CSE 114A: Fall 2021 Foundations of Programming Languages

Type classes

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Roadmap

This week: adding types

Modern language features for structuring programs

- Type classes
- Monads

Overloading Operators: Arithmetic

The + operator works for a bunch of different types.

For Integer:

```
λ> 2 + 3
5
```

for **Double** precision floats:

```
λ> 2.9 + 3.5
6.4
```

Overloading Operators: Arithmetic

Similarly we can *compare* different types of values

```
\lambda > 2 == 3
False
\lambda > [2.9, 3.5] == [2.9, 3.5]
True
\lambda> ("cat", 10) < ("cat", 2)
False
\lambda> ("cat", 10) < ("cat", 20)
True
```

Ad-Hoc Overloading

Seems unremarkable?

Languages since the dawn of time have supported "operator overloading"

- To support this kind of ad-hoc polymorphism
- Ad-hoc: "created or done for a particular purpose as necessary."

You really **need** to *add* and *compare* values of *multiple* types!

No distinction between operators and functions

All are first class citizens!
 But then, what type do we give to functions like + and == ?

Individual: Plus type

Which of the following would be appropriate types for (+)?

```
(A) (+) :: Integer -> Integer -> Integer
```

(C)
$$(+)$$
 :: a -> a -> a

- (D) All of the above
- (E) None of the above



https://tiny.cc/cse116-plus-type-ind

Individual: Plus type

Which of the following would be appropriate types for (+)?

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Integer -> Integer -> Integer is bad because?

Then we cannot add Doubles!

Double -> Double -> Double is bad because?

Then we cannot add Integer!

```
a -> a -> a is bad because?
```

 That doesn't make sense, e.g. to add two Bool or two [Int] or two functions!

Type Classes for Ad Hoc Polymorphism

Haskell solves this problem with an *insanely* slick mechanism called typeclasses, introduced by Wadler and Blott

How to make ad-hoc polymorphism less ad hoc

Philip Wadler and Stephen Blott University of Glasgow*

October 1988

Qualified Types

To see the right type, lets ask:

```
λ> :type (+)
(+) :: (Num a) => a -> a -> a
```

We call the above a qualified type. Read it as +

- takes in two a values and returns an a value for any type a that
 - is a Num or
 - implements the Num interface or
 - is an instance of a Num.

The name Num can be thought of as a *predicate* or *constraint* over types

Some types are Nums

- Examples include Integer, Double etc
- Any such values of those types can be passed to +.

Other types are not Nums

Examples include Char, String, functions etc,

Values of those types cannot be passed to +.

λ> True + False

```
<interactive>:15:6:
    No instance for (Num Bool) arising from a
use of '+'
    In the expression: True + False
```

In an equation for 'it': it = True + False

A *typeclass* is a collection of operations (functions) that must exist for the underlying type.

The Eq Type Class

The simplest typeclass is perhaps, Eq

```
class Eq a where
  (==) :: a -> a -> Bool
  (/=) :: a -> a -> Bool
```

A type a is an instance of Eq if there are two functions

```
• == and /=
```

That determine if two a values are respectively equal or unequal.

The Show Type Class

The typeclass Show requires that instances be convertible to String (which can then be printed out)

```
class Show a where
  show :: a -> String
Indeed, we can test this on different (built-in) types
\lambda show 2
"2"
\lambda show 3.14
"3,14"
λ> show (1, "two", ([],[],[]))
"(1,\"two\",([],[],[]))"
```

When we type an expression into ghci, it computes the value and then calls show on the result. Thus, if we create a *new* type by

data Unshowable = A | B | C and then create values of the type,

```
λ> let x = A
λ> :type x
x :: Unshowable
```

but then we cannot view them

```
\lambda x
<interactive>:1:0:
    No instance for (Show Unshowable)
        arising from a use of `print' at <interactive>:1:0
        Possible fix: add an instance declaration for (Show Unshowable)
        In a stmt of a 'do' expression: print it
```

and we cannot compare them!

```
\lambda x == x
<interactive>:1:0:
    No instance for (Eq Unshowable)
        arising from a use of `==' at <interactive>:1:0-5
        Possible fix: add an instance declaration for (Eq
Unshowable)
        In the expression: x == x
        In the definition of `it': it = x == x
```

Again, the previously incomprehensible type error message should make sense to you.

