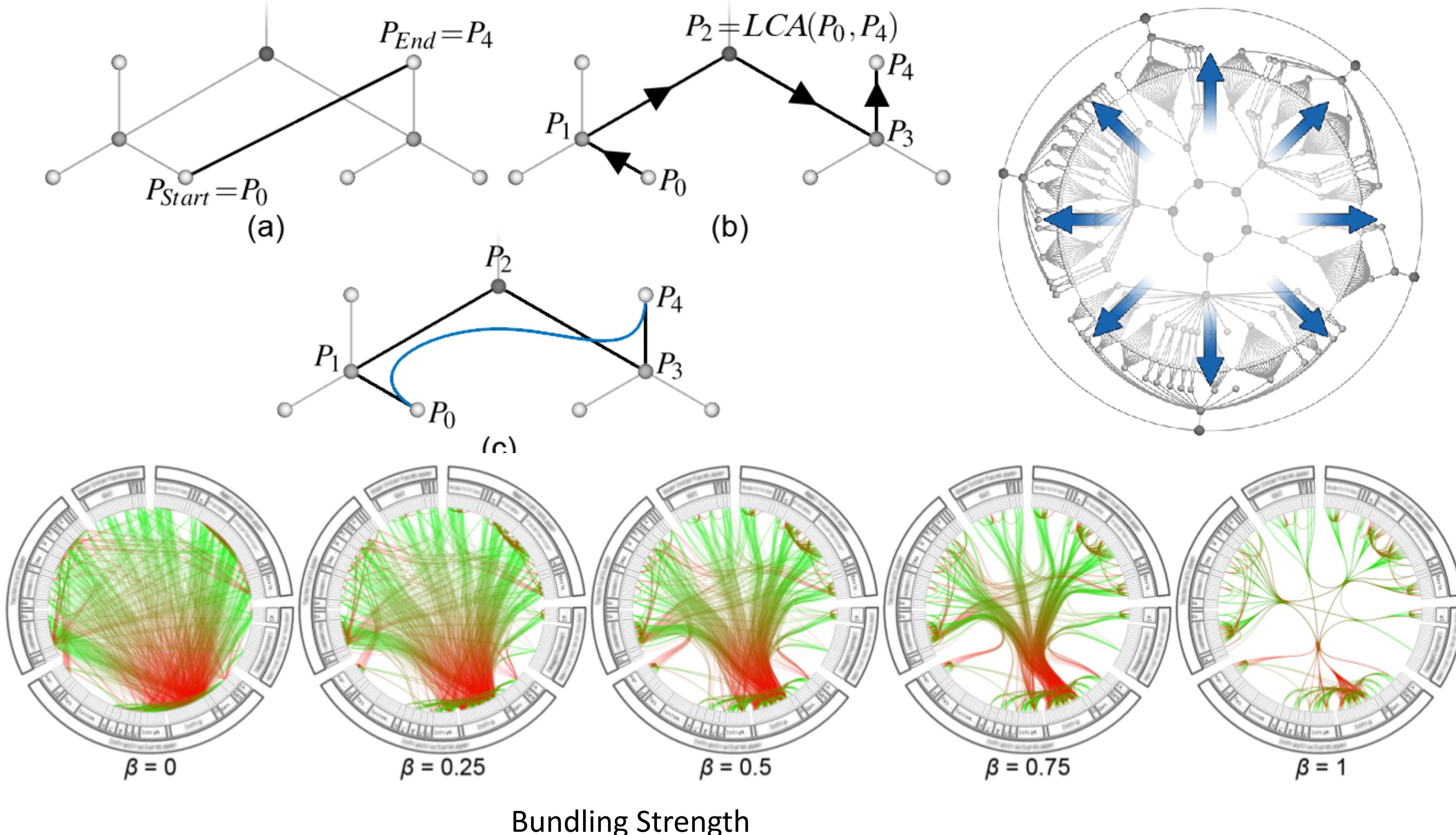
Edge Clutter



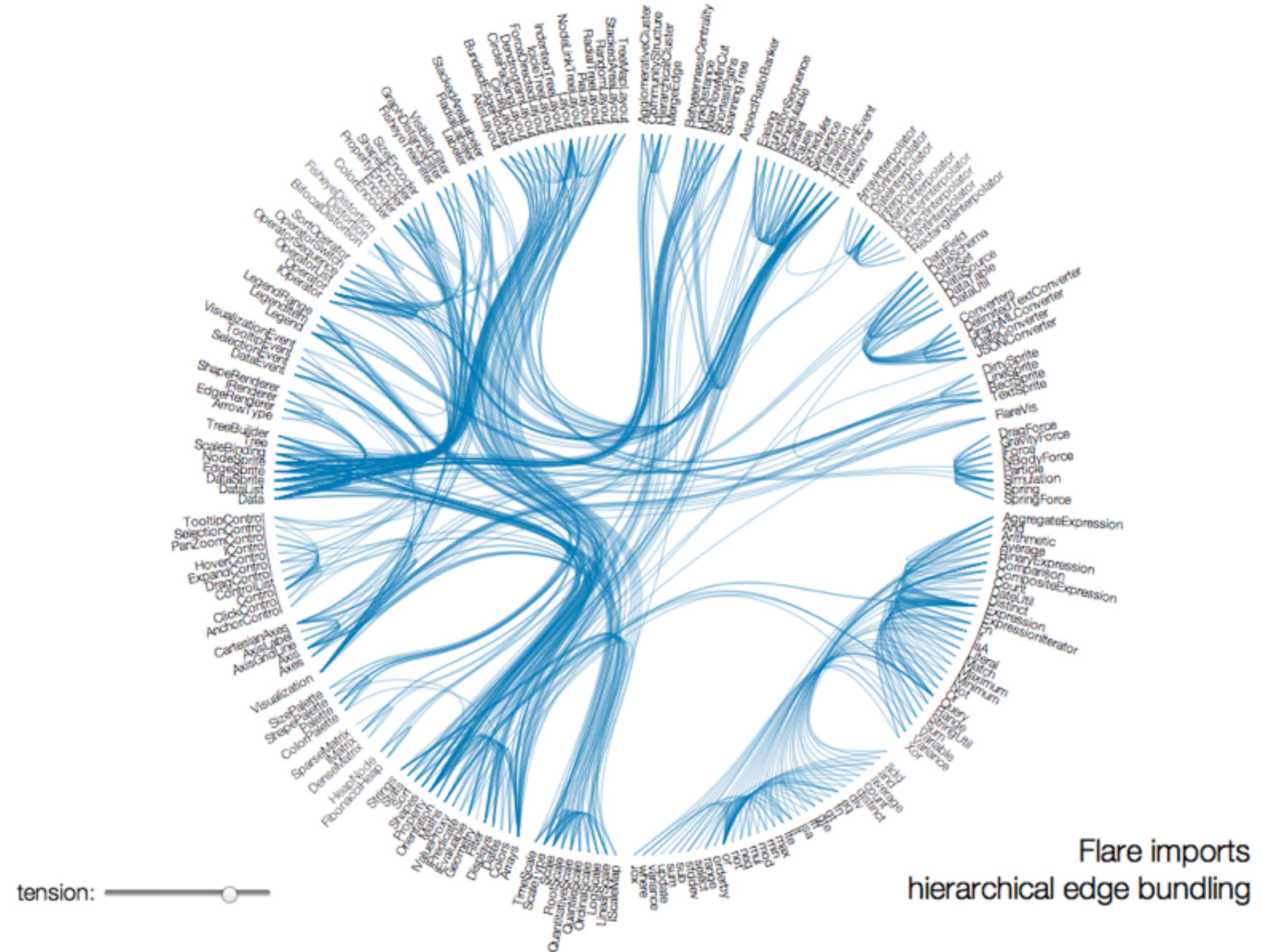
Reduce Clutter: Edge Bundling



Hierarchical Edge Bundling



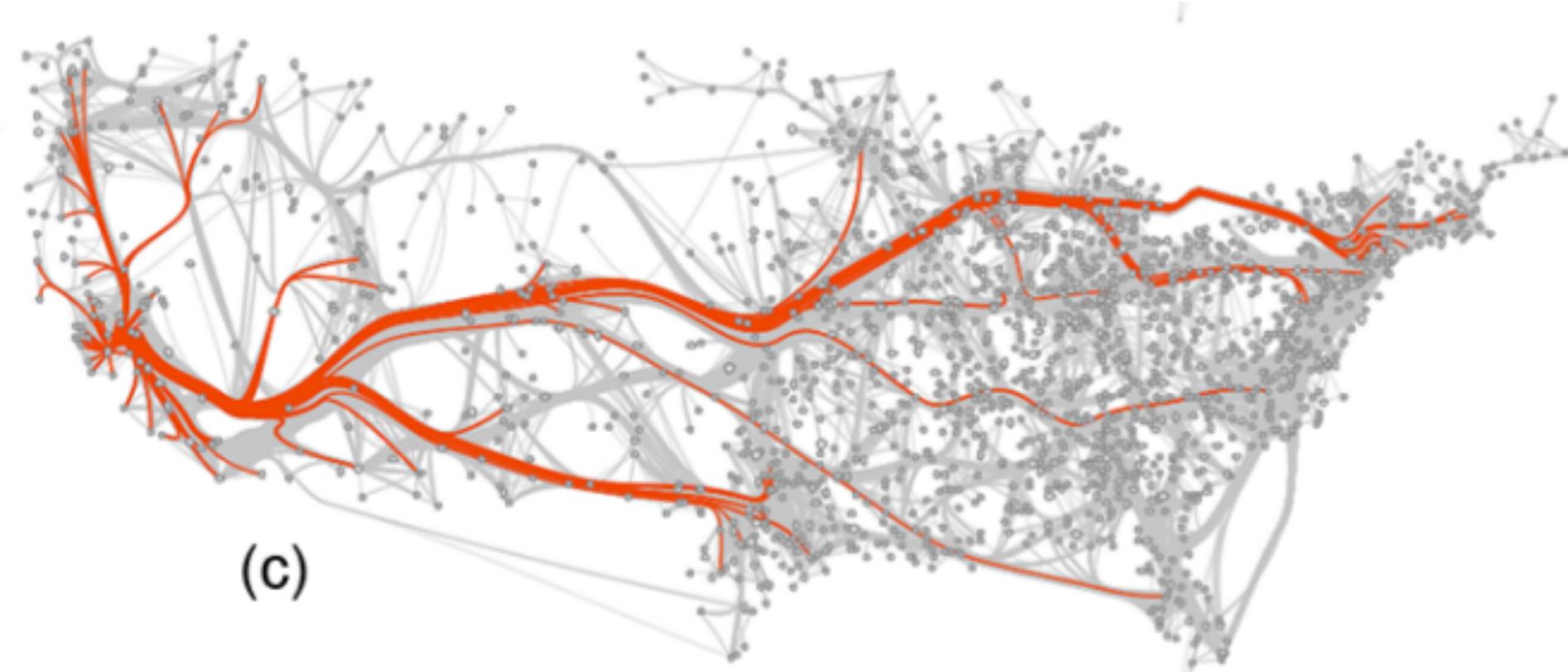
Bundling Strength



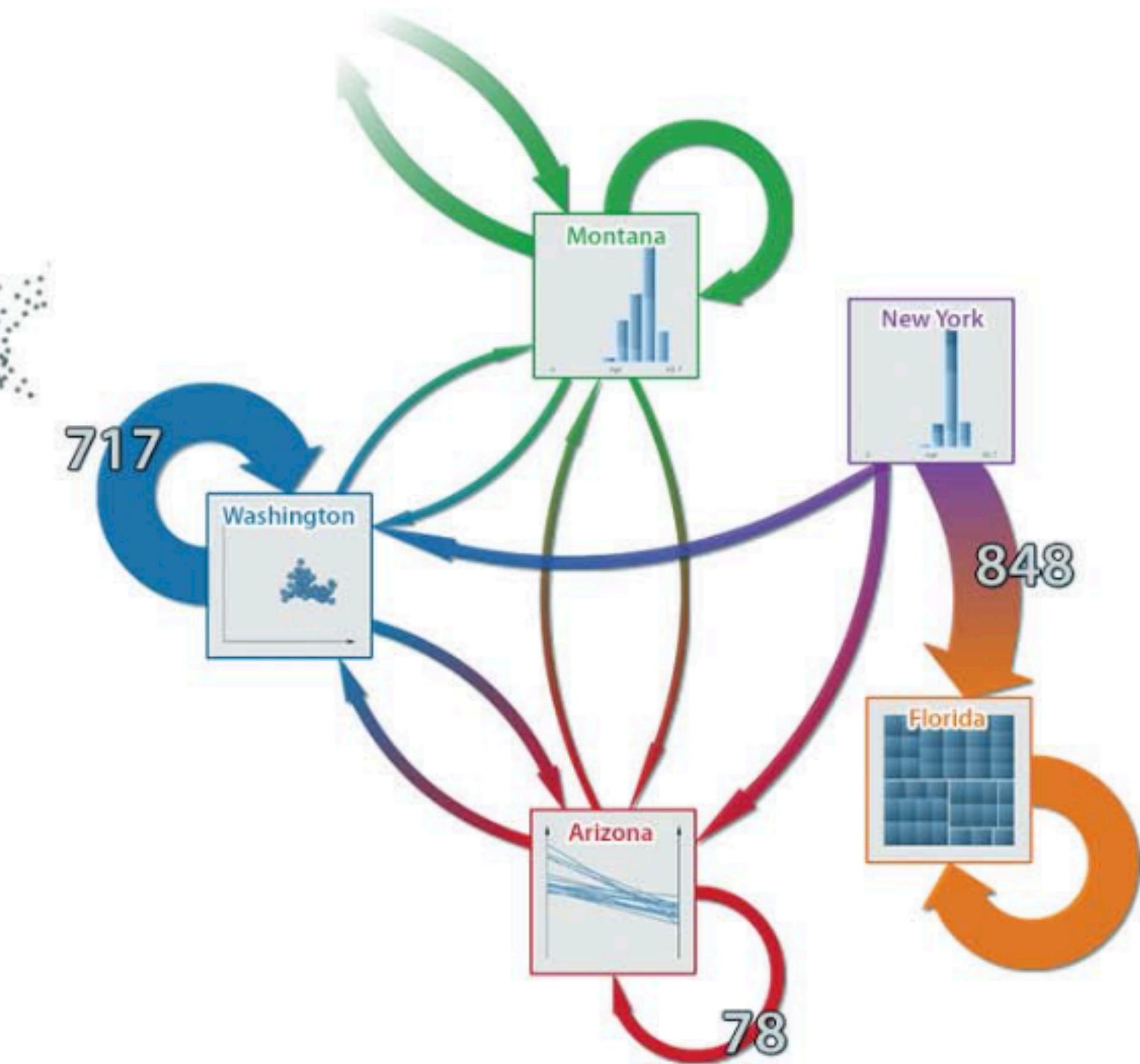
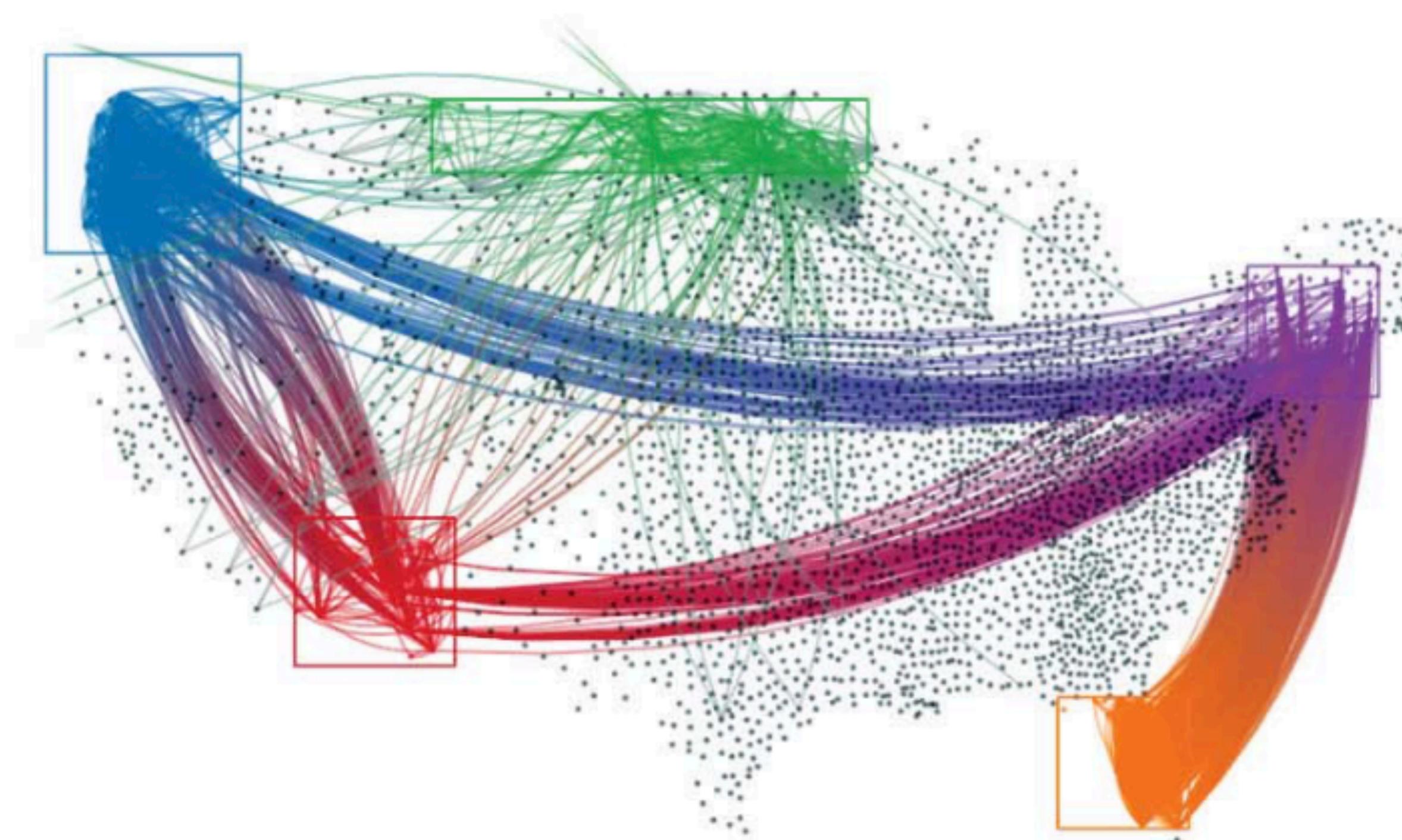
Fixed Layouts

