

Programming Foundations

Python Basics, Software Principles, and Lift Control

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ENGF0034 - Design and Professional Skills



Lecture Overview

Objectives

To explore the foundations of computer programming, the nature of algorithms, core Python concepts, essential software engineering principles, and a complex real-world computational challenge.

- 1 Algorithms and Computation
- 2 Python Foundations
- 3 Strings in Depth
- 4 Structuring Code and Software Principles
- 5 Computational Challenge: Lift Control Systems



Algorithms and Computation

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What is an Algorithm?

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Key Properties (Donald Knuth)

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- **Definiteness:** Each step must be precisely and unambiguously specified.
- Effectiveness: Operations must be sufficiently basic that they can be carried out exactly and in finite time.



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Analysis of Algorithms

We analyse algorithms primarily for their **correctness** (does it solve the problem?) and their **efficiency** (how do resource requirements scale? - Complexity Analysis).



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since GCD(390253, 228769) = 13457.



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The Computational Challenge

How do we compute the GCD efficiently? The naive approach, prime factorisation, is computationally hard (intractable for large numbers, which is the basis of RSA cryptography).



Euclid's Insight (The Invariant)

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$$GCD(a, b) = GCD(a - b, b)$$
 (if $a > b$)



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Example: GCD(42, 30)

 $(42, 30) \rightarrow (12, 30) \rightarrow (12, 18) \rightarrow (12, 6) \rightarrow (6, 6)$. Result: 6.



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Termination

In each step, we replace a number with a smaller positive integer. The sum $\mathfrak{a}+\mathfrak{b}$ strictly decreases in every iteration. Since the sum is bounded below by 0, the algorithm must terminate.



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Correctness (Setup)

We must show the GCD remains invariant. Let g = GCD(a, b). By definition we have

$$a = \alpha g$$

$$b = \beta g$$

where $GCD(\alpha, \beta) = 1$ (they are coprime). Assuming $\alpha > b$, the next value α' is $\alpha' = \alpha - b = (\alpha - \beta)q$.



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- Assume GCD(a', b) = g' > g.
- **2** This implies that the coefficients $(\alpha \beta)$ and β must share a common factor c > 1:

$$GCD(\alpha - \beta, \beta) = c > 1$$

If c divides β AND c divides $(\alpha - \beta)$, then c must also divide their sum:

$$c \mid ((\alpha - \beta) + \beta) \implies c \mid \alpha$$



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- 4 Therefore, c > 1 is a common divisor of both α and β.
- **5 Contradiction!** This contradicts our premise that $GCD(\alpha, \beta) = 1$.



Conclusion

Therefore, GCD(a', b) = g. The algorithm preserves the GCD (an invariant) while reducing the magnitude of the numbers until they are equal to the GCD.



Python Foundations

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From Algorithm to Program: Basic Concepts

Let's translate the steps into Python, understanding the underlying concepts.

Components

- **Statements:** Complete units of execution that perform an action (e.g., a = 42).
- **Expressions:** Fragments of code that evaluate to a value (e.g., 42, a b).
- **Assignments:** Statements that bind a name (LHS) to the value of an expression (RHS).

```
# Initial assignments
a = 42
b = 30

# Example step: RHS evaluated first, then assigned to LHS
a = a - b # a is now 12
```



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Python Idioms: Simultaneous Assignment

a, b = 42, 30. All expressions on the RHS are evaluated before any assignment occurs. This allows elegant swapping: a, b = b, a.



Understanding Types (I)

In Python, every value is an object, and every object has a type. The type defines the data and the permitted operations.

Python's Type System: Dynamic Typing

Type checking is performed at **runtime**, just before an operation is executed.

Variables are just names (labels) pointing to objects. The variable itself does not have a fixed type.

```
a = 42  # a refers to an int
a = "Hello" # a now refers to a str. This is fine.
```



Understanding Types (II)

In Python, every value is an object, and every object has a type. The type defines the data and the permitted operations.

Python's Type System: Strong Typing

The type of an object matters. Operations are strictly checked for compatibility. Python refuses implicit conversions between incompatible types.

```
>>> "The answer is " + 42
TypeError: can only concatenate str (not "int") to str
```

You must explicitly convert: "The answer is " + str(42).



The Role of Type Systems

Contrast: Static Typing (e.g., C++, Java)

Type checking is performed at **compile time**.

