CSE 116: Fall 2019

Introduction to Functional Programming

Intro to Haskell

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Based on course materials developed by Nadia Polikarpova

What is Haskell?

- A typed, lazy, purely functional programming language
 - Haskell = λ-calculus +
 - Better syntax
 - Types
 - Built-in features
 - Booleans, numbers, characters
 - Records (tuples)
 - Lists
 - Recursion

- ...

2

Why Haskell?

- Haskell programs tend to be simple and correct
- Quicksort in Haskell

```
sort [] = []
sort (x:xs) = sort ls ++ [x] ++ sort rs
where
    ls = [ l | l <- xs, l <= x ]
    rs = [ r | r <- xs, x < r ]</pre>
```

- Goals for this week
 - Understand the above code
 - Understand what typed, lazy, and purely functional means (and why you care)

Haskell vs λ-calculus: Programs

- A program is an expression (not a sequence of statements)
- It evaluates to a value (it does not perform actions)

```
- \(\lambda:\) (\x -> x) apple \(\tau--=-> apple\)
- Haskell:
\(\x -> x) "apple" \(\tau-=-> "apple"\)
```

4

Haskell vs λ-calculus: Functions

- Functions are first-class values:
 - can be *passed as arguments* to other functions
 - can be returned as results from other functions
 - can be partially applied (arguments passed one at a time)

```
(\x -> (\y -> x (x y))) (\z -> z + 1) 0 -- =\sim 2
```

• BUT: unlike λ -calculus, not everything is a function!

5

Haskell vs λ-calculus: top-level bindings

- Like in Elsa, we can name terms to use them later
- Elsa:

```
let T = \x y -> x
let F = \x y -> y

let PAIR = \x y -> \b -> ITE b x y
let FST = \p -> p T
let SND = \p -> p F

eval fst:
    FST (PAIR apple orange)
    =~> apple
```

Haskell vs λ-calculus: top-level bindings

- Like in Elsa, we can name terms to use them later
- Haskell:

```
haskellIsAwesome = True
pair = \x y -> \b -> if b then x else y
fst = \p -> p haskellIsAwesome
snd = \p -> p False
-- In GHCi:
> fst (pair "apple" "orange") -- "apple"
```

- The names are called top-level variables
- Their definitions are called top-level bindings

Syntax: Equations and Patterns

• You can define function bindings using equations:

```
pair x y b = if b then x else y -- pair = \langle x \ y \ b \ - \rangle \dots
fst p = p True -- fst = \langle p \ - \rangle \dots
snd p = p False -- snd = \langle p \ - \rangle \dots
```

8

Syntax: Equations and Patterns

• A single function binding can have *multiple* equations with different **patterns** of parameters:

- The first equation whose pattern matches the actual arguments is chosen
- For now, a pattern is:
 - a variable (matches any value)
 - or a value (matches only that value)

Syntax: Equations and Patterns

• A single function binding can have multiple equations with different patterns of parameters:

```
pair x y True = x -- If 3rd arg matches True,
                     -- use this equation;
  pair x y False = y -- Otherwise, if 3rd arg matches
                     -- False, use this equation.
• Same as:
  pair x y True = x -- If 3rd arg matches True,
                     -- use this equation;
              = y -- Otherwise use this equation.
  pair x y b
```

Syntax: Equations and Patterns

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```
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                     -- False, use this equation.
• Same as:
  pair x y True = x -- If 3rd arg matches True,
                     -- use this equation;
              = y -- Otherwise use this equation.
  pair x y _
```

QUIZ: Pair

Which of the following definitions of pair is incorrect? *

```
A. pair x y = b \rightarrow f b then x else y
B. pair x = y b \rightarrow if b then x else y
pair x _ True = x
pair _ y _ = y
pair x y b = x
pair x y False = y
E. all of the above
```



http://tiny.cc/cse116-pair-ind

12

QUIZ: Pair

Which of the following definitions of pair is incorrect? *

```
A. pair x y = \b -> if b then x else y

B. pair x = \y b -> if b then x else y

C.

pair x _ True = x
pair _ y _ = y

D.

pair x y b = x
pair x y False = y

E. all of the above
```

http://tiny.cc/cse116-pair-grp

13

Equations with guards

• An equation can have multiple guards (Boolean expressions):

• Same as:

```
cmpSquare x y | x > y*y = "bigger :)"
| x == y*y = "same :|"
| otherwise = "smaller :("
```

14

Recursion

• Recursion is built-in, so you can write:

• Or you can write:

```
sum 0 = 0
sum n = n + sum (n - 1)
```

Scope of variables

• Top-level variables have global scope

• Answer: f is isEven, g is isOdd

Scope of variables

• Is this allowed?

