

University of Central Florida

UCF Narcissus

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Contest (1)

```
template.cpp
#include <bits/stdc++.h>
#define all(x) begin(x), end(x)
using namespace std;
using 11 = long long;
int main() {
  cin.tie(0)->sync_with_stdio(0);
  cin.exceptions(cin.failbit);
```

Data structures (2)

Description: Query [l, r] sums, and point updates. kth() returns the smallest index i s.t. query(0, i) >= k

Time: $\mathcal{O}(\log n)$ for all ops.

10 lines

```
33f78c, 22 lines
template <typename T>
struct BIT {
  vector<T> s;
  int n;
  BIT(int n): s(n + 1), n(n) {}
  void update(int i, T v) {
    for (i++; i <= n; i += i & -i) s[i] += v;</pre>
  T query(int i) {
   T ans = 0;
    for (i++; i; i -= i & -i) ans += s[i];
    return ans;
  T query(int 1, int r) { return query(r) - query(1 - 1); }
  int kth(T k) { // returns n if k > sum of tree}
   if (k <= 0) return -1;
    int i = 0:
    for (int pw = 1 << __lg(n); pw; pw >>= 1)
     if (i + pw <= n && s[i + pw] < k) k -= s[i += pw];</pre>
    return i:
};
```

dsu.h

Description: Maintains a collection of disjoint sets.

Time: $\mathcal{O}(\alpha(1))$ amortized.

4d9c0b, 30 lines

```
class ufds {
    public:
    vi p, rank, size;
    int num_distincts;
    ufds(int n) {
        p.resize(n); rank.resize(n); size.resize(n);
        for (int i = 0; i < n; i++) {</pre>
           rank[i] = 0;
            size[i] = 1;
            p[i] = i;
        distincts = n;
    int find(int i) { return (p[i] == i) ? i : (p[i] = find(p[i
    bool same(int i, int j) { return find(i) == find(j); }
    void union_set(int i, int j) {
        int pi = find(i), pj = find_set(j);
        if (pi == pj) return;
        distincts--;
        size[pi] = size[pj] = size[pi] + size[pj];
        if (rank[pi] > rank[pj]) {
            p[pj] = pi;
        } else {
            p[pi] = p[pj];
            if (rank[pi] == rank[pj]) {
                rank[pj]++;
    }
} ;
```

Geometry (3)

```
closestpairpoints.cpp
```

993a04, 63 lines

```
struct vec{
    int x, v, id;
    explicit vec(int x=0, int y=0, int id=0) : x(x), y(y), id(
int n;
vector<vec> a, t;
double mindist:
pair<int, int> best;
void updClosest(const vec& a, const vec& b) {
    double dx = a.x - b.x, dy = a.y - b.y;
    double dist = sqrt(dx*dx + dy*dy);
    if(dist < mindist) {</pre>
        mindist = dist;
        best = {a.id, b.id};
bool cmpX(const vec& a, const vec& b) {
    return a.x < b.x || (a.x == b.x && a.y < b.y);
bool cmpY (const vec& a, const vec& b) {
    return a.y < b.y;</pre>
void solve(int 1, int r) {
    if(r-1 <= 3) {
        for(int i = 1; i < r; i++) {</pre>
```

for(int $j = i+1; j < r; j++){$

```
updClosest(a[i], a[i]);
        sort(a.begin()+l, a.begin()+r, cmpY);
        return:
    int m = (1+r)/2;
    int midx = a[m].x;
    solve(1, m);
    solve(m, r);
    merge(a.begin() + 1, a.begin() + m, a.begin() + m, a.begin
         () + r, t.begin(), cmpY);
    copy(t.begin(), t.begin() + (r-1), a.begin() + 1);
    int tSz = 0;
    for(int i = 1; i < r; i++) {</pre>
        if(abs(a[i].x-midx) < mindist){</pre>
             for(int j = tSz - 1; j >= 0 && a[i].y - t[j].y <</pre>
                 mindist; j--) {
                updClosest(a[i], t[j]);
            t[tSz++] = a[i];
void clstPts() {
   t.resize(n);
    sort(a.begin(), a.end(), cmpX);
    mindist = DBL_MAX;
    solve(0, n);
```

convexHull.cpp

Description: Given a set of vertices, find a set that creates a polygon such that all vertices lie within that polygon