- Pros: Catches errors early; better performance (types known ahead of time).
- Cons: More verbose (requires type annotations); sometimes less flexible.



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Types as Formal Methods

Type systems are the most popular lightweight formal methods that aid program correctness. They ensure only permissible operations are executed, eliminating a large class of trivial bugs. But they do not guarantee logical correctness.



Numeric Types: Integers (int)

Arbitrary Precision

A key feature of Python integers is that they have **arbitrary precision**.

■ Unlike fixed-width integers (e.g., 64-bit) in many languages, Python integers automatically expand, limited only by available memory.



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Note that / always returns a float, even if the operands are integers (e.g., 4 / 2 = 2.0).



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Computational Note: GCD Optimisation

The subtraction-based GCD can be slow if $a\gg b$. The standard implementation uses the modulo operator: GCD(a,b)=GCD(b,a mod b). This is much faster (logarithmic complexity).



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- **Iterative (Repetition):** Execute a block of code repeatedly (while, for).



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Indentation Defines Blocks

In Python, blocks of code are defined by their indentation level. This is crucial. Use 4 spaces consistently. Do not mix tabs and spaces.



Conditional Execution: The if Statement

```
Syntax
```

```
if condition:
    # Block 1 (executed if condition is True)
elif another_condition:
    # Block 2
else:
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■ Comparison Operators: ==, !=, <, >, etc.



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- Logical Operators: and, or, not.



Syntax

Repeatedly executes a block of statements as long as a condition remains True.

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while condition:
    # Loop body
    statement_1
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Execution Flow

■ Evaluate the condition.



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Danger: Infinite Loops

You must ensure that the state changes within the loop such that the condition eventually becomes False. (Euclid's algorithm is proven to terminate).



Automating Euclid's Algorithm

Combine while and if to fully automate algorithm

```
# GCD computation for 42 and 30
  a, b = 42, 30
  # Repeat until the numbers are equal
  while a != b:
      # Check which number is larger
      if a > b:
6
          # Subtract smaller from larger (update a)
          a = a - b
8
     else:
9
          # Subtract smaller from larger (update b)
          b = b - a
  # Now a == b, so the GCD is in a (or b).
  print(a)
```



Strings in Depth

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Strings (str)

Definition

A string in Python 3 is an immutable sequence of Unicode code points.

Unicode Representation

Python 3 uses Unicode (UTF-8 encoding by default for source files) to represent text, supporting characters from all languages and symbols.

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>>> s = "Hello"
>>> len(s)
5  # Length is the number of Unicode characters
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String Literals

Created using single ('), double ("), or triple quotes ("""). Triple quotes allow multi-line strings.



Indexing and Slicing (I)

As sequences, strings support indexing and slicing.

Indexing (Zero-Based)

Access individual characters. Negative indices count from the end.

```
s = "Python"

# P y t h o n

# 0 1 2 3 4 5

# -6-5-4-3-2-1

>>> s[0]

'P'

>>> s[-1]

'n'
```

Indexing and Slicing (II)

Slicing

Extracting a substring: s[start:stop:step].

- start is inclusive; stop is exclusive.
- Defaults: start=0, stop=len(s), step=1.

```
>>> s[0:2]
'Py'
>>> s[2:] # From index 2 to the end
'thon'
>>> s[::-1] # Reverse the string (step of -1)
'nohtyP'
```



String Immutability

Key Concept: Immutability

Strings in Python are immutable. Once created, they cannot be changed in place.

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TypeError: 'str' object does not support item assignment
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Modifying Strings

To "modify" a string, you must create a new string based on the old one.

```
s = "J" + s[1:] # Creates a new string 'Jython'
```



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Computational Implication

Immutability makes strings safe (e.g., as dictionary keys). However, repeatedly concatenating long strings in a loop (s += "...") is inefficient (O(N²)) as it creates many intermediate objects. Use .join() for efficient concatenation (O(N)).



String Formatting (f-Strings)

Formatted String Literals (f-Strings)

Introduced in Python 3.6, f-strings provide a concise and readable way to embed expressions inside string literals. Prefix the string with f.

```
name = "Alice"
age = 30
# Expressions inside {} are evaluated at runtime
message = f"My name is {name} and I am {age} years old."
>>> print(message)
My name is Alice and I am 30 years old.
```



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Advanced Formatting

f-strings support powerful formatting options (e.g., precision, padding).

