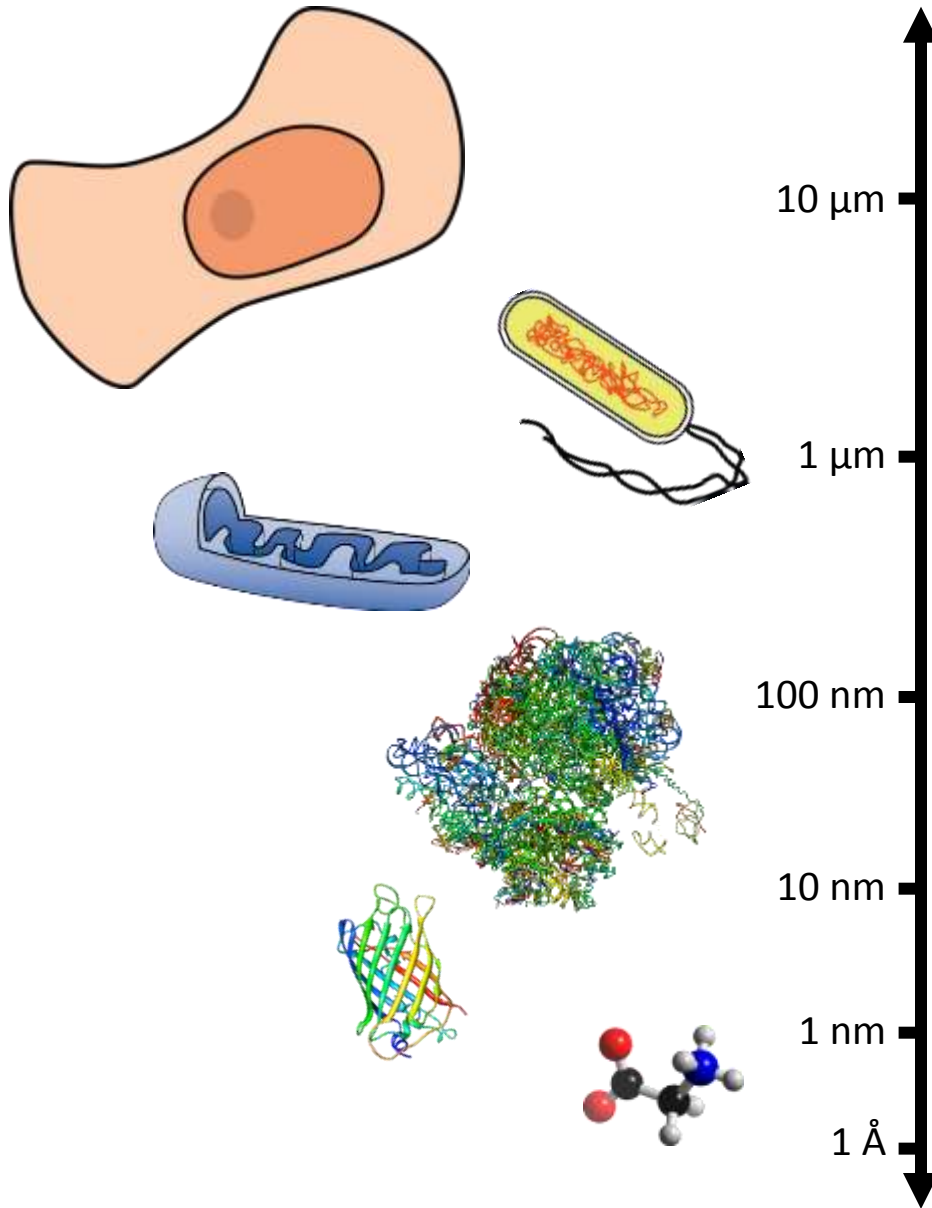


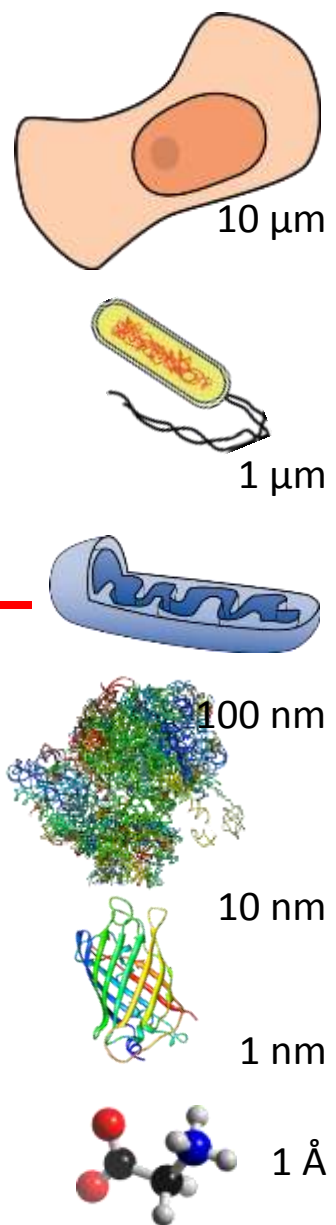
Super-Resolution Microscopy Structured Illumination



Bo Huang

Looking into microscopic world of life...

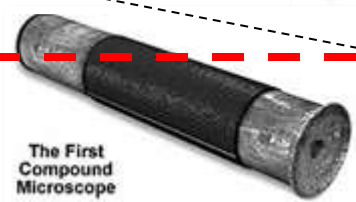




Naked eye: $\sim 50\text{-}100\ \mu\text{m}$

★ 1595, Zaccharias and Hans Janssen
First microscope, 9x magnification

★ Antonie van Leeuwenhoek
(1632-1723), 200x



Compound microscope
 $>1000\times$

★ Ernst Abbe (1840-1905)
The "physical" diffraction limit

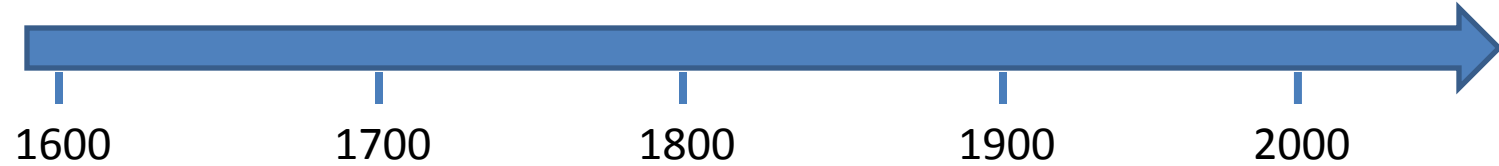


PLATE XXIV

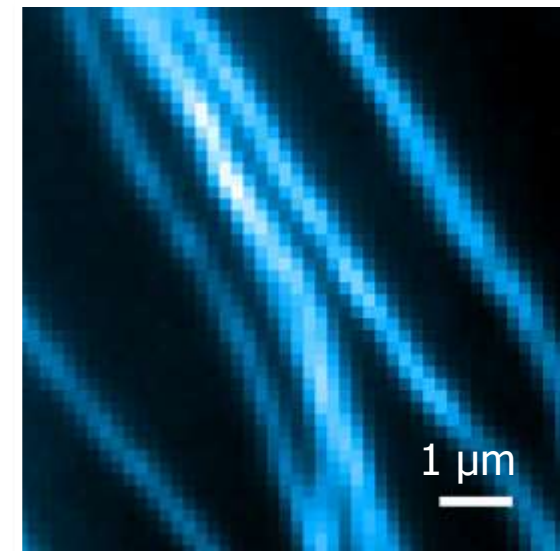
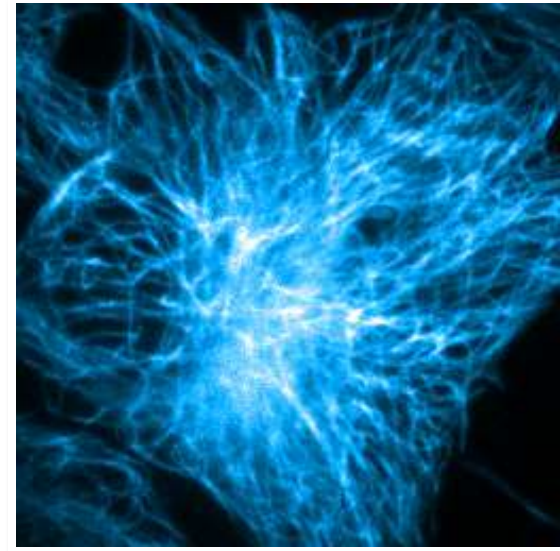
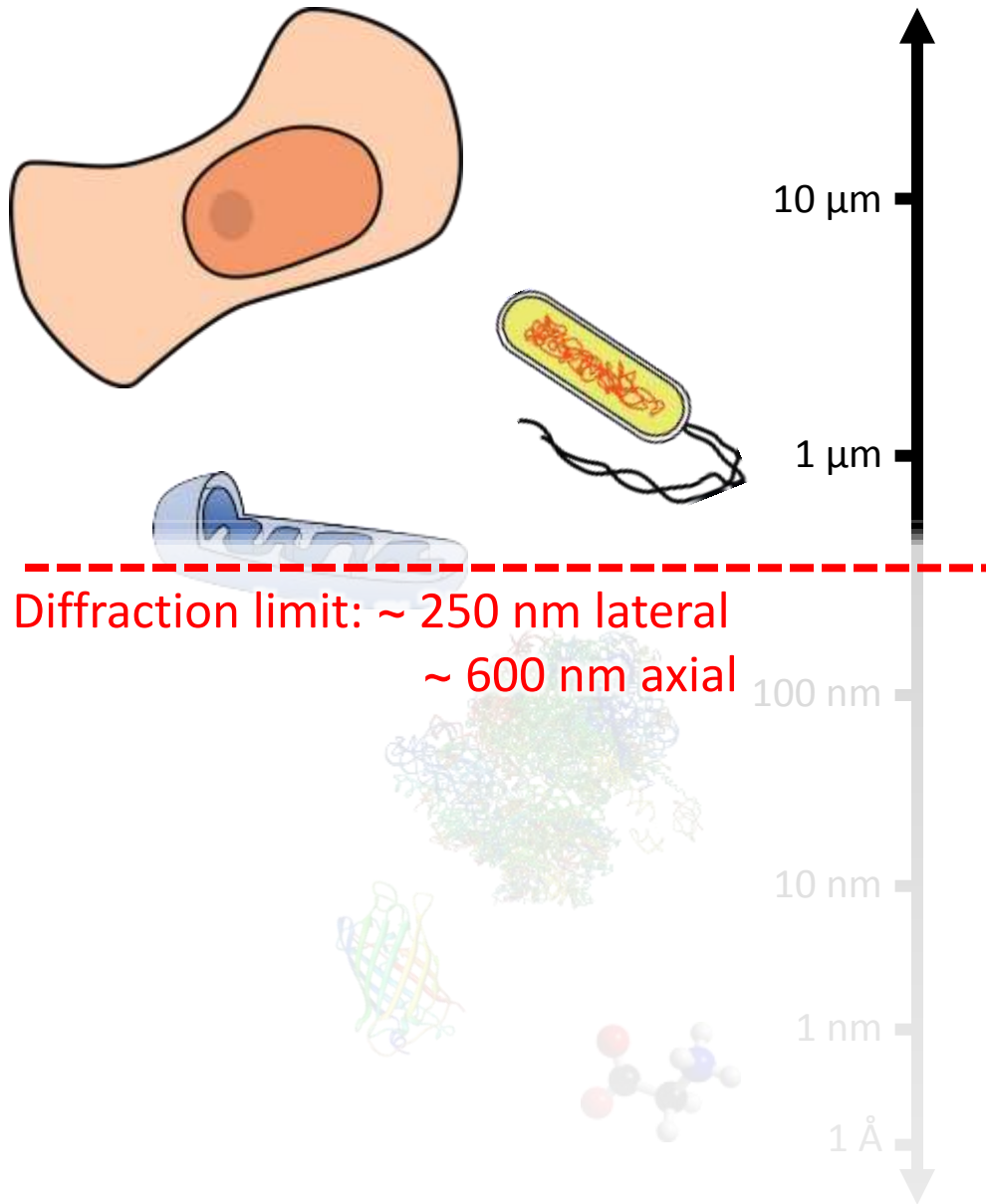
fig: A

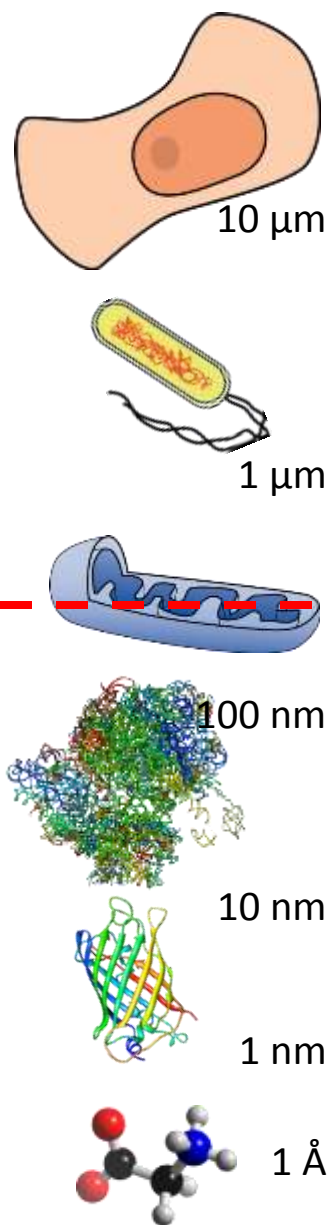
fig: B

fig: r



The diffraction barrier

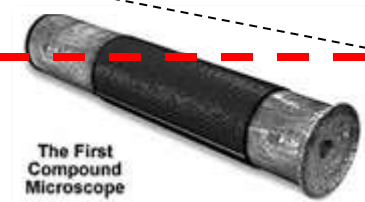
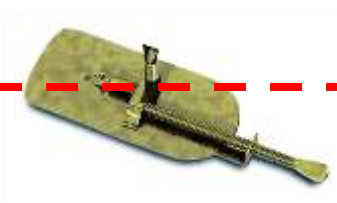




Naked eye: ~ 50-100 μm

★ 1595, Zaccharias and Hans Janssen
First microscope, 9x magnification

★ Antony Van Leeuwenhoek
(1632-1723), 200x

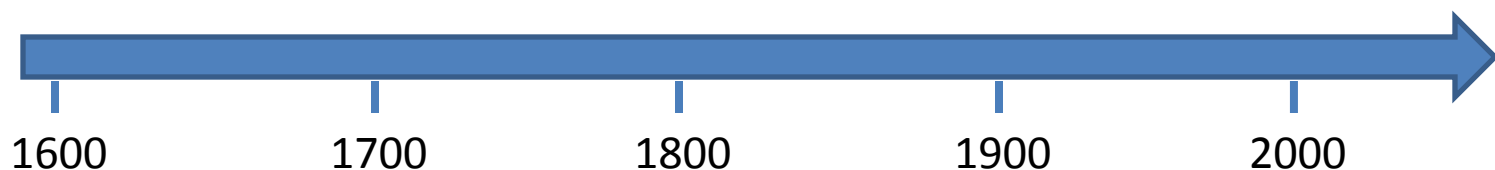
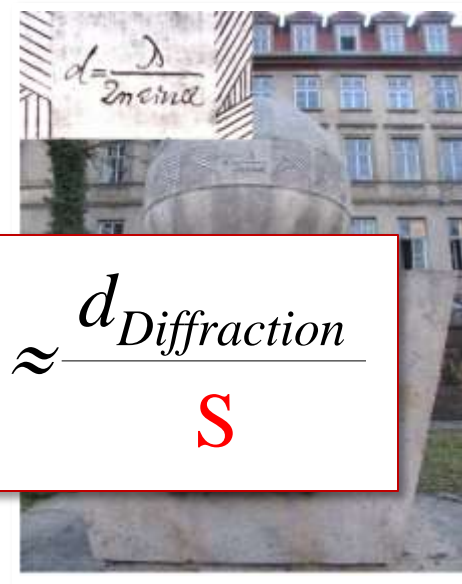


Compound microscope
>1000x

Ernst Abbe (1840-1905)
The "physical" diffraction limit

Super-resolution
Deconvolution
Optical Microscopy
4-Pi microscopy
...