Creating Instances

Tell Haskell how to show or compare values of type Unshowable

By creating instances of Eq and Show for that type:

instance Eq Unshowable where

EXERCISE Lets create an **instance** for Show Unshowable

Automatic Derivation

This is silly: we *should* be able to compare and view Unshowble "automatically"!

Haskell lets us *automatically derive* functions for some classes in the standard library.

To do so, we simply dress up the data type definition with

```
data Showable = A' | B' | C'
  deriving (Eq, Show) -- tells Haskell to automatically
generate instances
```

Automatic Derivation

```
data Showable = A' | B' | C'
  deriving (Eq, Show) -- tells Haskell to automatically
generate instances
Now we have
\lambda let x' = A'
\lambda> :type x'
x' :: Showable
\lambda > x
Α'
\lambda > x' == x'
True
\lambda > x' == B'
False
```

Standard Typeclass Hierarchy

Let us now peruse the definition of the Num typeclass.

```
λ> :info Num
class Num a where
    (+) :: a -> a -> a
    (*) :: a -> a -> a
    (-) :: a -> a -> a
    negate :: a -> a
    abs :: a -> a
    signum :: a -> a
    fromInteger :: Integer -> a
```

A type a is an instance of (i.e. implements) Num if there are functions for adding, multiplying, subtracting, negating etc values of that type.

The Ord Typeclass

Another typeclass you've used already is the one for Ordering values:

For example:

```
λ> 2 < 3
```

True

```
λ> "cat" < "dog"
True</pre>
```

A type a is an instance of (i.e. implements) Ord if

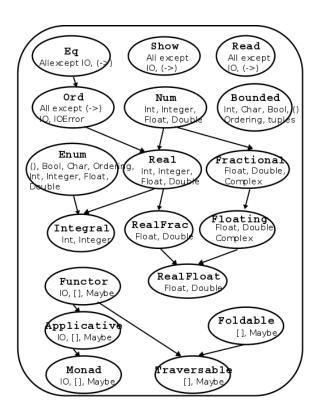
- 1. It has an instance of Eq
- there are functions for comparing the relative order of values of that type.

Standard Typeclass Hierarchy

In other words in addition to the "arithmetic" operations, we can compare two Num values and we can view them (as a String.)

Haskell comes equipped with a rich set of built-in classes.

In the picture, there is an edge from Eq to Ord because for something to be an Ord it must also be an Eq.



QUIZ

Recall the datatype:

data Showable = A' | B' | C' deriving (Eq, Show)

What is the result of:

- $\lambda > A' < B'$
- (A) True
- (B) False
- (C) Type error
- (D) Run-time exception



http://tiny.cc/cse116-ord-ind

QUIZ

Recall the datatype:

```
data Showable = A' | B' | C' deriving (Eq, Show)
```

What is the result of:

- $\lambda > A' < B'$
- (A) True
- (B) False
- (C) Type error
- (D) Run-time exception



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Using Typeclasses

Typeclasses integrate with the rest of Haskell's type system.

Lets build a small library for *Environments* mapping keys k to values v

An API for Env

Lets write a small API for Env

```
-- >>> Let env0 = add "cat" 10.0 (add "dog" 20.0 (Def 0))
-- >>> get "cat" env0
-- 10
-- >>> get "dog" env0
-- 20
-- >>> get "horse" env0
-- 0
```

An API for Env

Ok, lets implement!

```
-- | 'add key val env' returns a new env that additionally
maps `key` to `val`
add :: k -> v -> Env k v -> Env k v
add key val env = ???

-- | 'get key env' returns the value of `key` and the
"default" if no value is found
get :: k -> Env k v -> v
get key env = ???
```

An API for Env

Ok, lets implement! -- | 'add key val env' returns a new env that additionally maps `key` to `val` add :: $k \rightarrow v \rightarrow Env k v \rightarrow Env k v$ add key val env = Bind key val env -- | 'get key env' returns the value of `key` and the "default" if no value is found get :: k -> Env k v -> v get key (Def val) = val get key (Bind key' val env) | key == key' = val get key (Bind key' val env) | otherwise = get key env

Constraint Propagation

Lets delete the types of add and get and see what Haskell says their types are!

```
\lambda>:type get get: (Eq k) => k -> v -> Env k v -> Env k v Haskell tells us that we can use any k value as a key as long as the value is an instance of the Eq typeclass.
```

How, did GHC figure this out?