```
import math
>>> print(f"Pi is approximately {math.pi:.3f}")
Pi is approximately 3.142
```



Structuring Code and Software Principles

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Guiding Principles

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- DRY (Don't Repeat Yourself) Principle (Hunt & Thomas): "Every piece of knowledge must have a single, unambiguous, authoritative representation within a system."



Euclid as a Function

Refactoring

Encapsulating the logic within a function.

```
def GCD(a, b):
    """Compute the GCD of two positive integers."""
    # The parameters a and b are local to this function
    while a != b:
        if a > b:
            a = a - b
        else:
            b = b - a
    # Return the result
    return a
```



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Calling the Function

```
result1 = GCD(42, 30)
print(result1) # Output: 6

result2 = GCD(100, 15)
print(result2) # Output: 5
```



Variable Scope (LEGB Rule)

What is Scope?

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Best Practice

Minimise the use of global variables. Functions should ideally communicate only through parameters and return values.



Ensuring Correctness: Testing (I)

The Role of Testing

Testing verifies that the code behaves as expected. While tests cannot prove the absence of bugs (this is generally undecidable), they increase confidence in correctness.



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The assert Statement

A simple way to write tests. If the condition is False, it raises an AssertionError.

```
assert condition, "Optional error message"
```



Ensuring Correctness: Testing (II)

Testing Euclid

```
def test_euclid():
    """Unit tests for the GCD function."""
    assert GCD(42, 30) == 6
    assert GCD(30, 42) == 6 # Test commutativity
    assert GCD(17, 5) == 1 # Boundary condition (coprime)
    assert GCD(1, 1) == 1 # Boundary condition

test_euclid()
```



What Makes a Good Test?

Advice from Kernighan and Pike (The Practice of Programming)

- Coverage: Ensure all lines and code paths (e.g., both branches of an if) are exercised.
- Boundary Conditions: Test edge cases (e.g., smallest/largest values, empty inputs).
- Pre- and Post-conditions: Verify assumptions about inputs and guarantees about outputs.
- Error Paths: Test how the code handles invalid inputs or exceptional circumstances.



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Refactoring and Version Control

Comprehensive tests enable fearless **refactoring**—restructuring code without changing its external behaviour. **Version Control** (e.g., Git) allows tracking changes and reverting if refactoring introduces bugs.



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- Clarity: Error handling logic should not obscure the primary logic (the "happy path").

Exceptions in Python

Python uses exceptions (raise, try, except) rather than error return codes to handle runtime errors.



Raising Exceptions (Enforcing Preconditions)

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The raise Keyword

Interrupts the normal flow and signals an exception immediately.

```
def GCD(a, b):
    """Compute the GCD of two positive integers."""
    if not (a > 0 and b > 0):
        # Raise an appropriate exception type (ValueError for invalid values)
        raise ValueError(f"Inputs {a}, {b} must be positive.")

# To be continued...
```



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          raise ValueError(f"Inputs {a}, {b} must be positive.")
      # Algorithm logic (repeated here for completeness)
6
      while a != b:
          if a > b:
               a = a - b
          else:
              b = b - a
      return a
```



Handling Exceptions: try/except/finally

We use try/except blocks to handle exceptions gracefully.

Syntax (Conceptual)

```
try:
    # Block of code that might raise an exception
    risky_operation()

except ExceptionType as e:
    # Block executed if ExceptionType occurs
    handle_the_error(e)

finally:
    # Block always executed (for cleanup, e.g., closing files)
    cleanup()
```



Handling Exceptions: try/except/finally

Strategy: Detect Low, Handle High

- Detect errors at a low level where the violation occurs (e.g., inside GCD).
- Handle (recover from) errors at a high level where the context is known (e.g., asking the user for new input).
- Only handle errors if you can meaningfully recover; otherwise, let the exception propagate up the call stack.



Computational Challenge: Lift Control Systems

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The Lift (Elevator) Problem

We now apply algorithmic thinking to a complex, real-world engineering challenge: designing a lift control system.

The Challenge

To efficiently transport passengers within a building, minimising waiting times and travel times, while respecting physical constraints (capacity, speed, acceleration).