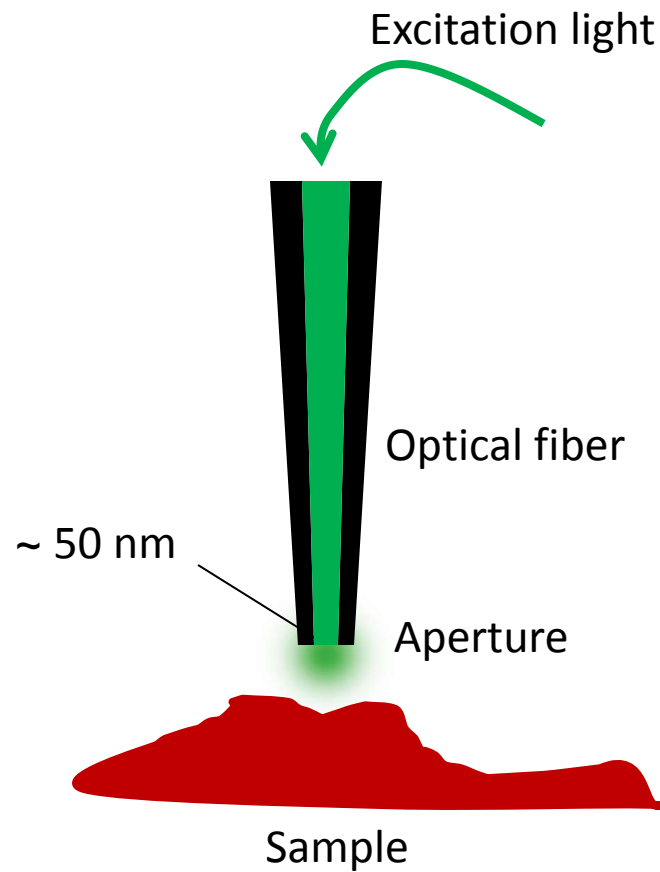
$$D \approx \frac{d_{\text{Diffraction}}}{S}$$



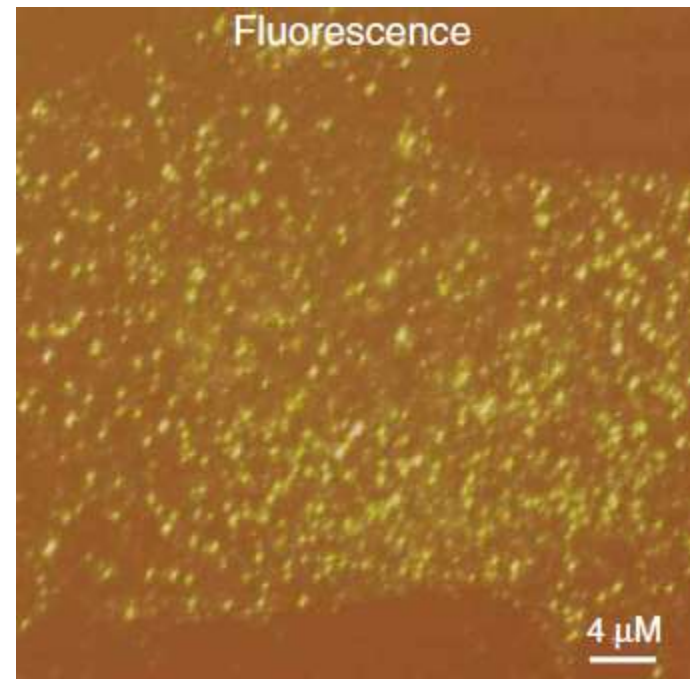
50 years to extend the resolution

- Confocal microscopy (1957)
- Near-field scanning optical microscopy (1972/1984)
- Multiphoton microscopy (1990)
- 4-Pi microscopy / I⁵M (1991-1995)
- Structured illumination microscopy (2000)
- Negative refractive index (2006)

Near-field scanning optical microscopy



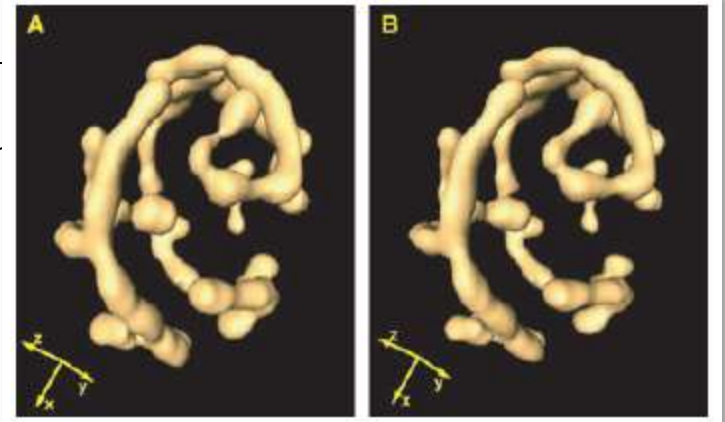
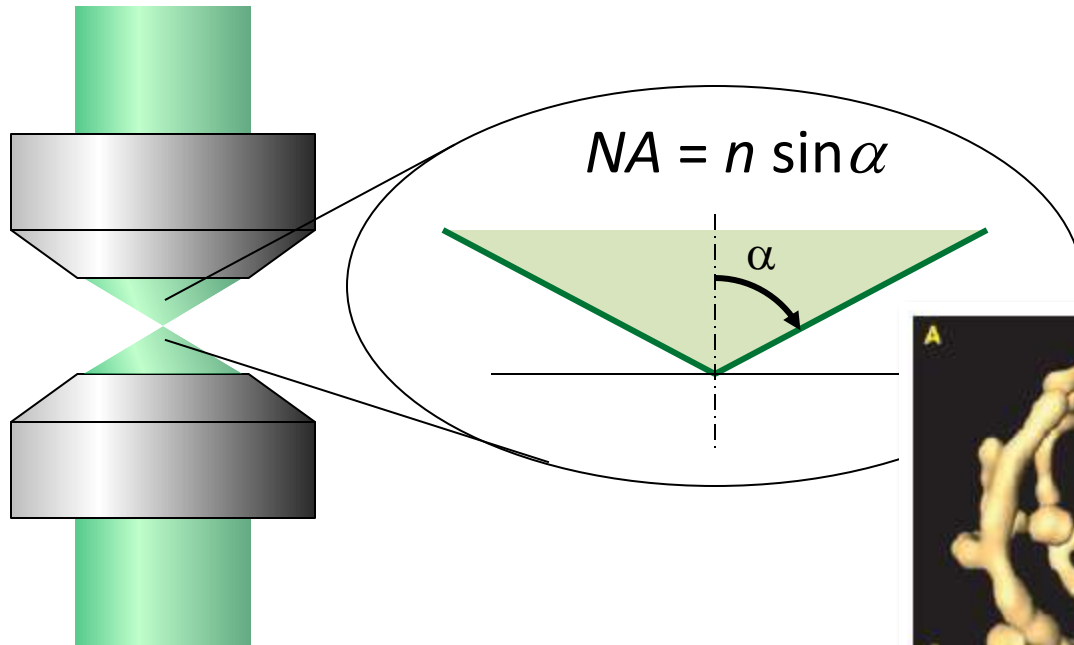
β_2 adrenergic receptor clusters
on the plasma membrane