 If you look at the code for get you'll see that we check if two keys are equal!

Exercise

Write an optimized version of

- add that ensures the keys are in increasing order,
- get that gives up and returns the "default" the moment we see a key thats larger than the one we're looking for.

(How) do you need to change the type of Env?

(How) do you need to change the types of get and add?

Explicit Signatures

While Haskell is pretty good about inferring types in general, there are cases when the use of type classes requires explicit annotations (which change the behavior of the code.)

For example, Read is a built-in typeclass, where any instance a of Read has a function

```
read :: (Read a) => String -> a
which can parse a string and turn it into an a.
```

That is, Read is the opposite of Show.

QUIZ

What does the expression read "2" evaluate to?

- (A) compile time error
- (B) "2" :: String
- (C) 2 :: Integer
- (D) 2.0 :: Double
- (E) run-time exception



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QUIZ

What does the expression read "2" evaluate to?

- (A) compile time error
- (B) "2" :: String
- (C) 2 :: Integer
- (D) 2.0 :: Double
- (E) run-time exception



https://tiny.cc/cse116-read-grp

Explicit Signatures

Haskell is confused!

- Doesn't know what type to convert the string to!
- Doesn't know which of the read functions to run!

Did we want an Int or a Double or maybe something else altogether?

Thus, here an **explicit type annotation** is needed to tell Haskell what to convert the string to:

```
λ> (read "2") :: Int
2
λ> (read "2") :: Float
2.0
```

Note the different results due to the different types.

Creating Typeclasses

Typeclasses are useful for many different things.

We will see some of those over the next few lectures.

Lets conclude today's class with a quick example that provides a small taste.

JSON

JavaScript Object Notation or JSON is a simple format for transferring data around. Here is an example:

```
{ "name" : "Elliot Alderson"
, "age" : 28
, "likes" : ["coffee", "hacking"]
, "hates" : [ "e-corp" ]
, "lunches" : [ {"day" : "monday", "loc" : "cafe iveta"}
             , {"day" : "tuesday", "loc" : "cruzn gourmet"}
             , {"day" : "wednesday", "loc" : "perk"}
             , {"day" : "thursday", "loc" : "burger."}
             , {"day" : "friday", "loc" : "ray's truck"} ]
```

JSON

In brief, each JSON object is either

- a base value like a string, a number or a boolean,
- an (ordered) array of objects, or
- a set of string-object pairs.

A JSON Datatype

We can represent (a subset of) JSON values with the Haskell datatype

```
data JVal
    = JStr String
    | JNum Double
    | JBool Bool
    | JObj [(String, JVal)]
    | JArr [JVal]
    deriving (Eq, Ord, Show)
```

A JSON Datatype

Thus, the above JSON value would be represented by the JVal

```
JObj [("name", JStr "Elliot Alderson")
     ,("age", JNum 28)
     ,("likes", JArr [ JStr "coffee", JStr "hacking"])
     ,("hates", JArr [ JStr "e-corp" ])
     ,("lunches", JArr [ JObj [("day", JStr "monday")
                              ,("loc", JStr "cafe iveta")]
                       , JObj [("day", JStr "tuesday")
                              ,("loc", JStr "cruzn gourmet")]
                       , JObj [("day", JStr "wednesday")
                              ,("loc", JStr "perk")]
                       , JObj [("day", JStr "thursday")
                              ,("loc", JStr "burger.")]
                       , JObj [("day", JStr "friday")
                              ,("loc", JStr "ray's truck")]
                       ])
```

Serializing Haskell Values to JSON

Let's write a small library to serialize Haskell values as JSON.