```
haskellIsAwesome = True
haskellIsAwesome = False -- changed my mind
```

 Answer: no, a variable can be defined once per scope; no mutation!

17

16

Local variables

 You can introduce a new (local) scope using a letexpression

• Syntactic sugar for nested 1et-expressions:

Local variables

• If you need a variable whose scope is an equation, use the where clause instead:

```
cmpSquare x y \mid x > z = "bigger :)" \mid x == z = "same :|" \mid x < z = "smaller :(" where z = y*y
```

19

Types

• What would Elsa say?

```
let FNORD = ONE ZERO
```

- **Answer**: Nothing. When evaluated, it will crunch to *something*, but it will be nonsensical.
 - λ -calculus is **untyped**.

20

Types

• What would Python say?

```
def fnord():
   return ∅(1)
```

- Answer: Nothing. When evaluated will cause a runtime error.
 - Python is dynamically typed

Types

• What would Java say?

```
void fnord() {
  int zero;
  zero(1);
}
```

- Answer: Java compiler will reject this.
 - Java is statically typed.

22

Types

- In Haskell every expression either has a type or is illtyped and rejected statically (at compile-time, before execution starts)
 - like in Java
 - unlike λ -calculus or Python

```
fnord = 1 0 -- rejected by GHC
```

23

Type Annotations

• You can annotate your bindings with their types using ::, like so:

Type Annotations

```
-- | This is a word-size integer
rating :: Int
rating = if haskellIsAwesome then 10 else 0
-- | This is an arbitrary precision integer
bigNumber :: Integer
bigNumber = factorial 100
```

- If you omit annotations, GHC will infer them for you
 - Inspect types in GHCi using :t
 - You should annotate all top-level bindings anyway! (Why?)

25

Function Types

• Functions have arrow types

```
- \x -> e has type A -> B
```

- If e has type B, assuming x has type A
- For example:

```
> :t (\x -> if x then 'a' else 'b')
(\x -> if x then 'a' else 'b') :: Bool -> Char
```

26

Function Types

• You should annotate your function bindings:

```
sum :: Int -> Int
sum 0 = 0
sum n = n + sum (n - 1)
```

• With multiple arguments:

```
pair :: String -> (String -> (Bool -> String))
pair x y b = if b then x else y
```

• Same as:

```
pair :: String -> String -> Bool -> String
pair x y b = if b then x else y
```

QUIZ: Type of Pair

```
With pair :: String -> String -> Bool -> String, what would GHCi say:

>:t pair "apple" "orange"

A. Syntax error

B. The term is ill-typed

C. String

D. Bool -> String

E. String -> String -> Bool -> String
```

http://tiny.cc/cse116-tpair-ind

28

QUIZ: Type of Pair

With pair :: String -> String -> Bool -> String, what would GHCi say
>:t pair "apple" "orange"

A. Syntax error

B. The term is ill-typed

C. String

D. Bool -> String

E. String -> String -> Bool -> String

http://tiny.cc/cse116-tpair-grp

29

Lists

- A list is
 - either an empty list

[] -- pronounced "nil"

- or a head element attached to a tail list

x:xs -- pronounced "x cons xs"

Terminology: constructors and values

31

Lists

- [] and (:) are called the list constructors
- We've seen constructors before:
 - True and False are Bool constructors
 - 0, 1, 2 are... well, it's complicated, but you can think of them as Int constructors
 - these constructions didn't take any parameters, so we just called them *values*
- In general, a **value** is a constructor applied to *other* values (e.g., *list values* on previous slide)

32

33

Type of a list

- A list has type [A] if each one of its elements has type A
- Examples:

Functions on lists: range

• There is also syntactic sugar for this!