Ianoul et al., 2005

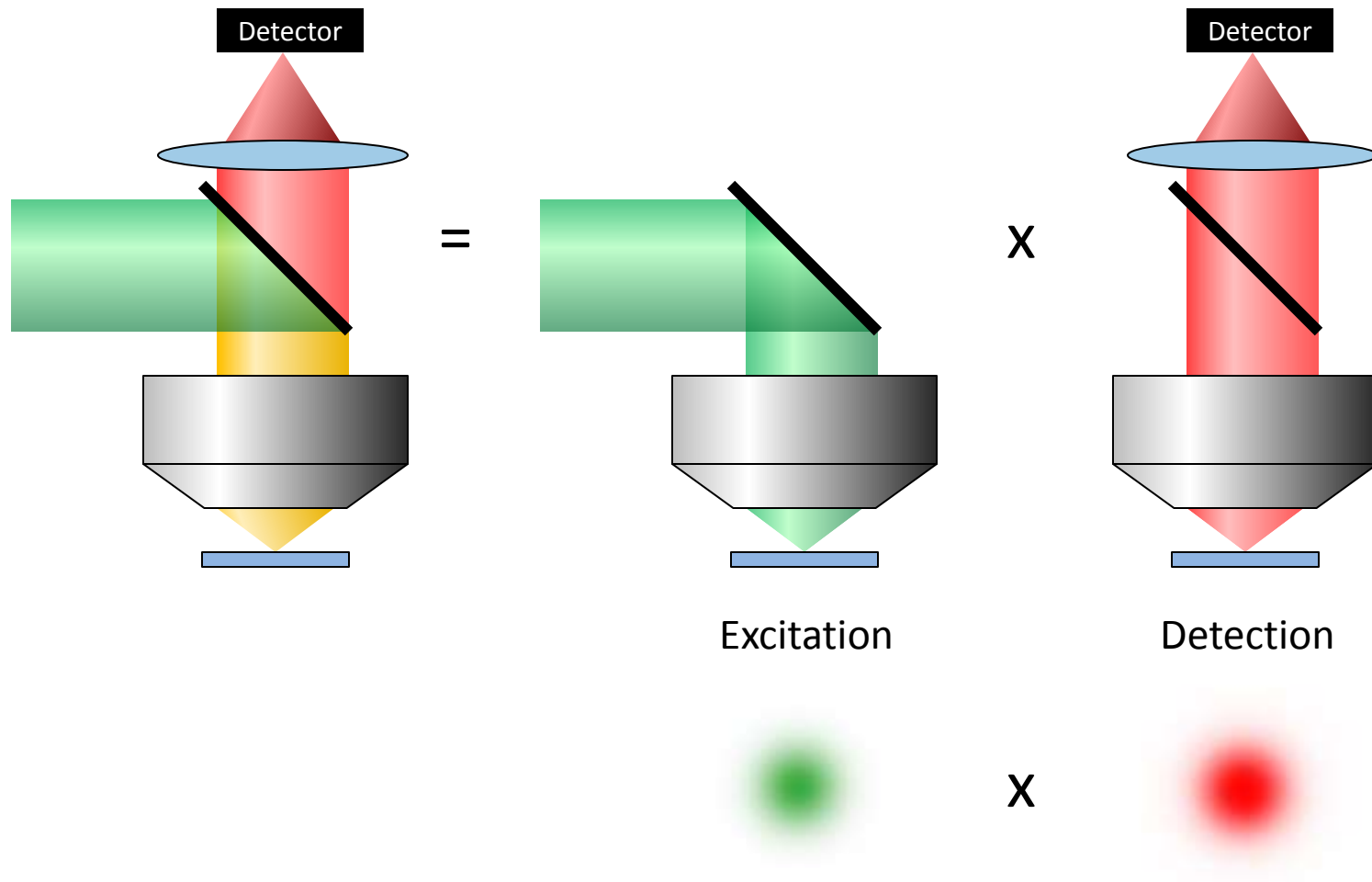
4-Pi / I⁵M

$$d \approx \frac{\lambda}{2 NA}$$

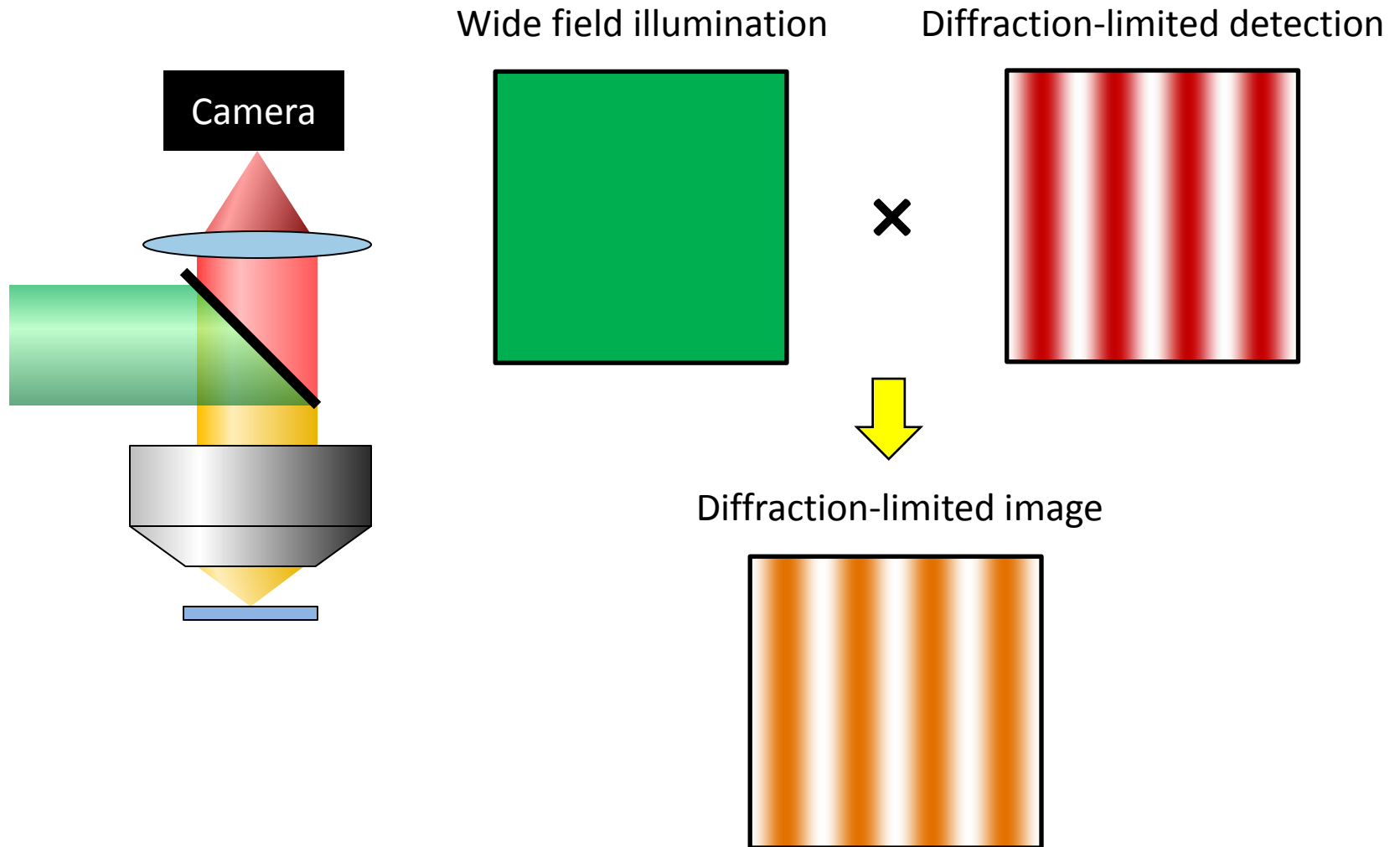


Major advantage:
Similar z resolution as x-y resolution

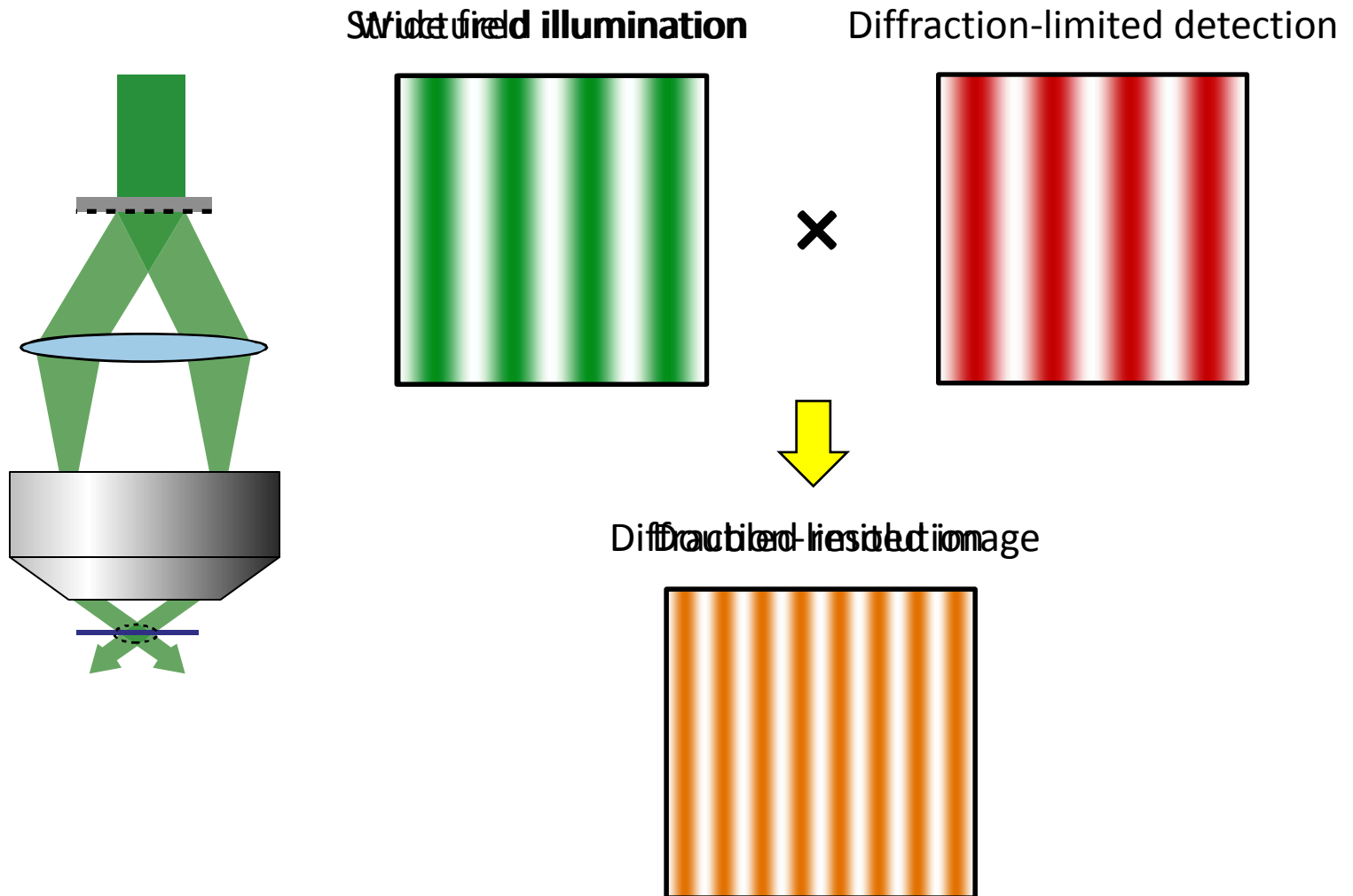
Patterned illumination



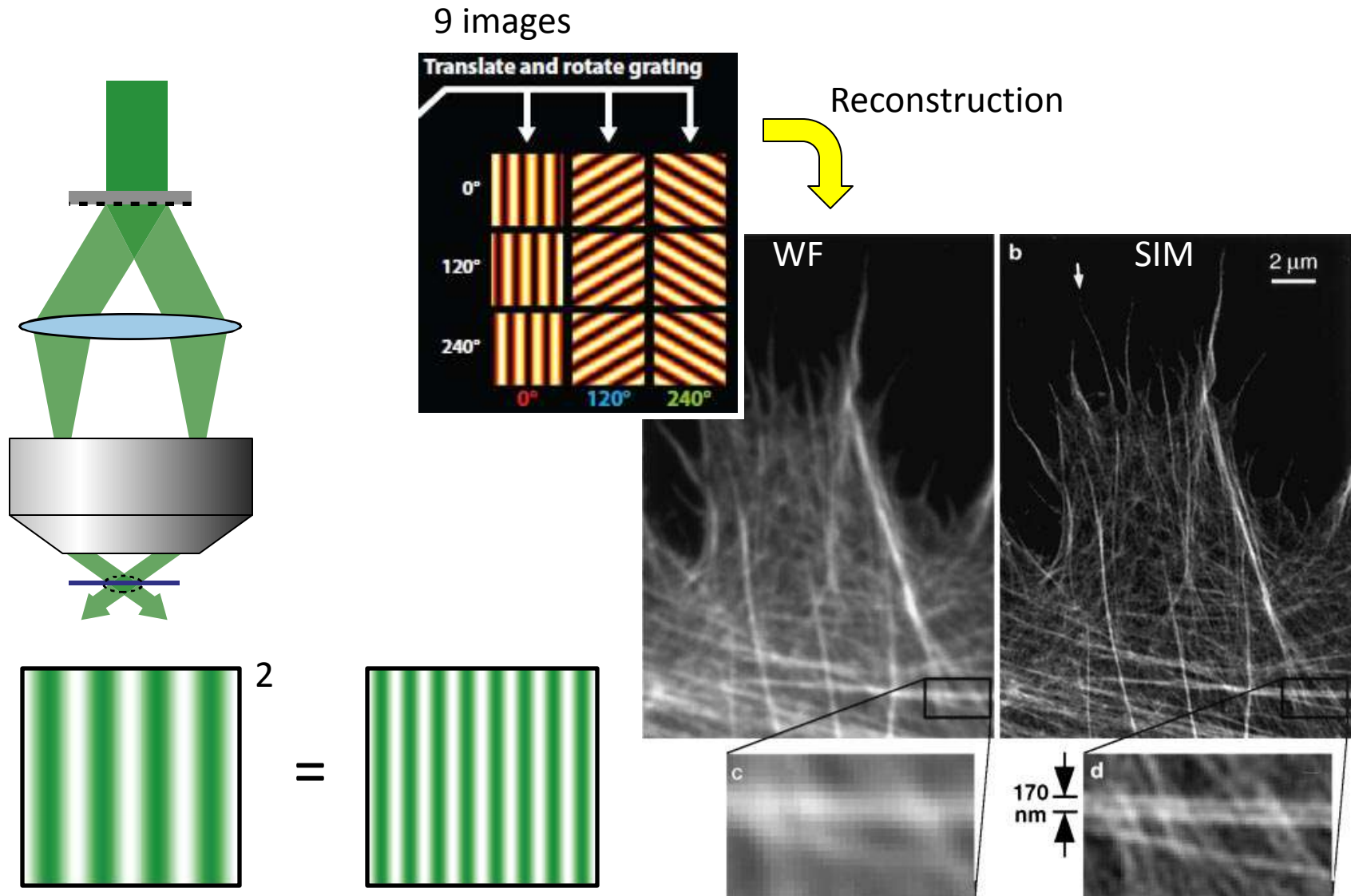
Structured Illumination Microscopy (SIM)



Structured Illumination Microscopy (SIM)



Structured Illumination Microscopy (SIM)

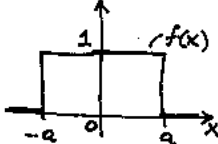


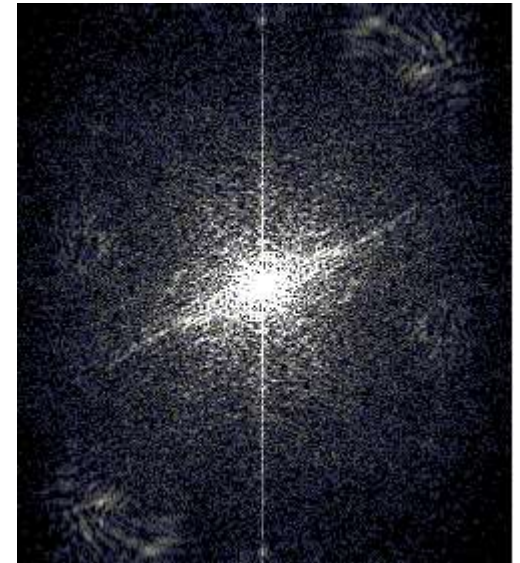
Being (slightly) more rigorous about SIM



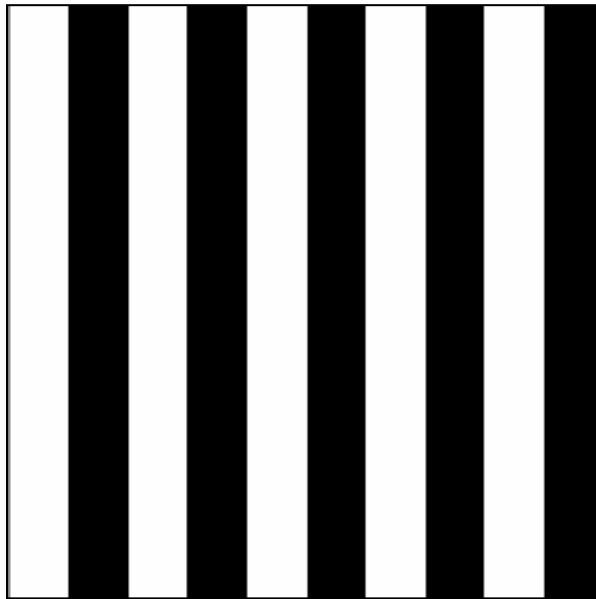
Fourier transforms: Examples

- $f(x) = \delta(x) \quad \rightarrow \quad \tilde{f}(k) = 1$
- $f(x) = 1 \quad \rightarrow \quad \tilde{f}(k) = 2\pi \delta(k)$
- $f(x) = e^{-a|x|} \quad \rightarrow \quad \tilde{f}(k) = \frac{2a}{k^2 + a^2}$
- $f(x) = \frac{1}{x^2 + a^2} \quad \rightarrow \quad \tilde{f}(k) = \frac{\pi}{a} e^{-a|k|}$
- $f(x) = e^{-a\frac{x^2}{2}} \quad \rightarrow \quad \tilde{f}(k) = \sqrt{\frac{2\pi}{a}} e^{-\frac{1}{a}\frac{k^2}{2}}$

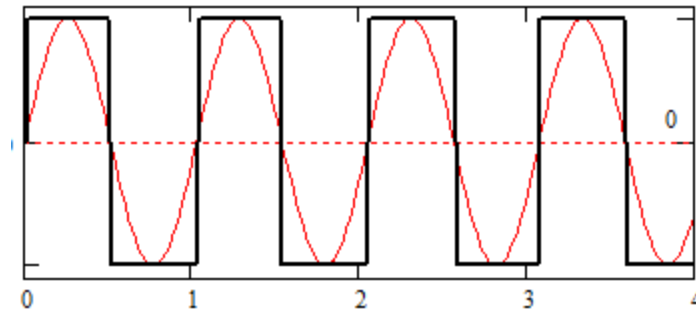
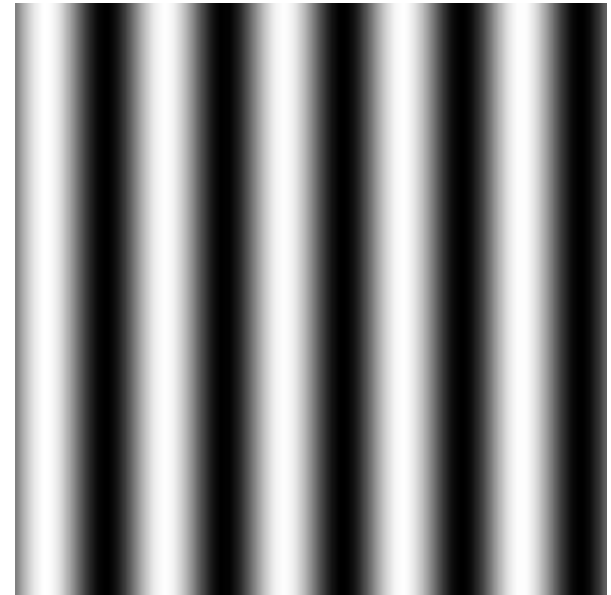
-  $\rightarrow \quad \tilde{f}(k) = 2 \frac{\sin(ak)}{k}$



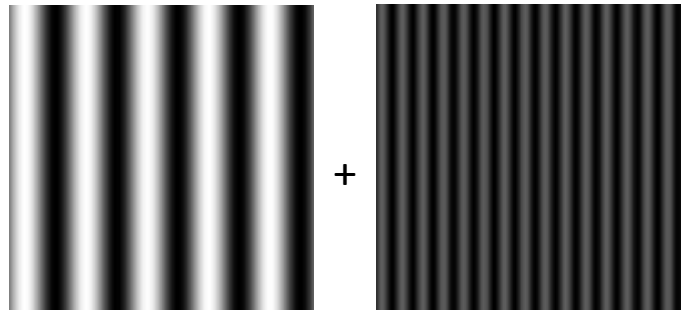
Fourier transform and spatial frequencies



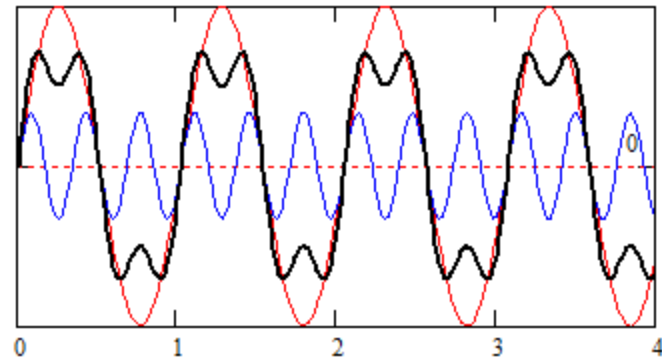
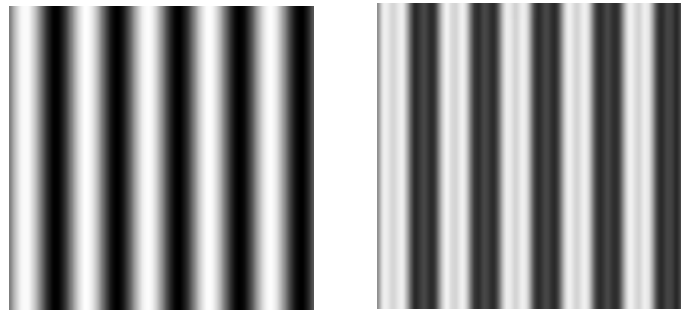
$\hat{=}$
?



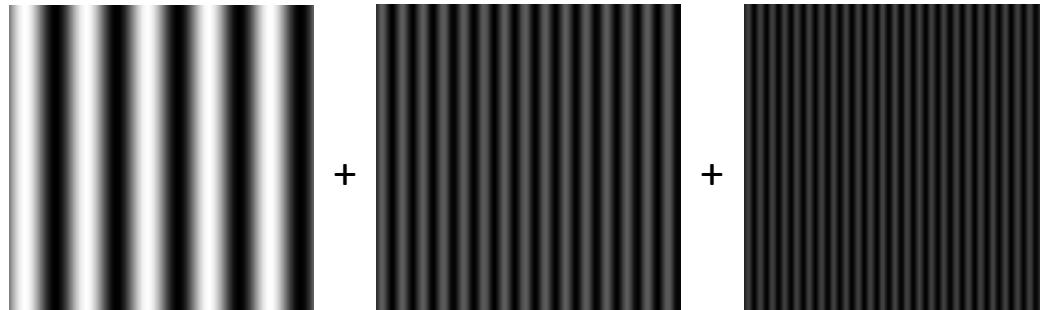
Fourier transform and spatial frequencies