Can't vary position of nodes

Edge routing important



Aggregation

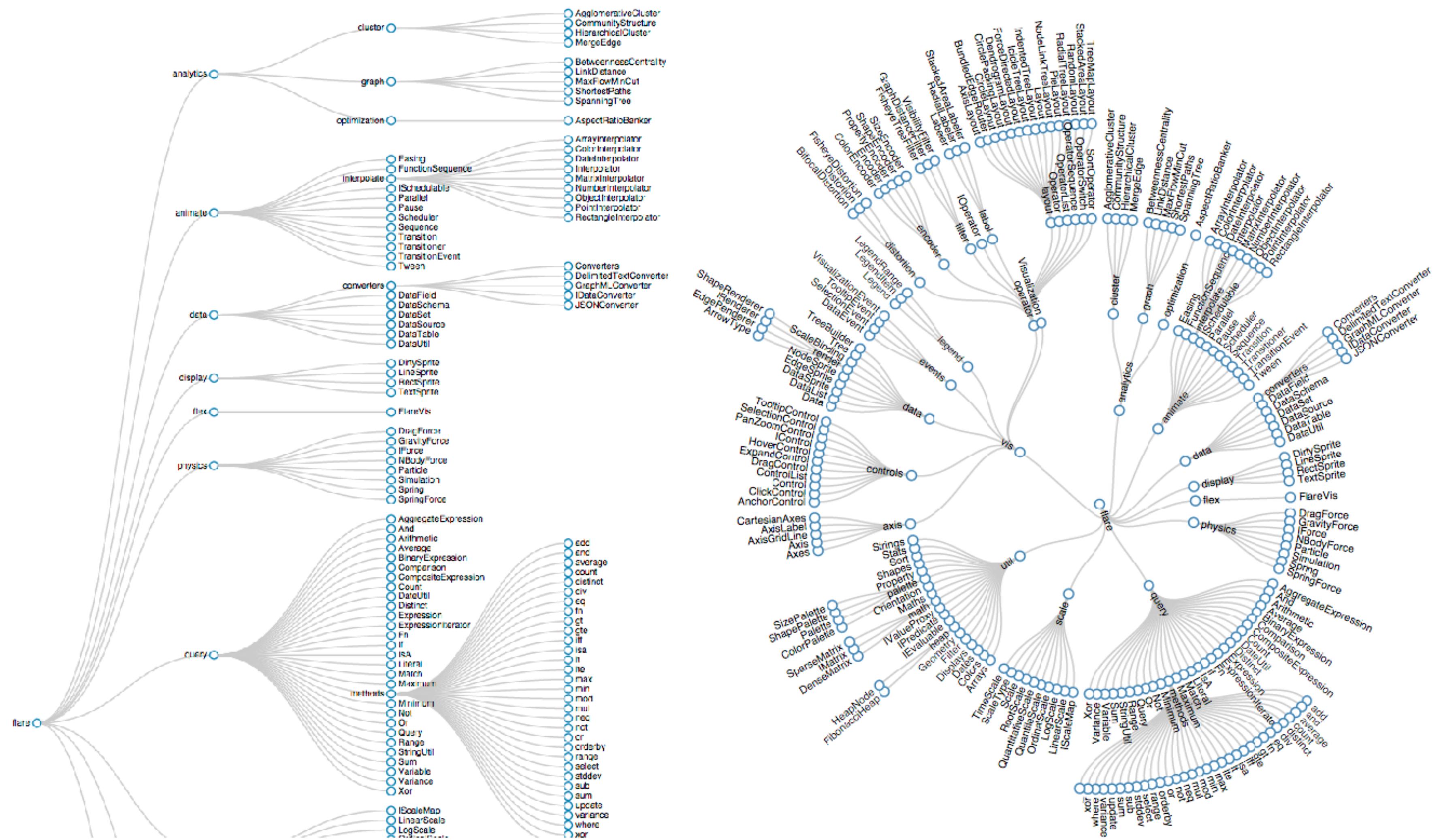


<https://www.youtube.com/watch?v=E1PVTitj7h0>

Explicit Tree visualization

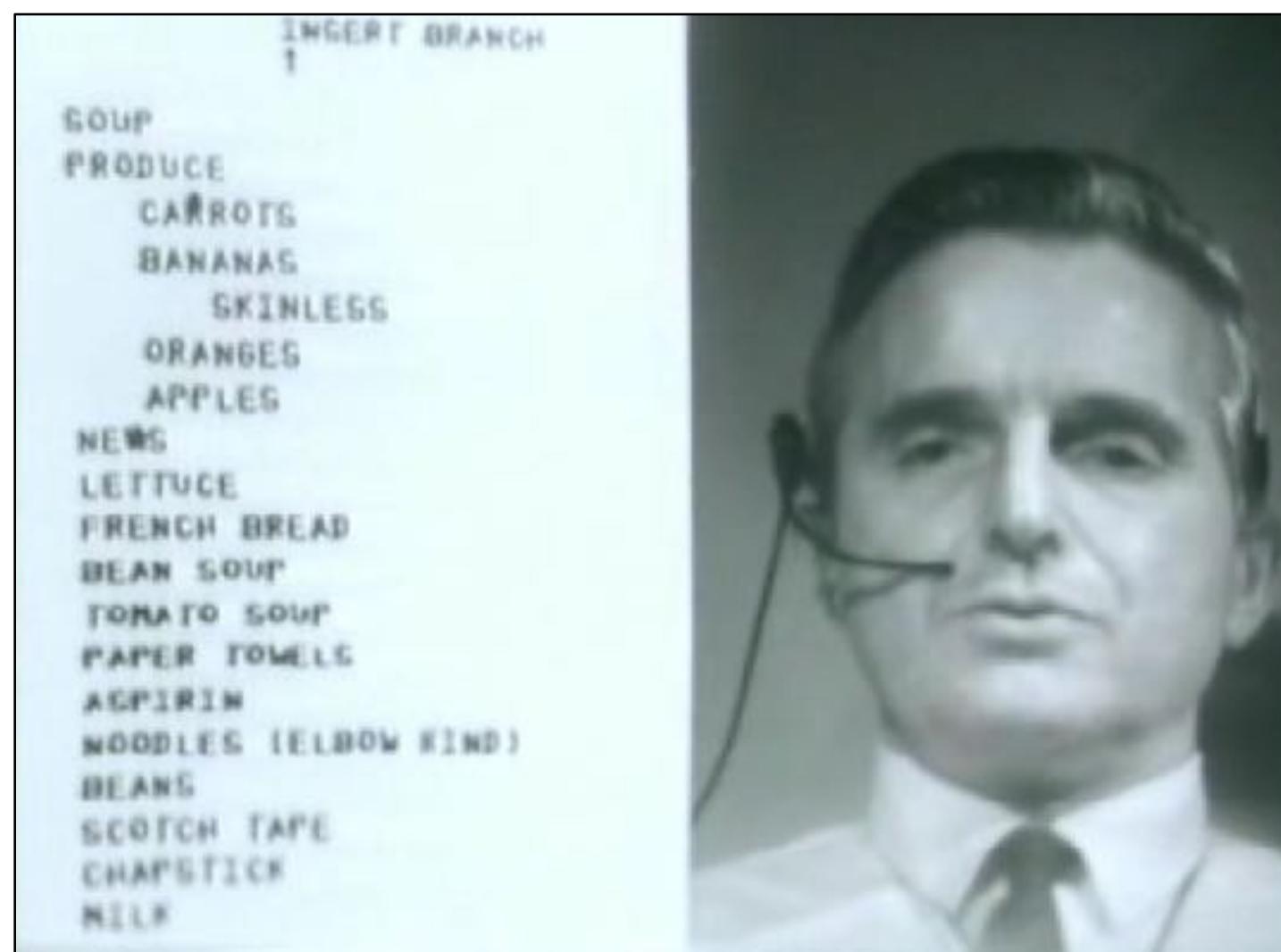
Reingold– Tilford layout

<http://billmill.org/pymag-trees/>

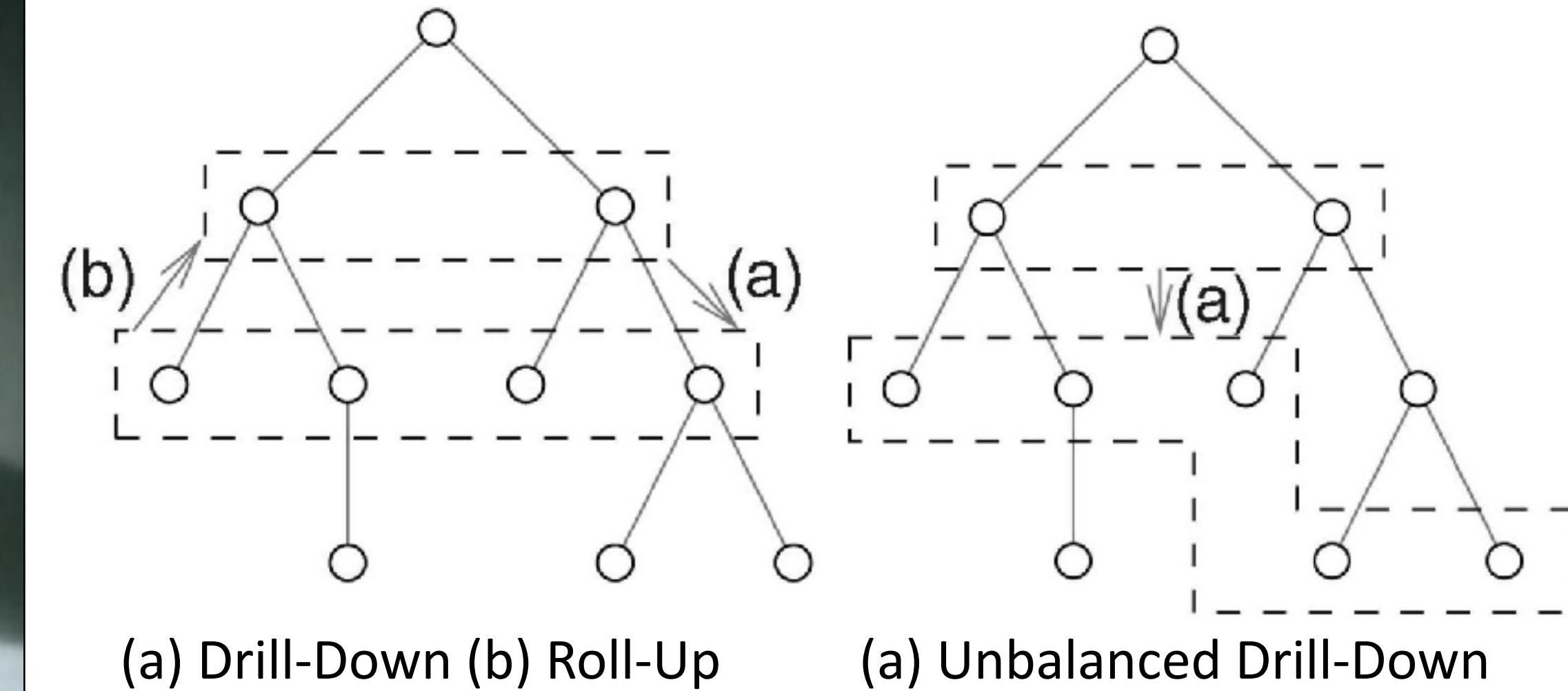


Manipulating Aggregation Levels

First interactive tree manipulation



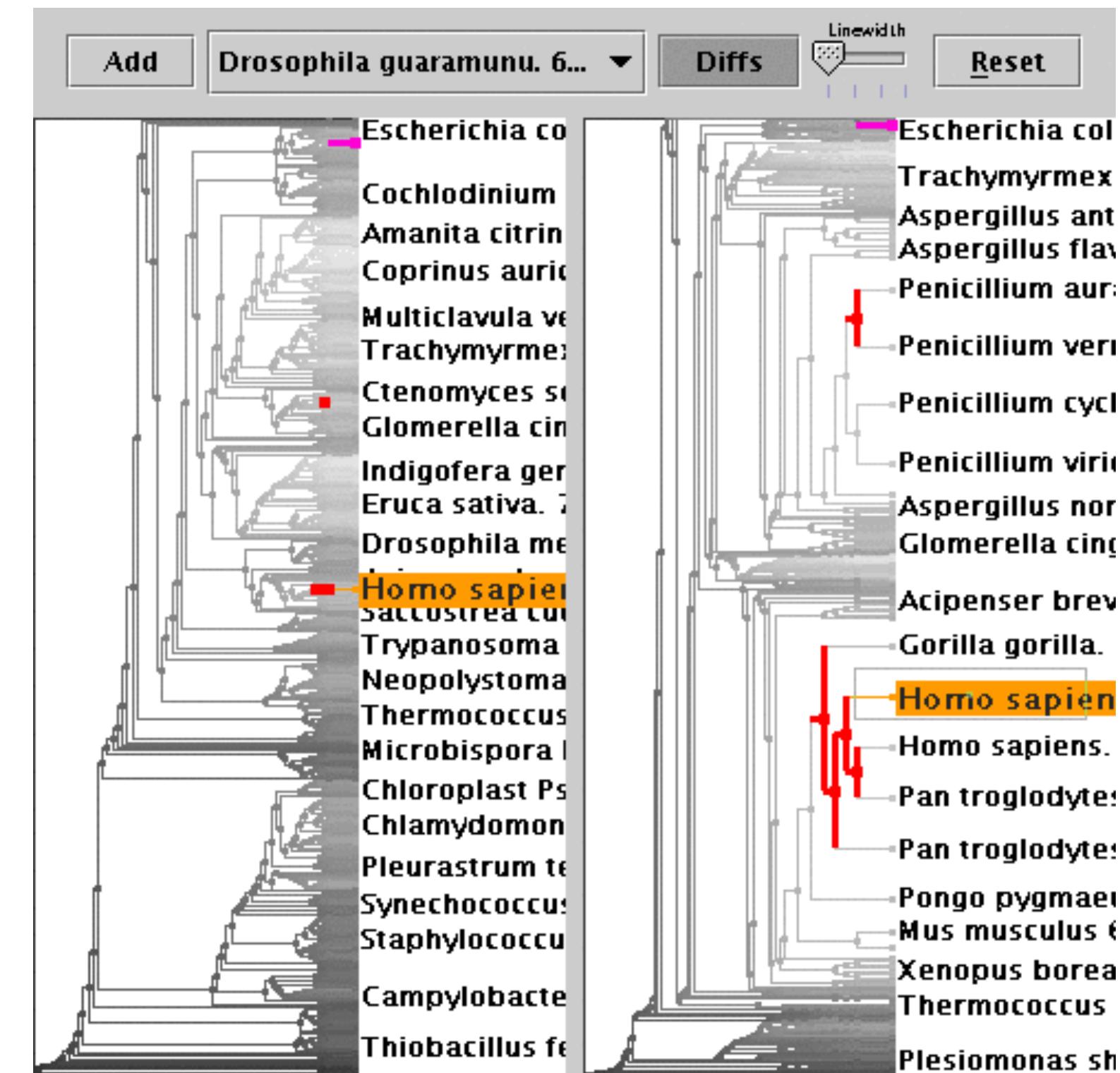
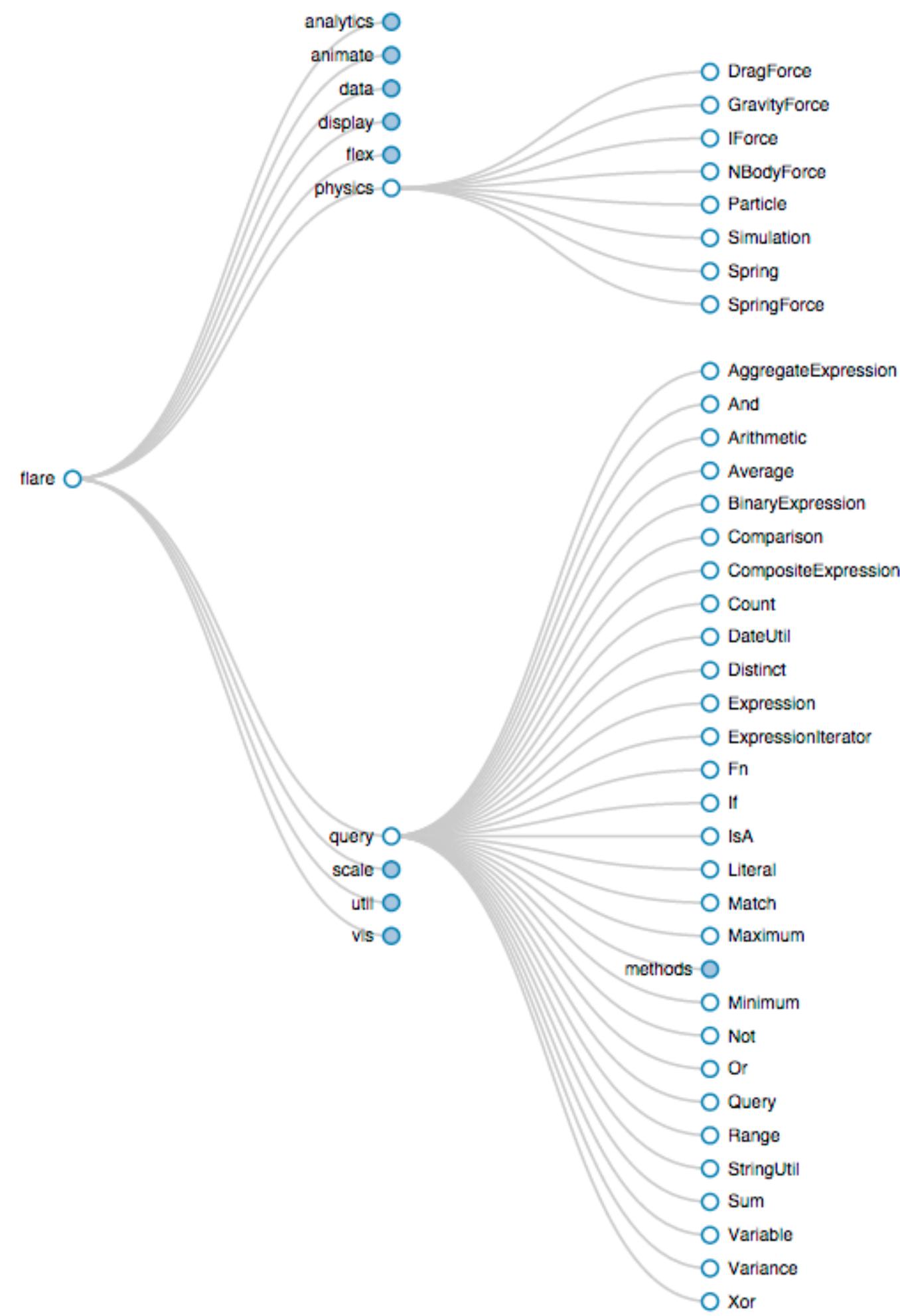
Douglas Engelbart 1968 - <http://www.1968demo.org>



“The mother of all demos”

<https://www.youtube.com/watch?v=yJDv-zdhzMY>

Tree Interaction, Tree Comparison



Explicit Representations

Pros:

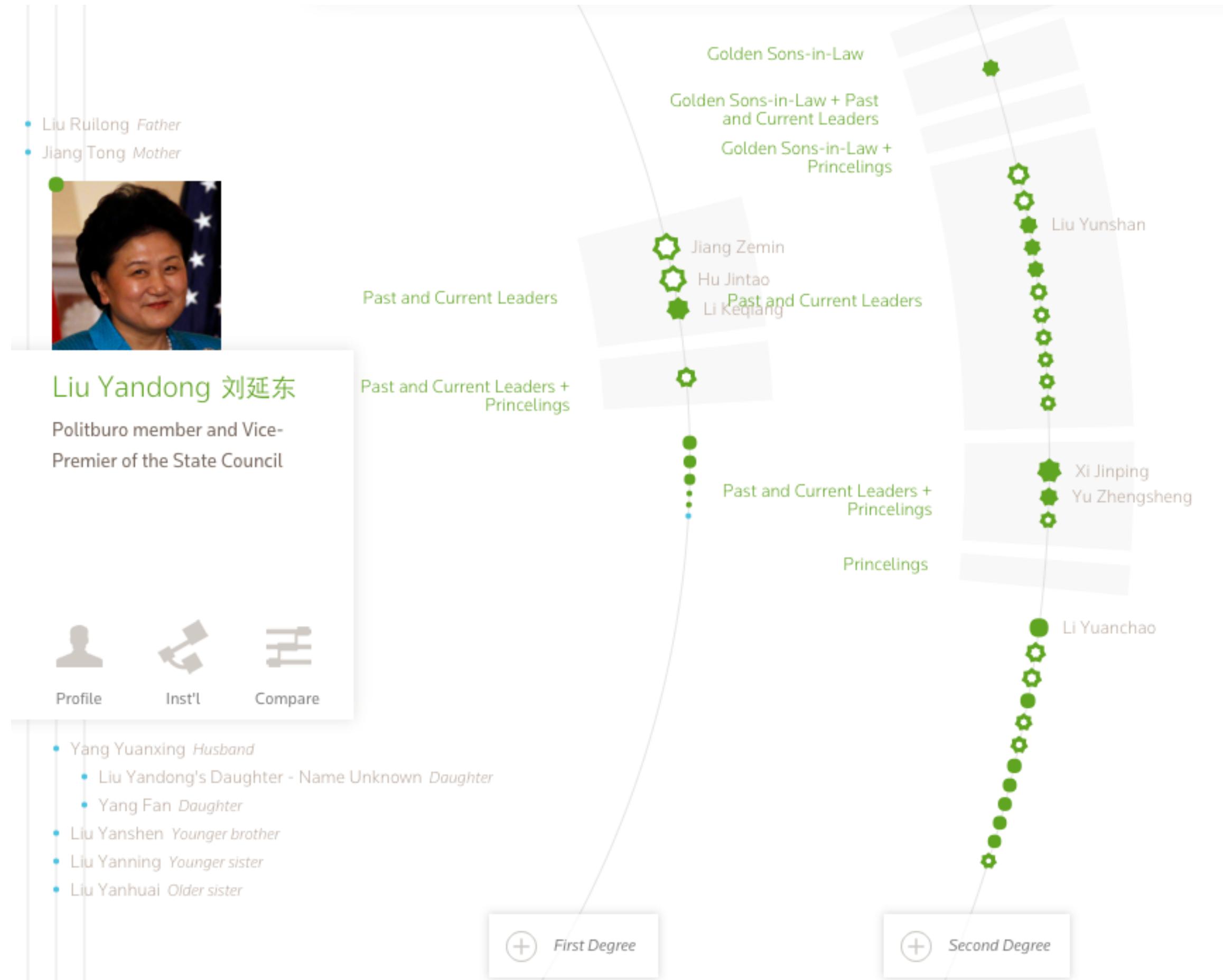
- is able to depict all graph classes
- can be customized by weighing the layout constraints
- very well suited for TBTs, if also a suitable layout is chosen

Cons:

- computation of an optimal graph layout is in NP
(even just achieving minimal edge crossings is already in NP)
- even heuristics are still slow/complex (e.g., naïve spring embedder is in $O(n^2)$)
- has a tendency to clutter (edge clutter, “hairball”)

Design Critique

Connected China



<https://goo.gl/YXkWYX>

<http://china.fathom.info/>

Multivariate Graphs

Networks and Attributes

Attributes can influence topology

Path can be slow / blocked

best route when driving depends on traffic

biological network depends on many factors

Challenge: Data Scale & Heterogeneity

Large number of values

Large datasets have more than 500 experiments

Multiple groups/conditions

Different types of data

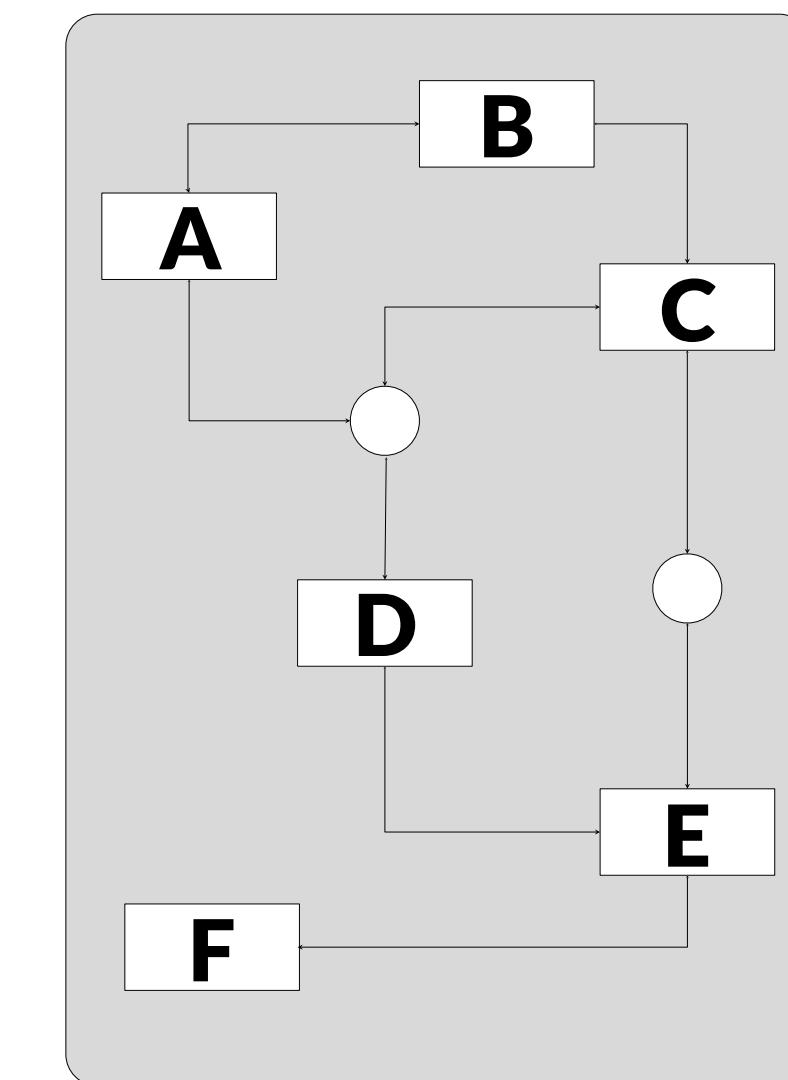
Challenge: Supporting Multiple Tasks

Two central tasks:

Explore *topology* of network

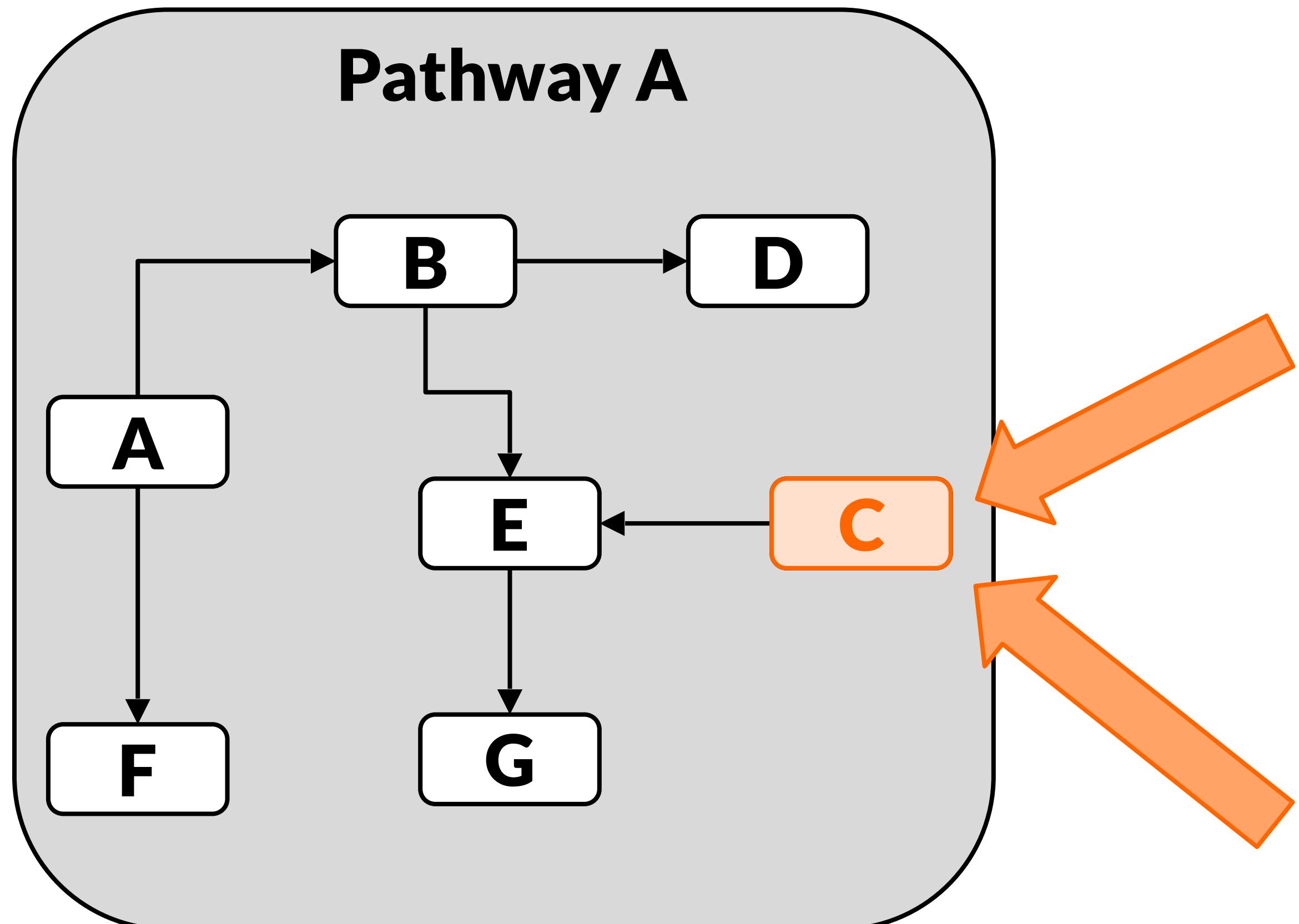
**Explore the *attributes* of the nodes
(experimental data)**

Need to support both!



	Sample 1	Sample 2	Sample 3
Gene 1	1	1.1	0.4
Gene 2	2	0.5	1.2
Gene 3	1.4	0.2	0.5
Gene 4	0.3	0.5	0.7

Many Node Attributes

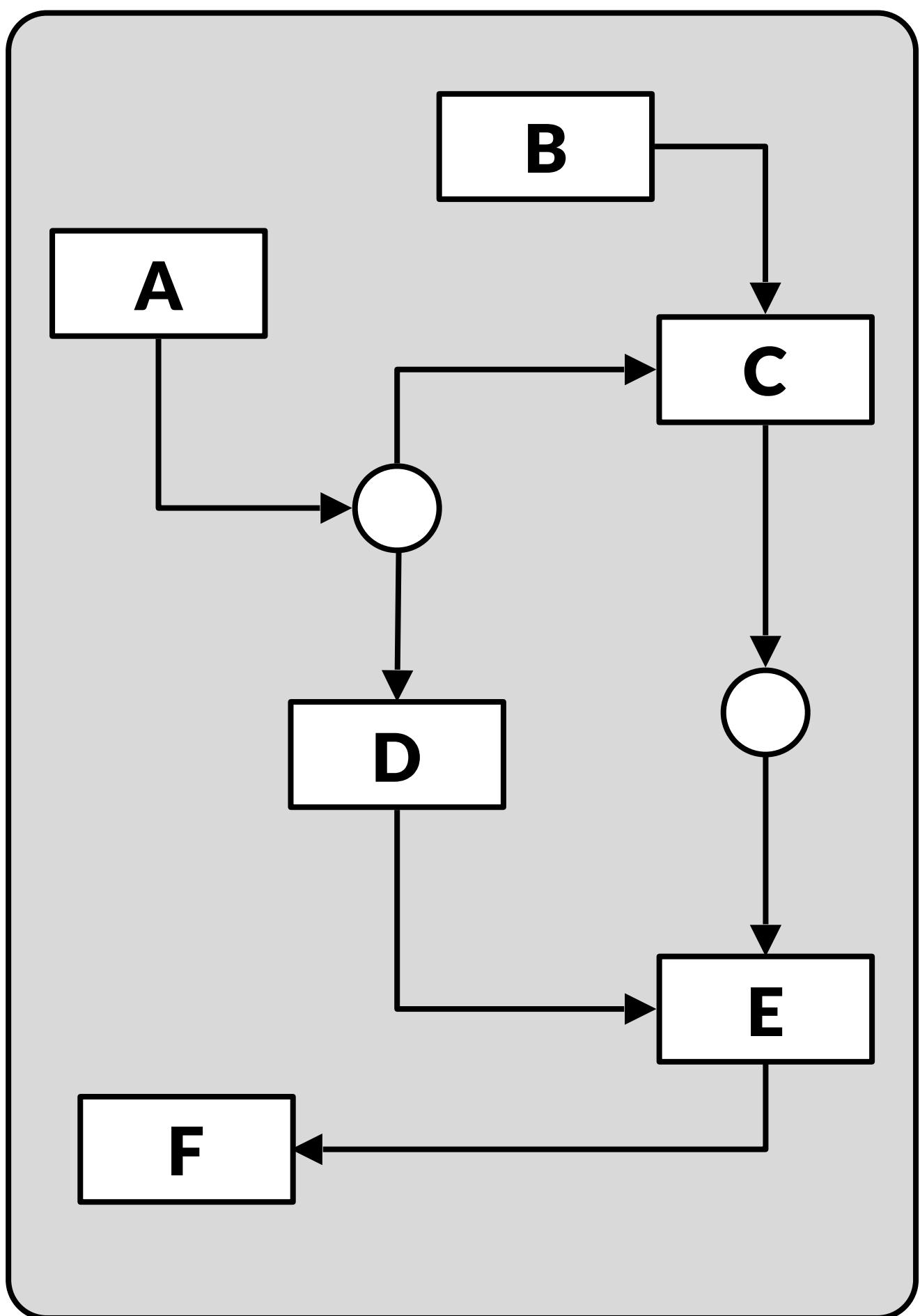


Node	Sample 1	Sample 2	Sample 3	...
A	0.55	0.95	0.83	...
B	0.12	0.42	0.16	...
C	0.33	0.65	0.38	...
...

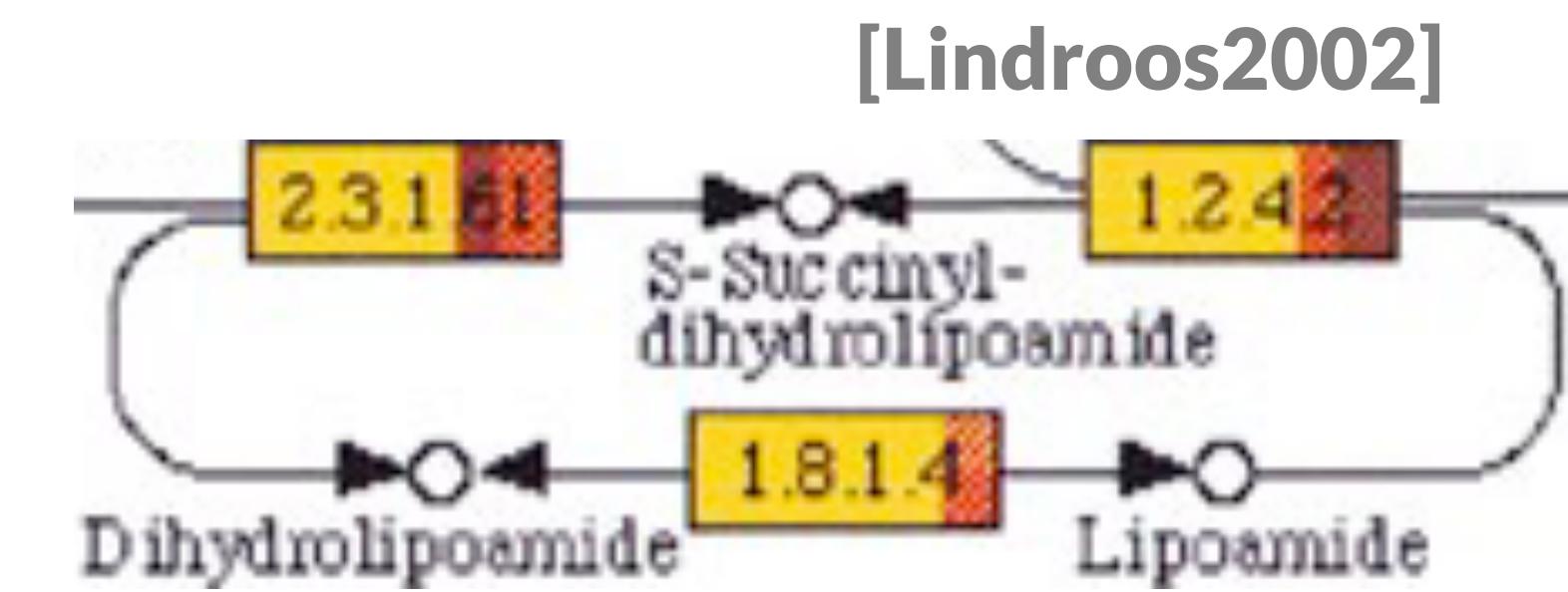
Node	Sample 1	Sample 2	Sample 3	...
A	low	low	very high	...
B	normal	low	high	...
C	high	very low	normal	...
...

How to visualize attribute data on networks?