Memory: $\mathcal{O}(n)$ Time: $\mathcal{O}(n)$

```
1e3255, 40 lines
using point = pair<int, int>;
#define xx first
#define yy second
int cross(point o, point a, point b){
    int dx1 = a.xx-o.xx, dy1 = a.yy-o.yy;
    int dx2 = o.xx-b.xx, dy2 = o.yy-b.yy;
    return dx1*dy2-dx2*dy1;
vector<point> convexHull(vector<point> p, int n) {
    vector<point> hull(n);
    if(n <= 3){
        for(int i = 0; i < n; i++)</pre>
            hull[i] = p[i];
        return;
    sort(p.begin(), p.end());
    int k = 0;
    for(int i = 0; i < n; i++){</pre>
        while (k \ge 2 \&\& cross(hull[k-2], hull[k-1], p[i]) \le 0)
            k--;
        hull[k++] = p[i];
```

```
for (int i = n-1, t = k+1; i > 0; i--) {
        while (k \ge t \&\& cross(hull[k-2], hull[k-1], p[i-1]) \le
            k--;
        hull[k++] = p[i];
    hull.resize(k);
    return hull;
seg.cpp
Description: Line segment geometry
Memory: \mathcal{O}(1)
Time: \mathcal{O}(1)
                                                      3199ec, 66 lines
#define eps 1e9
using vec = pair<double, double>;
#define xx first
#define yy second
vec operator+(const vec & v, const vec & u) { return {v.xx+u.xx
     , v.yy+u.yy}; }
vec operator-(const vec & v, const vec & u) { return {v.xx-u.xx
     , v.yy-u.yy}; }
vec operator*(const vec & v, const double & c) { return {v.xx *
     c, v.yy * c}; }
double dotProd(vec v, vec u) { return v.xx*u.xx + v.yy*u.yy; }
double crossProd(vec v, vec u) { return v.xx*u.yy - v.yy*u.xx;
double mag2(vec v) { return dotProd(v, v); }
double mag(vec v) { return sqrt(mag2(v)); }
vec unit(vec v) { return v * (1.0/mag(v)); }
vec rotate (vec v, double th) {
    double newX = v.xx*cos(th) + v.yy*sin(th);
    double newY = v.xx*sin(th) + v.yy*cos(th);
    return {newX, newY};
double angle(vec v) { return atan2(v.yy, v.xx); }
//start
using seg = pair<vec, vec>;
vec lineIntersection(seg a, seg b){
    vec dirA = a.second - a.first, dirB = b.second - b.first;
    double det = crossProd(dirB, dirA);
    if(det == 0) return {INT_MAX, INT_MAX};
    double t = (crossProd(dirB, b.first-a.first)) / det;
    return a.first + dirA * t;
bool containsPoint(seg s, vec p) {
    vec dir = s.second-s.first;
    double dist = crossProd(dir, p-s.first)/mag(dir);
    if(abs(dist) < eps) return false;</pre>
    return (mag(dir)-mag(s.first-p)-mag(s.second-p) < eps);</pre>
vec segIntersection(seg a, seg b){
    vec intersect = lineIntersection(a, b);
```

```
if(intersect.first == INT_MAX && intersect.first == INT_MAX
        return {INT_MAX, INT_MAX};
    if (containsPoint (a, intersect) && containsPoint (b,
         intersect))
        return intersect;
    return {INT_MAX, INT_MAX};
//returns 1 if above, 0 if on, -1 if below
int side(seg s, vec p) {
    vec dir = s.second-s.first;
    double dist = crossProd(dir, p-s.first)/mag(dir);
    if(abs(dist) < eps) return 0;</pre>
    if(dist < 0) return -1;</pre>
    else return 1;
bool intersects(seg a, seg b) {
    return side(a, b.first)!=side(a, b.second) &&
           side(b, a.first)!=side(b, a.second);
vec.cpp
Description: Vector code
Memory: \mathcal{O}(1)
Time: \mathcal{O}(1)
                                                      00645f, 24 lines
using vec = pair<double, double>;
#define xx first
#define yy second
vec operator+(const vec & v, const vec & u) { return {v.xx+u.xx}
    , v.yy+u.yy}; }
vec operator-(const vec & v, const vec & u) { return {v.xx-u.xx
vec operator*(const vec & v, const double & c) { return {v.xx *
      c, v.yy * c}; }
double dotProd(vec v, vec u) { return v.xx*u.xx + v.yy*u.yy; }
double crossProd(vec v, vec u) { return v.xx*u.yy - v.yy*u.xx;
double mag2(vec v) { return dotProd(v, v); }
double mag(vec v) { return sqrt(mag2(v)); }
vec unit(vec v) { return v * (1.0/mag(v)); }
vec rotate90(vec v) { return{-v.yy, v.xx}; }
vec rotate270(vec v) { return{v.yy, -v.xx}; }
vec rotate (vec v, double th) {
    double newX = v.xx*cos(th) + v.yy*sin(th);
    double newY = v.xx*sin(th) + v.yy*cos(th);
    return {newX, newY};
double angle(vec v) { return atan2(v.yy, v.xx); }
```