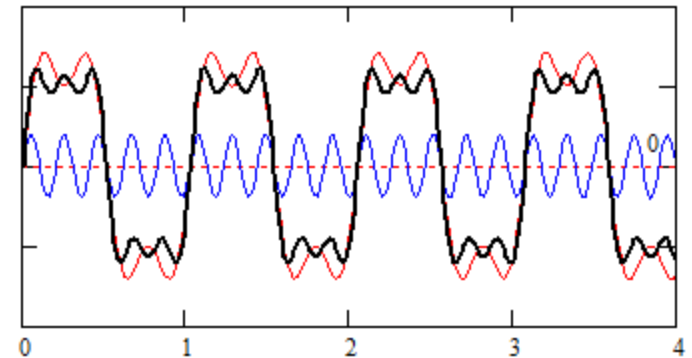
Summed image



Fourier transform and spatial frequencies

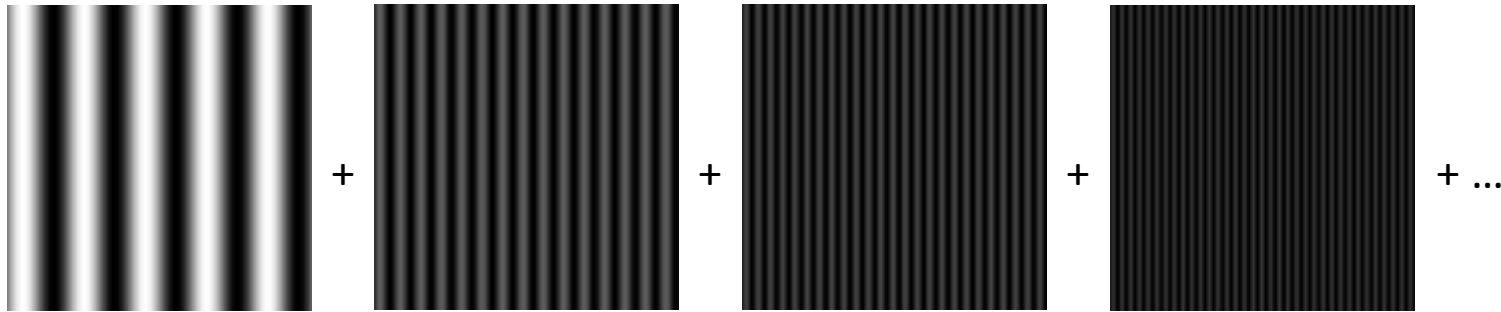


Summed image



Fourier transform and spatial frequencies

Discrete spatial frequencies



Summed image

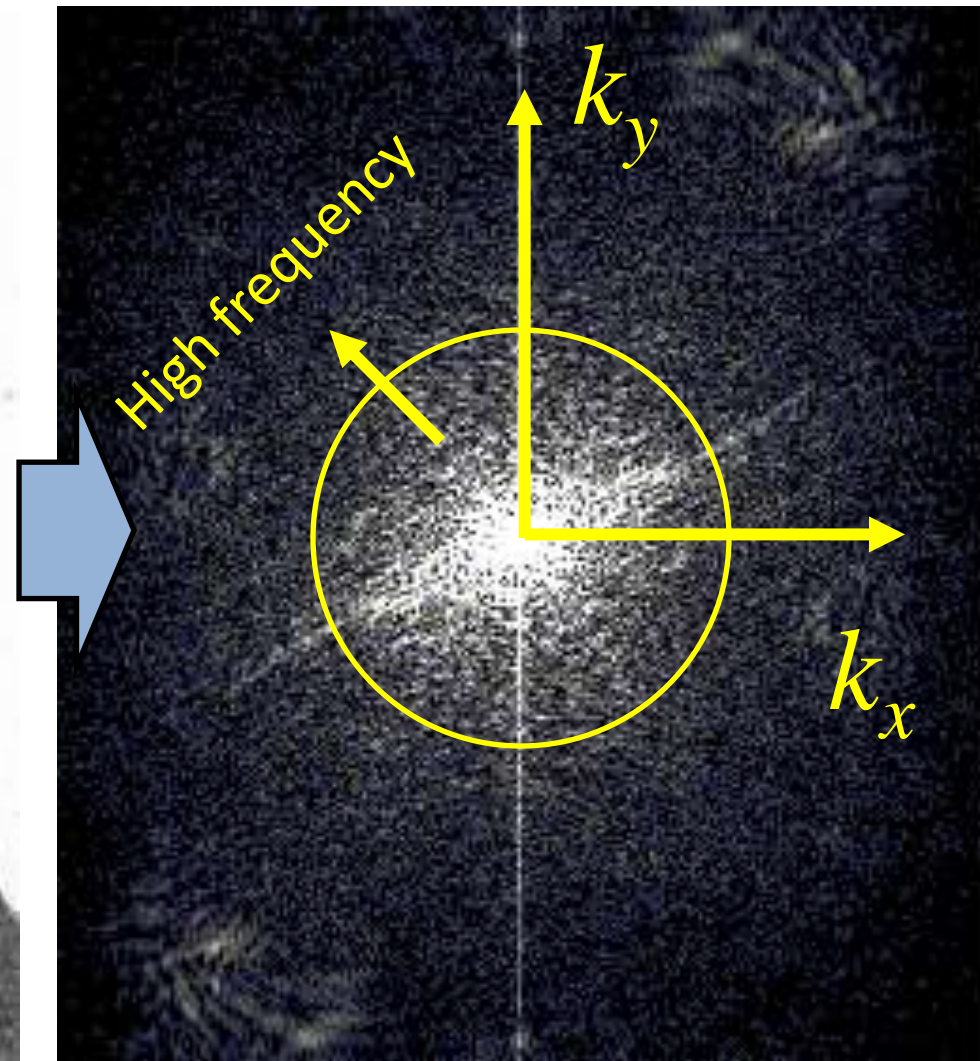


$$G(x) = \sum F(k) \sin(k x)$$

Fourier transform and spatial frequencies

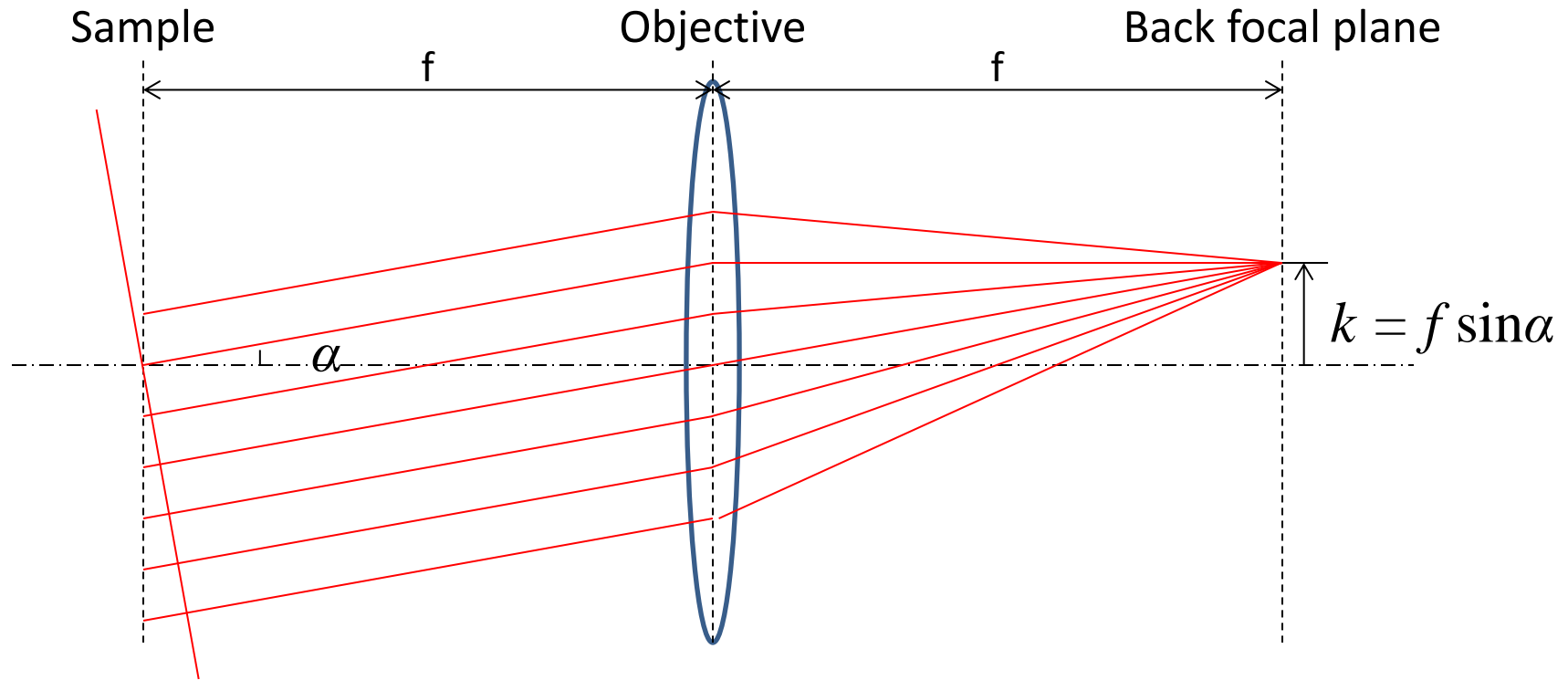


Original Image (real space)

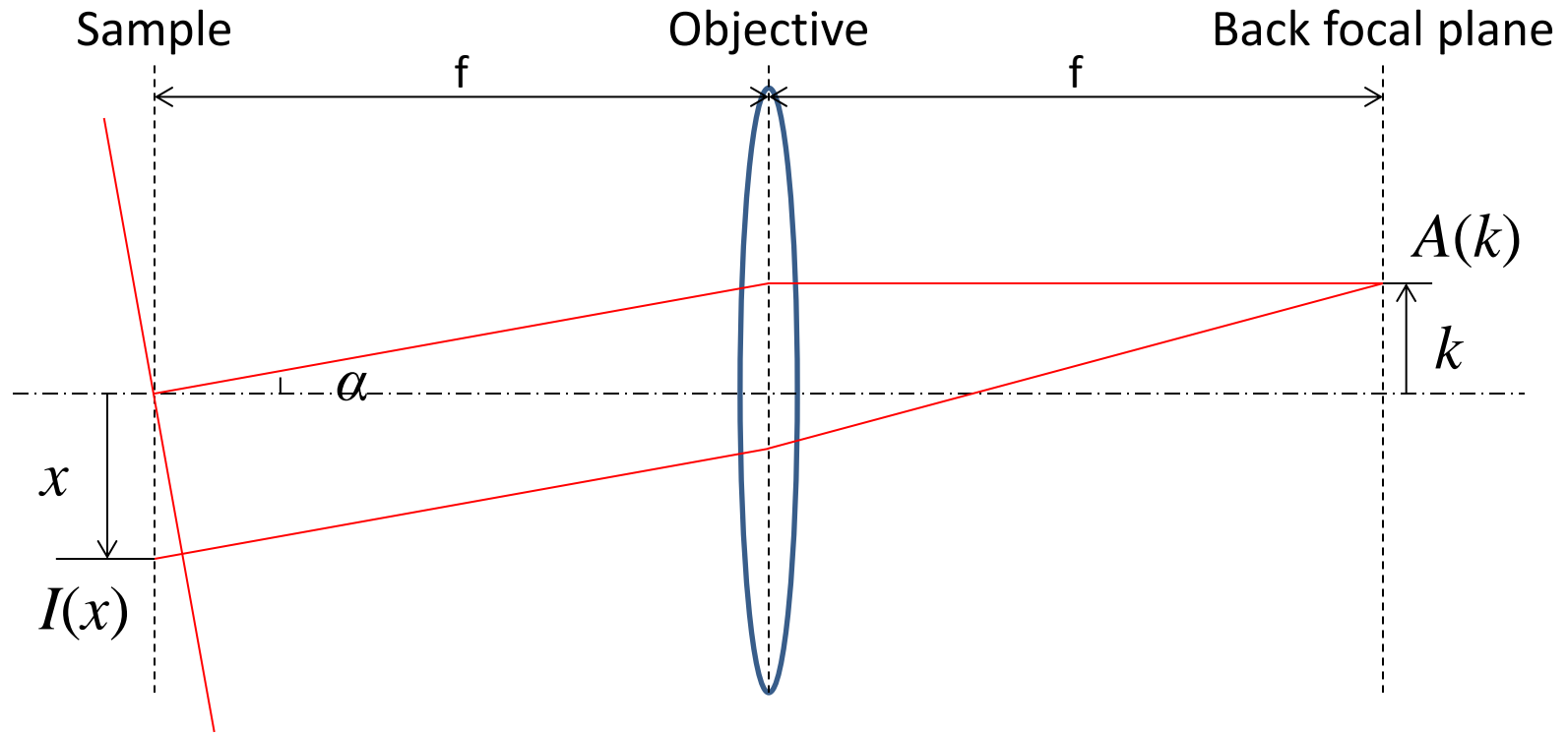


Fourier transform (frequency space)

Fourier optics and microscope resolution



Fourier optics and microscope resolution



Phase delay from the mid-point

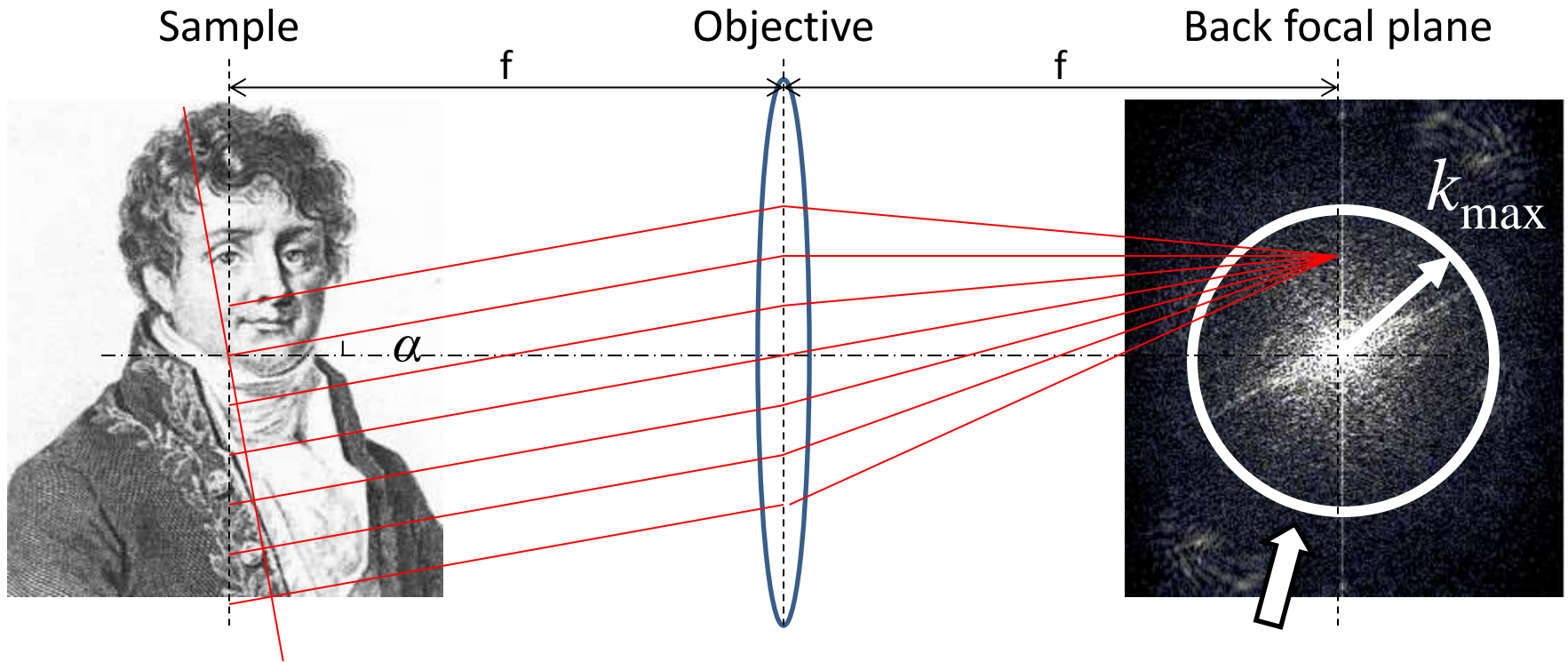
$$\Delta\varphi = x \sin\alpha (2\pi/\lambda) = x (k / f) (2\pi/\lambda) \text{ assuming refractive index} = 1$$

Light intensity at the sample plane

Fourier Transform!