Good Old Color Coding



A	-3.4	4.2	5.1	4.2
B	2.8	1.8	1.3	1.1
C	3.1	-2.2	2.4	2.2
D	-3	-2.8	1.6	1.0
E	0.5	0.3	-1.1	1.3
F	0.3	0.3	1.8	-0.3

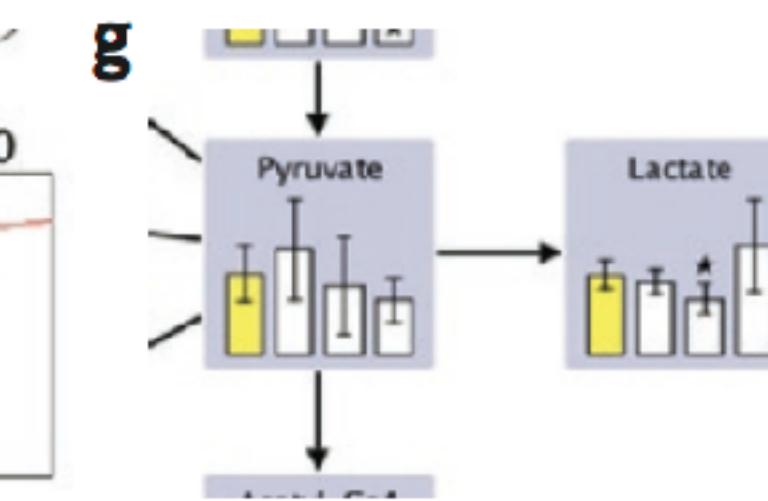
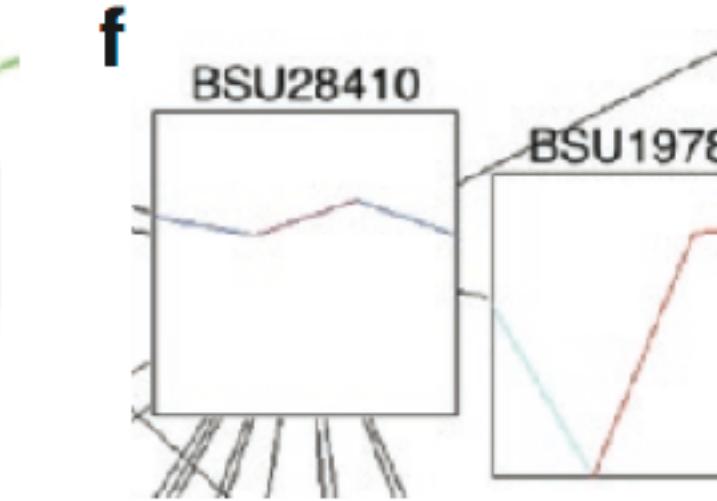
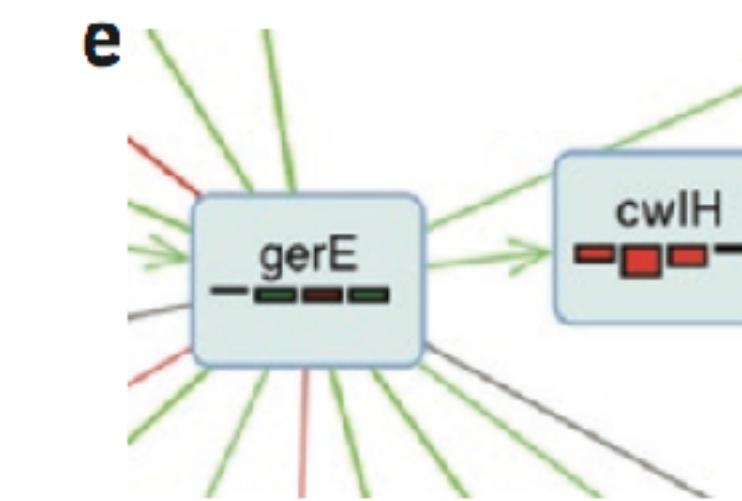
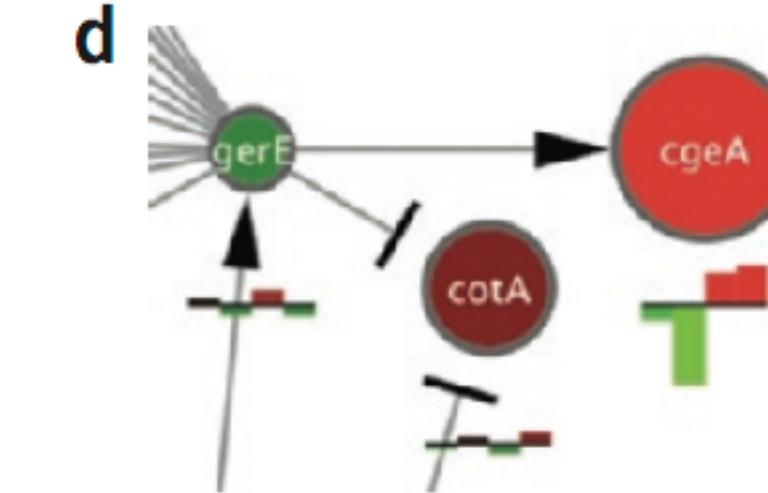
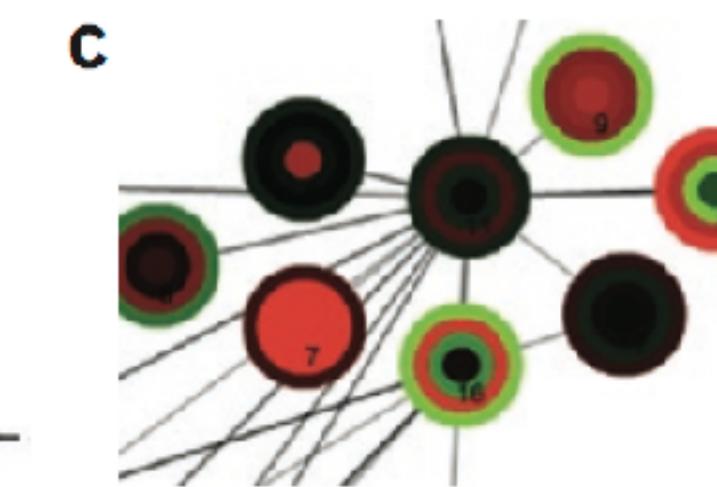
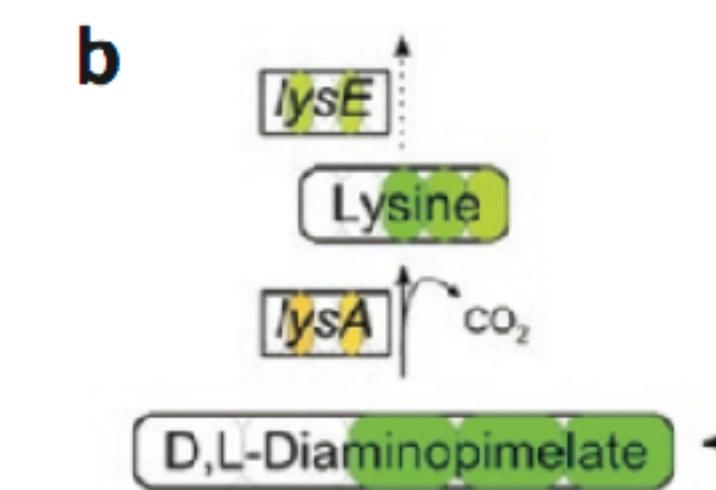
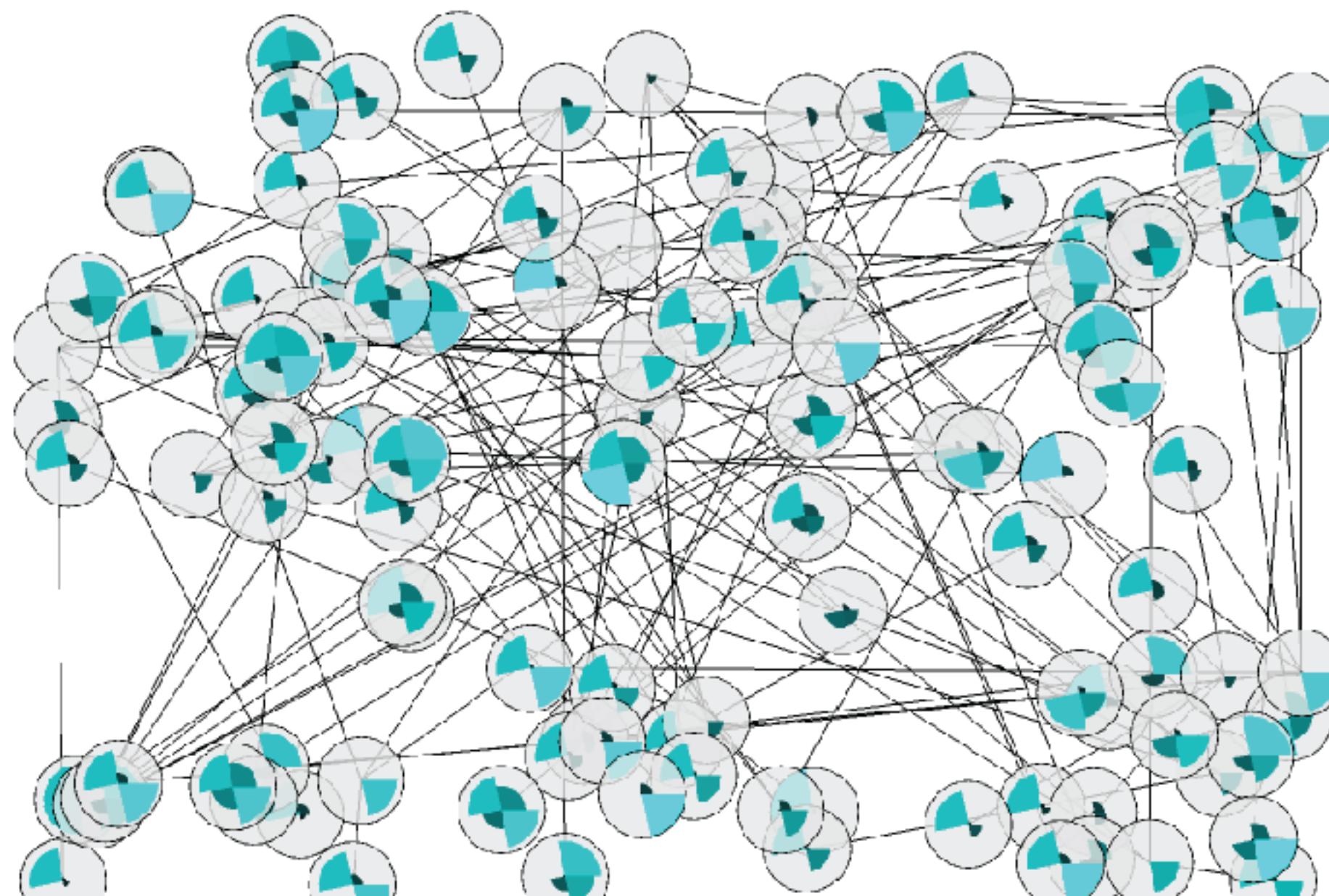


Node Attributes

Coloring

Glyphs

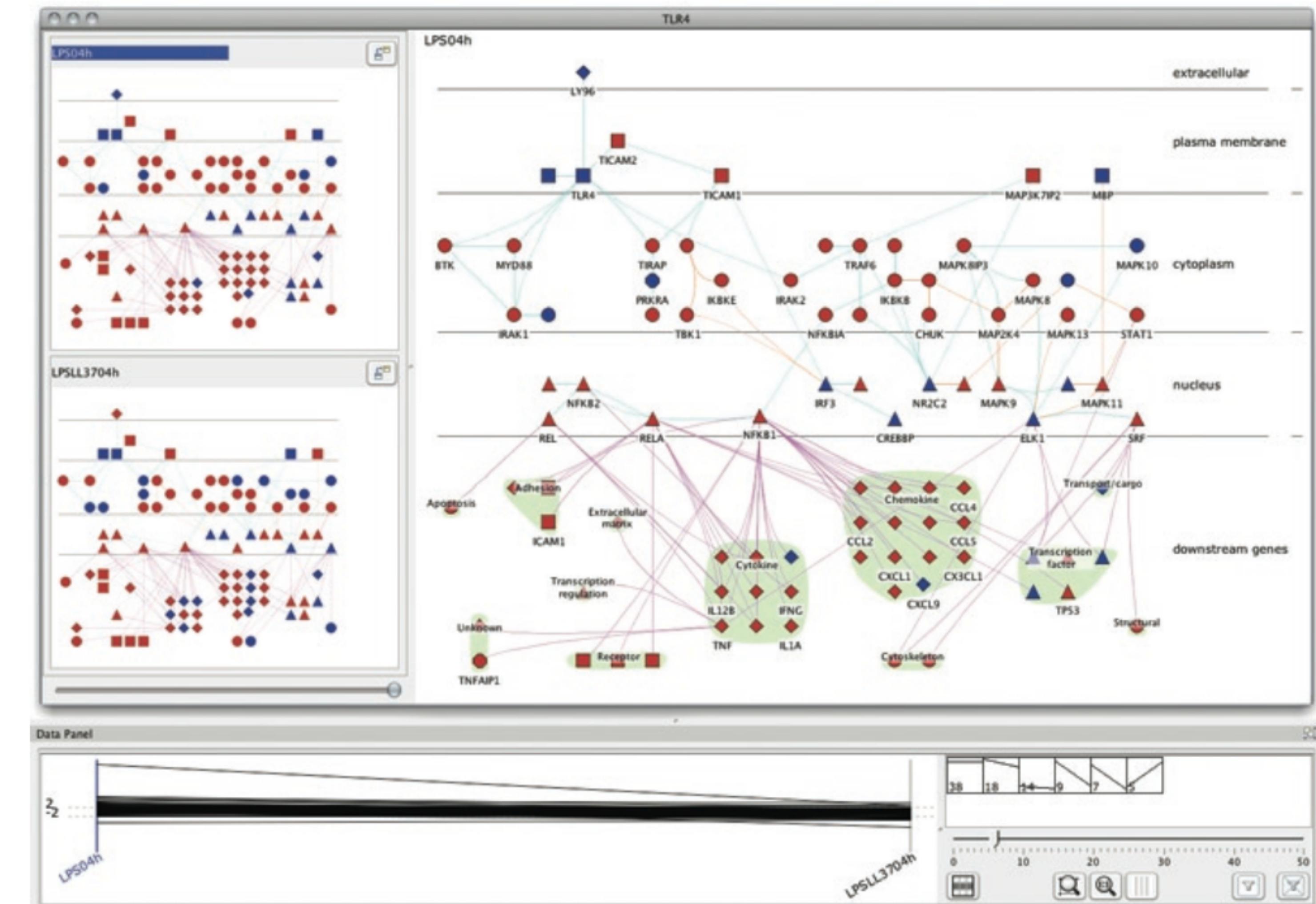
-> Limited in scalability



Small Multiples

Cerebral [Barsky, 2008]

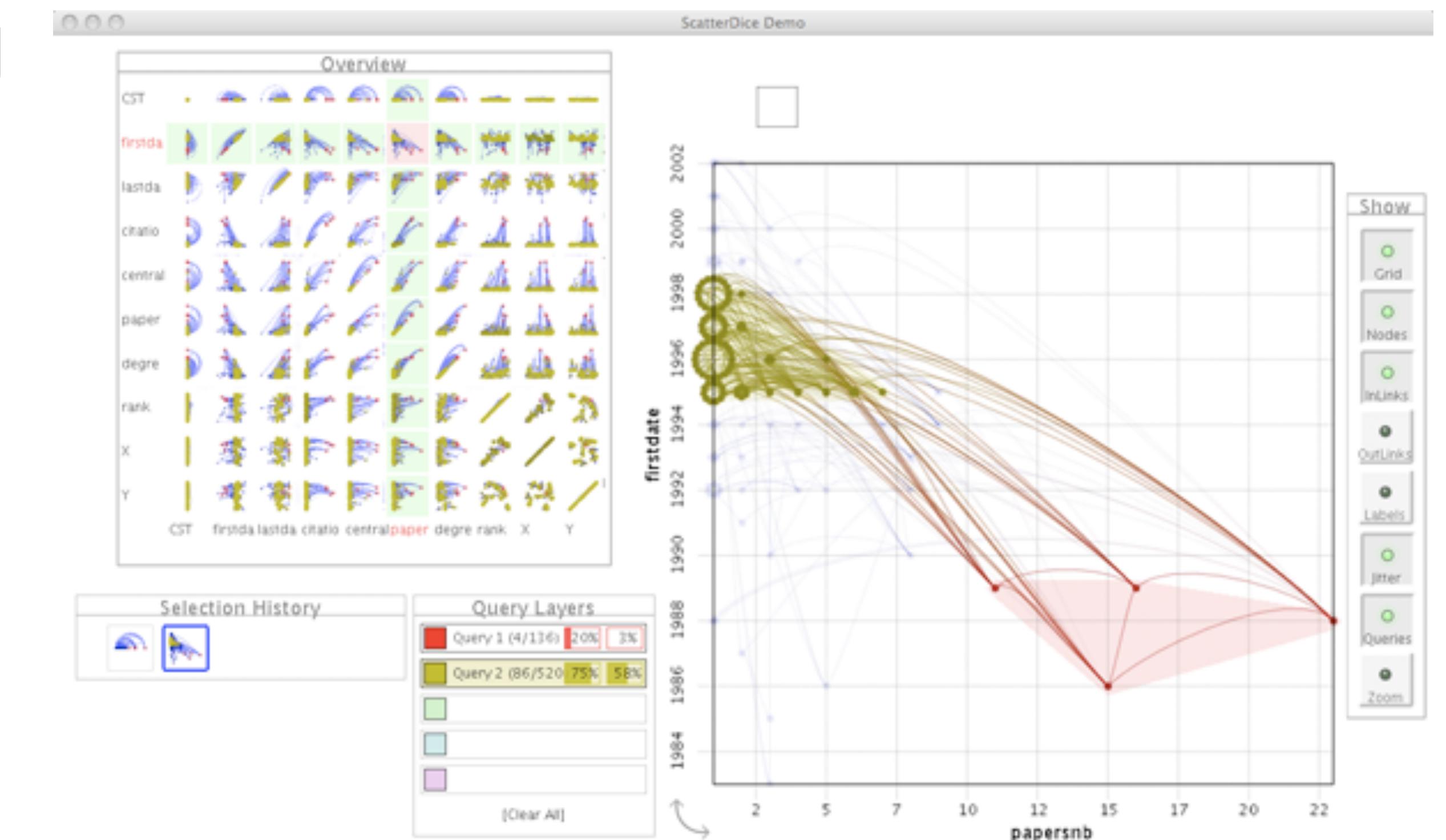
Each dimension in its own window



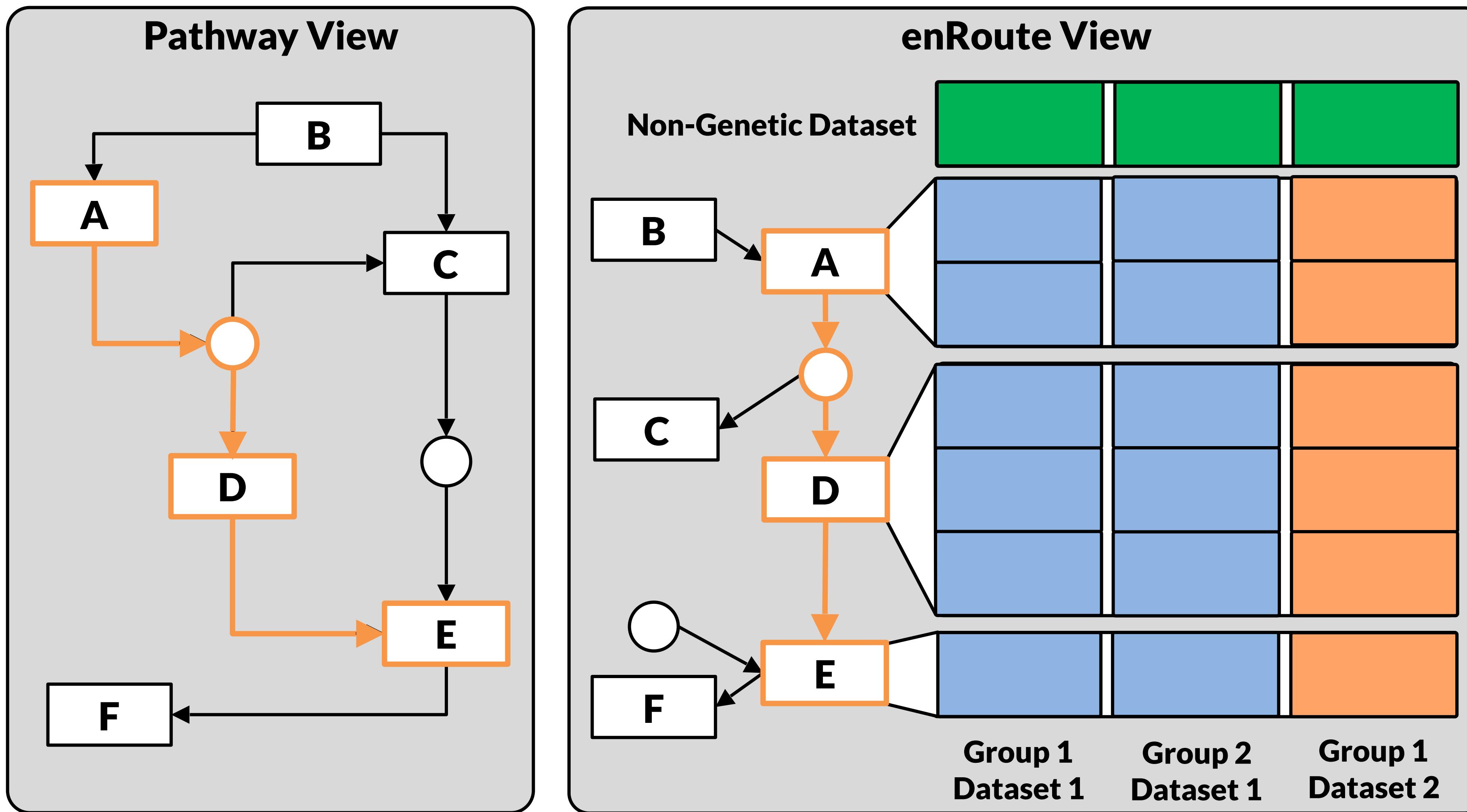
Data-driven node positioning

GraphDice

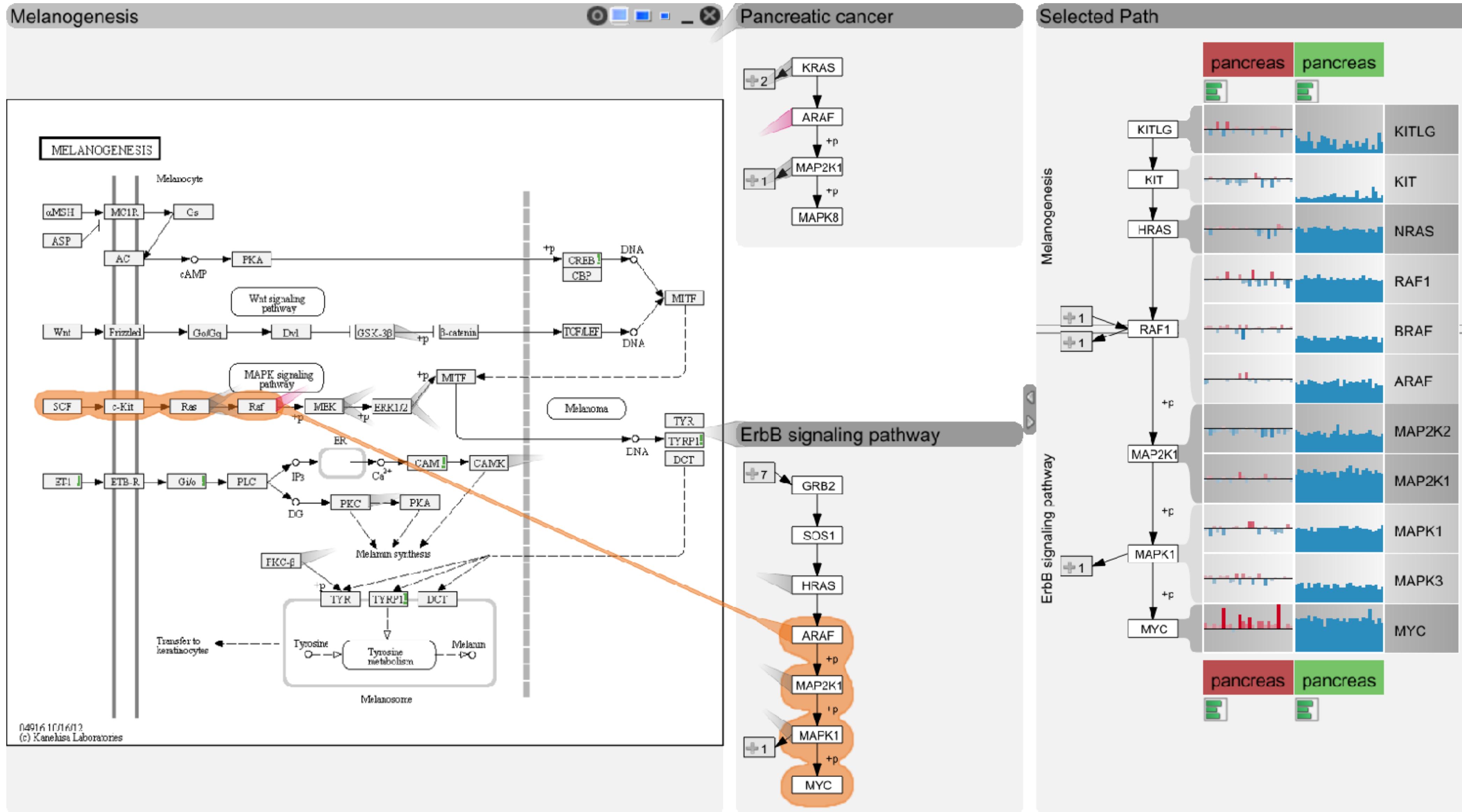
Nodes are laid out according to attribute values



Path Extraction: enRoute



enRoute



File Data Window View Help

Entourage

Pathways

Pathway

Filter:
<None>

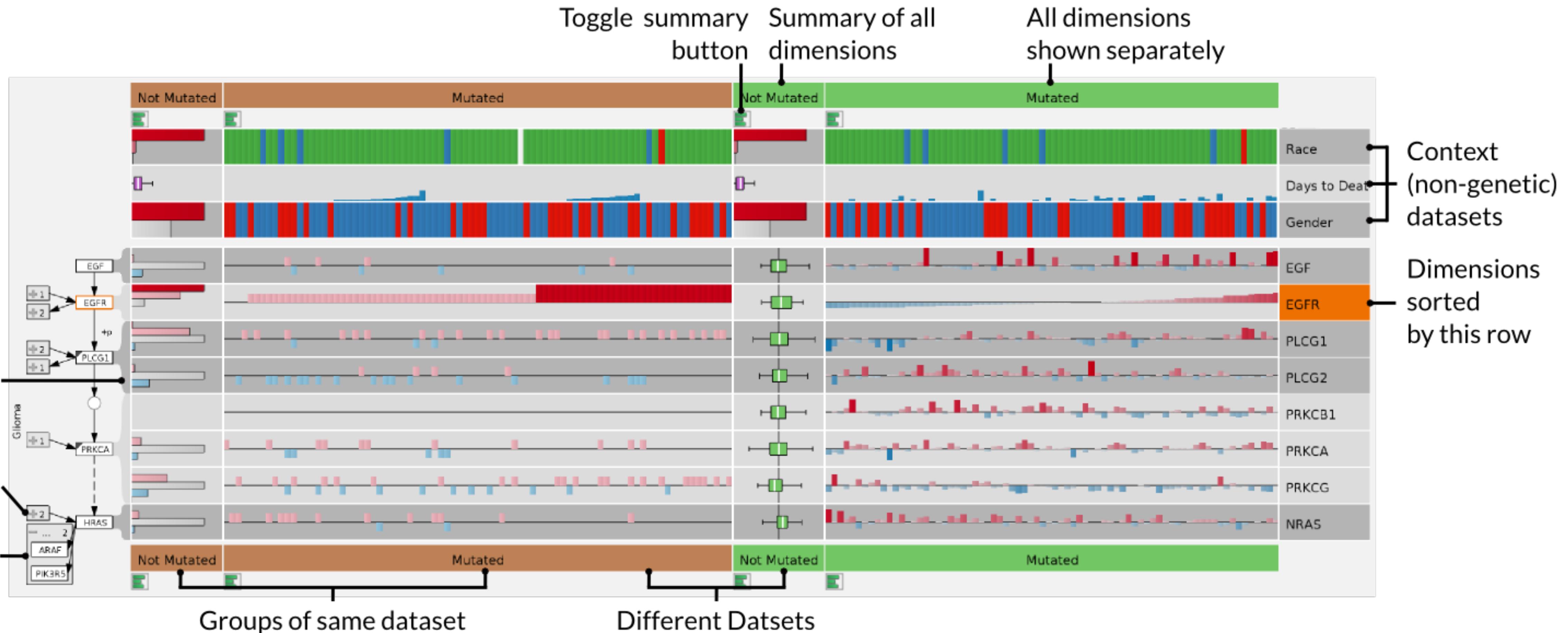
- 1 C donor
- 2-Oxocarboxylic acid
- ABC transporters
- ABC-family proteins
- ACE Inhibitor Pathwa
- Acetylcholine Synthes
- Acute myeloid leukem
- Adherens junction
- Adipocyte TarBase
- Adipocytokine signali
- Adipogenesis
- Advanced glycosylatio
- Aflatoxin B1 metaboli
- African trypanosomias
- AGE/RAGE pathway
- AhR pathway
- Alanine and aspartate
- Alanine, aspartate an
- Alcoholism
- Aldosterone-regulated
- Allograft rejection
- Allograft rejection
- Alpha 6 Beta 4 signal
- alpha-Linolenic acid
- Alzheimer's disease
- Alzheimers Disease
- amino acid conjugatio
- amino acid conjugatio
- Amino sugar and nucl
- Aminoacyl-tRNA bios
- Amoebiasis
- Amphetamine addicti
- AMPK signaling
- Amyotrophic lateral sc
- Androgen receptor si
- Angiogenesis
- Angiogenesis
- angiogenesis overvie
- Antigen processing an
- APC/C-mediated degra
- Apoptosis
- Apoptosis
- Apoptosis Meta Path
- Apoptosis Modulation
- Apoptosis Modulation
- Apoptosis, anoikis an