```
[1..7] -- [1,2,3,4,5,6,7]
[1,3..7] -- [1,3,5,7]
```

34

Functions on lists: length

```
-- | Length of the list
length :: ???
length xs = ???
```

35

Pattern matching on lists

```
-- | Length of the List
length :: [Int] -> Int
length [] = 0
length (_:xs) = 1 + length xs
```

- A pattern is either a variable (incl. _) or a value
- A pattern is
 - either a *variable* (incl. _)
 - or a *constructor* applied to other *patterns*
- Pattern matching attempts to match values against patterns and, if desired, bind variables to successful matches.

QUIZ: Patterns

Which of the following is not a pattern? *

A. (1 : xs)

O B. (_:_:_)

O. [x]

O. [1+2, x, y]

E. all of the above



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37

QUIZ: Patterns (wrong url)

Which of the following is not a pattern? *

A. (1 : xs)

O B.(_:_:_)

O. [x]

O. [1+2, x, y]

E. all of the above



http://tiny.cc/cse116-pattern-grp

38

Some useful library functions

```
-- | Is the list empty?
null :: [t] -> Bool

-- | Head of the list
head :: [t] -> t -- careful: partial function!

-- | Tail of the list
tail :: [t] -> [t] -- careful: partial function!

-- | Length of the list
length :: [t] -> Int

-- | Append two lists
(++) :: [t] -> [t] -> [t]

-- | Are two lists equal?
(==) :: [t] -> [t] -> Bool
```

Pairs

```
myPair :: (String, Int) -- pair of String and Int
   myPair = ("apple", 3)
• (,) is the pair constructor
   -- Field access using library functions:
whichFruit = fst myPair -- "apple"
howMany = snd myPair -- 3
   -- Field access using pattern matching:
   isEmpty (x, y) = y == 0
                                                    You can use pattern
                                                     matching not only
   -- same as:
                                                     in equations, but
   isEmpty
                       = \setminus (x, y) \rightarrow y == 0
                                                     also in \lambda-bindings
                                                      and let-bindings!
   -- same as:
                       = let (x, y) = p in y == 0
   isEmpty p
                                                                        40
```

Pattern matching with pairs

 Is this pattern matching correct? What does this function do?

41

Pattern matching with pairs

 Is this pattern matching correct? What does this function do?

• Answer: a list of pairs represents key-value pairs in a dictionary; f performs lookup by key

Tuples

- Can we implement triples like in λ -calculus?
- Sure! But Haskell has native support for *n*-tuples:

```
myPair :: (String, Int)
myPair = ("apple", 3)

myTriple :: (Bool, Int, [Int])
myTriple = (True, 1, [1,2,3])

my4tuple :: (Float, Float, Float, Float)
my4tuple = (pi, sin pi, cos pi, sqrt 2)
...
-- And also:
myUnit :: ()
myUnit = ()
```

43

List comprehensions

• A convenient way to construct lists from other lists:

44

Quicksort in Haskell

```
sort [] = []
sort (x:xs) = sort ls ++ [x] ++ sort rs
where
    ls = [ l | l <- xs, l <= x ]
    rs = [ r | r <- xs, x > r ]
```

What is Haskell?

• A typed, lazy, purely functional programming language

46

Haskell is statically typed

- Every expression either has a type, or is *ill-typed* and rejected at compile time
- Why is this good?
 - catches errors early
 - types are contracts (you don't have to handle illtyped inputs!)
 - enables compiler optimizations

47

Haskell is purely functional

- Functional = functions are first-class values
- Pure = a program is an expression that evaluates to a value
 - No side effects! unlike in Python, Java, etc:

 in Haskell, a function of type Int -> Int computes a single integer output from a single integer input and does nothing else

Haskell is purely functional

- **Referential transparency:** The same expression always evaluates to the same value
 - More precisely: In a scope where x1, ..., xn are defined, all occurrences of e with
 FV(e) = {x1, ..., xn} have the same value
- Why is this good?
 - easier to reason about (remember x++ vs ++x in C?)
 - enables compiler optimizations
 - especially great for parallelization (e1 + e2: we can always compute e1 and e2 in parallel!)

49

Haskell is lazy

- An expression is evaluated only when its result is needed
- Example: take 2 [1 .. (factorial 100)]

```
take 2 ( upto 1 (factorial 100))

=> take 2 ( upto 1 933262154439...)

=> take 2 (1:(upto 2 933262154439...)) -- def upto

=> 1: (take 1 ( upto 2 933262154439...)) -- def take 3

=> 1: (take 1 (2:(upto 3 933262154439...)) -- def upto

=> 1:2:(take 0 ( upto 3 933262154439...)) -- def take 3

=> 1:2:[] -- def take 1
```

50

Haskell is lazy

- · Why is this good?
 - Can implement cool stuff like infinite lists: [1..]

```
-- first n pairs of co-primes:
take n [(i,j) | i <- [1..],
j <- [1..i],
gcd i j == 1]
```

- encourages simple, general solutions
- but has its problems too :(