Graphs (4)

bellmanFord.cpp

Memory: $\mathcal{O}(V^2)$

Time: $\mathcal{O}\left(V^3\right)$

Description: Single Source Shortest Path (SSSP)

e3cbb3, 24 lines

```
#define vv first
#define ww second
using edge = pair<int, int>;
void bellmanFord(vector<edge> g[], int v, int s){
    int dist[v];
   memset(dist, 0, sizeof(0));
    for (int i = 0; i < v-1; i++)
        for(int u = 0; u < v; u++)
            for(edge e : q[u])
                if(dist[u] + e.ww < dist[e.vv])</pre>
                    dist[e.vv] = dist[u] + e.ww;
    //check for negative cycles
    for (int u = 0; u < v; u++) {
        for(edge e : g[u]){
            if (dist[u]!=INT_MAX && dist[u] + e.ww < dist[e.vv])</pre>
                //negative cycle reached
                return;
diikstraTvlerM.cpp
                                                      1faf48, 28 lines
using namespace std;
#define vv first
#define ww second
using edge = pair<int, int>;
void djikstras(vector<edge> g[], int v, int s){
    priority_queue<edge, vector<edge>, greater<edge>> pg;
   vector<int> dist(v, INT_MAX);
   dist[s] = 0:
   pq.push(make_pair(0,s));
    while(!pq.empty()){
        if(pq.top().first > dist[pq.top().first])
            continue;
        int u = pq.top().second;
        pq.pop();
        for(edge e : g[u]){
            if(dist[e.vv] > dist[u] + e.ww) {
                dist[e.vv] = dist[u] + e.ww;
                pq.push(make_pair(dist[e.vv], e.vv));
floydWarshall.cpp
Description: FindAll-Pairs Shortest Paths (APSP)
Memory: \mathcal{O}(n^2)
```

```
Time: \mathcal{O}\left(n^3\right)
#define vv first
#define ww second
using edge = pair<int, int>;
void floydWarshall(vector<edge> g[], int n) {
    int d[n][n];
    memset(d, INT_MAX, sizeof(d));
    for(int i = 0; i < n; i++) d[i][i] = 0;</pre>
    for (int i = 0; i < n; i++) {
        for(edge e : q[i]){
            if(e.ww < d[i][e.vv])
                 d[i][e.vv] = d[e.vv][i] = e.ww;
    for(int k = 0; k < n; k++) {
        for(int i = 0; i < n; i++) {</pre>
            for (int j = 0; j < n; j++) {
                 d[i][j] = min(d[i][j], d[i][k] + d[k][j]);
kruskalMST.cpp
Description: Construct a Minimum Spanning Tree using Kruskal's algo-
rithm
Time: \mathcal{O}\left(E\alpha\right)
                                                        30806f, 50 lines
#define vv first
#define ww second
using edge = tuple<int, int, int>;
struct disjoint_set{
    int n:
    int *par, *height;
    disjoint_set(int nn){
        n = nn:
        par = new int[n];
        memset(par, -1, sizeof(par));
        height = new int[n];
        memset (height, 1, sizeof (height));
    int parent(int i){
        return par[i] == -1 ? i : (par[i] = parent(par[i]));
    void unionize(int a, int b) {
        a = parent(a);
        b = parent(b);
        if(a==b) return;
        if(height[a] == height[b])
            height[a]++;
        if(height[a] >= height[b])
            par[b] = a;
        else par[a] = b;
};
vector<edge> kruskalMST(vector<edge> edges, int n) {
    sort(edges.begin(), edges.end(), [&](edge & a, edge & b) ->
          bool { return get<2>(a) < get<2>(b); });
```

```
disjoint set ds(n);
    int tot = 0;
    vector<edge> out;
    for(edge e : edges){
        if (ds.parent (get<0>(e)) != ds.parent (get<1>(e))) {
            tot += qet<2>(e);
            out.push_back(e);
            ds.unionize(get<0>(e), get<1>(e));
    return out;
Dinic.cpp
Description: Compute maximum flow in a graph. The basic principle is
that a Maximum flow = minimum cut and Breadth First Search is used as a
sub-routine.
Memory: \mathcal{O}(E+V)
Time: \mathcal{O}\left(EV^2\right)
                                                      5ee184, 47 lines
#define 11 long long
struct Dinic {
  struct Edge {
    int to, rev;
    11 flow() { return max(oc - c, OLL); } // if you need flows
        Edge(int tt, int rr, ll cc, ll oo){
            to = tt; rev = rr; c = cc; oc = oo;
  vector<int> lvl, ptr, q;