Selected Path

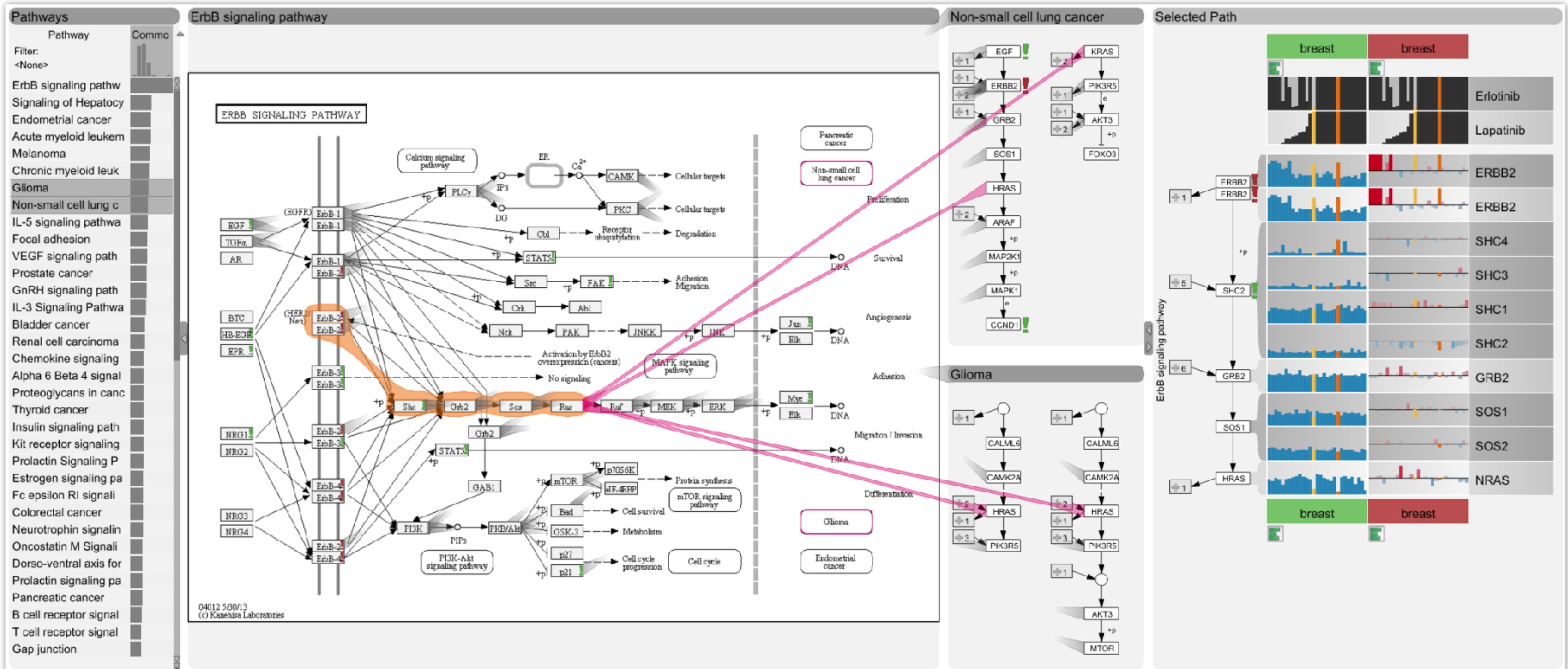
Multi-mapping
of gene family

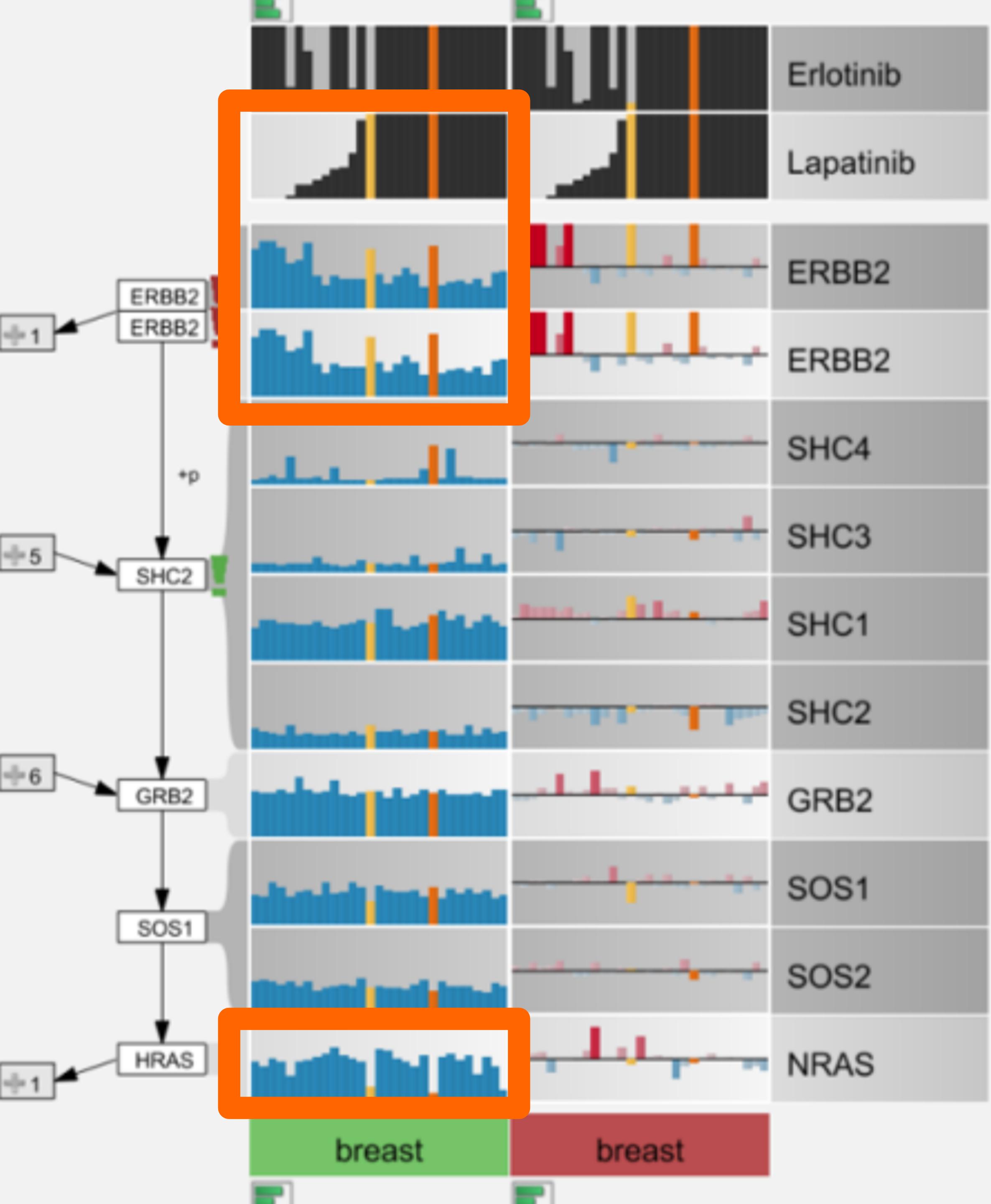
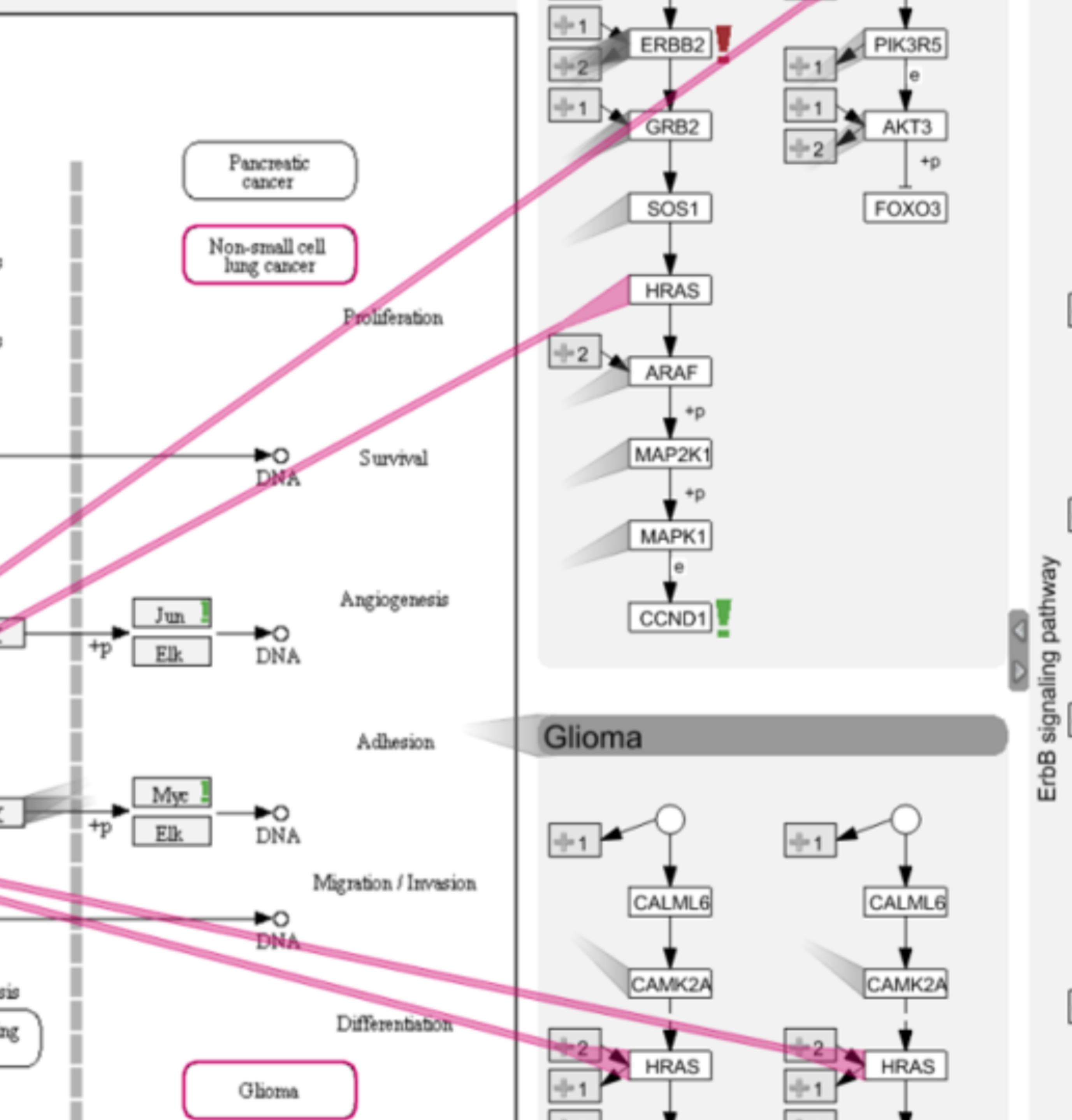
 Collapsed
incoming node

 Expanded
outgoing
nodes



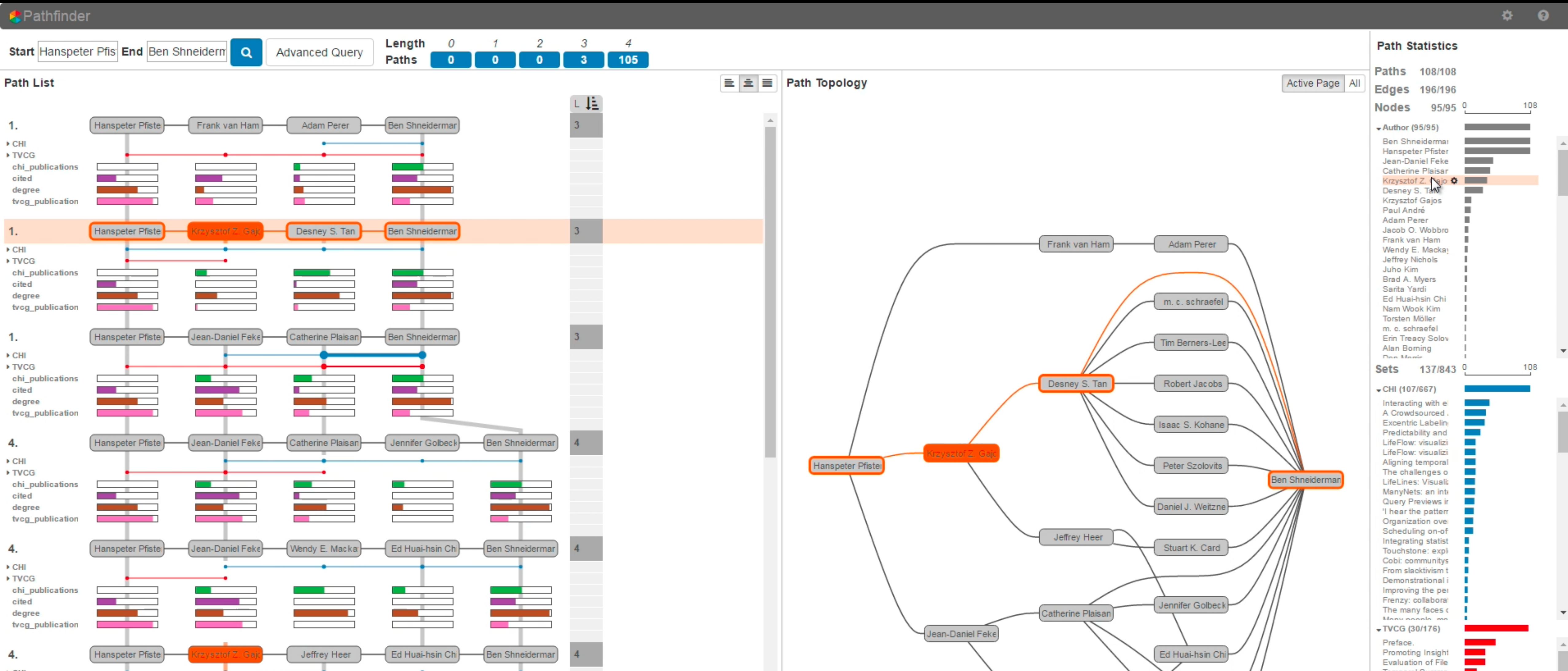
Case Study: CCLE Data

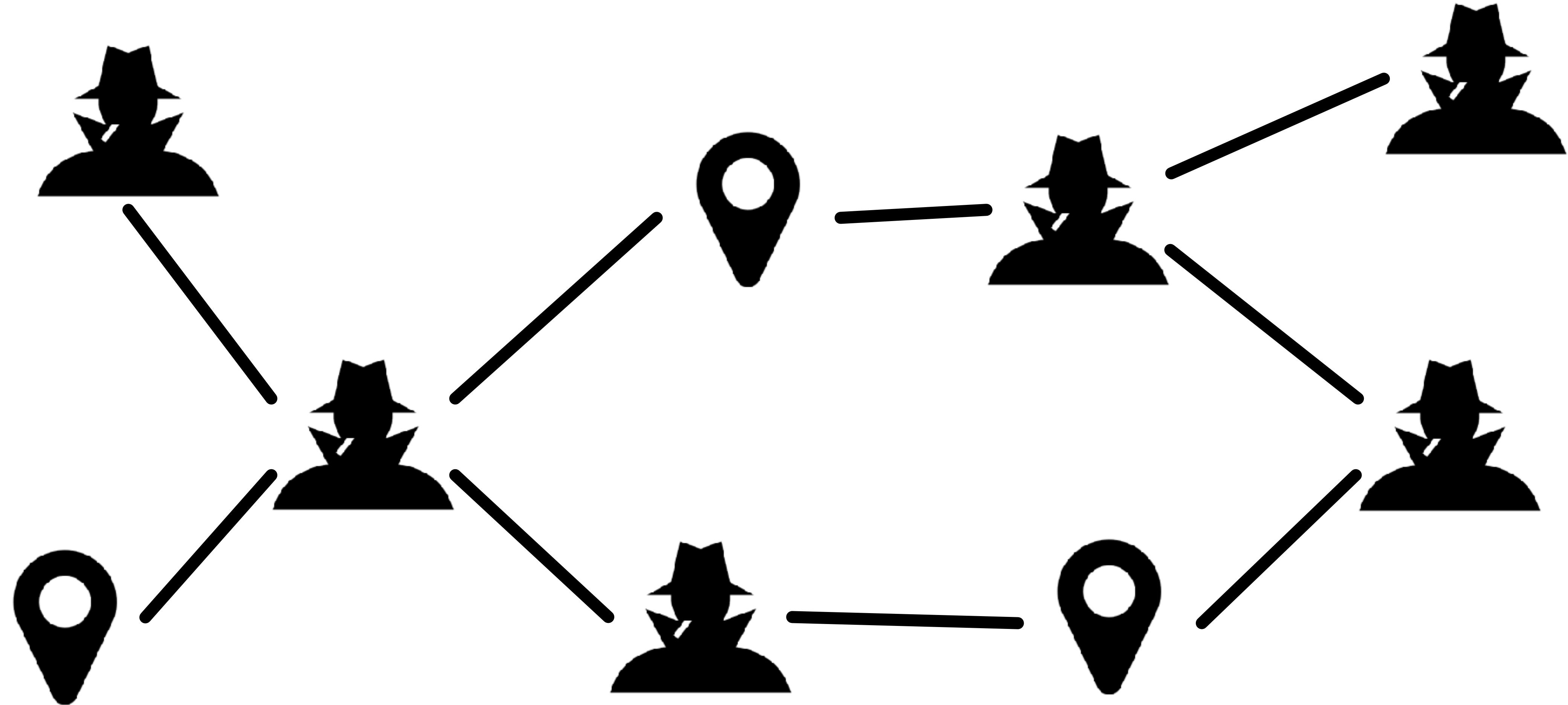




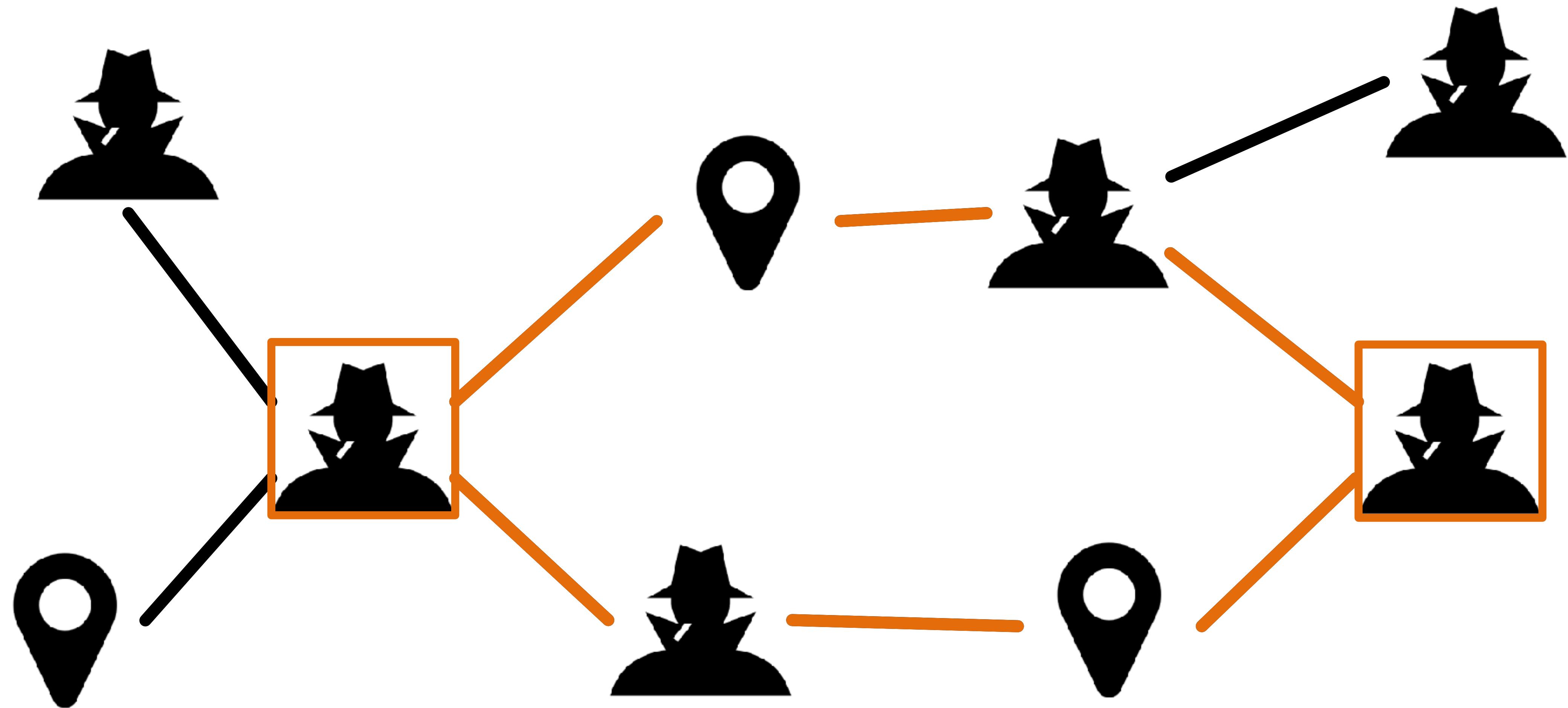
Pathfinder:

Visual Analysis of Paths in Graphs

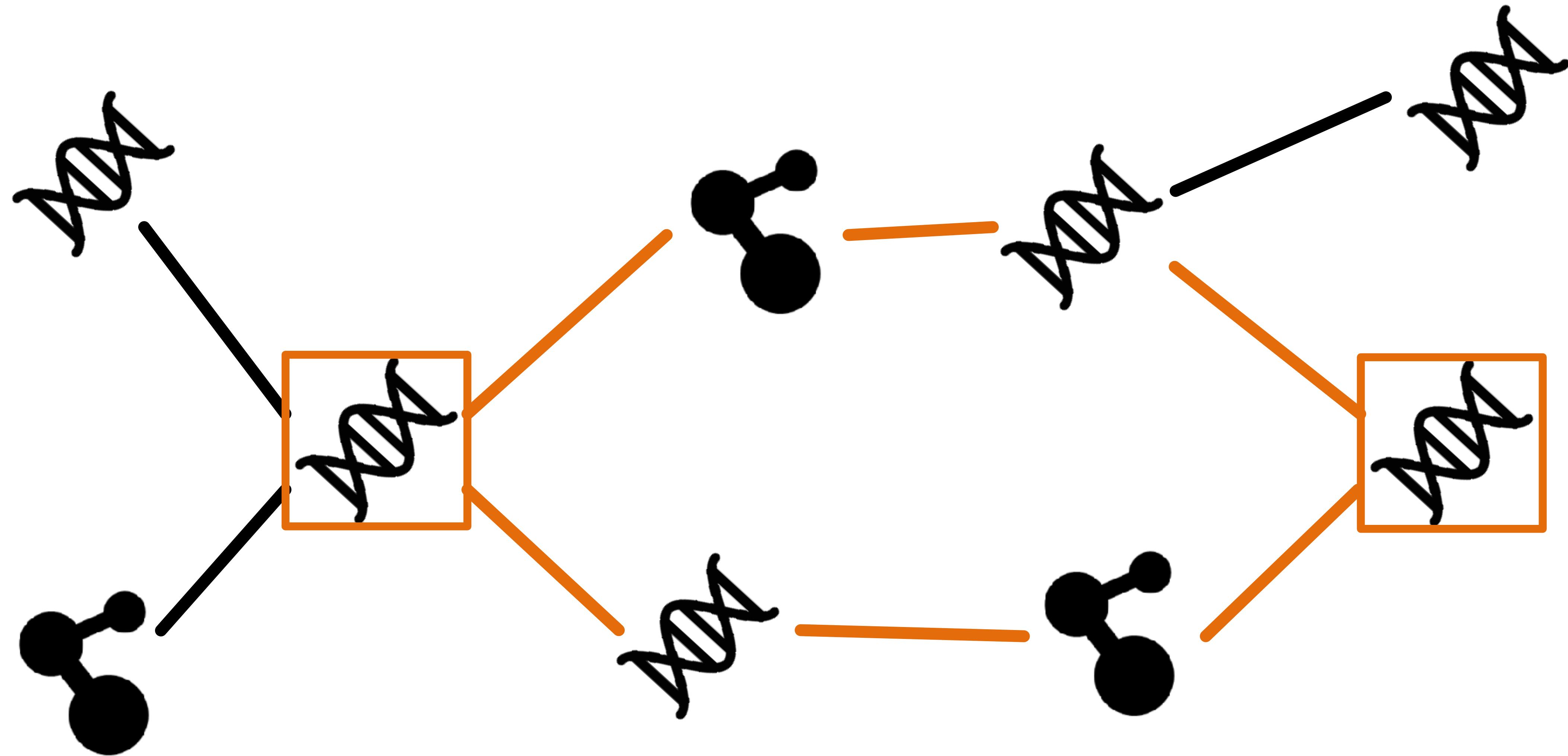




Intelligence Data: How are two suspects connected?



Intelligence Data: How are two suspects connected?



Biological Network: How do two genes interact?

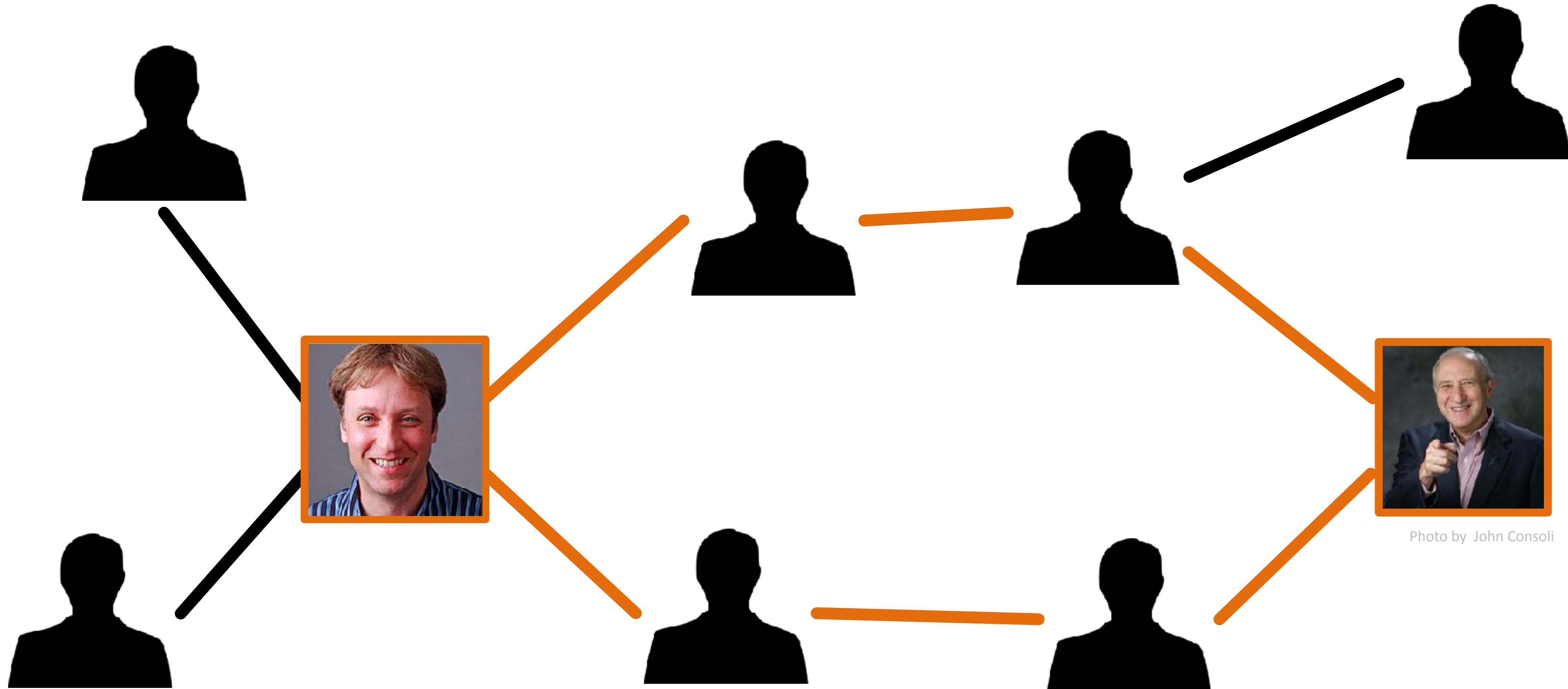
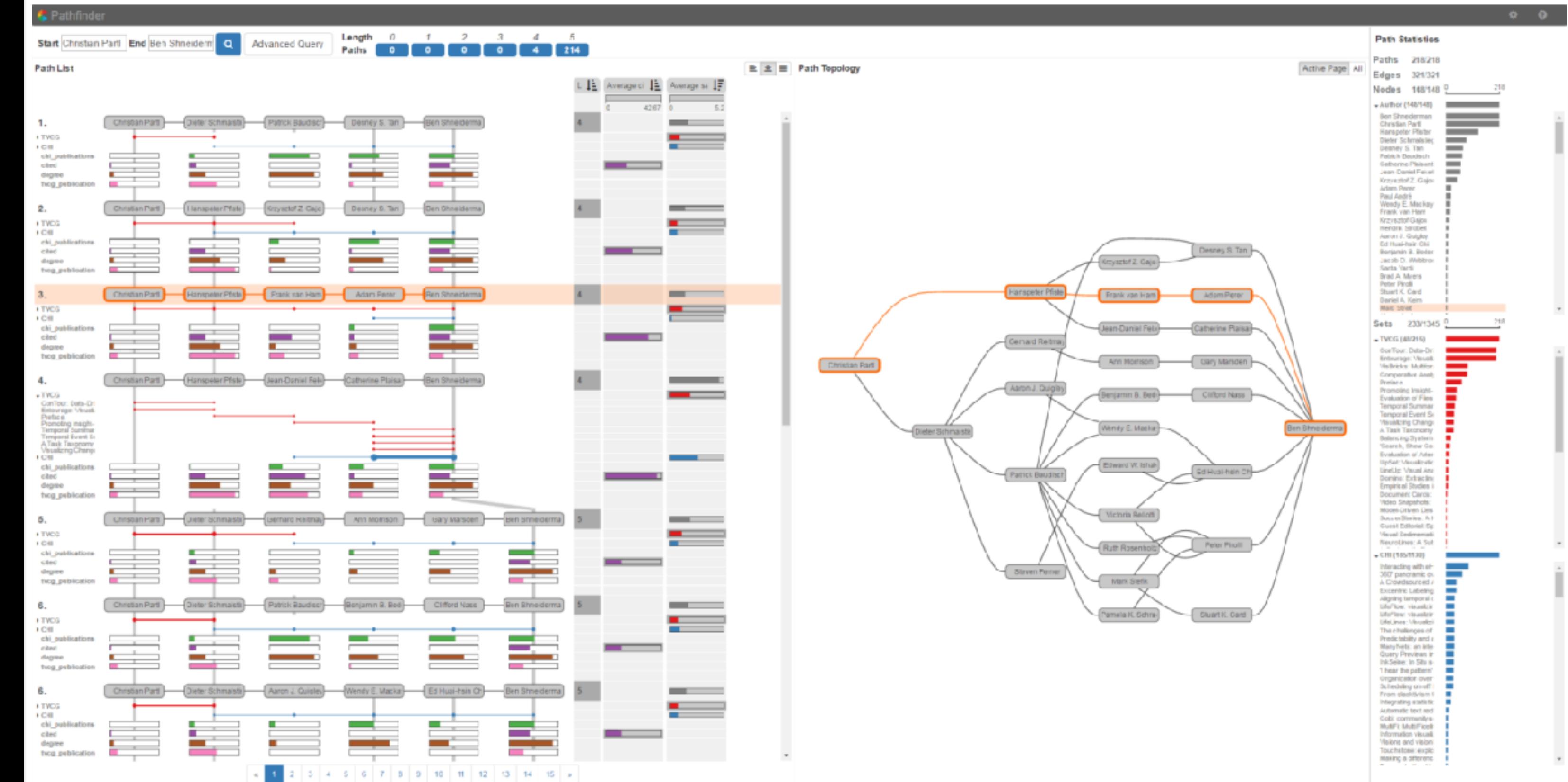


Photo by John Consoli

Coauthor Network: How is HP Pfister connected to Ben Shneiderman?