We could write a bunch of functions like

```
doubleToJSON :: Double -> JVal
doubleToJSON = JNum

stringToJSON :: String -> JVal
stringToJSON = JStr

boolToJSON :: Bool -> JVal
boolToJSON = JBool
```

Serializing Collections

```
But what about collections, namely lists of things?
doublesToJSON :: [Double] -> JVal
doublesToJSON xs = JArr (map doubleToJSON xs)

boolsToJSON :: [Bool] -> JVal
boolsToJSON xs = JArr (map boolToJSON xs)

stringsToJSON :: [String] -> JVal
stringsToJSON xs = JArr (map stringToJSON xs)
```

This is getting rather tedious

We are rewriting the same code :(

Serializing Collections (with HOFs)

You could abstract by making the *individual-element-converter* a parameter

```
xsToJSON :: (a -> JVal) -> [a] -> JVal
xsToJSON f xs = JArr (map f xs)

xysToJSON :: (a -> JVal) -> [(String, a)] -> JVal
xysToJSON f kvs = JObj [ (k, f v) | (k, v) <- kvs ]</pre>
```

Serializing Collections (with HOFs)

But this is *still rather tedious** as you have to pass in the individual data converter (yuck)

```
λ> doubleToJSON 4
JNum 4.0

λ> xsToJSON stringToJSON ["coffee", "hacking"]
JArr [JStr "coffee", JStr "hacking"]

λ> xysToJSON stringToJSON [("day", "monday"), ("loc", "cafe iveta")]
JObj [("day", JStr "monday"), ("loc", JStr "cafe iveta")]
```

Serializing Collections (with HOFs)

This gets more hideous when you have richer objects like

because we have to go through gymnastics like

So much for *readability*

Is it too much to ask for a magical toJSON that *just works?*

Typeclasses To The Rescue

Lets define a typeclass that describes types a that can be converted to JSON.

```
class JSON a where
  toJSON :: a -> JVal
Now, just make all the above instances of JSON like so
instance JSON Double where
  toJSON = JNum
instance JSON Bool where
  toJSON = JBool
instance JSON String where
  toJSON = JStr
```

Typeclasses To The Rescue

```
This lets us uniformly write
```

```
λ> toJSON 4
JNum 4.0

λ> toJSON True
JBool True

λ> toJSON "hacking"
JStr "hacking"
```

The real fun begins when we get Haskell to automatically bootstrap the above functions to work for lists and key-value lists!

```
instance JSON a => JSON [a] where
toJSON xs = JArr [toJSON x | x <- xs]</pre>
```

The above says, if a is an instance of JSON, that is, if you can convert a to JVal then here's a generic recipe to convert lists of a values!

```
\lambda toJSON [True, False, True]

JArr [JBool True, JBool False, JBool True]

\lambda toJSON ["cat", "dog", "Mouse"]

JArr [JStr "cat", JStr "dog", JStr "Mouse"]

or even lists-of-lists!

\lambda toJSON [["cat", "dog"], ["mouse", "rabbit"]]

JArr [JArr [JStr "cat", JStr "dog"], JArr [JStr "mouse", JStr "rabbit"]]
```

It is also useful to bootstrap the serialization for tuples (up to some fixed size) so we can easily write "non-uniform" JSON objects where keys are bound to values with different shapes.

```
instance (JSON a, JSON b) => JSON ((String, a), (String, b)) where
  toJSON ((k1, v1), (k2, v2)) =
    JObj [(k1, toJSON v1), (k2, toJSON v2)]

instance (JSON a, JSON b, JSON c) => JSON ((String, a), (String, b),
(String, c)) where
  toJSON ((k1, v1), (k2, v2), (k3, v3)) =
    JObj [(k1, toJSON v1), (k2, toJSON v2), (k3, toJSON v3)]
```

• • •

Now, we can simply write

```
hs = (("name" , "Elliot Alderson")
   ,("age" , 28)
   ,("likes" , ["coffee", "hacking"])
   ,("hates" , ["e-corp"])
   ,("lunches", lunches)
)
```

which is a Haskell value that describes our running JSON example, and can convert it directly like so

```
js2 = toJSON hs
```

Serializing Environments

To wrap everything up, lets write a routine to serialize our Env instance JSON (Env k v) where toJSON env = ???and presto! our serializer just works $\lambda > env0$ Bind "cat" 10.0 (Bind "dog" 20.0 (Def 0)) λ> toJSON env0 JObj [("cat", JNum 10.0) , ("dog", JNum 20.0) , ("def", JNum 0.0)