$$I(x) = \sum A(k) \sin(\Delta\varphi) = \sum A(k) \sin(x k 2\pi/\lambda f)$$

Fourier optics and microscope resolution



$$\text{Spatial frequency} = k \cdot 2\pi/\lambda f$$

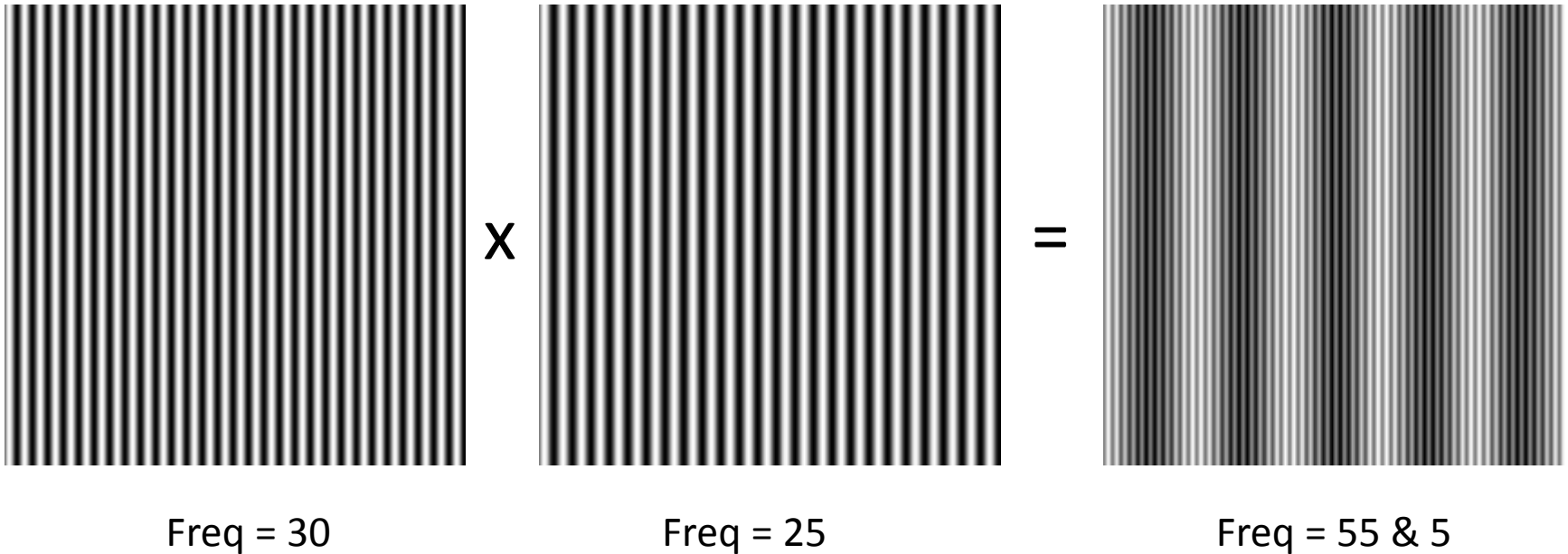
$$k_{\text{max}} = f \sin \alpha_{\text{max}} = f \cdot NA$$

$$\text{Resolution} = \lambda / 2NA$$

Size of the back focal plane

Extending the measurable freq. range

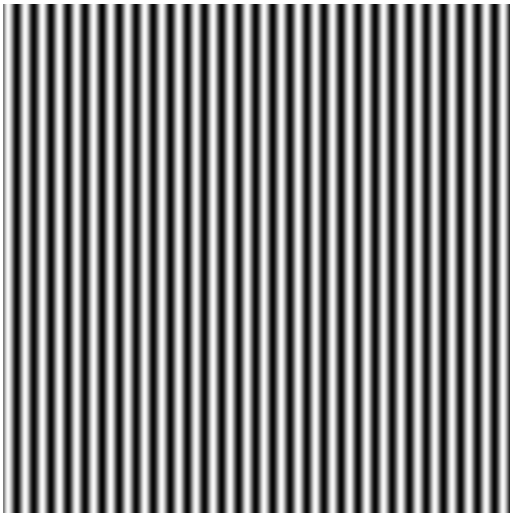
$$\text{Excitation}(x) \times \text{Sample}(x) = \text{Observed Signal}(x)$$



$$\sin A \cdot \sin B = (\cos(A - B) - \cos(A + B)) / 2$$

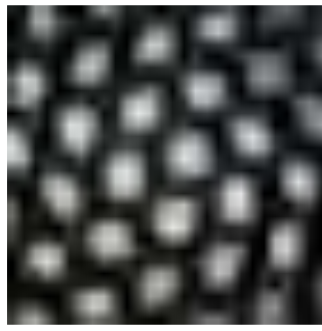
Extending the measurable freq. range

$$\text{Excitation}(x) \times \text{Sample}(x) = \text{Observed Signal}(x)$$



Freq = 30

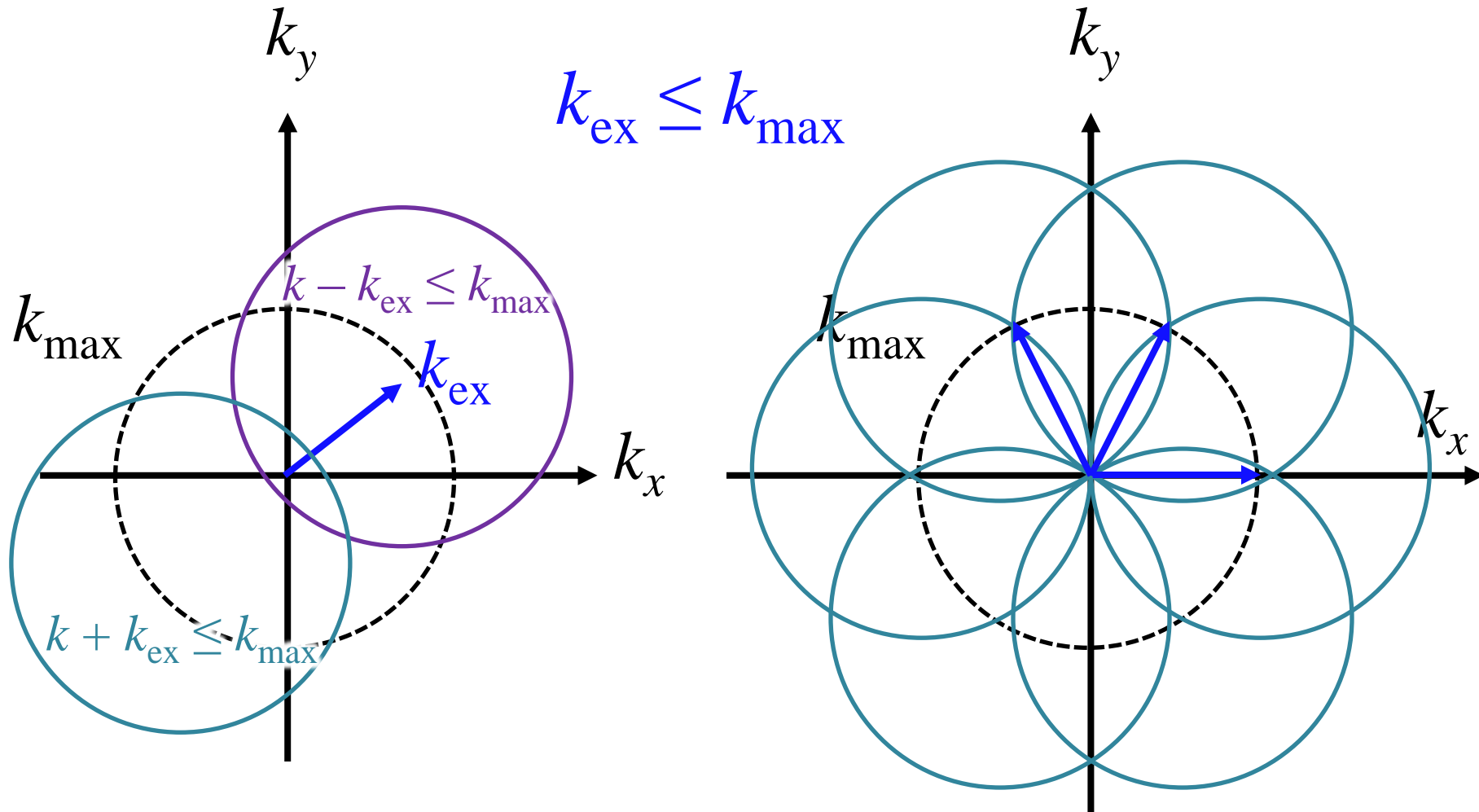
x



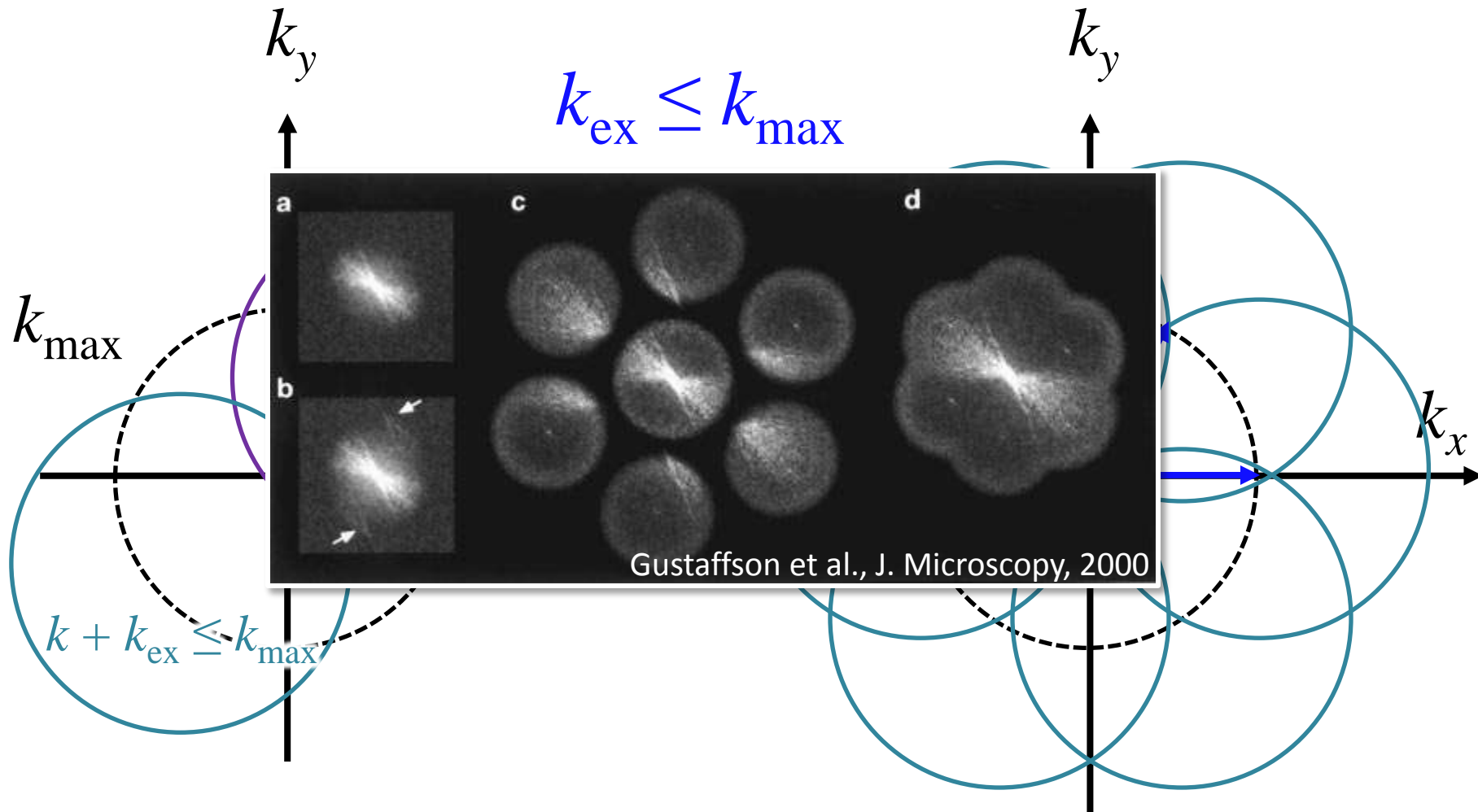
$\sin A \cdot \sin$



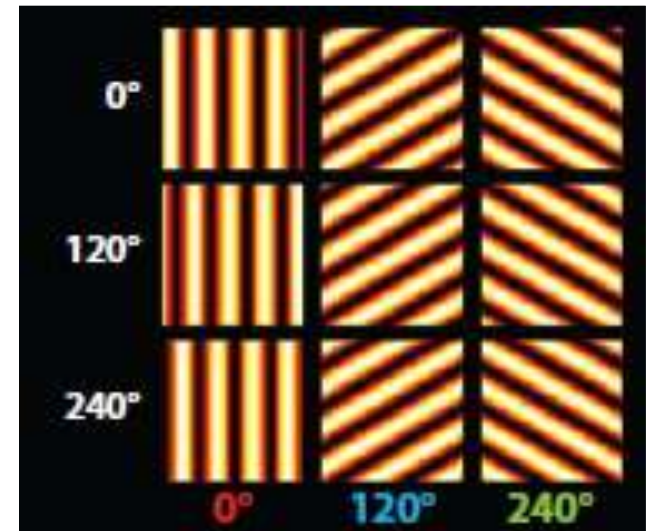
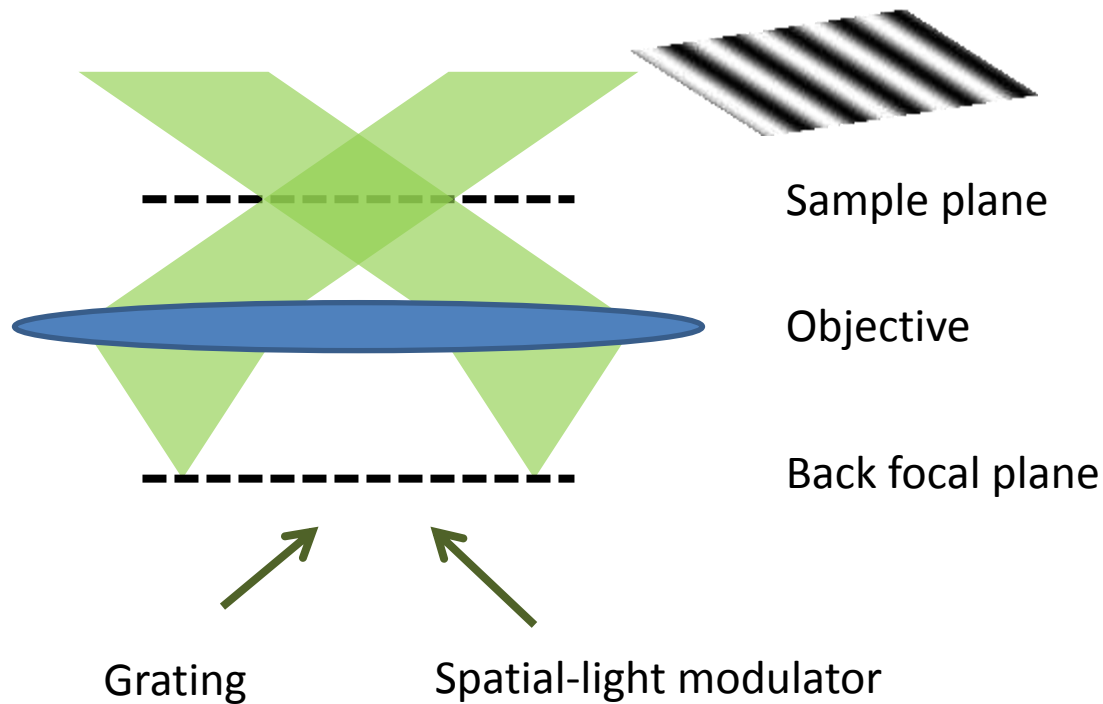
Extending the measurable freq. range