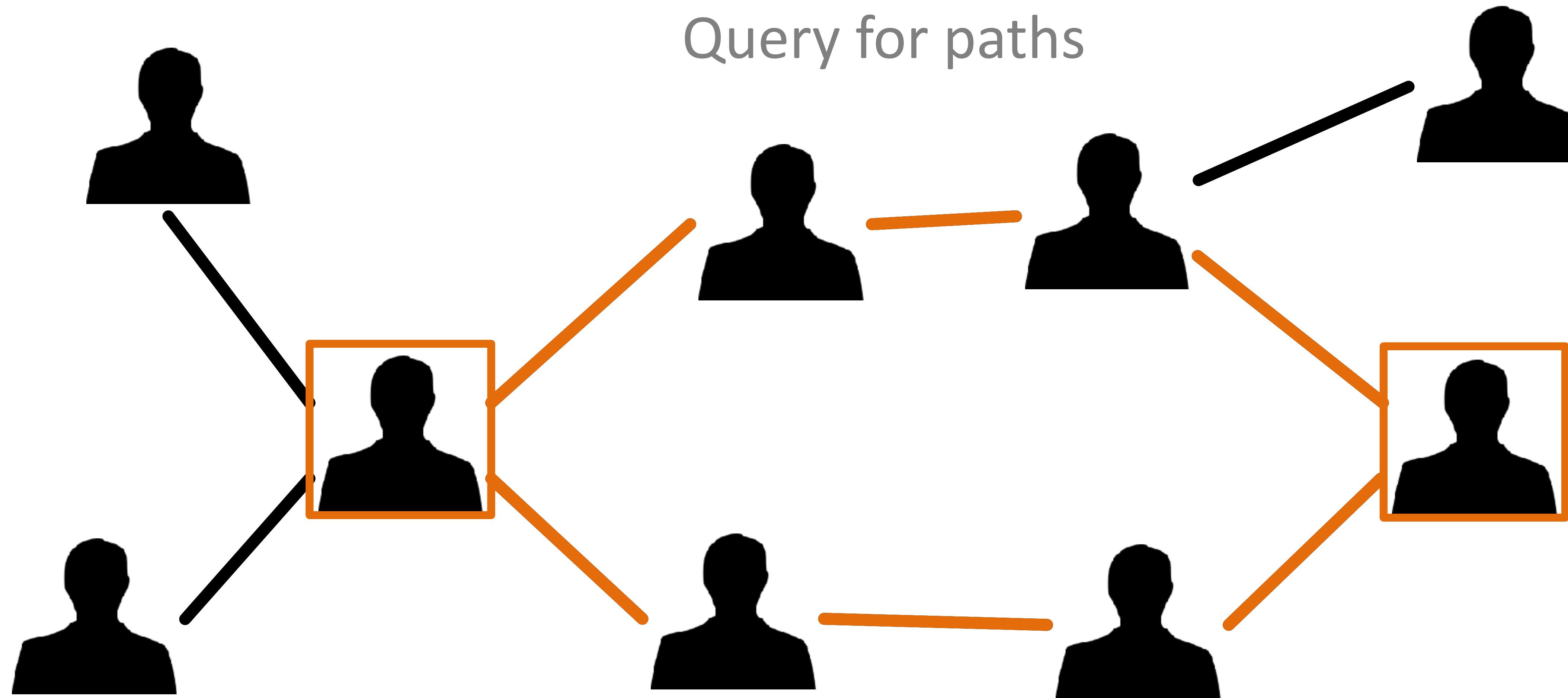
Pathfinder



Visual Analysis of Paths in Large Multivariate Graphs

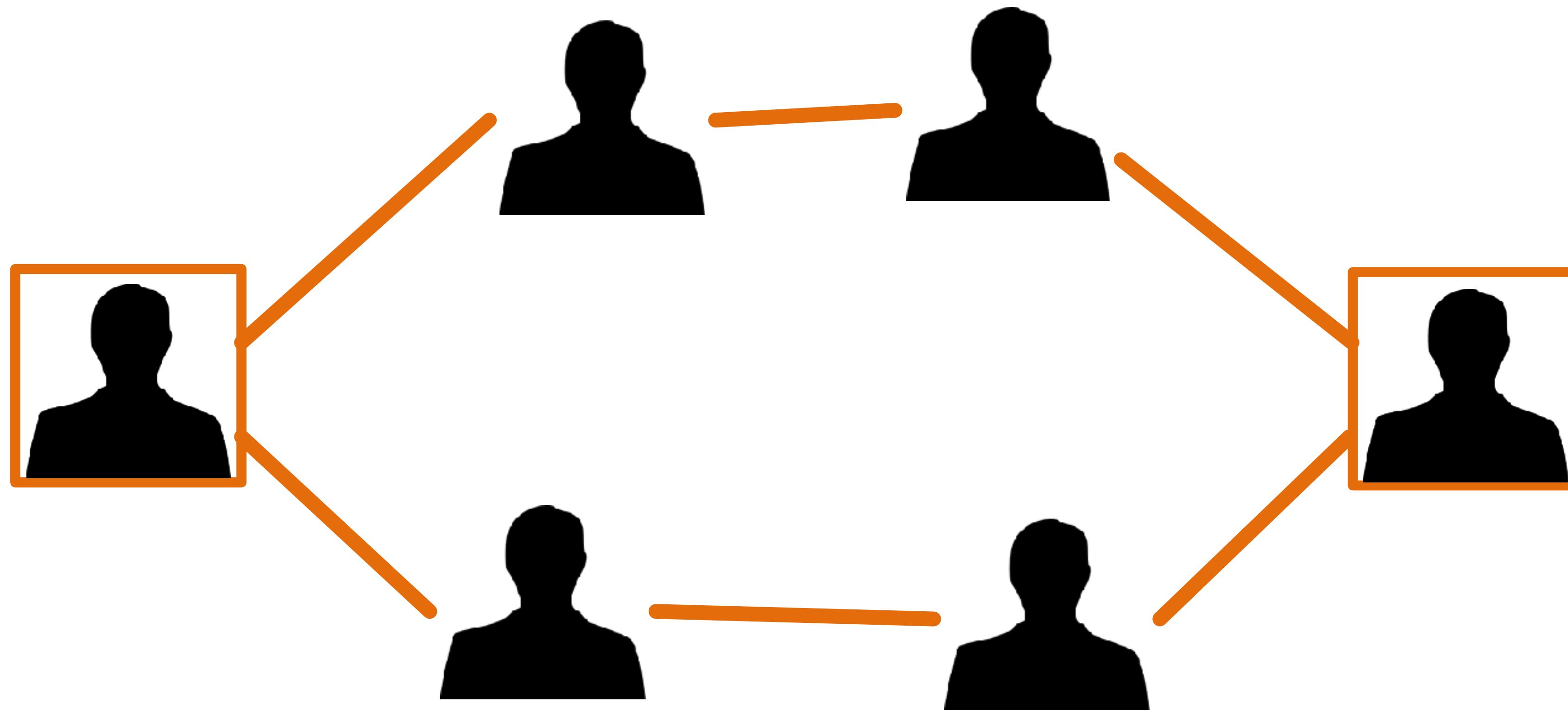
Pathfinder Approach

Query for paths



Pathfinder Approach

Show me a real life diagram..

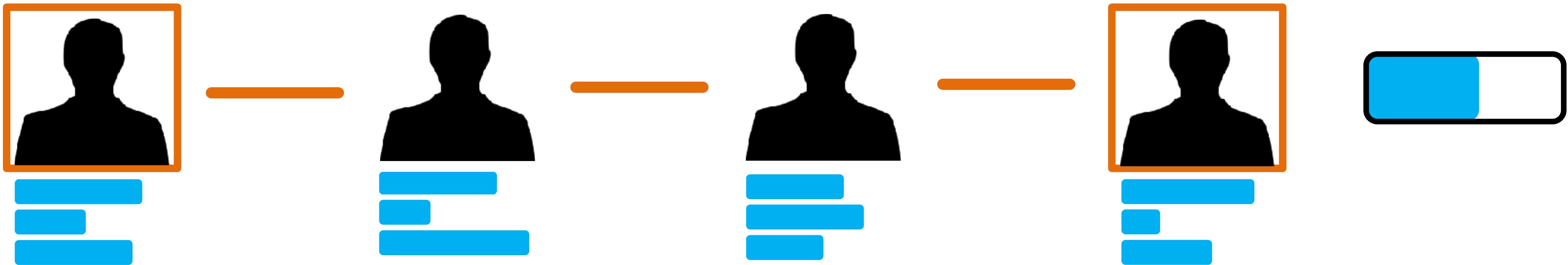


Pathfinder Approach

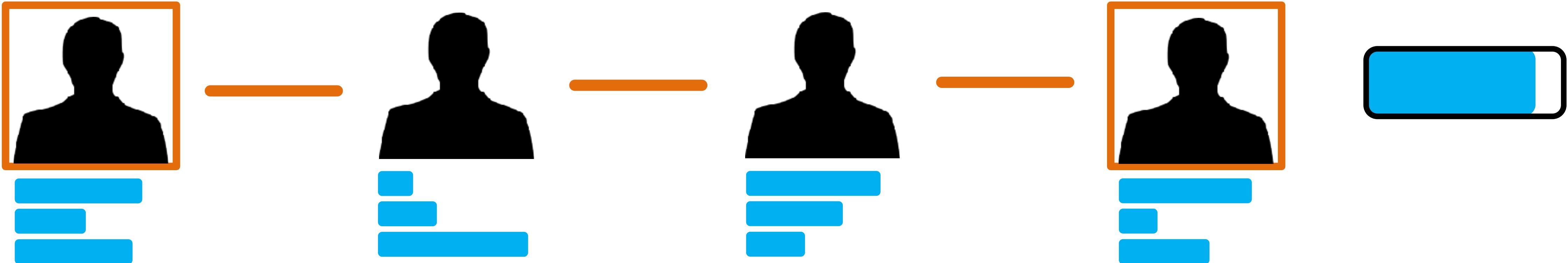
Update ranking to alternative important paths

Path Score

1.



2.

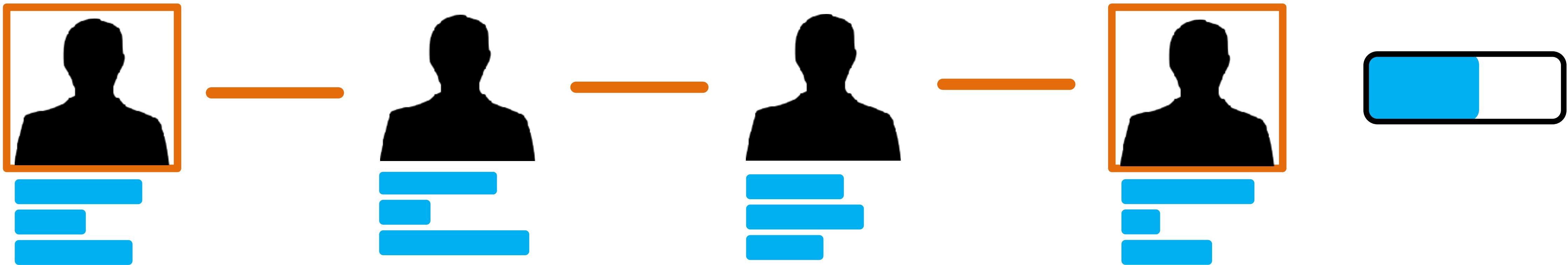


Pathfinder Approach

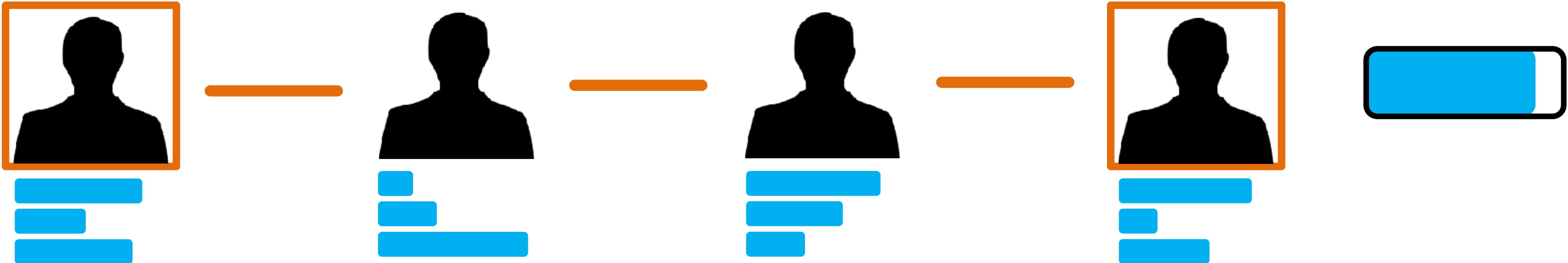
Update ranking to identify important paths

Path Score

1.



2.



Start End Advanced Query Length Paths

Path List

Query Interface

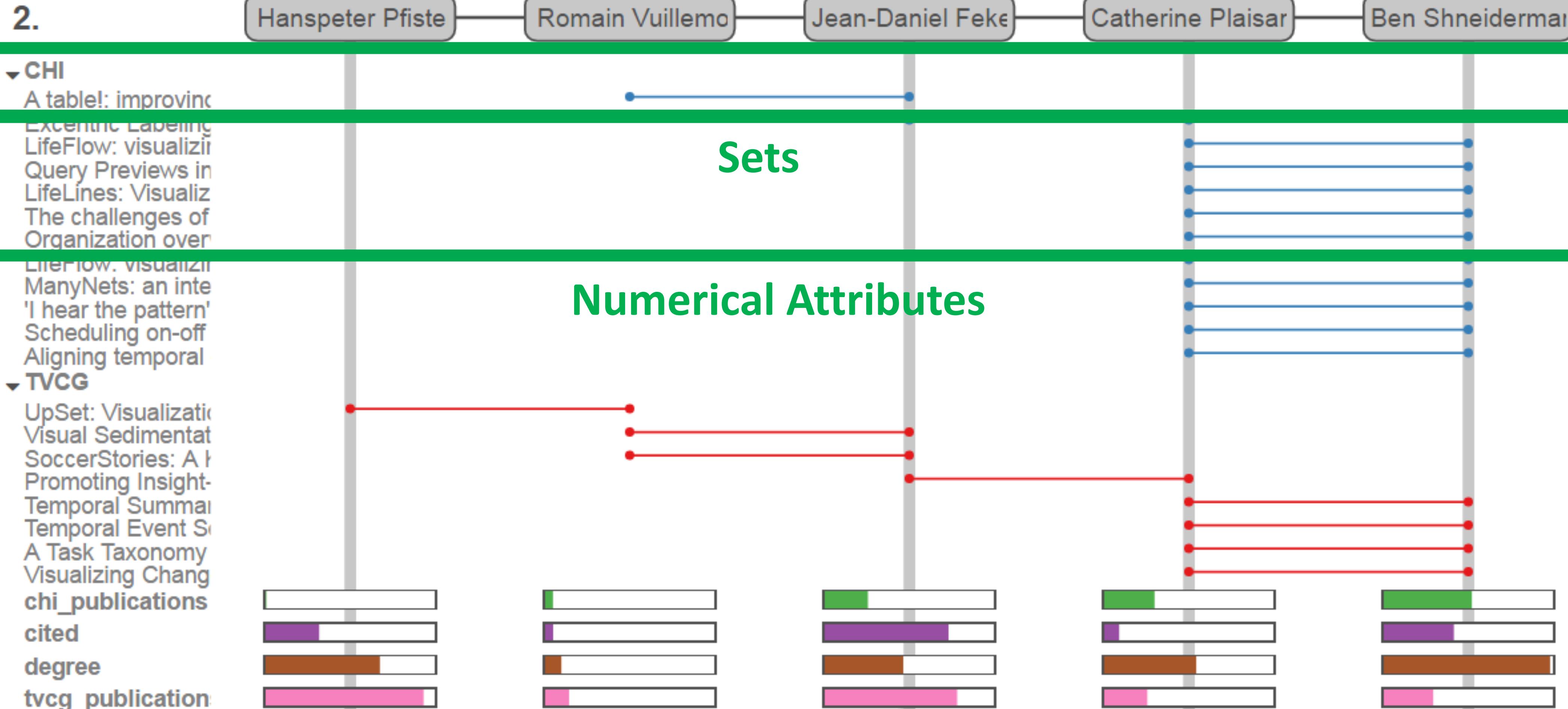


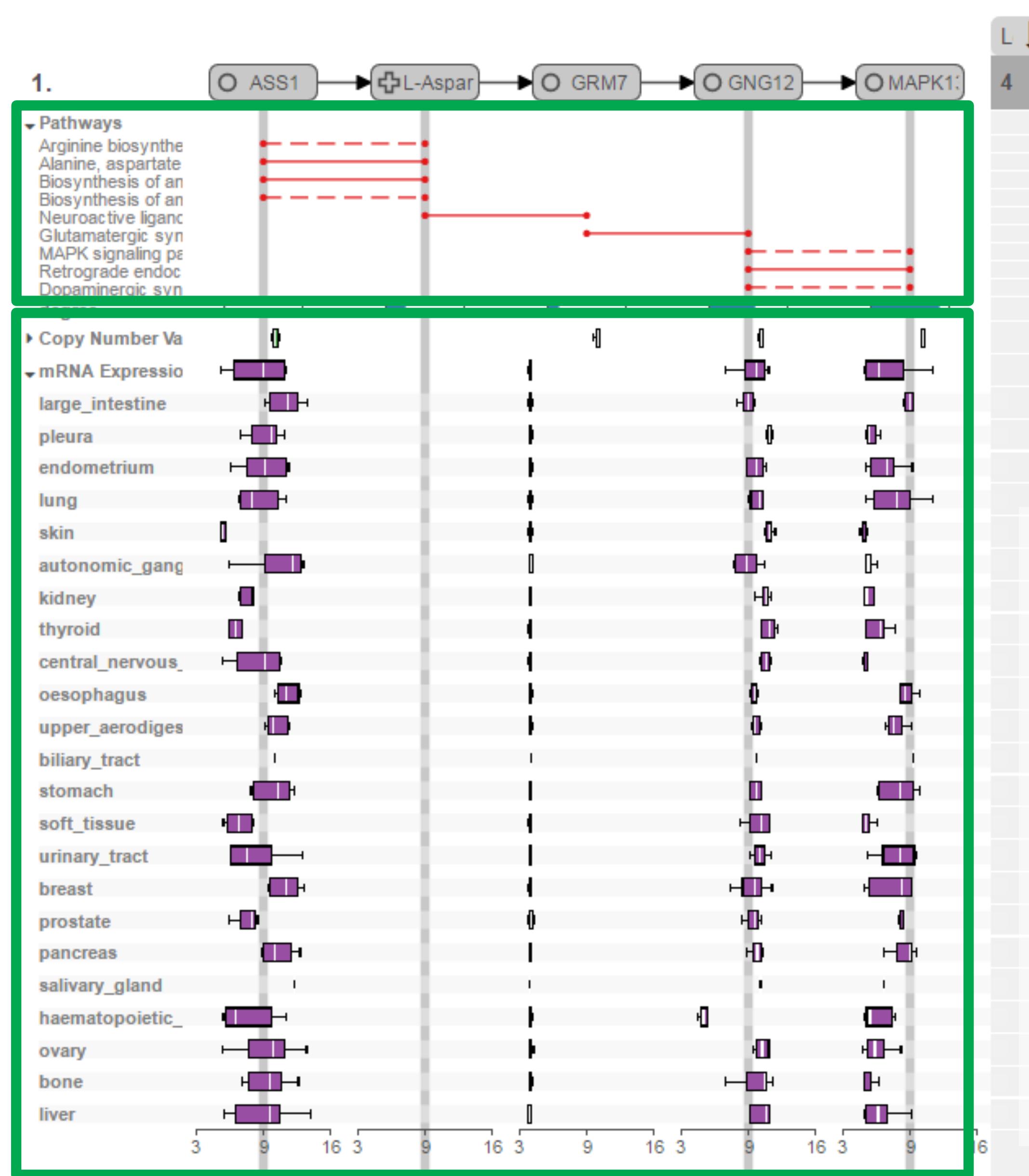
Path Topology

Active Page All

Path Statistics

Path Representation

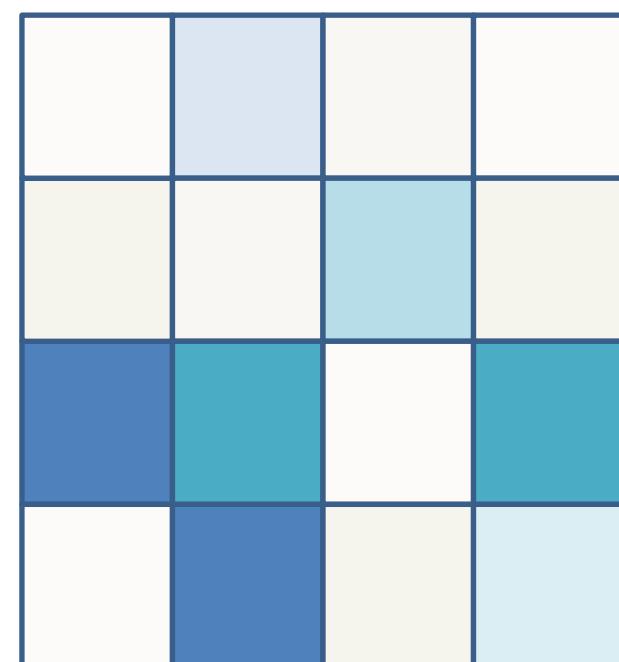




Pathways

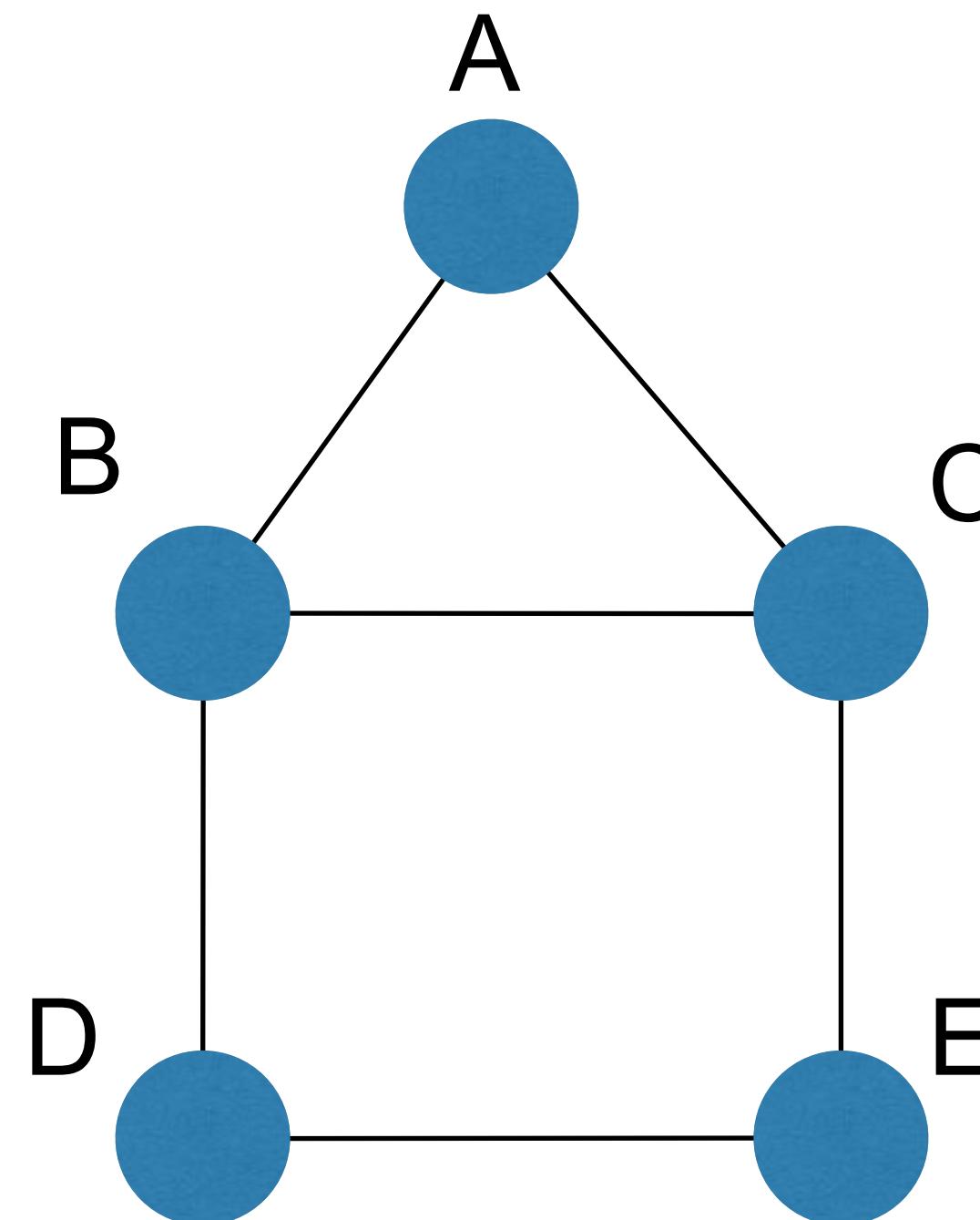
Grouped Copy Number and Gene Expression Data

Matrix Representations



Matrix Representations

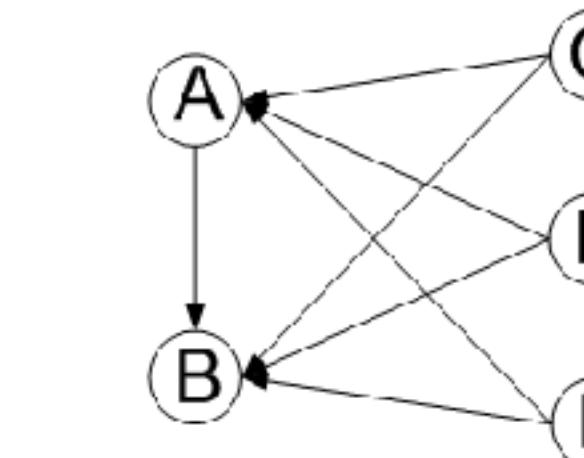
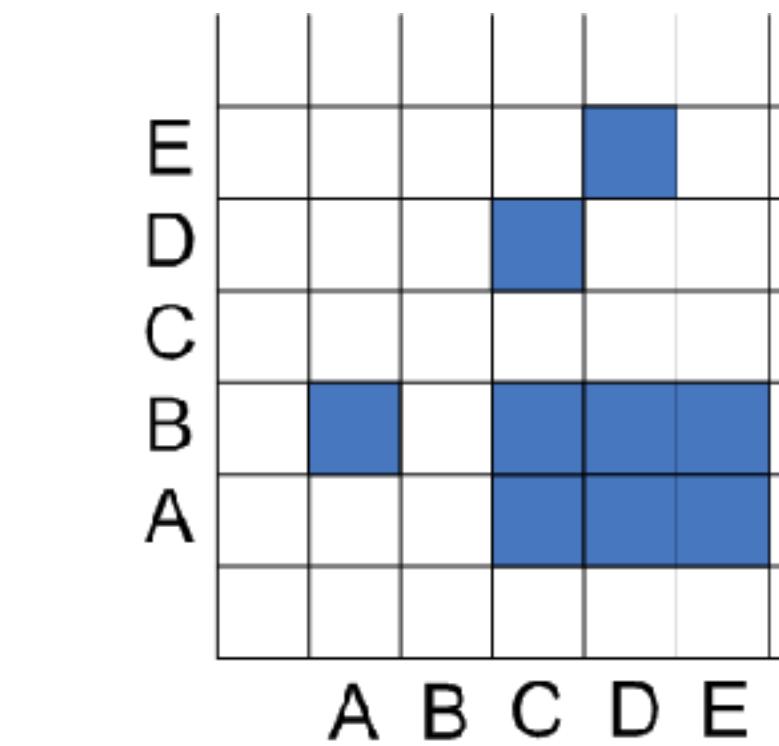
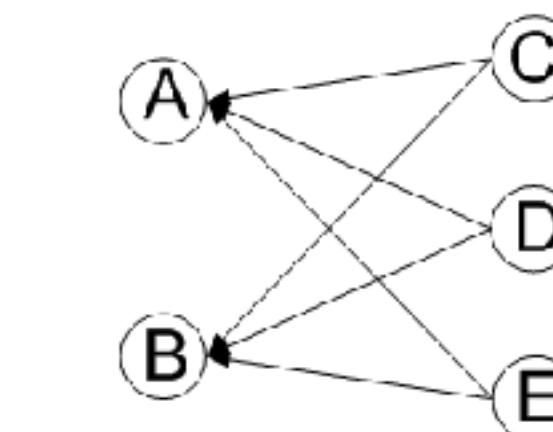
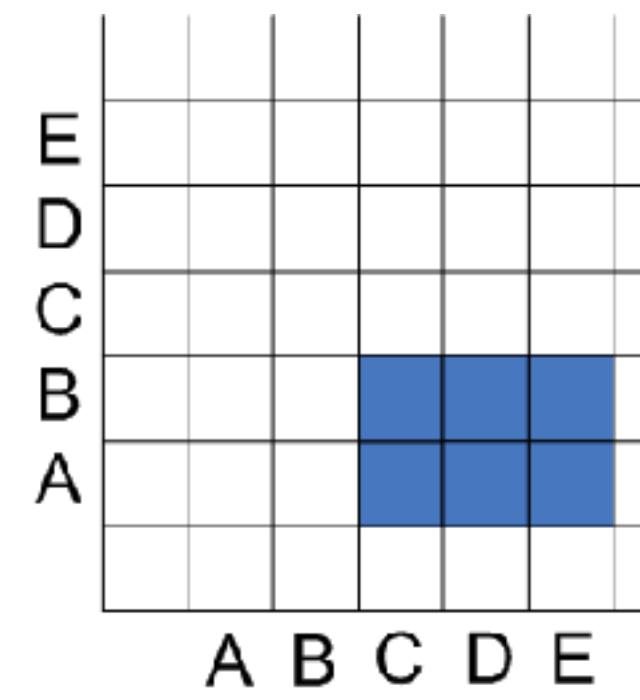
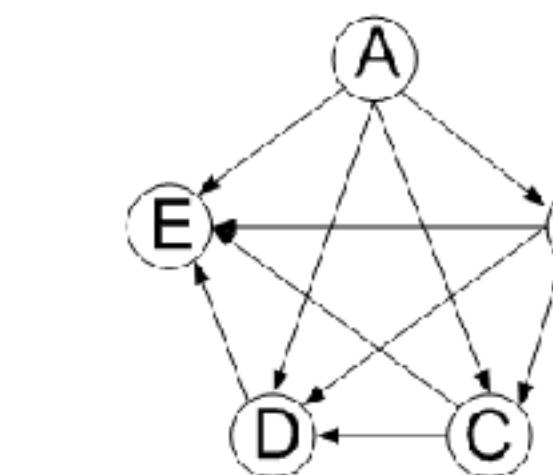
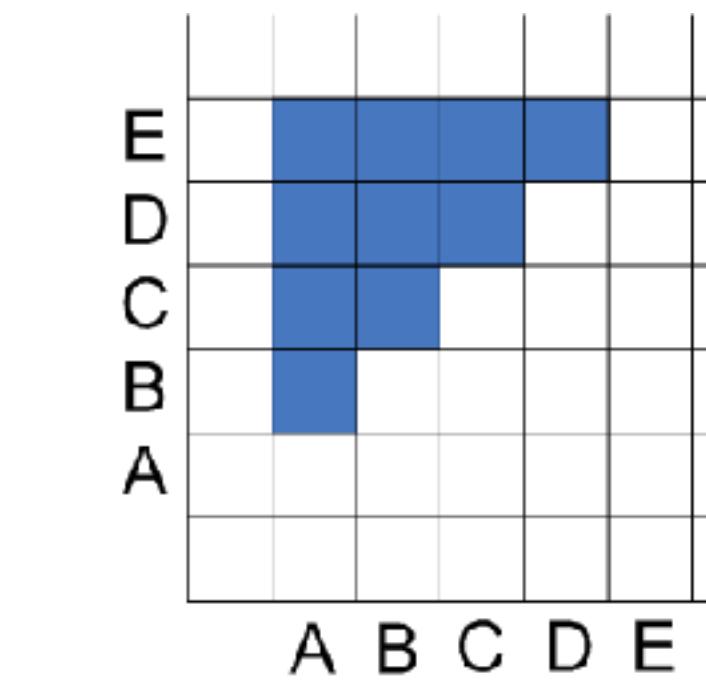
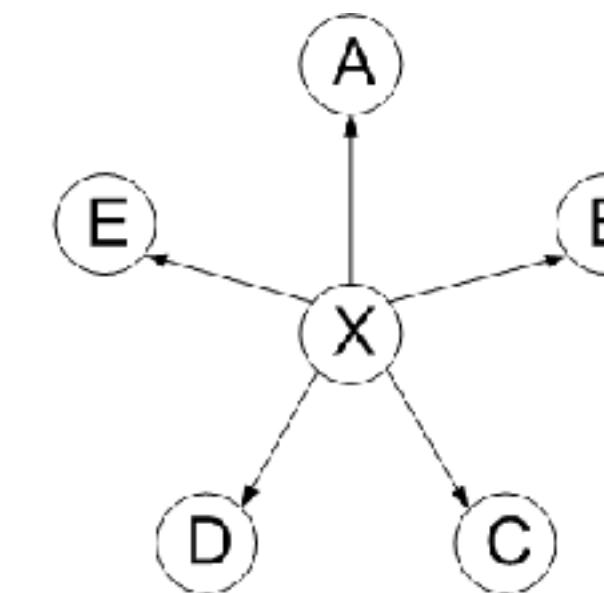
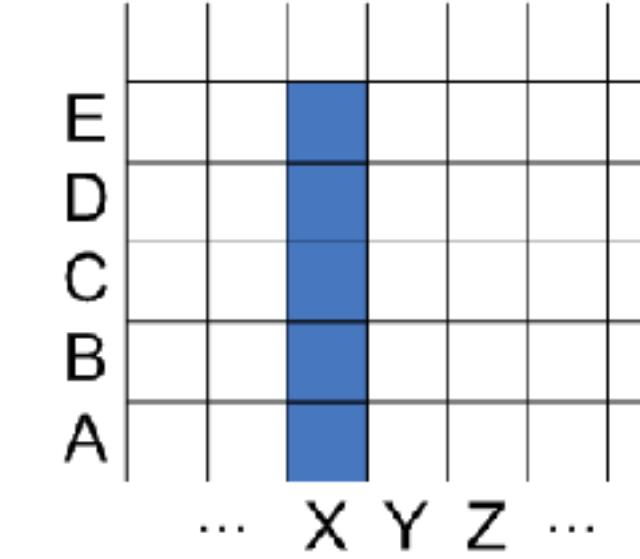
Instead of node link diagram, use adjacency matrix