- This is a highly complex stochastic optimisation problem.
- Inputs (passenger arrivals) are uncertain and dynamic.
- Involves multiple agents (lifts) acting concurrently.
- It is NP-hard in its general form.



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Energy Consumption Minimising unnecessary movement.

Trade-offs

Objectives often conflict. Minimising AWT might increase the AJT for passengers already on board. The control system must balance these trade-offs.



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Serve requests in the order they arrive.



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Shortest Seek Time First (SSTF)

Always move to the nearest outstanding request. (Analogy: Disk I/O scheduling).



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- Pros: Reduces immediate travel time.
- Cons: Leads to starvation. Requests far from the current activity may wait indefinitely. Does not account for direction of travel.



The Standard "Elevator Algorithm": SCAN

The basis for most traditional lift systems, balancing efficiency and fairness.

SCAN Algorithm

The lift travels continuously in one direction (Up or Down). It only reverses direction at the physical ends of the shaft.



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- Cons: Unnecessary travel to the absolute top/bottom floors.



LOOK Algorithm

The standard improvement over SCAN.

■ The car only travels as far as the **furthest outstanding request** in the current direction.



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C-LOOK (Circular LOOK)

- Serves requests only in *one* direction (e.g., always Up).
- When it reaches the furthest request, it quickly returns (express) to the lowest request.
- Provides more uniform waiting times across all floors compared to LOOK, as the middle floors aren't visited twice in a cycle.



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The Problem of Bunching

Lifts tend to cluster together over time, moving as a platoon. This is a major source of inefficiency.



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Consequence

Long gaps in service (high AWT) followed by the arrival of multiple lifts simultaneously.



Zoning (Static Allocation)

Divide the building into vertical zones. Each lift serves only its zone. Simple but inflexible to changing traffic patterns.



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The Core Problem (HCA)

When a new hall call is registered (e.g., Floor 5 Up), which lift should serve it?



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Optimisation Goal

Minimise a cost function (e.g., Estimated Time of Arrival (ETA), impact on existing passengers, energy use, etc.).



The Computational Complexity of HCA

Finding the optimal allocation is computationally hard.

The Optimisation Problem

Minimise the global cost function (e.g., total AWT + AJT) over a time horizon, considering all current and (predicted) future requests.



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Implications

- Finding the exact optimum is intractable in real-time.
- Practical systems must rely on **heuristics** (e.g., Nearest Car, Minimum Cost Insertion) and approximations.



The Information Deficit and DDS

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Traditional systems (HCA) only know the passenger's starting floor and direction (Up/Down). They do not know the destination until the passenger is inside the car. This severely limits optimisation potential.



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A Paradigm Shift: Destination Dispatch Systems (DDS)

Modern systems change the input mechanism to gain crucial information earlier. Passengers enter their exact **destination floor** on a keypad in the lobby *before* entering the lift.





Knowing the destination upfront significantly improves optimisation potential.



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Key Benefits

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Computational Perspective

DDS reduces uncertainty. In HCA, the controller must guess the destination, leading to suboptimal commitments. DDS allows the optimiser to solve the (still NP-hard) problem more effectively using advanced techniques like Genetic Algorithms (GAs) or heuristic search (A*).



Modern Approaches: Machine Learning and RL

Applying modern computational techniques to the lift control problem.

Traffic Prediction

Using historical data and ML to predict future passenger arrival rates and Origin-Destination (OD) matrices.

■ Allows proactive positioning of lifts (e.g., moving lifts to lobby before the morning rush).



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Treating lift control as a sequential decision-making problem (Markov Decision Process).

- Agents: The lifts or a centralised controller.
- State: Positions of lifts, loads, pending calls.
- Actions: Move up, move down, stop.
- **Reward:** Minimised waiting/journey time.



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RL agents can learn complex policies that adapt to dynamic traffic patterns and potentially outperform traditional heuristics.



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Programming Foundations

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- Robustness: Testing (assert) and Error Handling (Exceptions).



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- Information is key: DDS outperforms traditional systems (SCAN/LOOK) by reducing uncertainty.



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Computational Challenges (Lift Control)

- A complex stochastic optimisation problem (NP-hard).
- Balancing conflicting metrics (AWT vs. AJT).
- Information is key: DDS outperforms traditional systems (SCAN/LOOK) by reducing uncertainty.
- Modern techniques (ML/RL) offer potential for adaptive control.