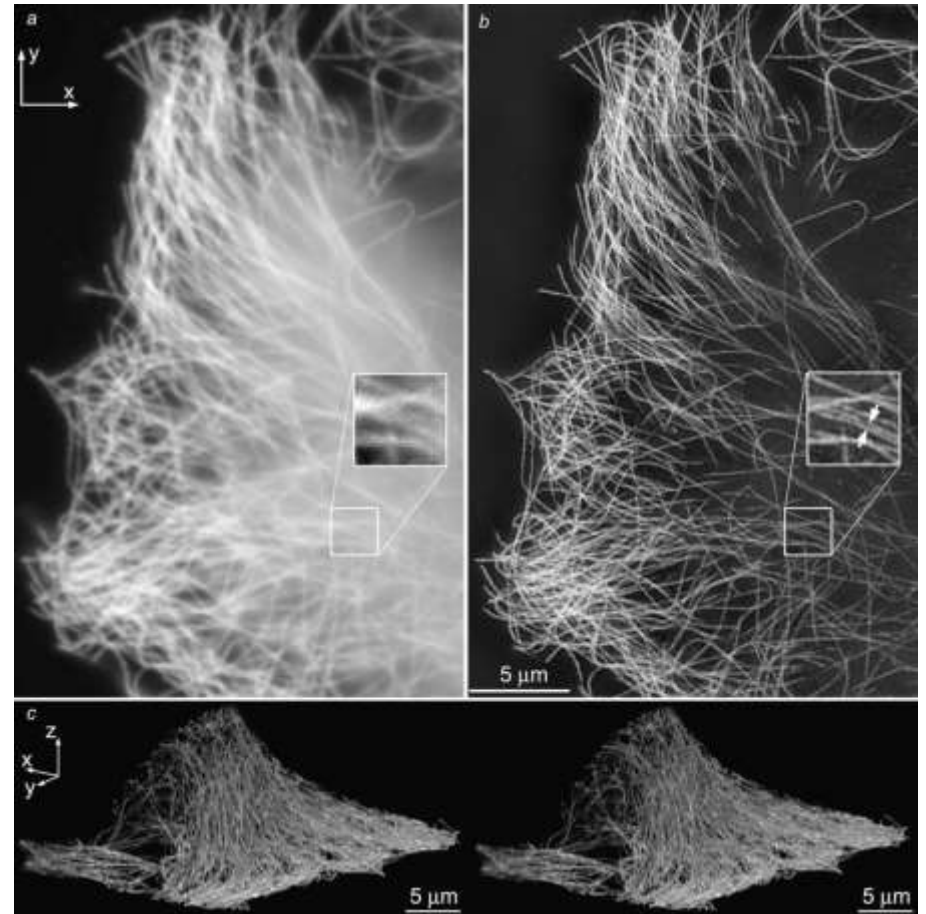
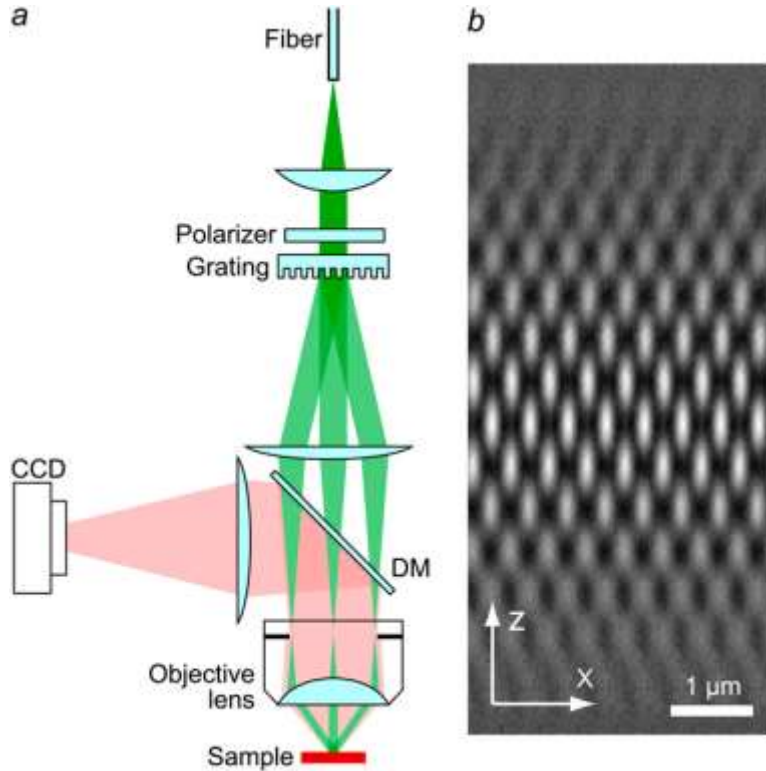
Extending the measurable freq. range



Generating the illumination pattern

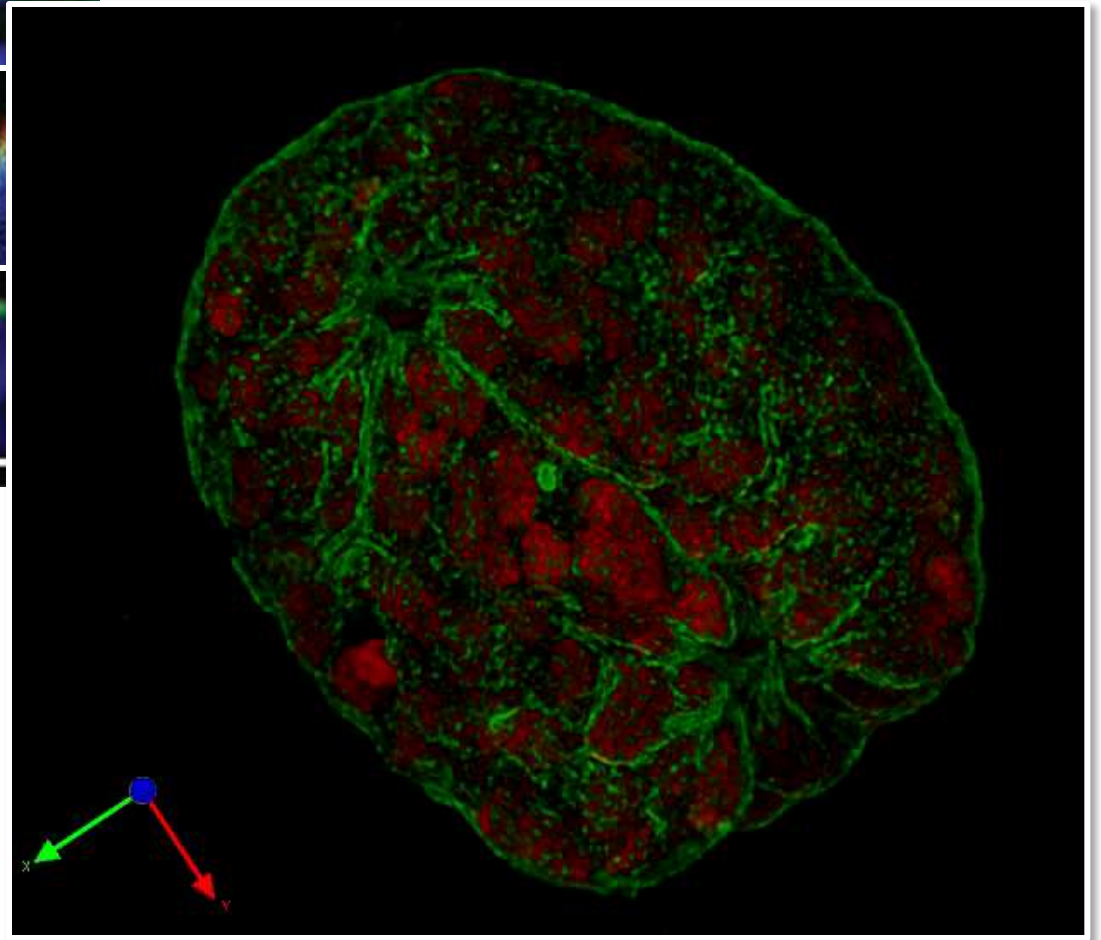
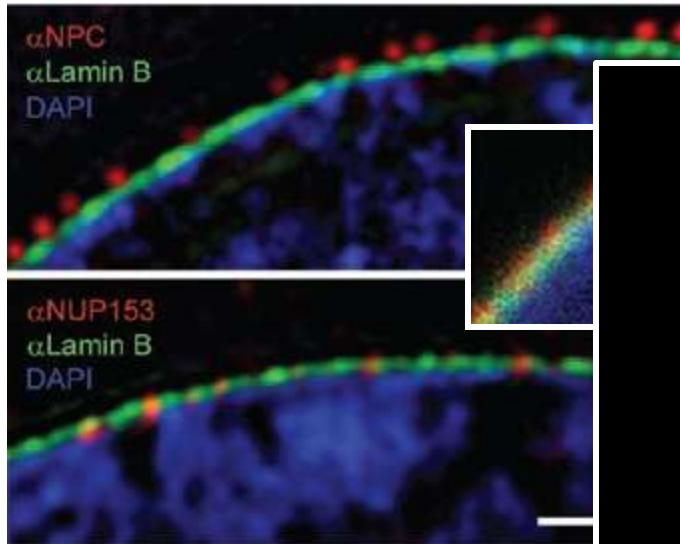


3D SIM: better resolution + optical sectioning

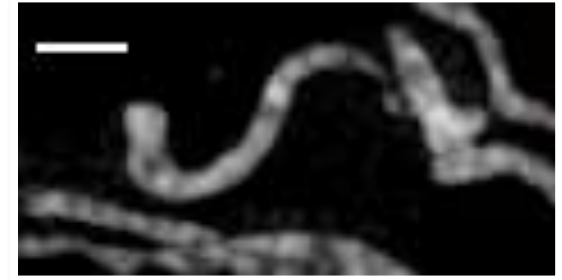
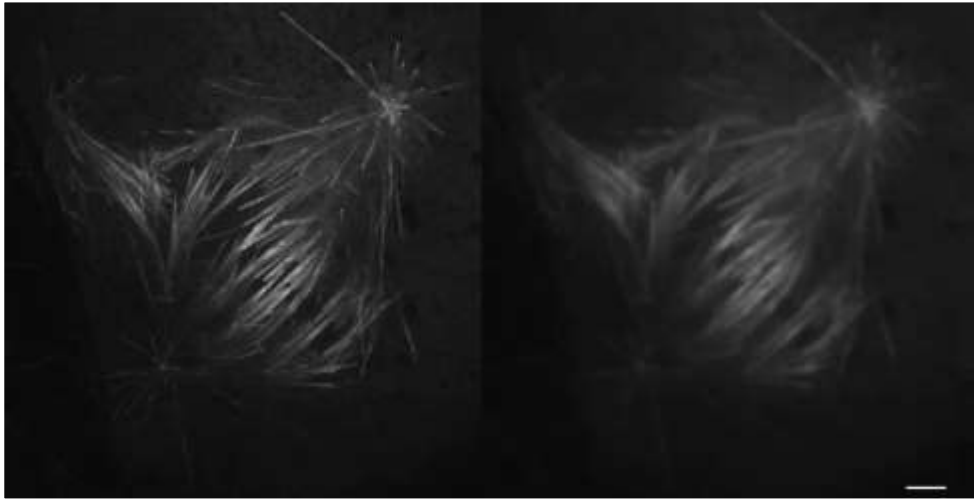


Multicolor SIM

Same as conventional fluorescence microscopy!



Live imaging with SIM



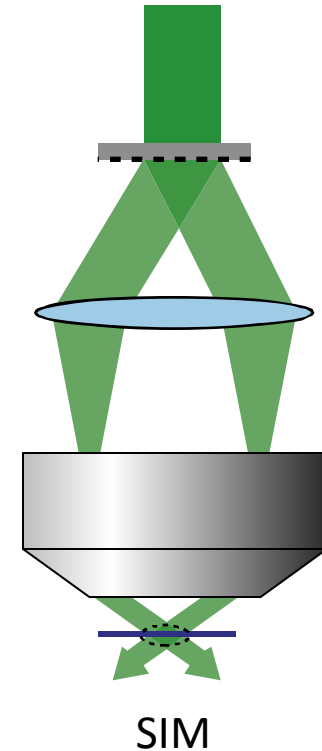
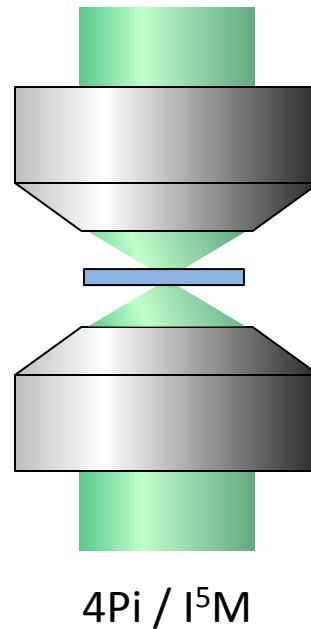
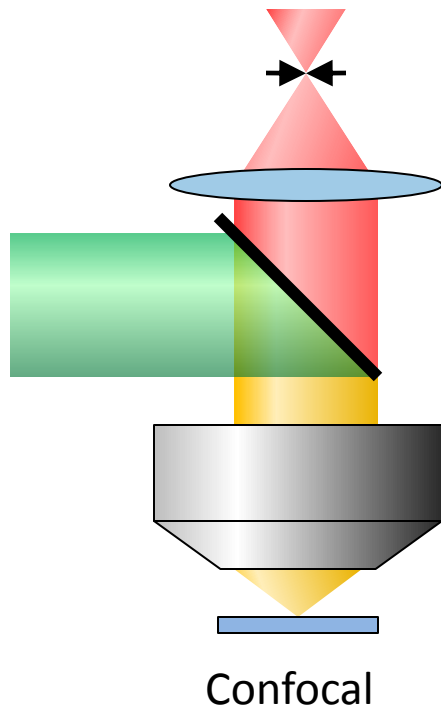
Kner, Chhun et al., Nat Methods,

Shao et al., Nat Methods, 2011



The diffraction limit still exists

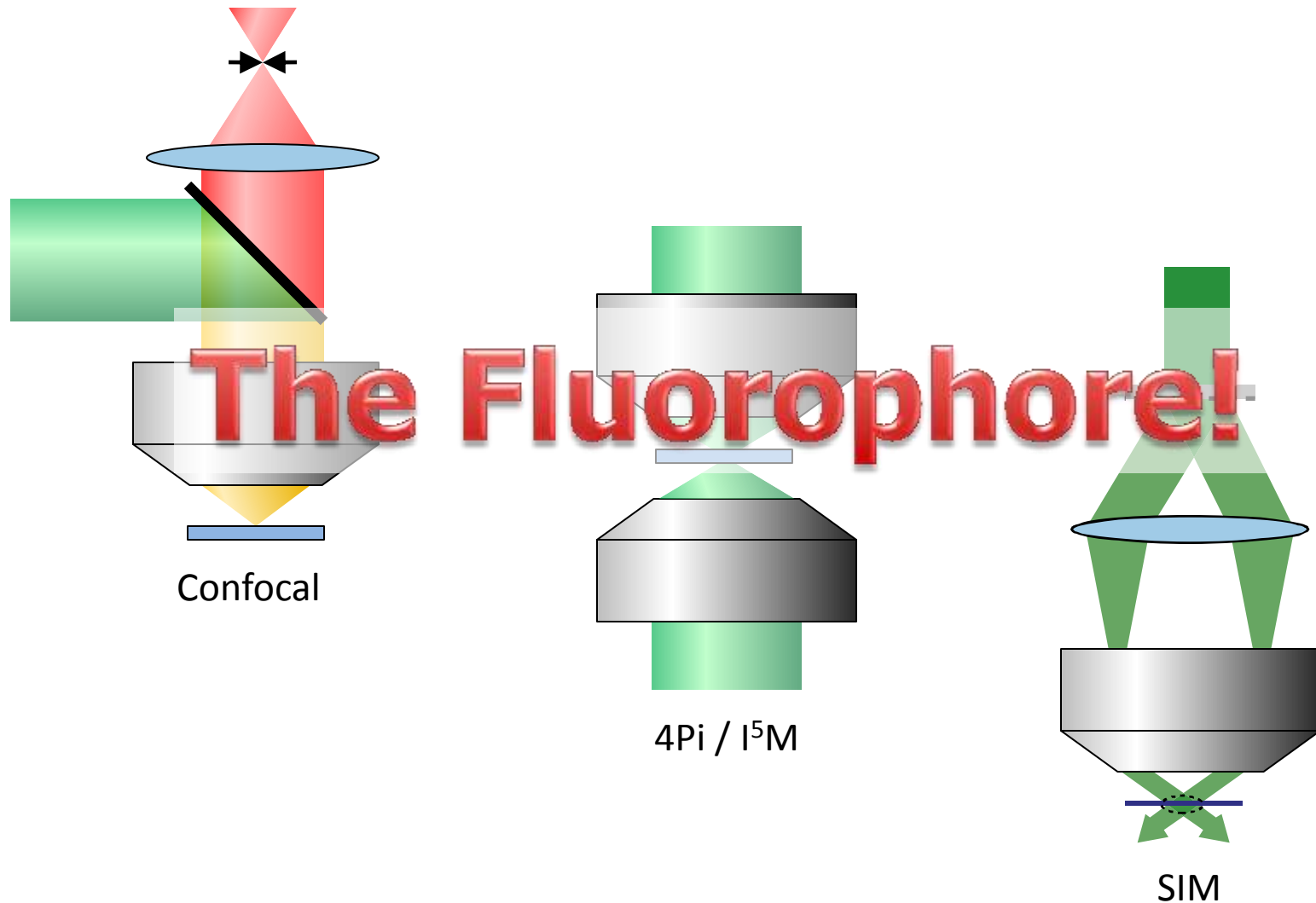
$$d \geq \frac{1}{2} \cdot \frac{\lambda}{2NA}$$