A	B	C	D	E
A				
B				
C				
D				
E				

Matrix Representations

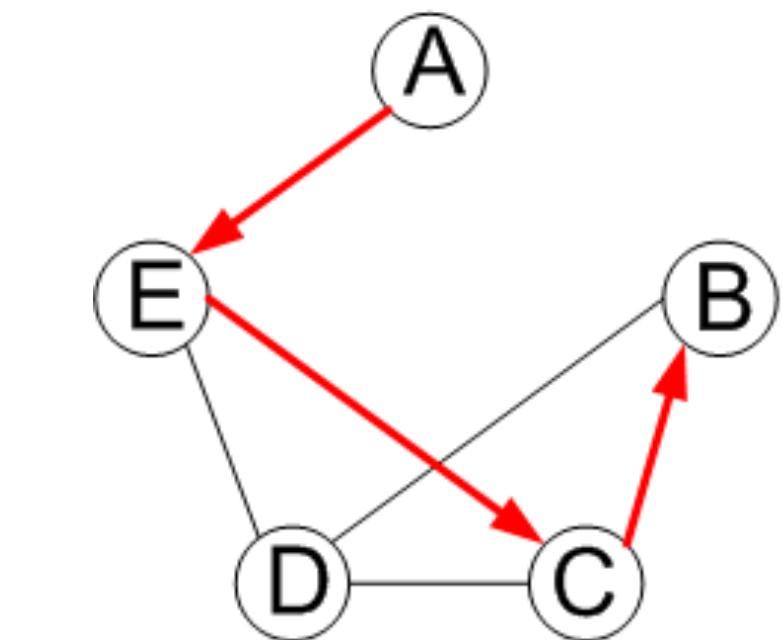
Examples:



Matrix Representations

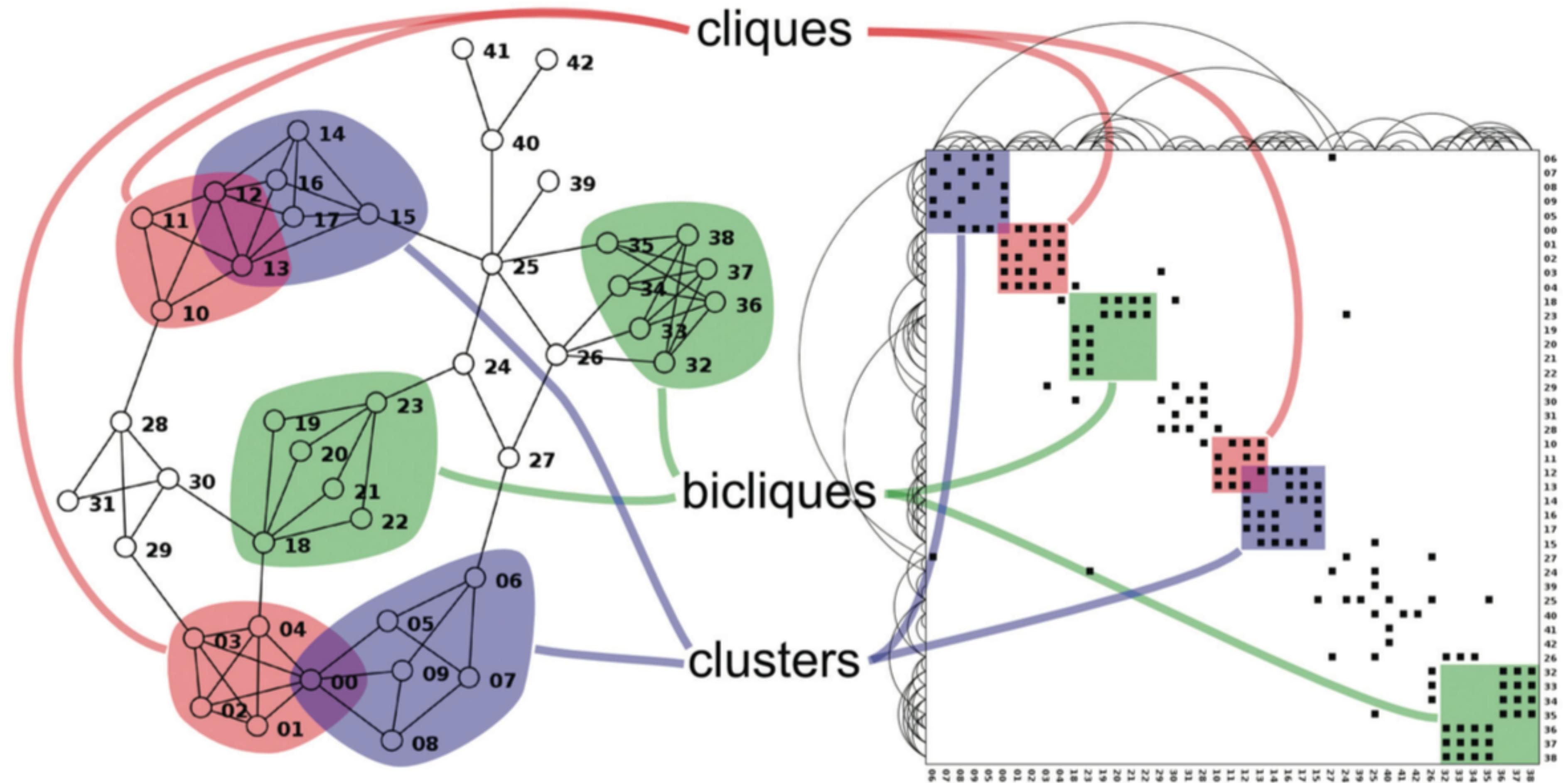
	A	B	C	D	E	F	G	H
A								
B								
C								
D								
R								
O								
M								
F								
G								
H								

Well suited for
neighborhood-related TBTs

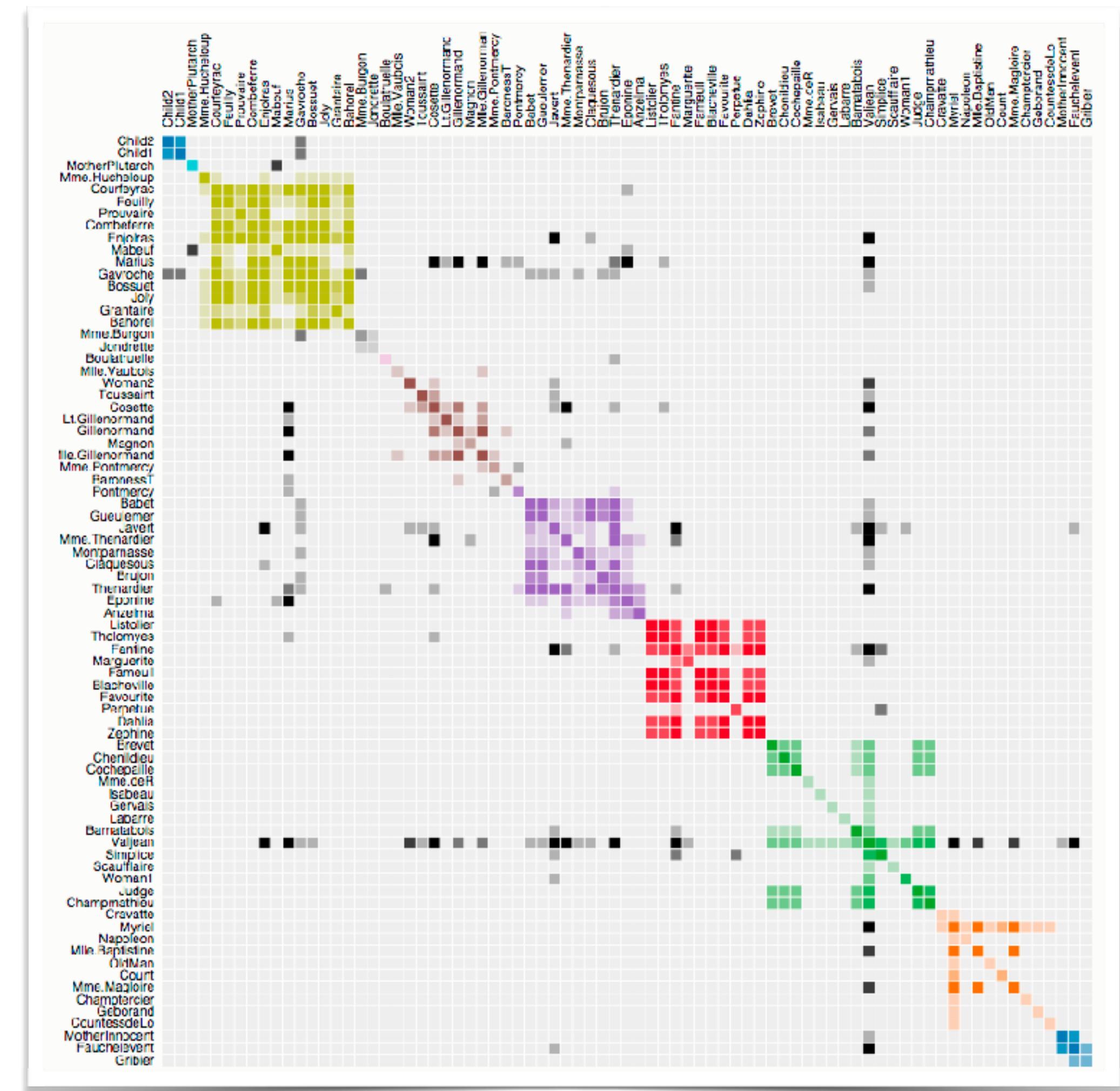
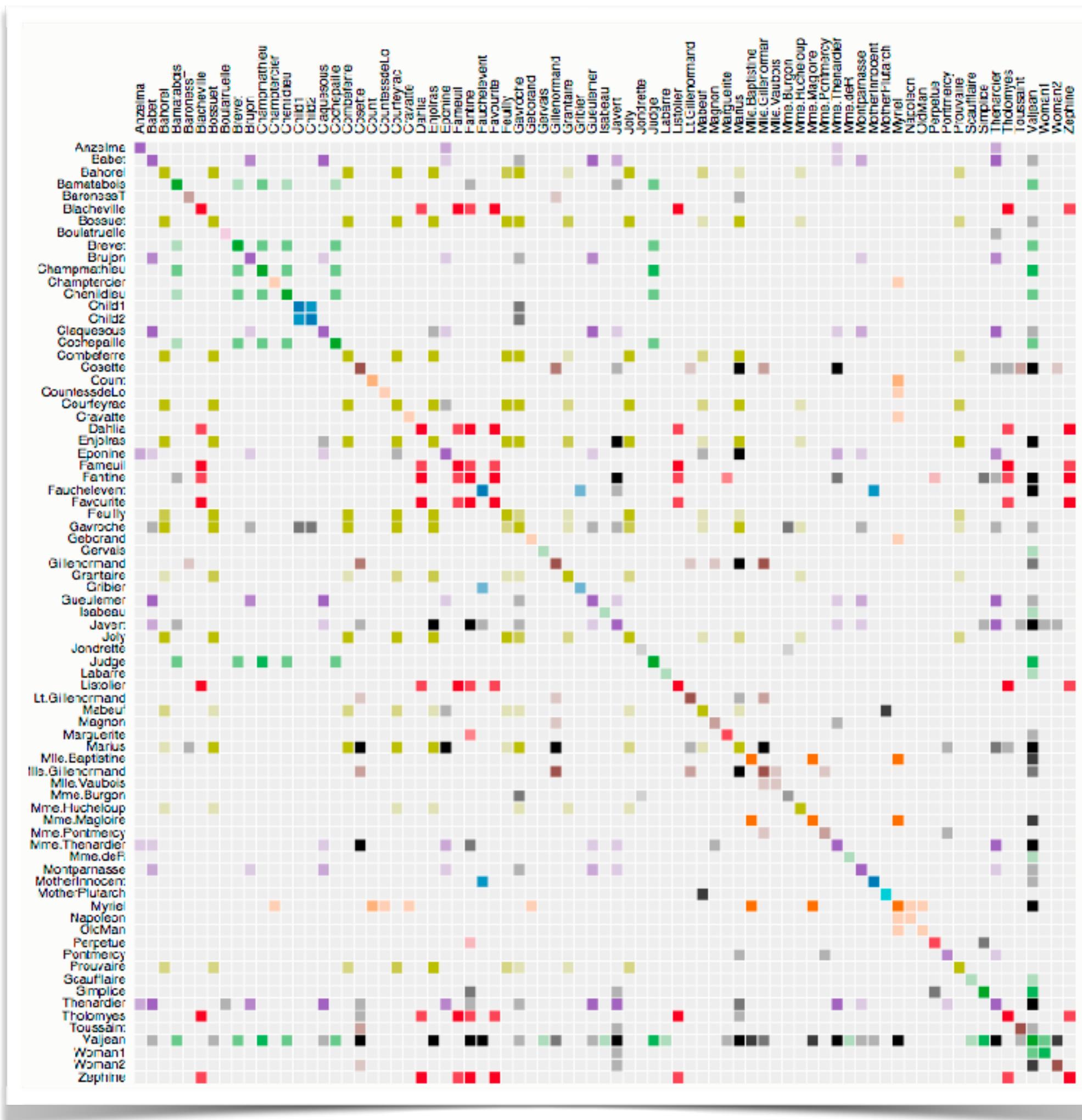


	A	B	C	D	E
E				■	■
D			■	■	■
C					
B				■	
A					

Not suited for
path-related TBTs



Order Critical!



Matrix Representations

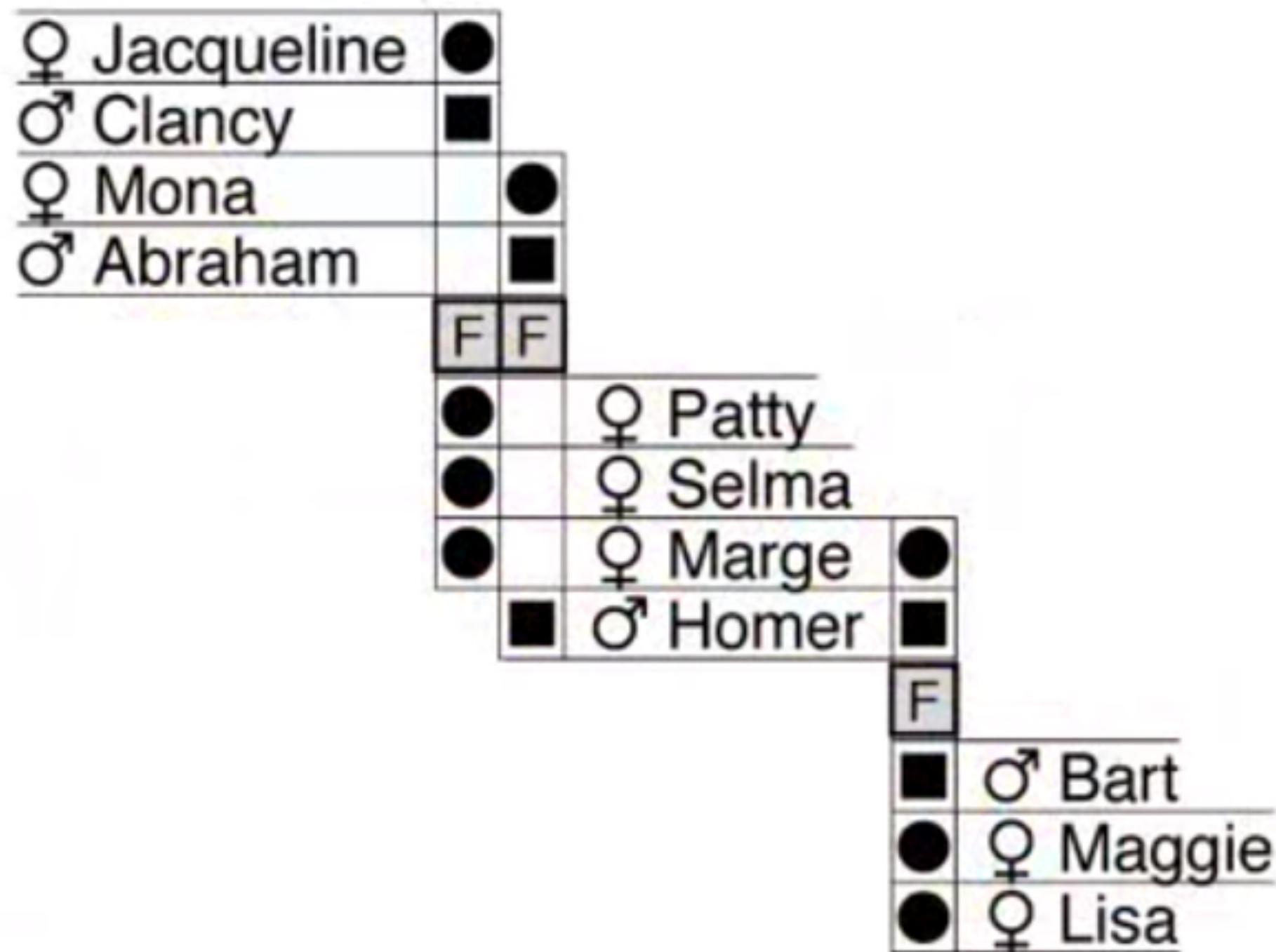
Pros:

- can represent **all graph classes** except for hypergraphs
- puts **focus on the edge set**, not so much on the node set
- simple grid -> **no elaborate layout** or rendering needed
- well suited for **ABT on edges** via coloring of the matrix cells
- well suited for **neighborhood-related TBTs** via traversing rows/columns

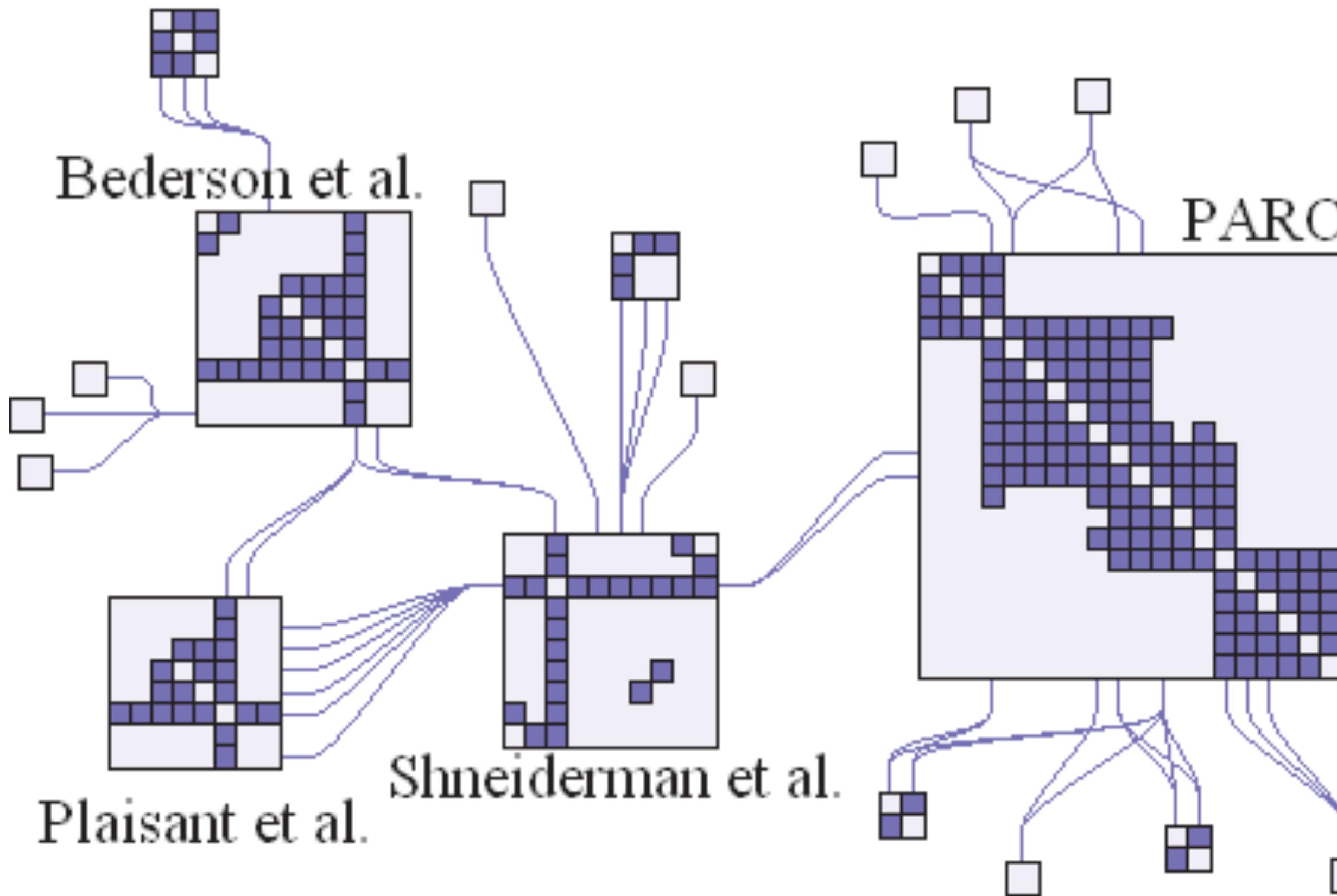
Cons:

- quadratic screen space requirement (any possible edge takes up space)
- not suited for path-related TBTs

Special Case: Genealogy



Hybrid Explicit/Matrix

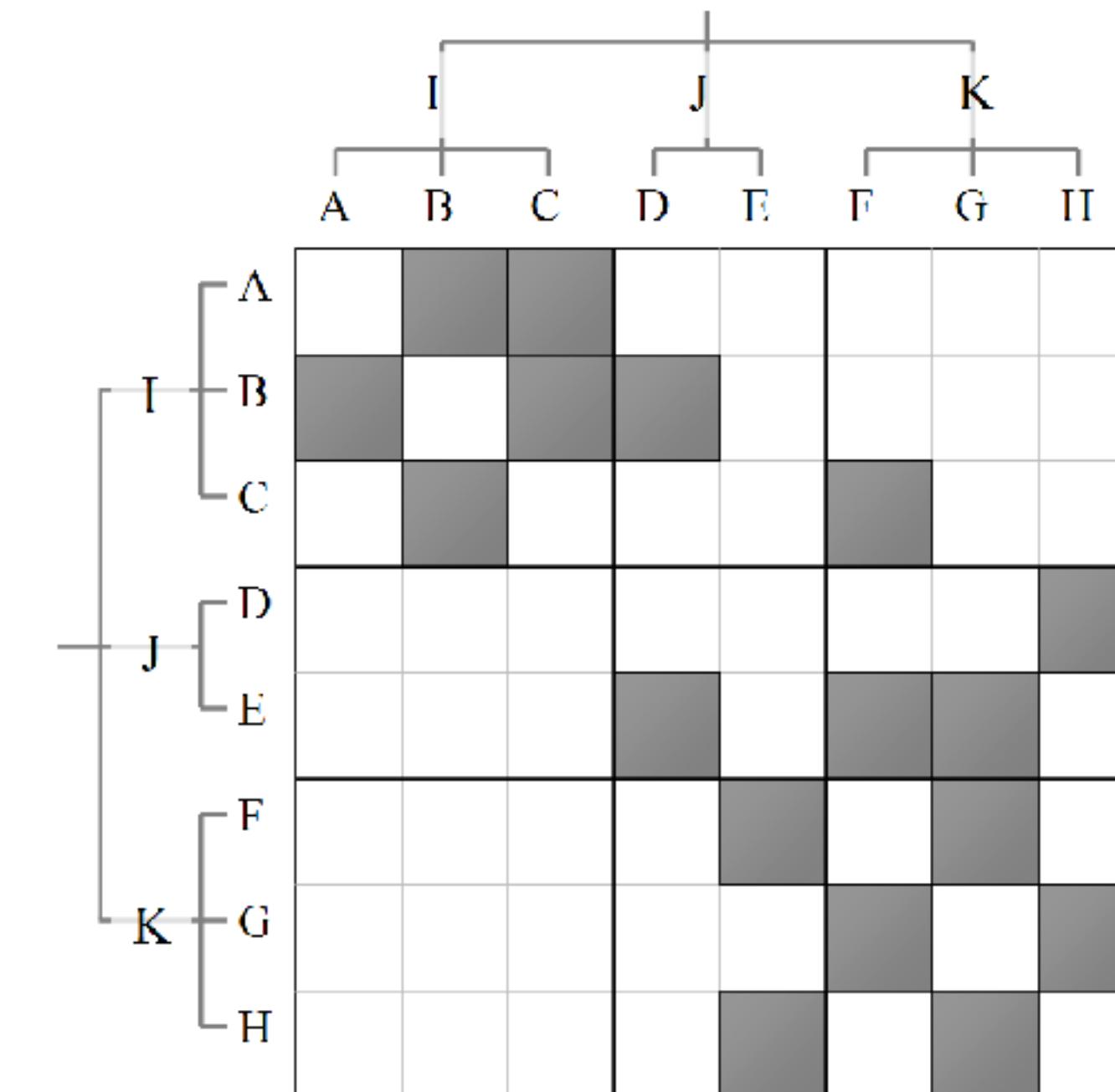
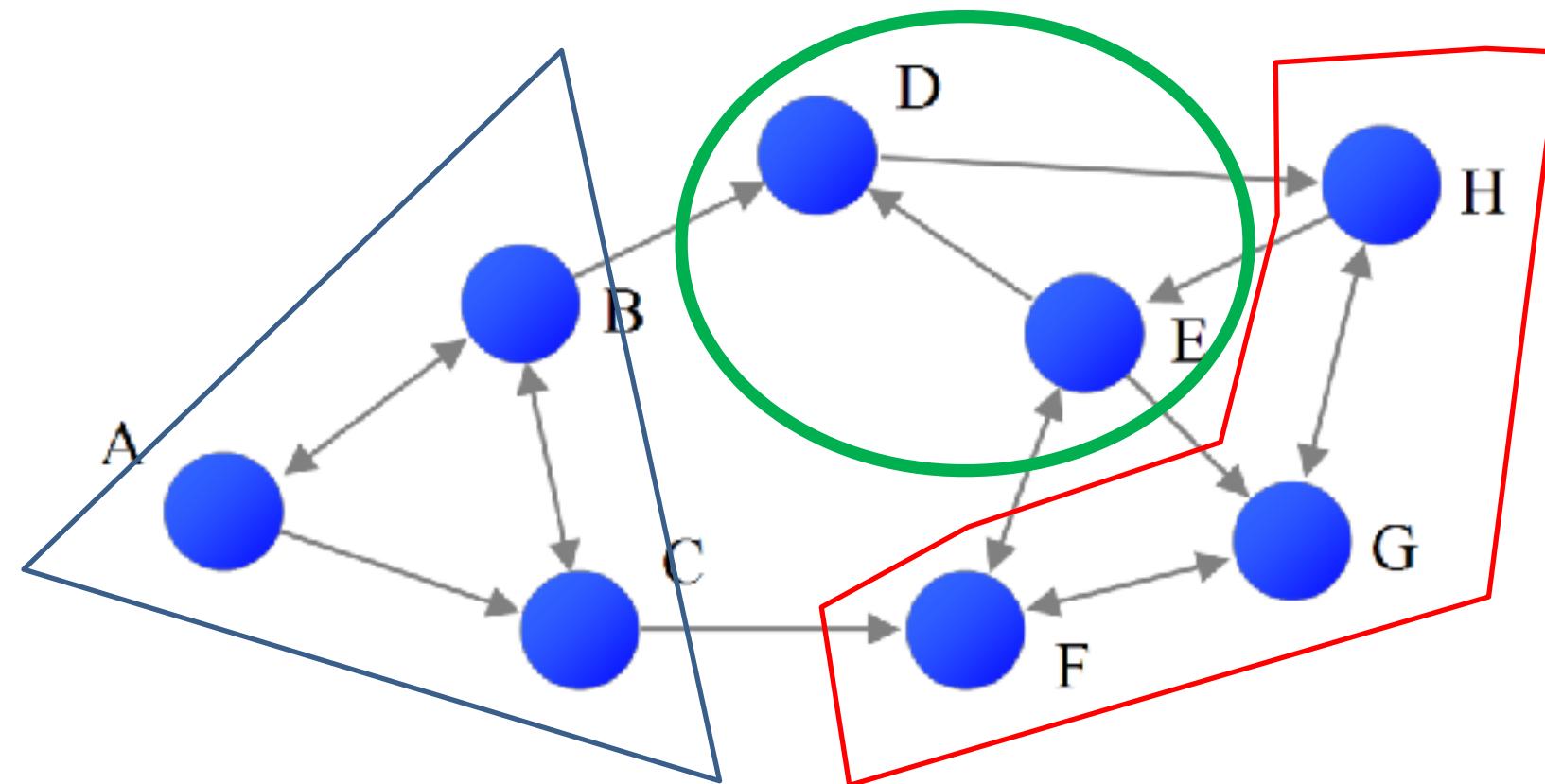


NodeTrix
[Henry et al. 2007]