  vector<vector<Edge>> adi;
  Dinic(int n) : lvl(n), ptr(n), q(n), adj(n) {}
  void add(int a, int b, 11 c, 11 rcap = 0) {
    adj[a].push_back(Edge((ll)b, adj[b].size(), c, c));
    adj[b].push_back({a, (int)adj[a].size() - 1, rcap, rcap});
 11 dfs(int v, int t, 11 f) {
    if (v == t || !f) return f;
    for (int& i = ptr[v]; i < adj[v].size(); i++) {</pre>
      Edge& e = adj[v][i];
      if (lvl[e.to] == lvl[v] + 1)
        if (ll p = dfs(e.to, t, min(f, e.c))) {
          e.c -= p, adj[e.to][e.rev].c += p;
          return p;
    return 0:
 11 calc(int s, int t) {
    11 flow = 0; q[0] = s;
    for (int L = 0; L < 31; L++) do { // 'int L=30' maybe faster
          for random data
      lvl = ptr = vector<int>(q.size());
      int qi = 0, qe = lvl[s] = 1;
      while (qi < qe && !lvl[t]) {</pre>
        int v = q[qi++];
        for (Edge e : adj[v])
          if (!lvl[e.to] && e.c >> (30 - L))
            q[qe++] = e.to, lvl[e.to] = lvl[v] + 1;
      while (ll p = dfs(s, t, LLONG_MAX)) flow += p;
    } while (lvl[t]);
    return flow;
  bool leftOfMinCut(int a) { return lvl[a] != 0; }
```

```
};
topSort.cpp
<br/>
<br/>
dits/stdc++.h>
                                                       36bfac, 32 lines
using namespace std;
#define vv first
#define ww second
using edge = pair<int, int>;
void topSortUtil(vector<edge> q[], int v, stack<int> s, bool
    seen[v] = true;
    for(edge e : g[v])
        if(!seen[e.vv])
            topSortUtil(q, e.vv, s, seen);
    s.push(v);
vector<int> topSort(vector<edge> q[], int v) {
    stack<int> out;
   bool seen[v];
    for(int i = 0; i < v; i++)
        if(!seen[i])
            topSortUtil(q, i, out, seen);
    vector<int> ts(v);
    for(int i = v-1; i >= 0; i--) {
        ts[i] = out.top();
        out.pop();
    return ts:
SCCTarjan.h
Description: Finds strongly connected components of a directed graph.
Visits/indexes SCCs in reverse topological order.
Usage: scc(graph) returns an array that has the ID of each
node's SCC. scc(graph, [&](vector<int>& v) { ... }) calls
the lambda on each SCC, and returns the same array.
Time: \mathcal{O}(|V| + |E|)
namespace SCCTarjan {
 vector<int> val, comp, z, cont;
  int Time, ncomps;
  template <class G, class F>
  int dfs(int j, G& g, F& f) {
```

```
358d18, 37 lines
 int low = val[j] = ++Time, x;
 z.push_back(j);
 for (auto e : g[j])
   if (comp[e] < 0) low = min(low, val[e] ?: dfs(e, g, f));</pre>
 if (low == val[j]) {
   do {
     x = z.back();
     z.pop back();
     comp[x] = ncomps;
     cont.push_back(x);
   } while (x != j);
   f(cont);
   cont.clear();
   ncomps++;
  return val[j] = low;
template <class G, class F>
```

```
vector<int> scc(G& g, F f) {
    int n = q.size();
   val.assign(n, 0);
    comp.assign(n, -1);
    Time = ncomps = 0;
    for (int i = 0; i < n; i++)
     if (comp[i] < 0) dfs(i, g, f);</pre>
   return comp;
 template <class G> // convenience function w/o lambda
 vector<int> scc(G& g) {
    return scc(g, [](auto& v) {});
} // namespace SCCTarjan
SCCKosaraju.h
Description: Finds strongly connected components of a directed graph.
Visits/indexes SCCs in topological order.
Usage: scc(graph) returns an array that has the ID
of each node's SCC.
Time: \mathcal{O}\left(|V| + |E|\right)
                                                      9b78e7, 29 lines
namespace SCCKosaraju {
 vector<vector<int>> adj, radj;
 vector<int> todo, comp;
 vector<bool> vis;
 void dfs1(int x) {
   vis[x] = 1;
   for (int y : adj[x])
     if (!vis[y]) dfs1(y);
   todo.push back(x);
 void dfs2(int x, int i) {
   comp[x] = i;
    for (int y : radj[x])
     if (comp[v] == -1) dfs2(v, i);
 vector<int> scc(vector<vector<int>>& _adj) {
   adi = adi;
    int time = 0, n = adj.size();
    comp.resize(n, -1), radj.resize(n), vis.resize(n);
    for (int x = 0; x < n; x++)
     for (int y : adj[x]) radj[y].push_back(x);
    for (int x = 0; x < n; x++)
     if (!vis[x]) dfs1(x);
```