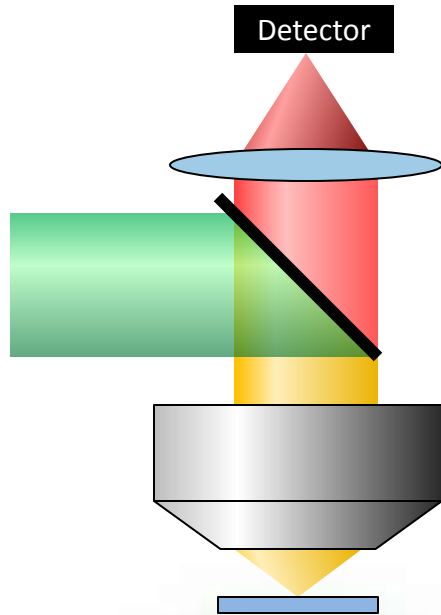
Breaking the diffraction barrier



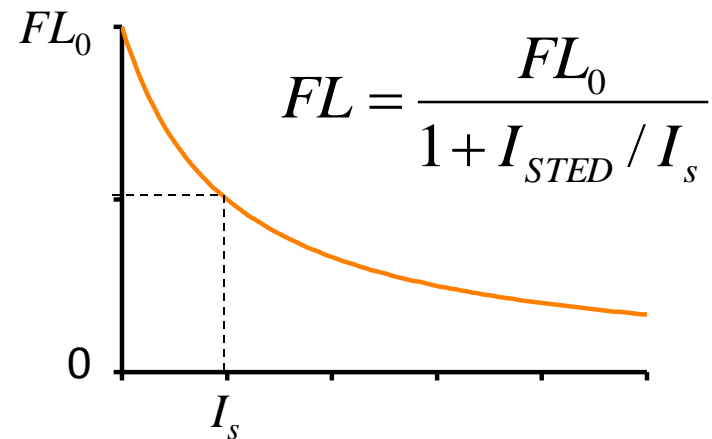
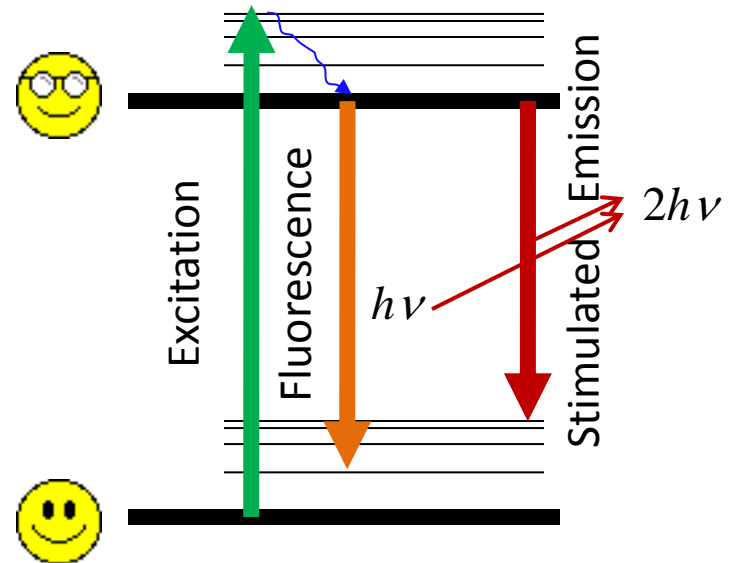
Breaking the diffraction barrier



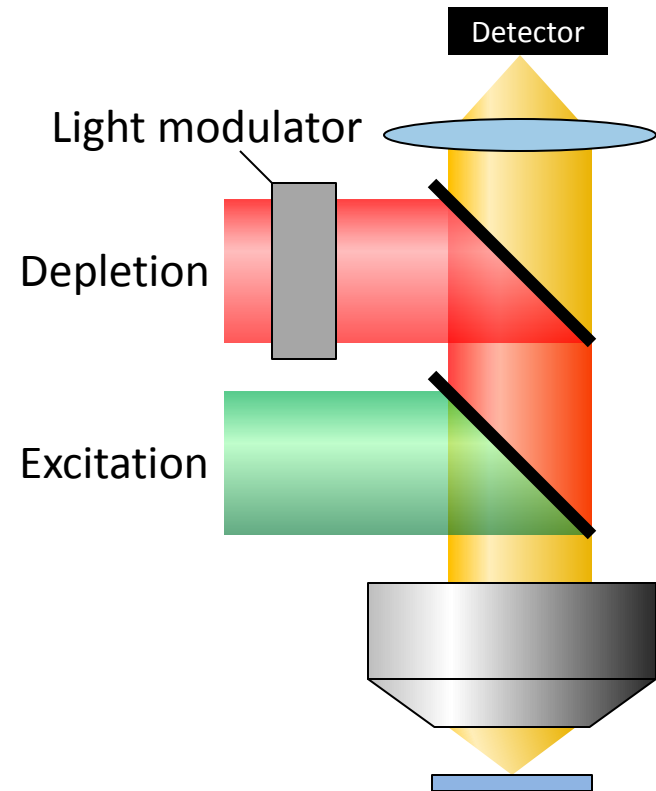
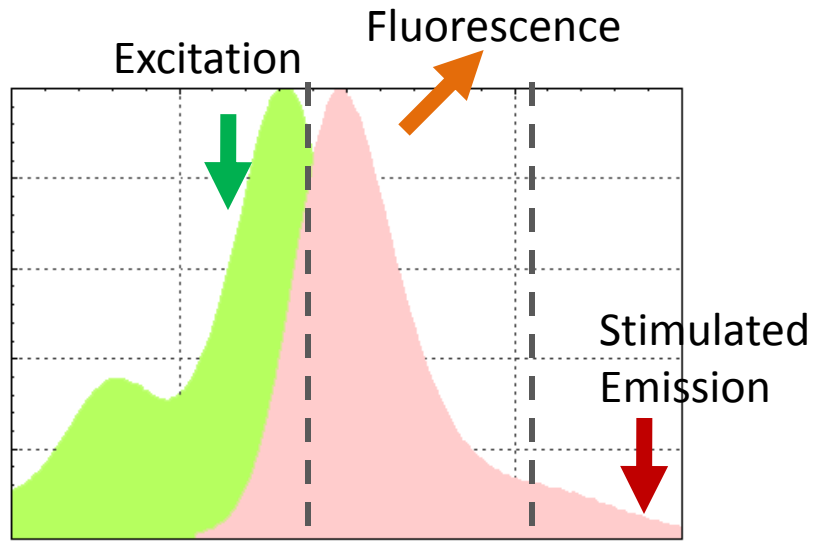
Stimulated Emission Depletion (STED)



Send to a dark state



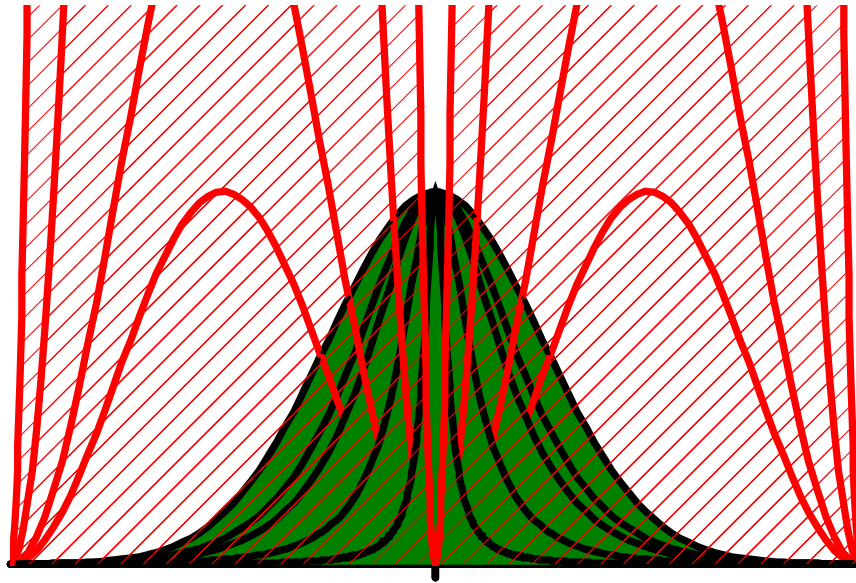
STED microscopy



Excitation STED pattern Effective PSF

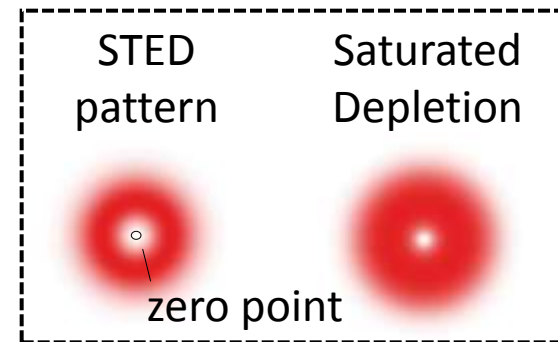
$$\text{Excitation} \div \text{STED pattern} = \text{Effective PSF} \quad ?$$

Saturated depletion

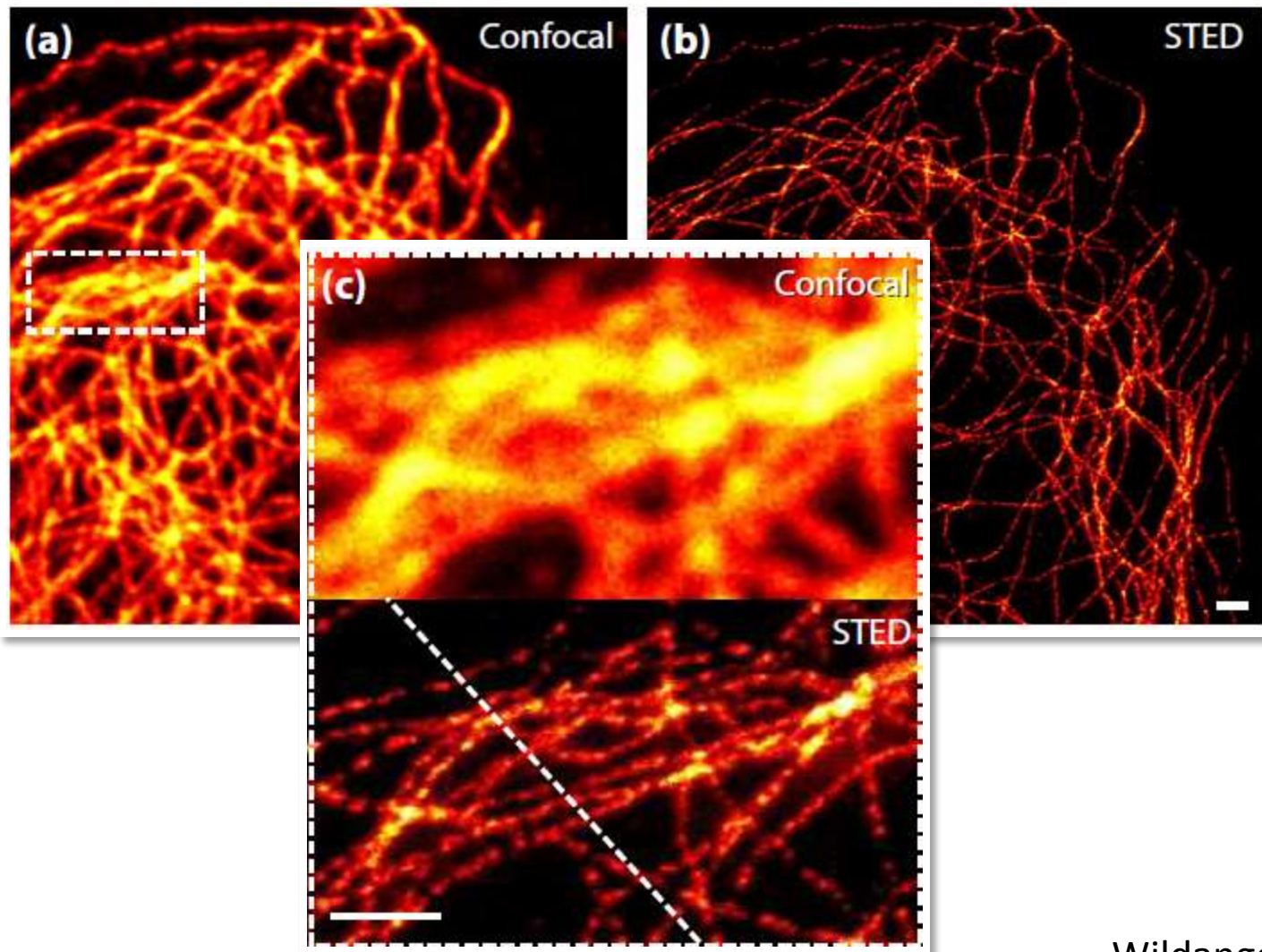


$$I_{\text{STED}} = 200 I_s$$

$$D = \frac{1}{\sqrt{1 + I/I_s}} \cdot \frac{\lambda}{2NA}$$

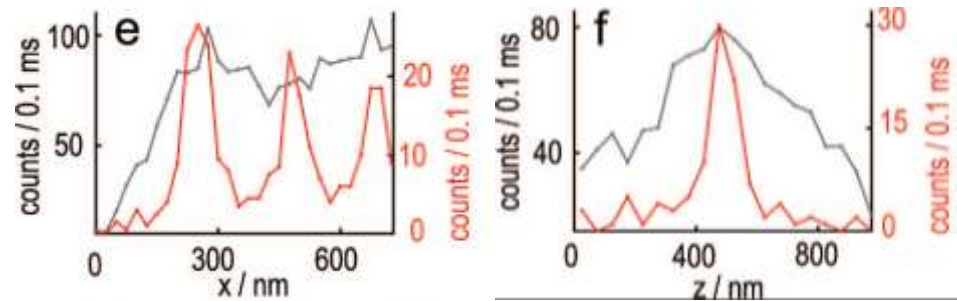
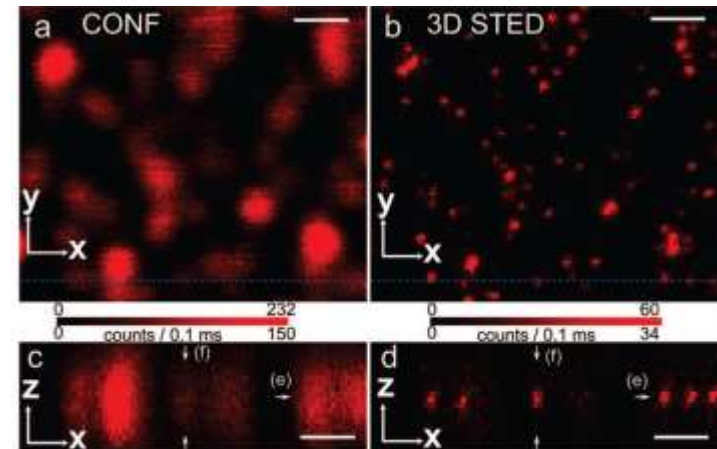
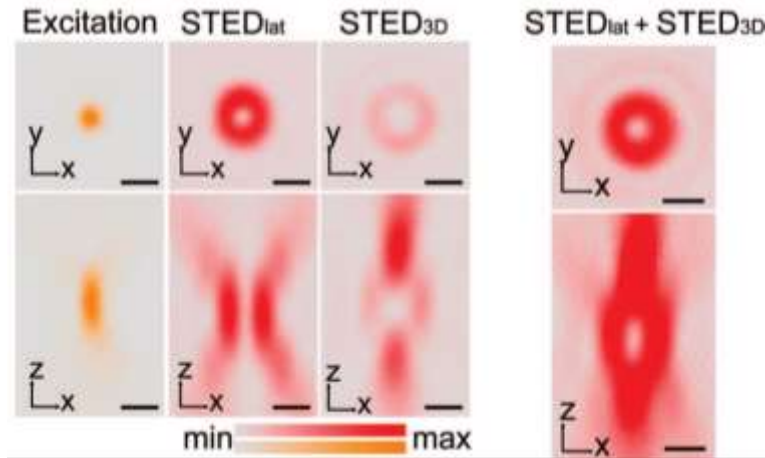