Matrix Representations

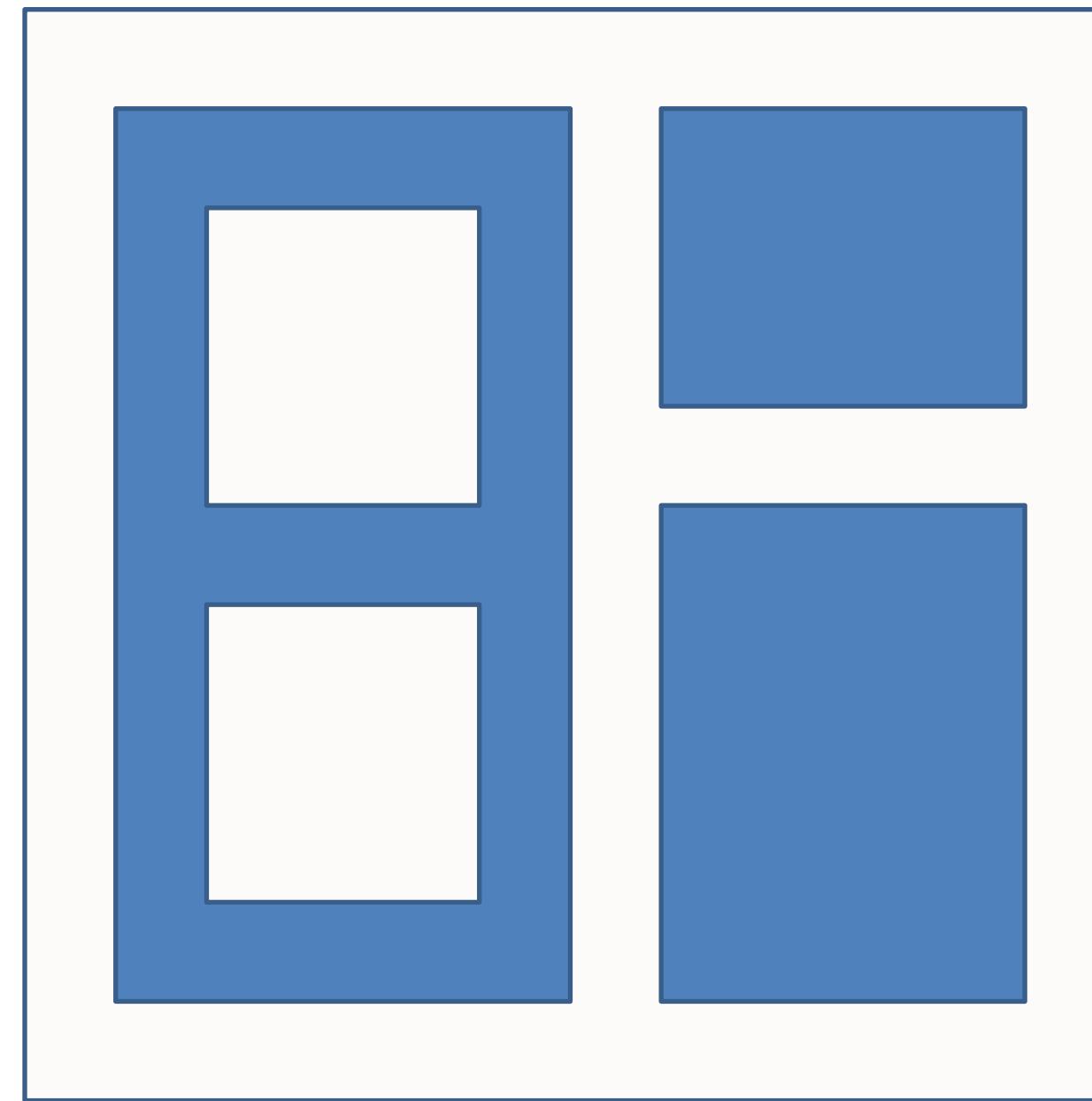
Problem #1: used screen real estate is quadratic in the number of nodes

Solution approach: hierarchization of the representation

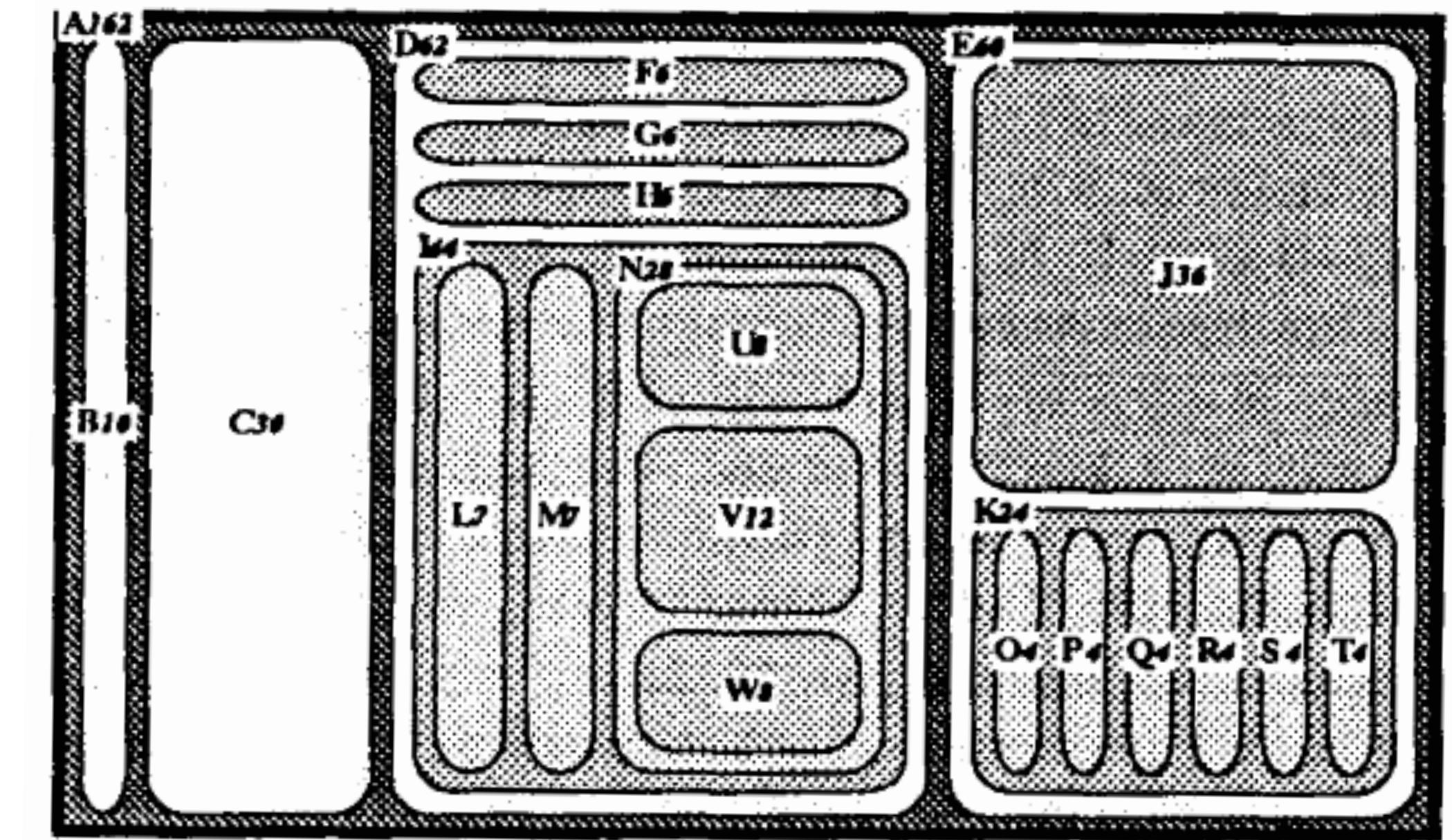
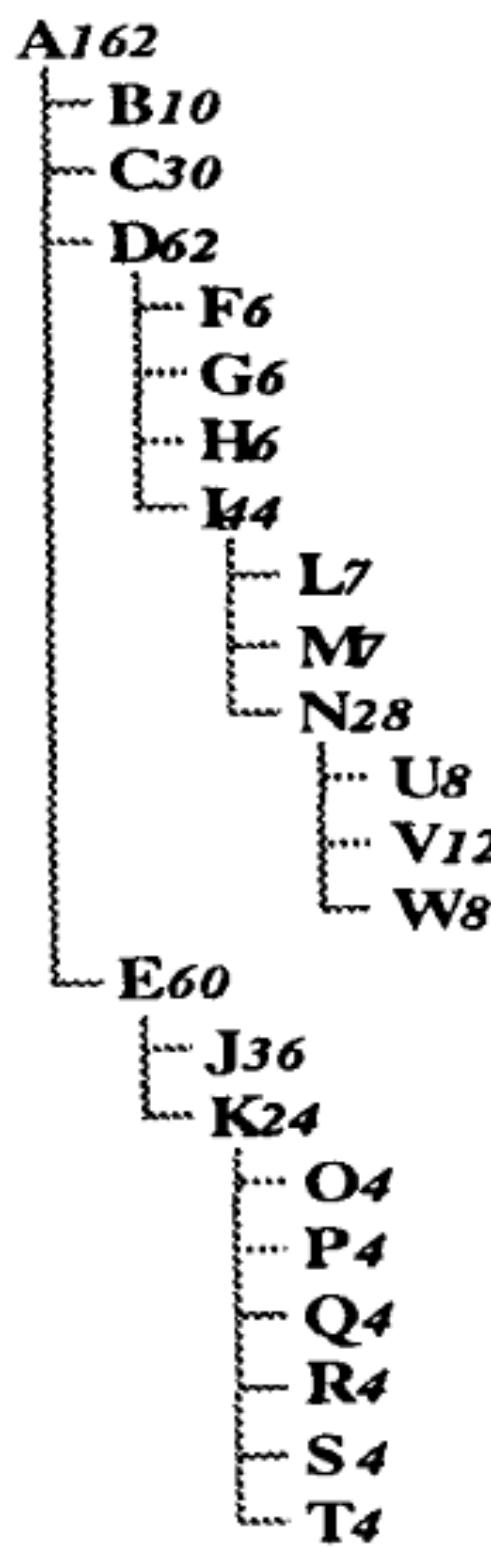
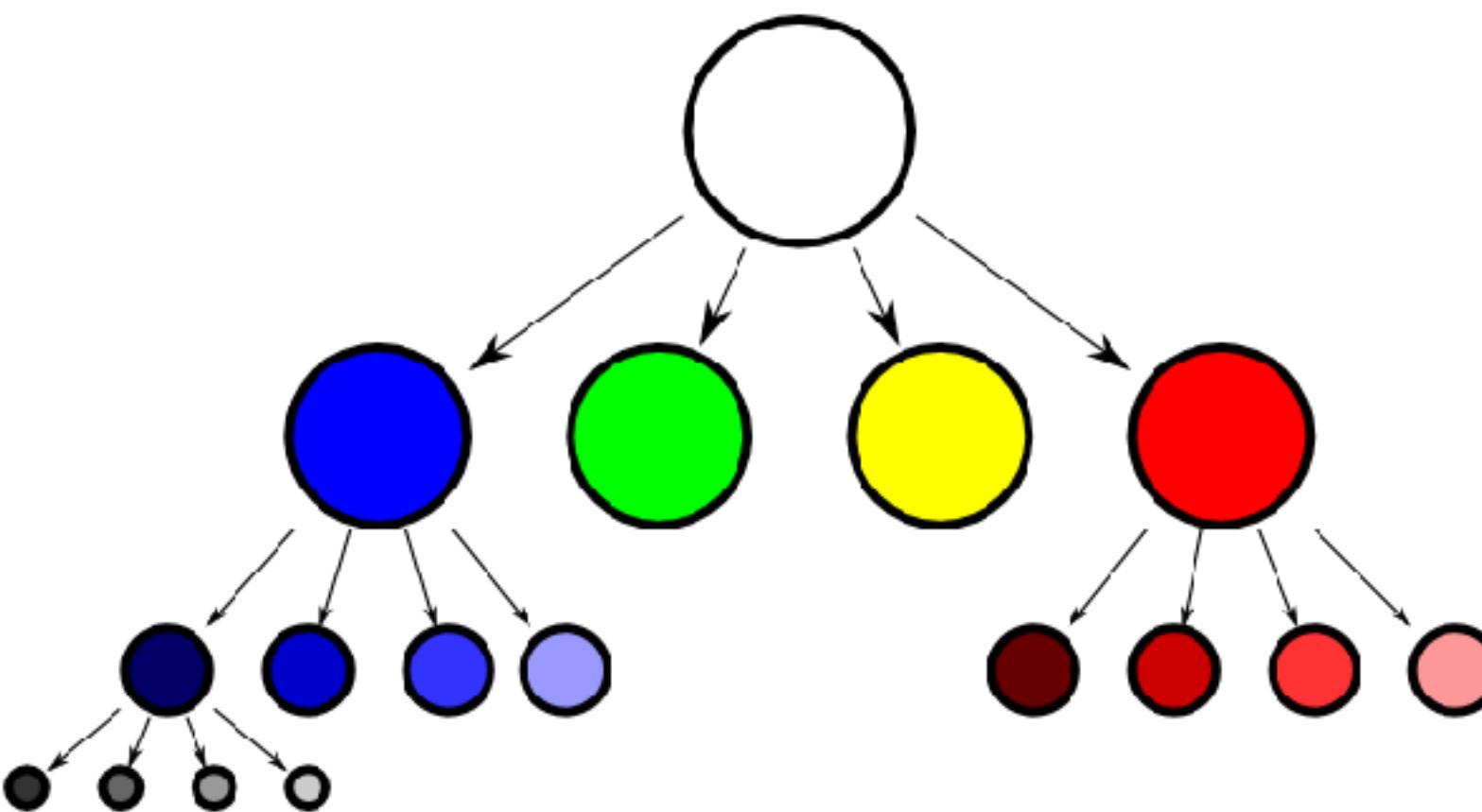
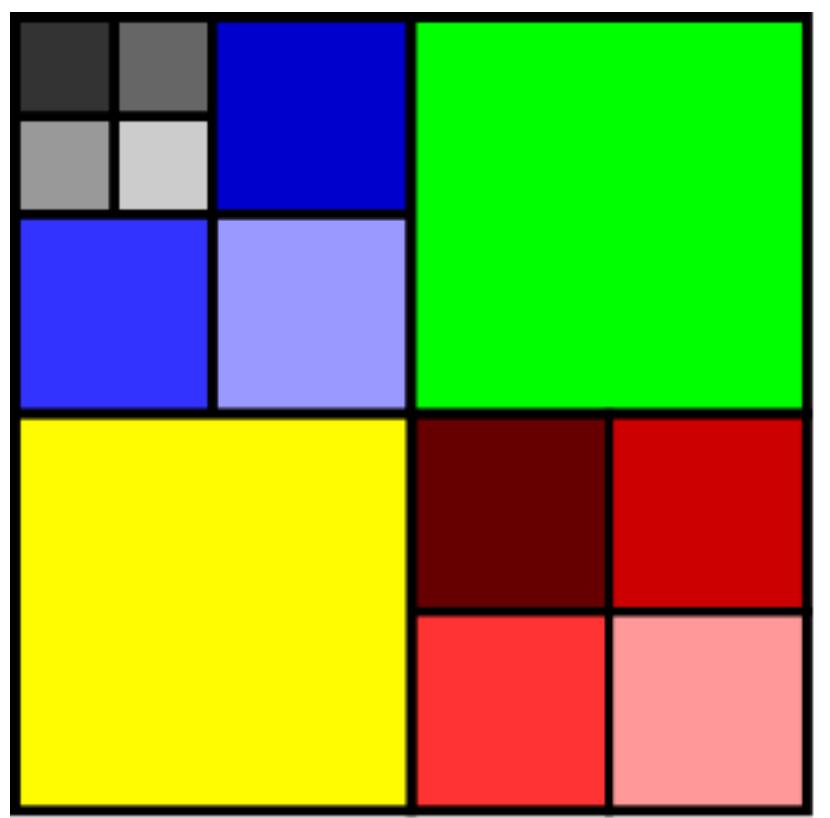


[van Ham et al. 2009]

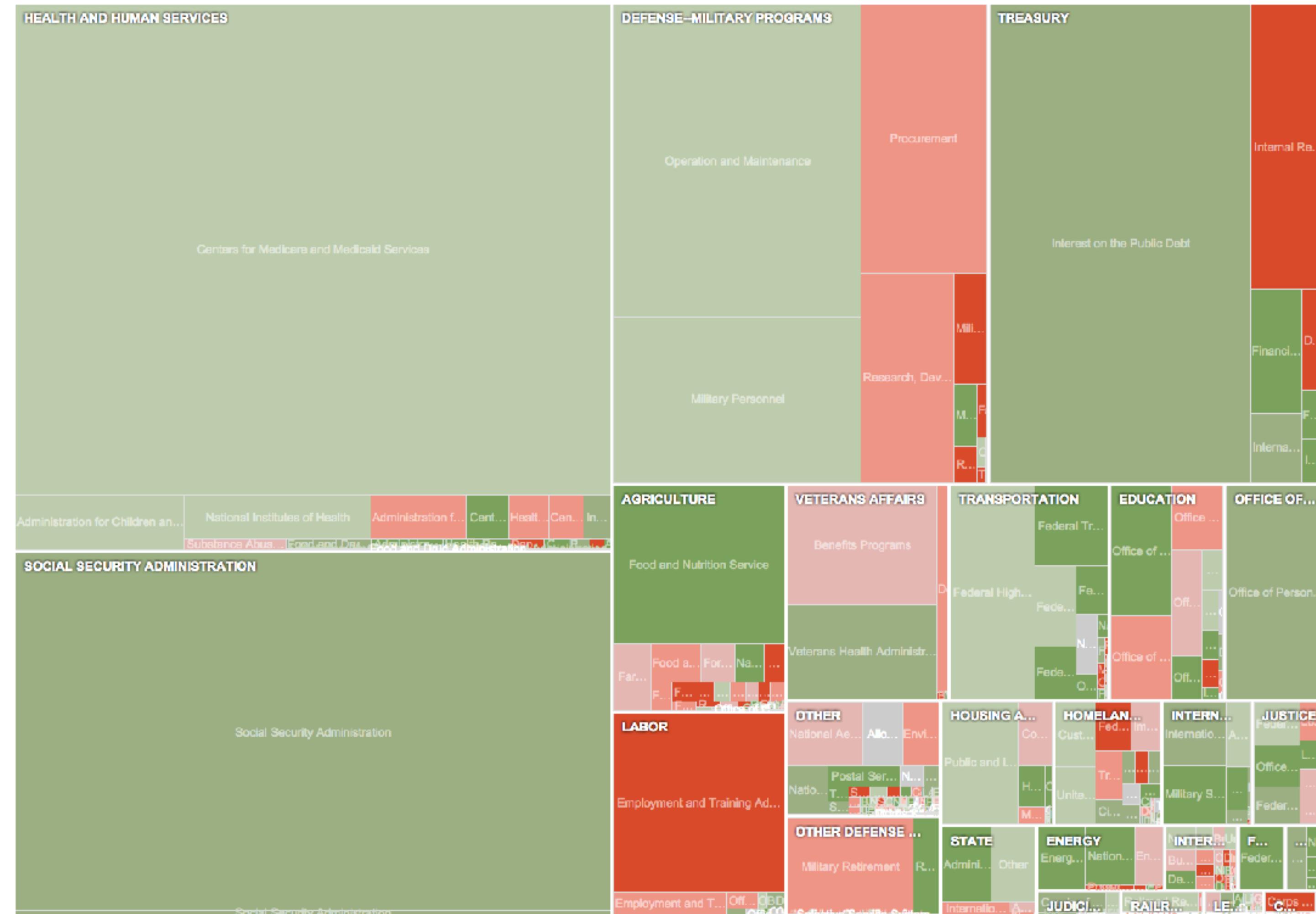
Implicit Layouts for Trees



Tree Maps



Zoomable Treemap



Example: Interactive TreeMap of a Million Items



Sunburst: Radial Layout



[Sunburst by John Stasko, Implementation in Caleydo by Christian Partl]

Implicit Representations

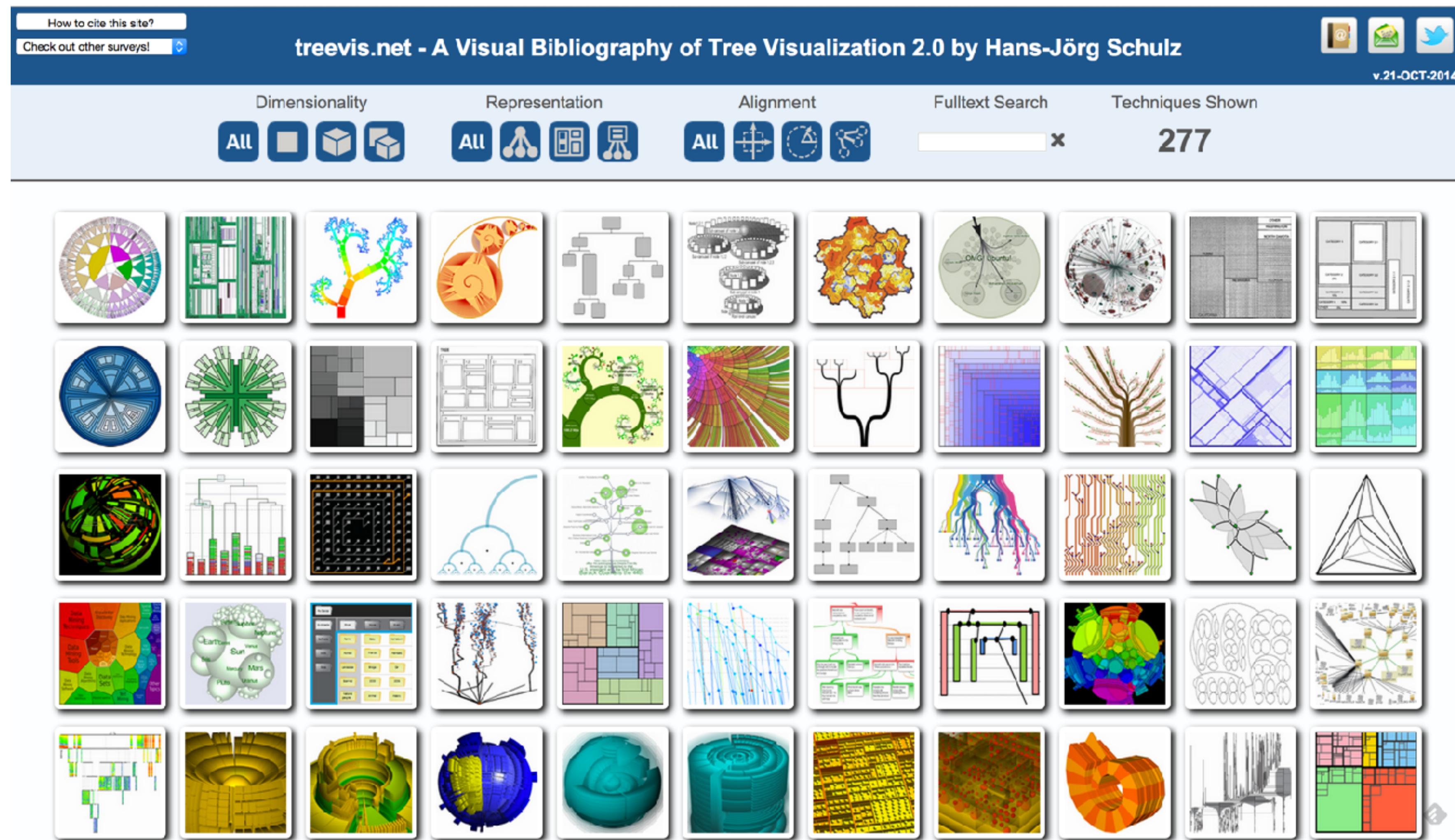
Pros:

- space-efficient because of the lack of explicitly drawn edges: scale well up to very large graphs
- in most cases well suited for ABTs on the node set
- depending on the spatial encoding also useful for TBTs

Cons:

- can only represent trees
- since the node positions are used to represent edges, they can no longer be freely arranged (e.g., to reflect geographical positions)
- useless to pursue any task on the edges
- spatial relations such as overlap or inclusion lead to occlusion

Tree Visualization Reference



Visualizing Time Varying Graphs

Up to now: given graphs were **static**

Extension: given is a **sequence of graphs**

either the sequence is given in full (offline)

or the sequence is streamed (online)

Variants:

varying linkage:

node set is fixed, only edges change over time

varying attributes:

