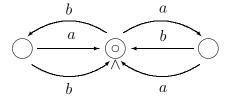
Math 166A Exam Spring Quarter June 1991 Buss

(1) Convert the following DFA into a regular expression.



- (2) Convert the following NFA into an equivalent DFA
- (3) Show that $\{a^ib^jc^k: i+j=k, i, j, k \geq 0\}$ is a CFL.
- (4) Convert this NFA to DFA.
- (5) Prove or disprove: $\{a^ib^j: i \leq j \text{ or } i \text{ is a perfect square}\}$ is not regular.
- (6) Give a CFG G_1 such that $L(G_1) = (a \cup b)^*(b \cup c)^*$.
- (7) Prove that if L_1 is a regular language then $L_2 = \{w : w^R \in L_1\}$ is regular. [Hint: Two approaches are possible: (1) induction on regular expressions or (2) convert on FA for L_1 into an DFA for L_2 .]