dijkstra.h

Description: Computes shortest paths from s to any node reachable from s. Pass in an adjacency list of pairs (node, weight) and a starting node s. **Time:** $\mathcal{O}((|V| + |E|) \log |V|)$

reverse(todo.begin(), todo.end());

if (comp[x] == -1) dfs2(x, time++);

for (int x : todo)

}; // namespace SCCKosaraju

return comp;

```
pq.push(ii(dist[v] = d + w, v));
}
return dist;
```

Mathematics (5)

Fraction.h

Description: Struct for representing fractions/rationals. All ops are $O(\log N)$ due to GCD in constructor. Uses cross multiplication alde34, 27 lines

```
template <typename T>
struct 0 {
 Ta, b;
 Q(T p, T q = 1) {
   T g = gcd(p, q);
    a = p / q;
   b = q / q;
    if (b < 0) a = -a, b = -b;
  T gcd(T x, T y) const { return __gcd(x, y); }
  O operator+(const O& O) const {
    return {a * o.b + o.a * b, b * o.b};
 O operator-(const O& O) const {
    return *this + Q(-o.a, o.b);
 Q operator*(const Q& o) const { return {a * o.a, b * o.b}; }
 Q operator/(const Q& o) const { return *this * Q(o.b, o.a); }
  Q recip() const { return {b, a}; }
  int signum() const { return (a > 0) - (a < 0); }</pre>
 bool operator<(const Q& o) const {
    return a * o.b < o.a * b;
 friend ostream& operator<<(ostream& cout, const Q& o) {</pre>
    return cout << o.a << "/" << o.b;</pre>
};
```