graph structure is fixed, only attributes change

Visualizing Time Varying Graphs

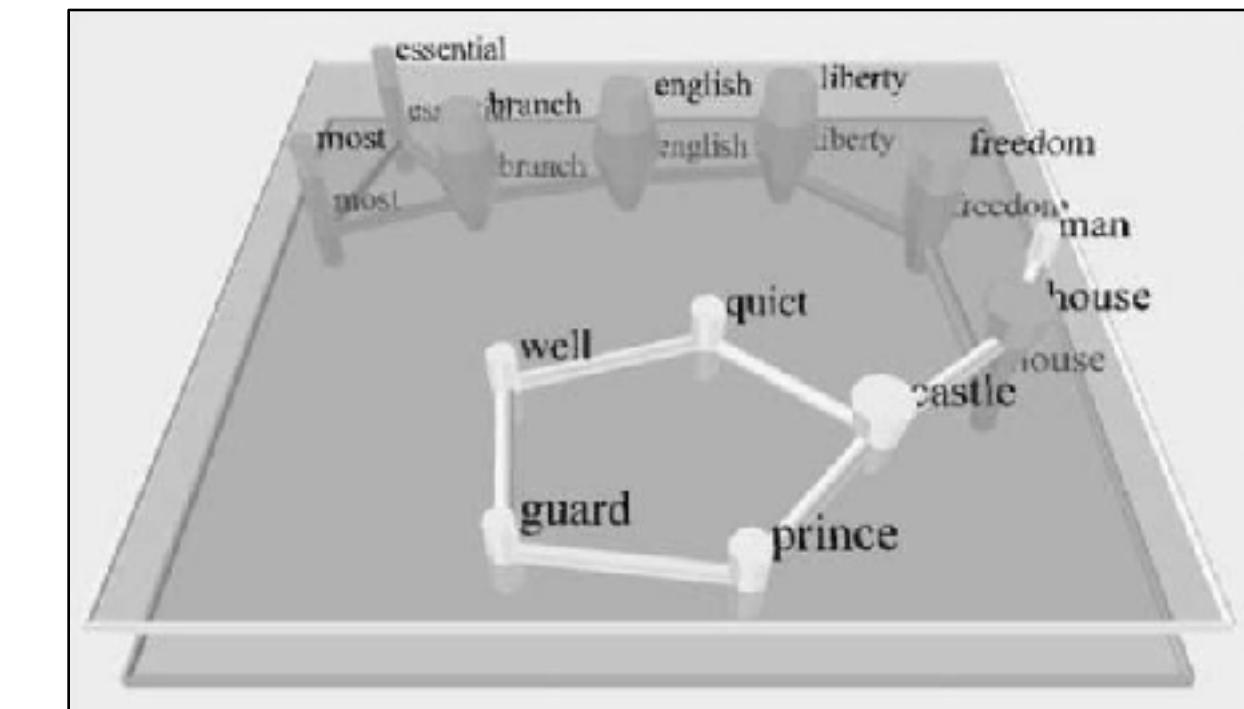
Animation

Map time to time

Layering

Layout graph in 2D and use 3rd dimension to show time

For small graphs with few time steps

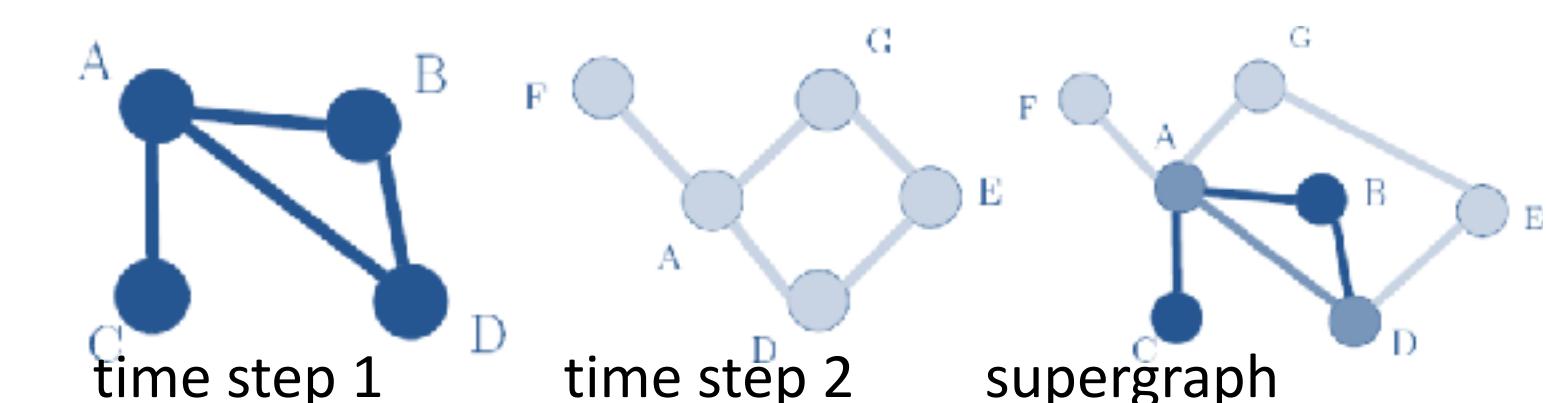


Brandes & Corman 2003

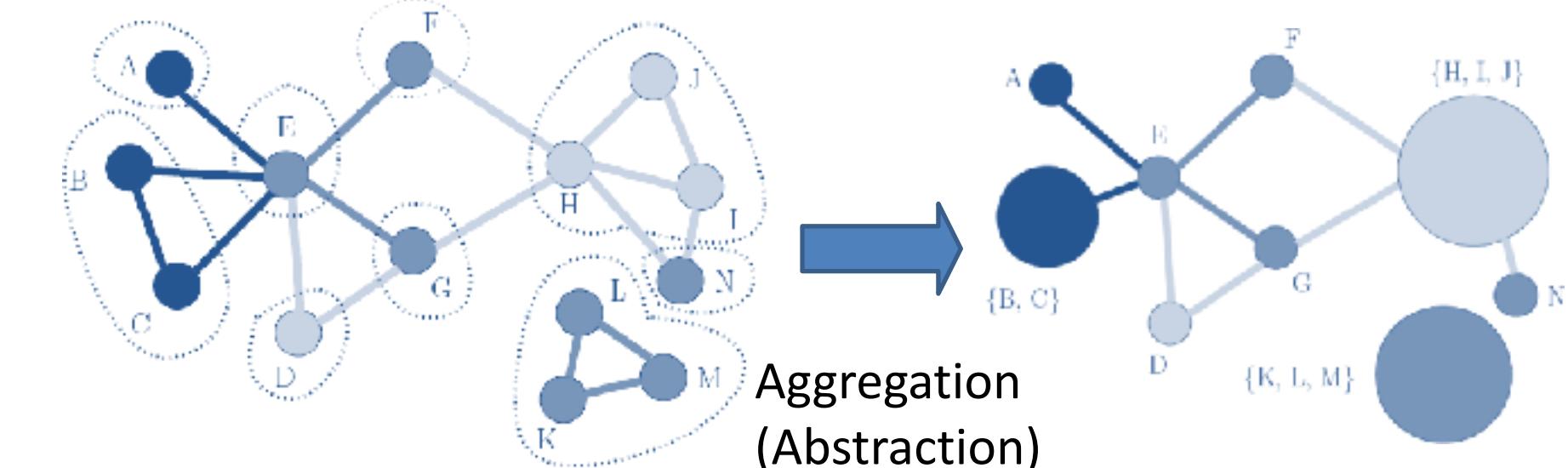
Supergraph

Aggregate all time steps into a supergraph

Use colors etc. to represent time



Aggregation



Visualizing Edge Attributes

Most common ways to encode edge attributes

Quantitative: Width



Ordinal: Saturation



Nominal: Style



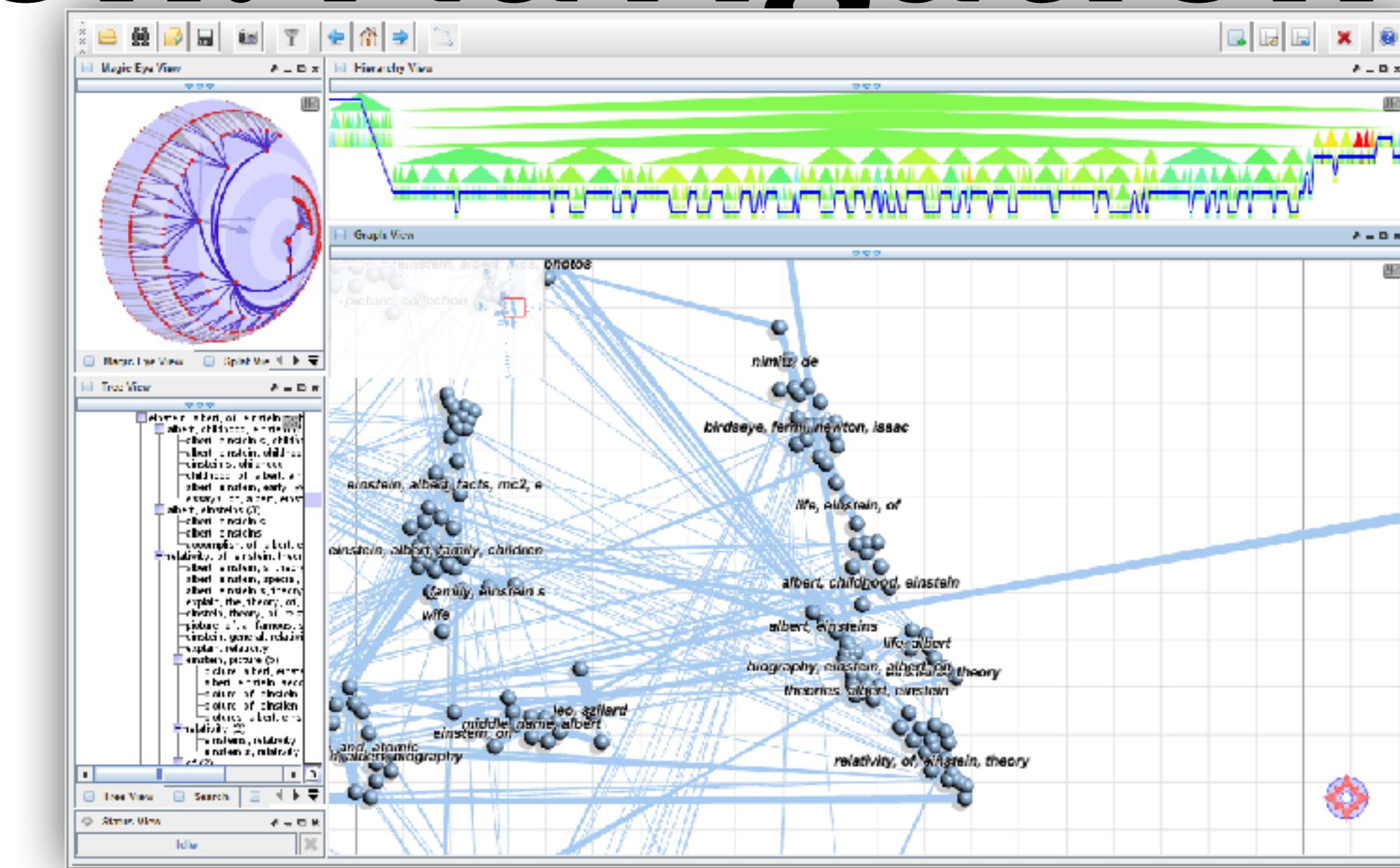
Graph Interaction: Navigation

Standard techniques

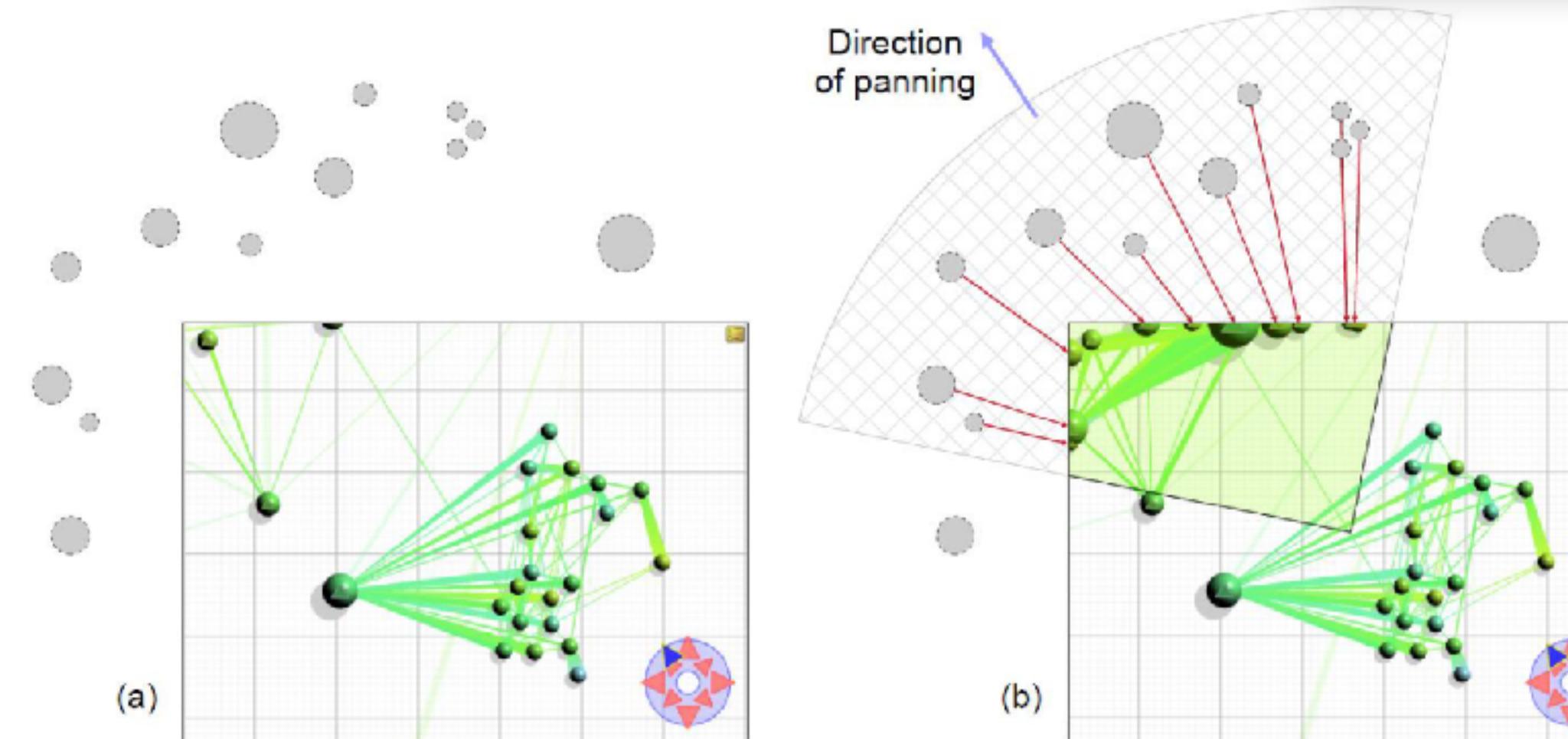
e.g., overview+detail

Edge-based traveling

Radar view for
foresighted panning



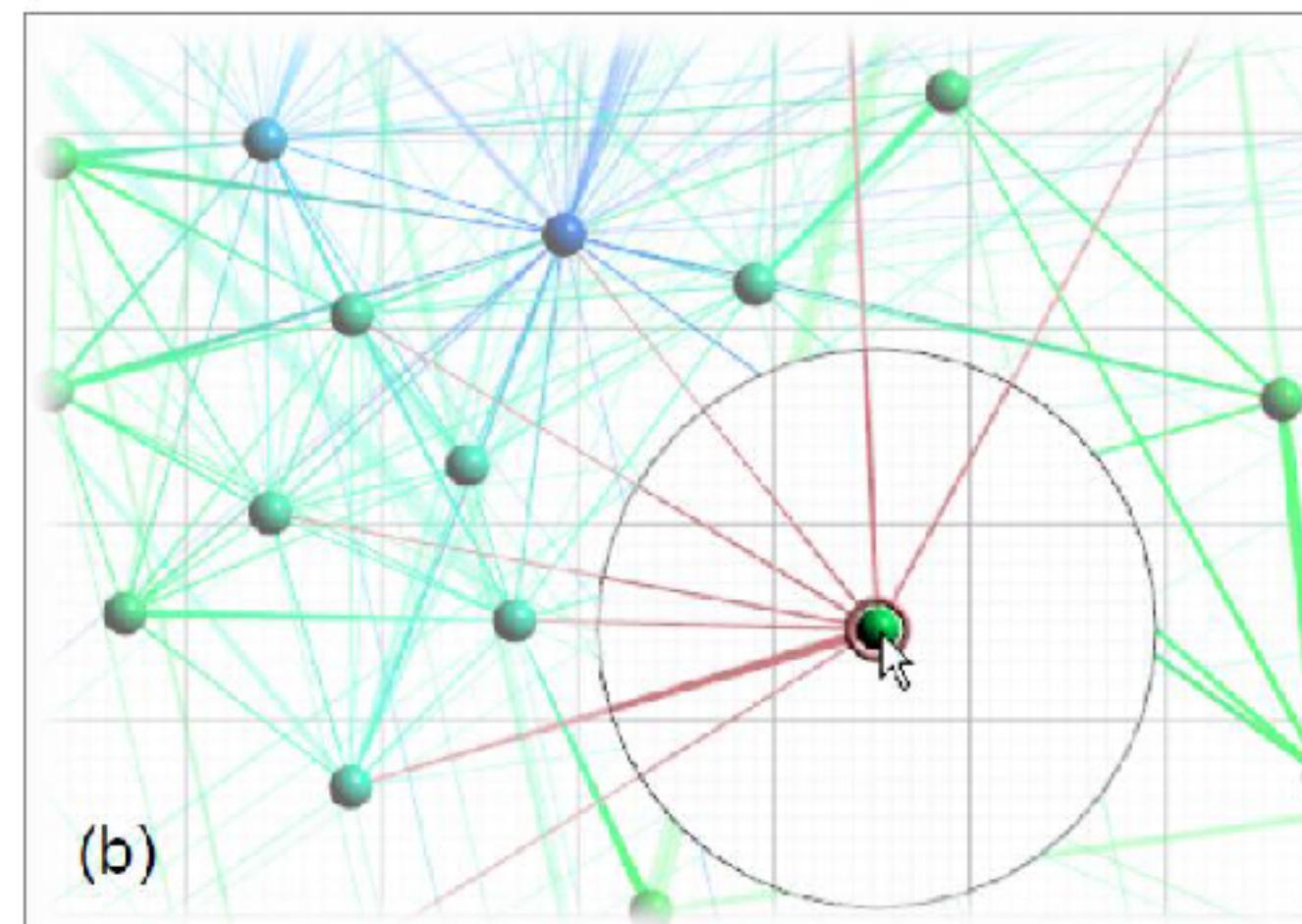
[Tominski et al. 2010]



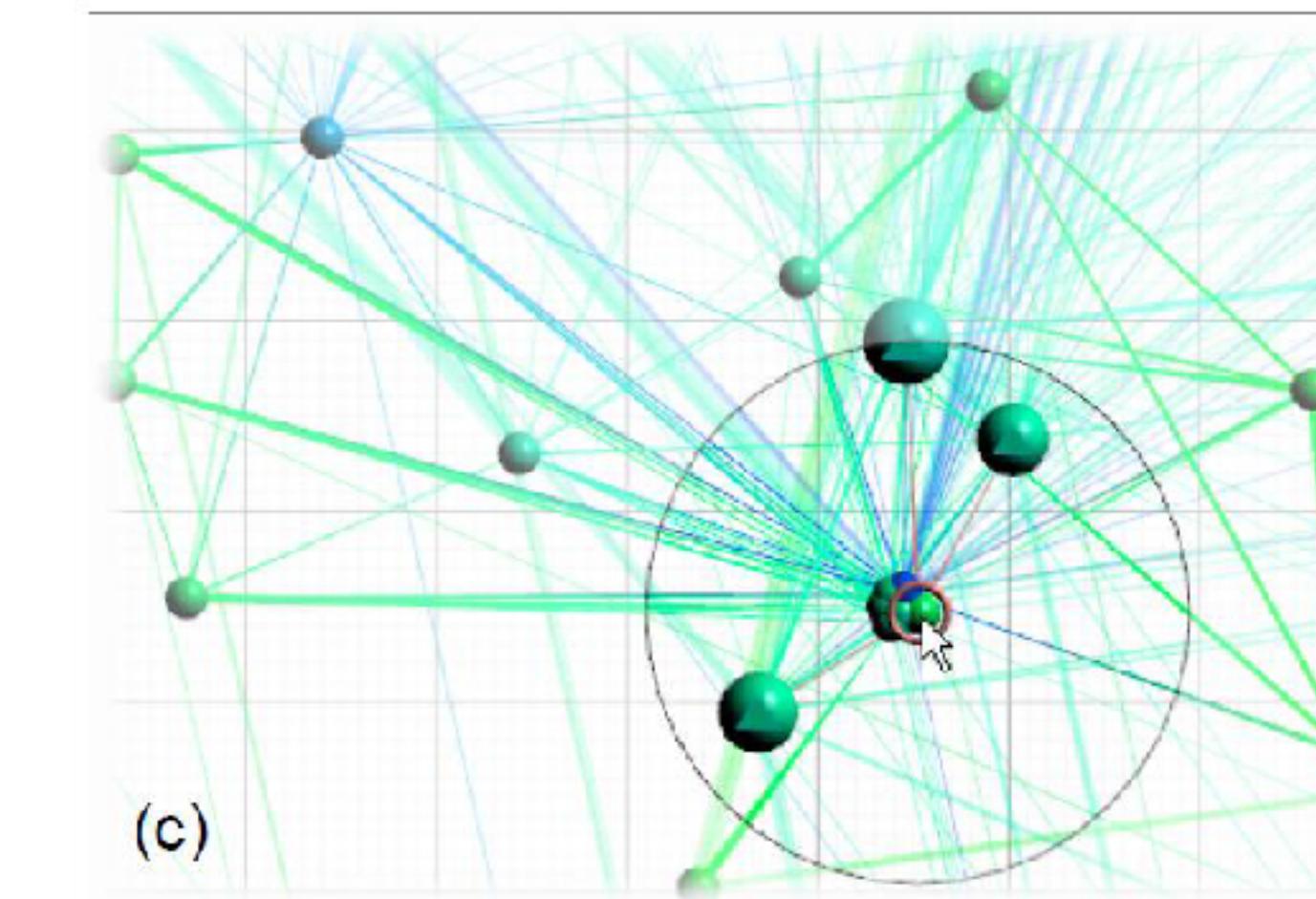
[Tominski et al. 2010]

Graph Interaction: Manipulation

Details-on-demand: smart lenses (semantic lenses)



Local-Edge-Lens shows only edges
incident to the nodes inside



Bring-Neighbors-Lens gathers all
neighbors of the center node

[Tominski et al. 2009]

Graph Tools & Applications

Gephi

<http://gephi.org>

The screenshot shows the official Gephi website. At the top left is the Gephi logo with the tagline "Gephi makes graphs handy". To the right is a navigation bar with links: Download, Blog, Wiki, Forum, Support, Bug tracker, Home, Features, Plugins, Users, Developers, and Partners. Below the navigation is a large image of the Gephi software interface displaying a complex network graph.

The Open Graph Viz Platform

Gephi is a visualization and exploration [platform](#) for all kinds of networks and complex systems, dynamic and hierarchical graphs.

Runs on Windows, Linux and Mac OS X. Gephi is open-source and free.

[Learn More on Gephi Platform »](#)

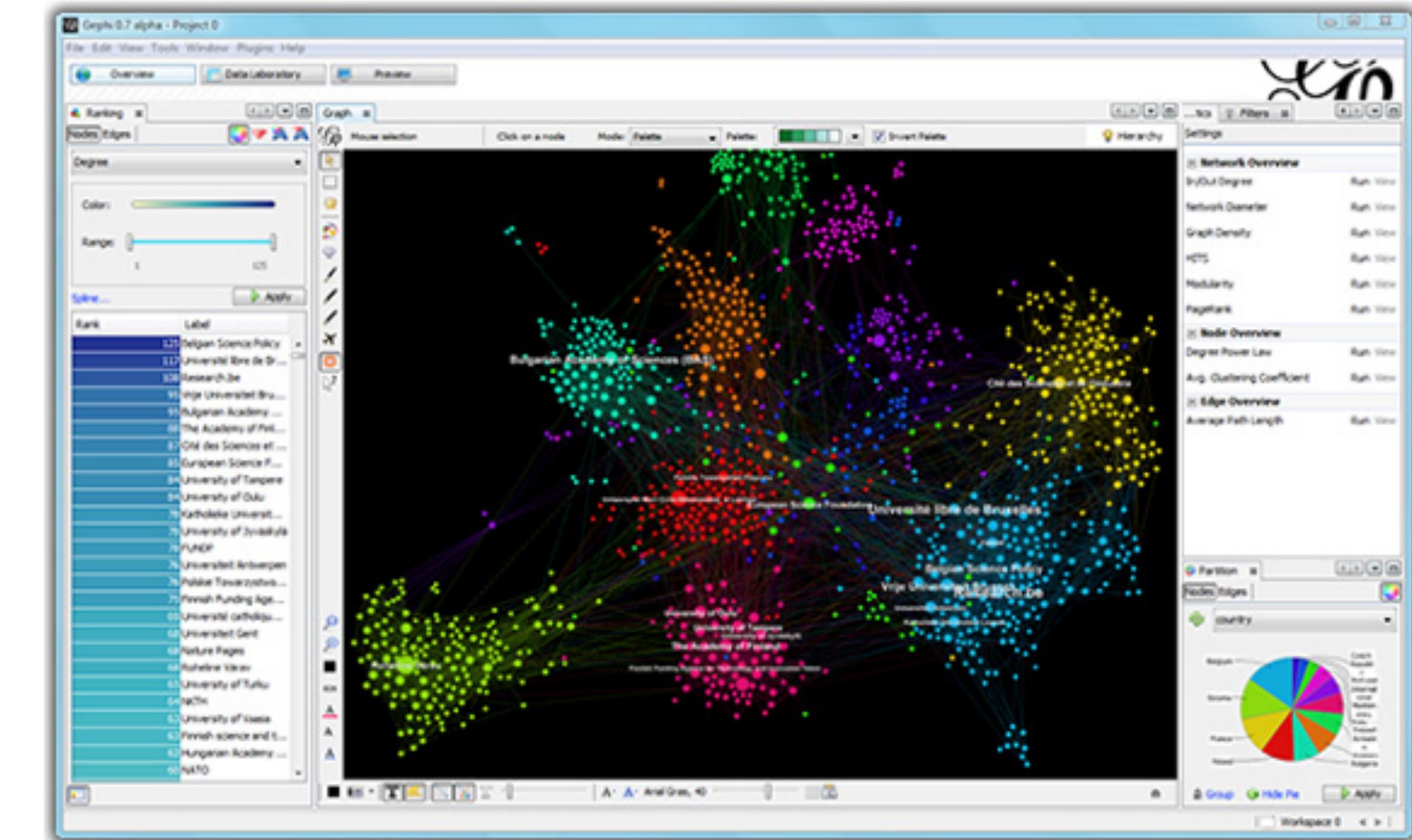


Download FREE
Gephi 0.7 alpha

[Release Notes](#) | [System Requirements](#)

► [Features](#)
► [Quick start](#)

► [Screenshots](#)
► [Videos](#)



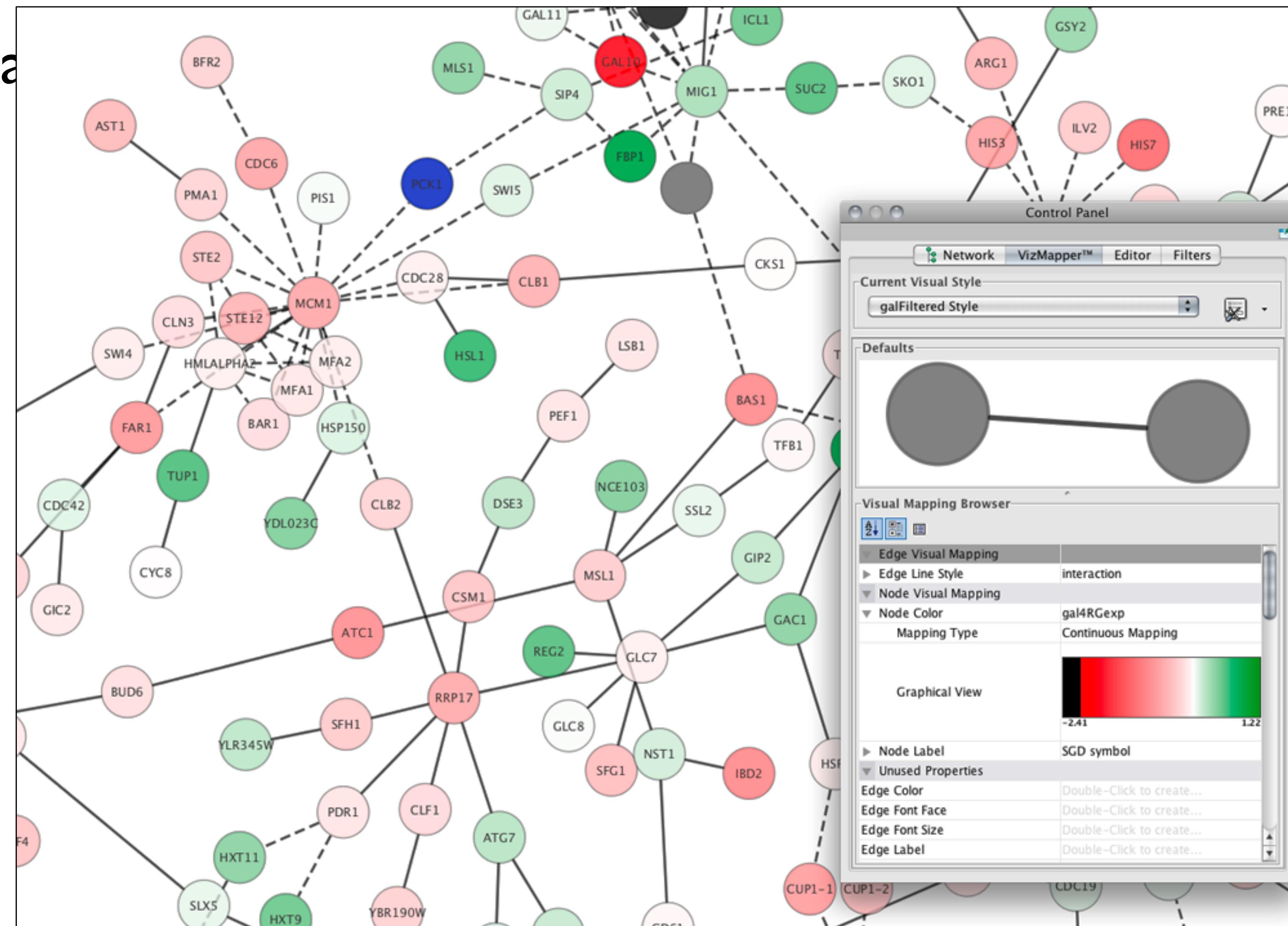
Gephi has been accepted again for Google Summer of Code! The program is the best way for students around the world to start contributing to an open-source project. Students, apply now for Gephi proposals. Come to the GSOC forum section and say Hi! to this [topic](#).

[Learn More »](#)

Cytoscape

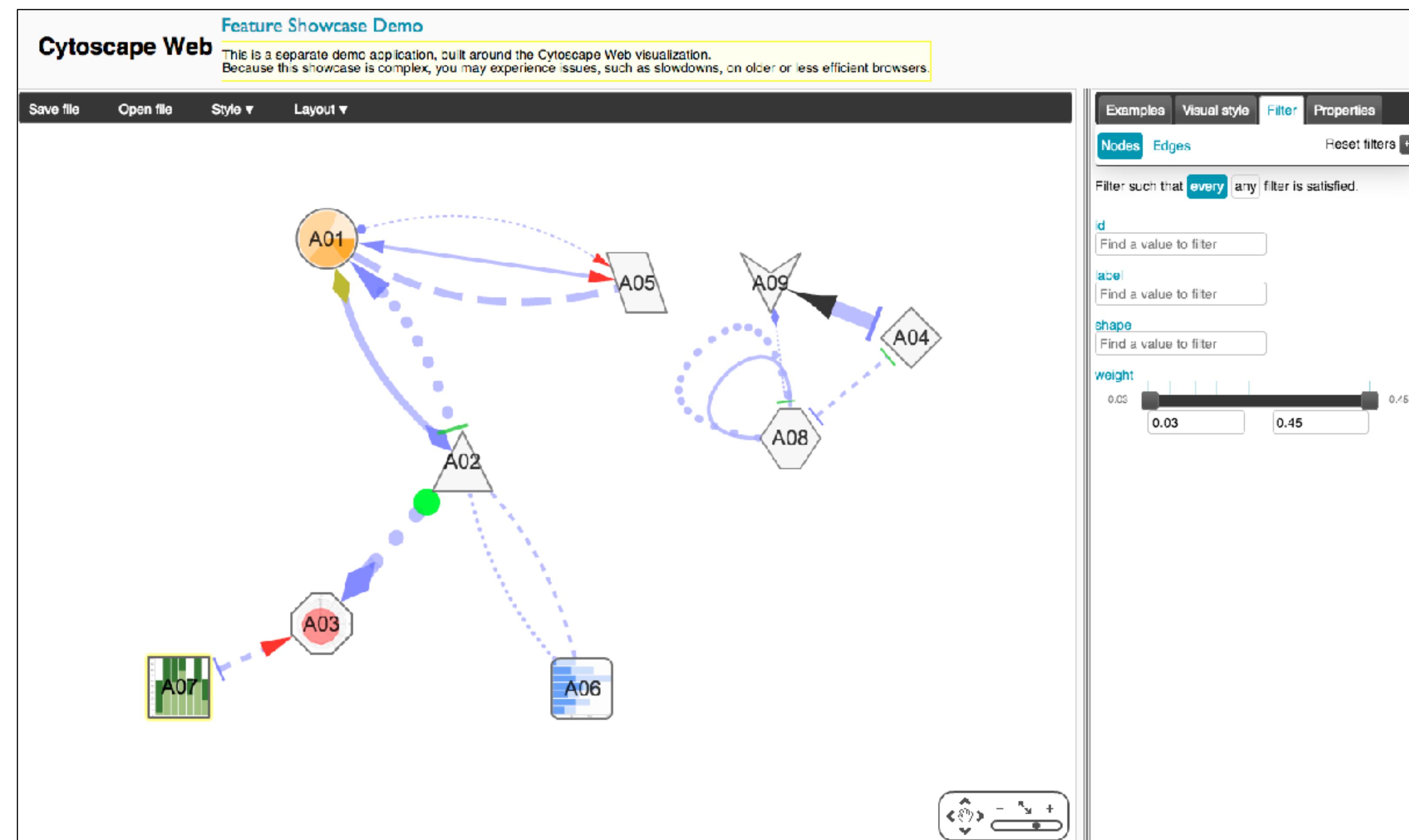
<http://www.cytoscape.org/>

Open source plat



Cytoscape Web

<http://cytoscapeweb.cytoscape.org/>



NetworkX

<https://networkx.github.io/>

NetworkX

[NetworkX Home](#) | [Documentation](#) | [Download](#) | [Developer \(Github\)](#)

High-productivity software for complex networks

NetworkX is a Python language software package for the creation, manipulation, and study of the structure, dynamics, and functions of complex networks.

[Documentation](#)
all documentation

[Examples](#)
using the library

[Features](#)

- Python language data structures for graphs, digraphs, and multigraphs.
- Nodes can be "anything" (e.g. text, images, XML records)
- Edges can hold arbitrary data (e.g. weights, time-series)
- Generators for classic graphs, random graphs, and synthetic networks
- Standard graph algorithms
- Network structure and analysis measures
- Open source [BSD license](#)
- Well tested: more than 1800 unit tests, >90% code coverage
- Additional benefits from Python: fast prototyping, easy to teach, multi-platform



[Reference](#)
all functions and methods

Versions

Latest Release
1.8.1 - 4 August 2013
[downloads](#) | [docs](#) | [pdf](#)

Development
1.9dev
[github](#) | [docs](#) | [pdf](#)
[build](#) passing
[coverage](#) 83%

Contact
[Mailing list](#)
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[Developer guide](#)