FractionOverflow.h

Description: Safer struct for representing fractions/rationals. Comparison is 100% overflow safe; other ops are safer but can still overflow. All ops are $O(\log N)$.

```
template <typename T>
struct 00 {
 T a, b;
 QO(T p, T q = 1) {
   T g = gcd(p, q);
   a = p / q;
   b = q / q;
   if (b < 0) a = -a, b = -b;
 T gcd(T x, T y) const { return __gcd(x, y); }
 QO operator+(const QO& o) const {
   T = gcd(b, o.b), bb = b / q, obb = o.b / q;
    return {a * obb + o.a * bb, b * obb};
 QO operator-(const QO& o) const {
    return *this + QO(-o.a, o.b);
 QO operator* (const QO& o) const {
   T g1 = gcd(a, o.b), g2 = gcd(o.a, b);
   return { (a / g1) * (o.a / g2), (b / g2) * (o.b / g1) };
 QO operator/(const QO& o) const {
    return *this * QO(o.b, o.a);
```

```
QO recip() const { return {b, a}; }
  int signum() const { return (a > 0) - (a < 0); }
  static bool lessThan(T a, T b, T x, T y) {
   if (a / b != x / y) return a / b < x / y;</pre>
   if (x % y == 0) return false;
   if (a % b == 0) return true;
   return lessThan(y, x % y, b, a % b);
  bool operator<(const QO& o) const {
   if (this->signum() != o.signum() || a == 0) return a < o.a;
   if (a < 0)
     return lessThan(abs(o.a), o.b, abs(a), b);
   else
     return lessThan(a, b, o.a, o.b);
  friend ostream& operator<<(ostream& cout, const QO& o) {</pre>
    return cout << o.a << "/" << o.b;
};
```

PrimeSieve.h

Description: Prime sieve for generating all primes up to a certain limit. isprime [i] is true iff i is a prime.

Time: $\lim_{n\to\infty} 100'000'000 \approx 0.8$ s. Runs 30% faster if only odd indices are stored.

dc4f55, 14 lines

```
const int MAX_PR = 5'000'000;
bitset<MAX_PR> isprime;
vector<int> primeSieve(int lim) {
   isprime.set();
   isprime[0] = isprime[1] = 0;
   for (int i = 4; i < lim; i += 2) isprime[i] = 0;
   for (int i = 3; i * i < lim; i += 2)
        if (isprime[i])
        for (int j = i * i; j < lim; j += i * 2) isprime[j] = 0;
vector<int> pr;
for (int i = 2; i < lim; i++)
        if (isprime[i]) pr.push_back(i);
   return pr;
}</pre>
```

PrimeSieveFast.h

Description: Prime sieve for generating all primes smaller than LIM.

```
Time: LIM=1e9 \approx 1.5s a1933d, 23 lines
```

```
const int LIM = 1e8;
bitset<LIM> isPrime;
vector<int> primeSieve() {
  const int S = round(sqrt(LIM)), R = LIM / 2;
  vector < int > pr = {2}, sieve(S + 1);
  pr.reserve(int(LIM / log(LIM) * 1.1));
  vector<pair<int, int>> cp;
  for (int i = 3; i \le S; i += 2)
    if (!sieve[i]) {
      cp.push_back(\{i, i * i / 2\});
      for (int j = i * i; j <= S; j += 2 * i) sieve[j] = 1;</pre>
  for (int L = 1; L \leftarrow R; L \leftarrow S) {
    array<bool, S> block{};
    for (auto& [p, idx] : cp)
      for (int i = idx; i < S + L; idx = (i += p))</pre>
        block[i - L] = 1;
    for (int i = 0; i < min(S, R - L); i++)</pre>
      if (!block[i]) pr.push_back((L + i) * 2 + 1);
  for (int i : pr) isPrime[i] = 1;
  return pr;
```

Miscellaneous (6)

```
NDimensional Vector.h
                                                      3c0f61, 12 lines
template <int D, typename T>
struct Vec : public vector<Vec<D - 1, T>> {
  static_assert(D >= 1,
                 "Vector dimension must be greater than zero!");
  template <typename... Args>
  Vec(int n = 0, Args... args):
    vector < Vec < D - 1, T >> (n, Vec < D - 1, T > (args...)) {}
template <typename T>
struct Vec<1, T> : public vector<T> {
 Vec(int n = 0, const T& val = T()): vector<T>(n, val) {}
Submasks.h
                                                       35424b, 3 lines
for (int mask = 0; mask < (1 << n); mask++)
 for (int sub = mask; sub; sub = (sub - 1) & mask)
// do thing
```

Strings (7)

ZValues.h

151ee3, 10 lines

```
vector<int> zValues(string& s) {
  int n = ( int ) s.length();
  vector<int> z(n);
  for (int i = 1, 1 = 0, r = 0; i < n; ++i) {
    if (i <= r) z[i] = min(r - i + 1, z[i - 1]);
    while (i + z[i] < n && s[z[i]] == s[i + z[i]]) ++z[i];
    if (i + z[i] - 1 > r) l = i, r = i + z[i] - 1;
  }
  return z;
}
```