STED images of microtubules

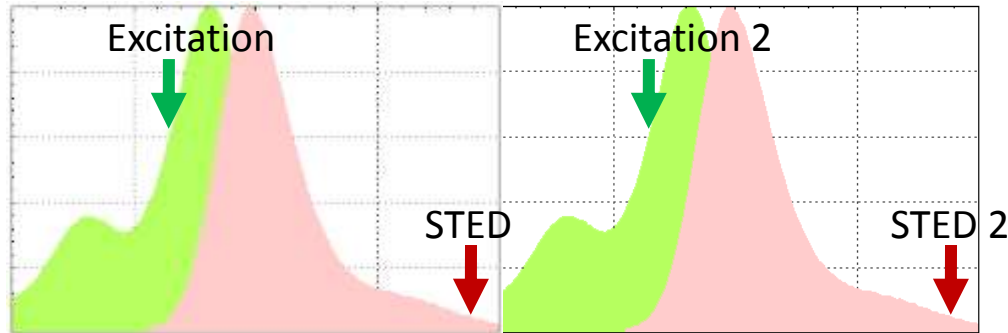


Wildanger et al., 2009

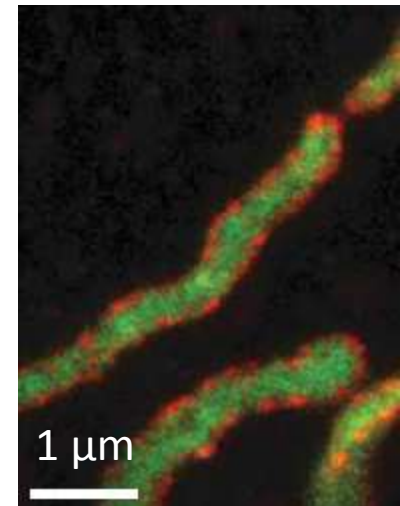
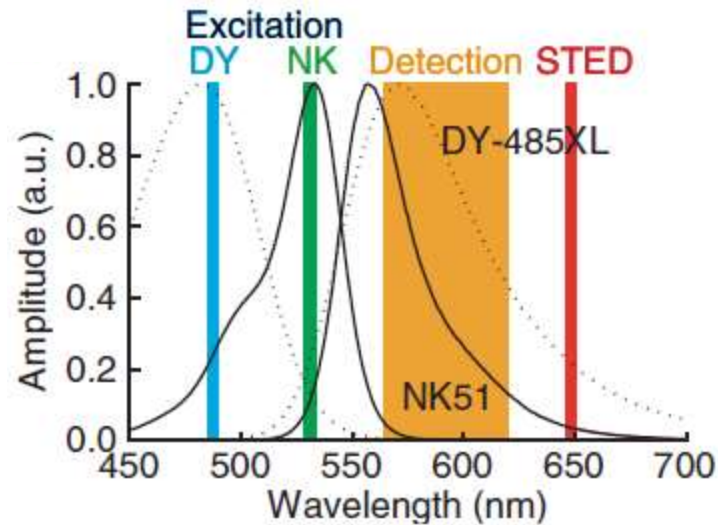
3D STED



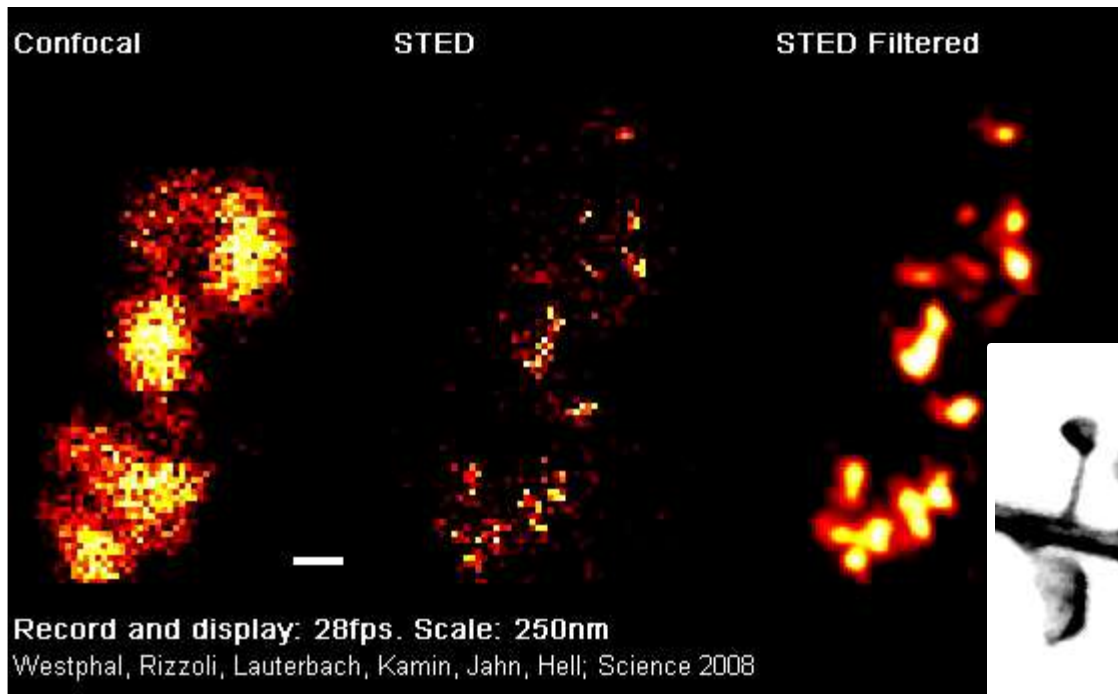
Multicolor STED



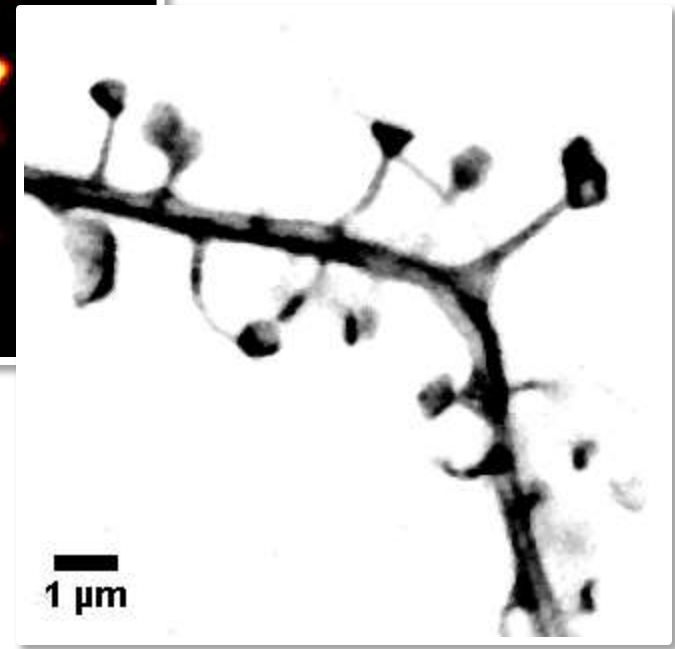
2 color isoSTED resolving
the inner and outer membrane
of mitochondria



Live STED



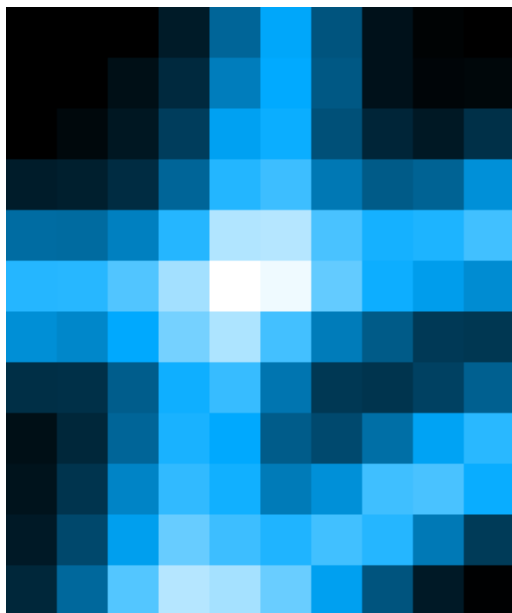
Westphal et al., Science, 2008



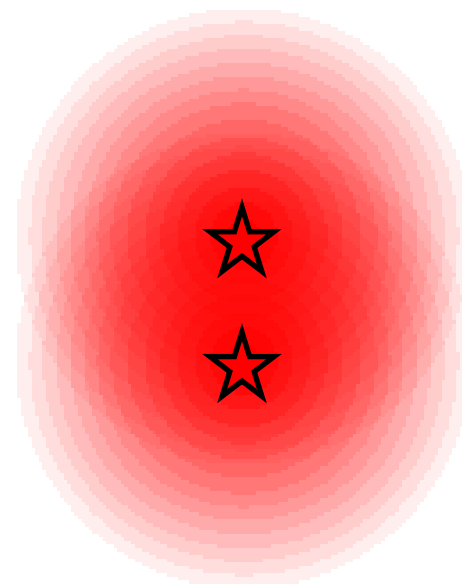
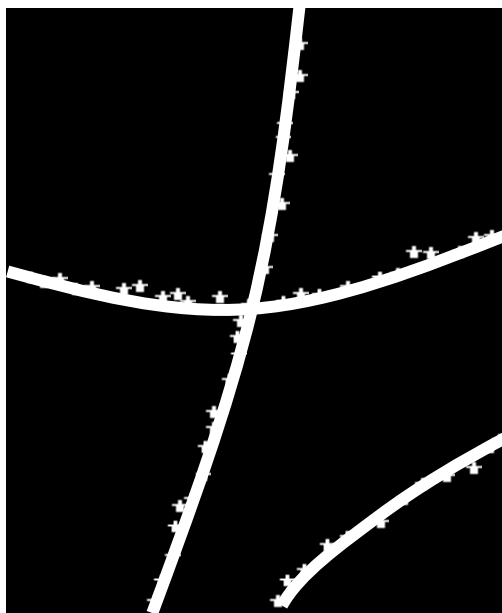
Nagerl et al., PNAS, 2008

Super-resolution by...

Fluorescence image

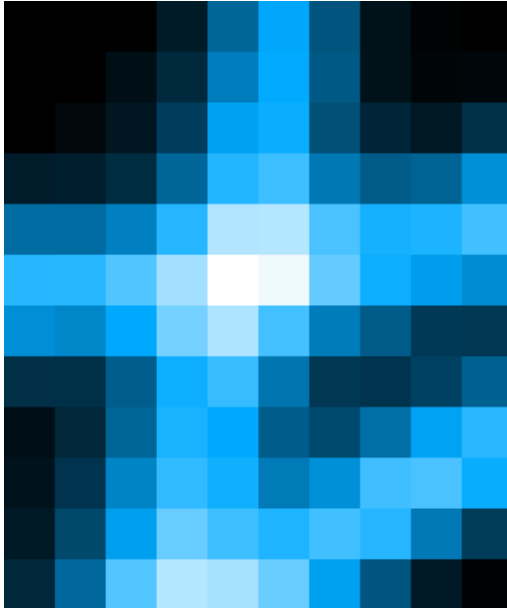


Underlying structure

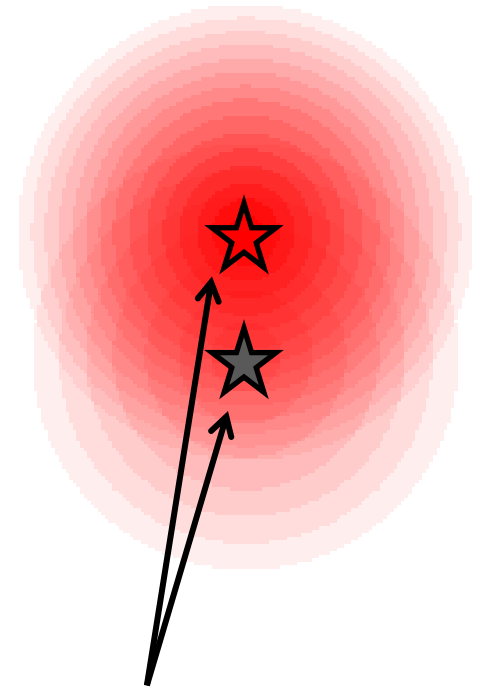
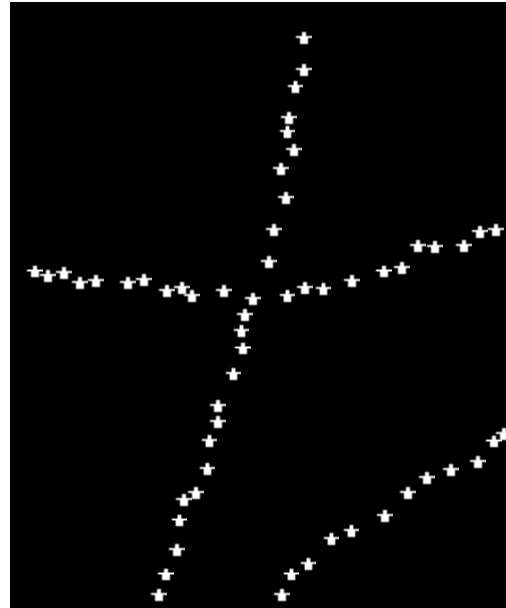


Super-resolution by spatial modulation

Fluorescence image



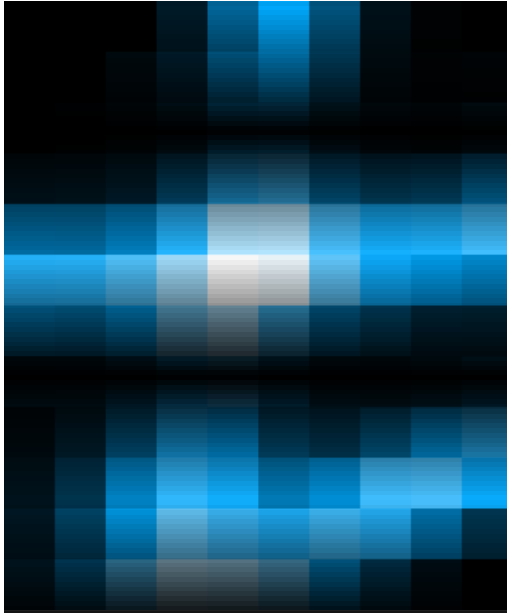
Underlying structure



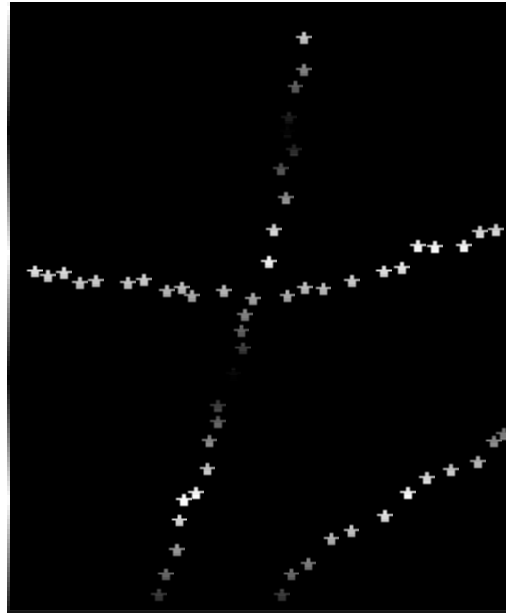
Differential modulation
of the fluorescence response

Super-resolution by differential excitation

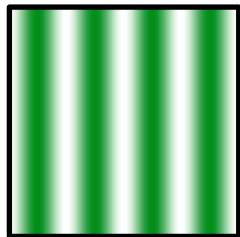
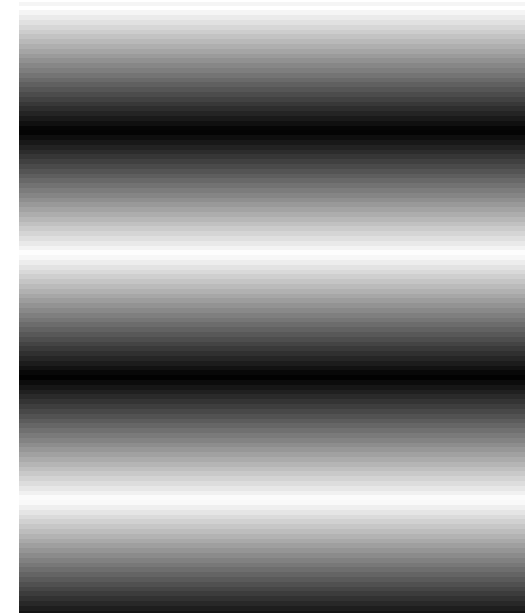
Fluorescence image



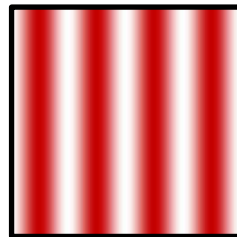
Underlying structure



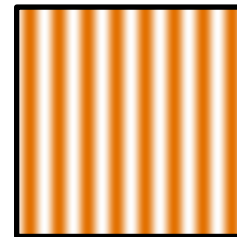
Excitation pattern



×



=



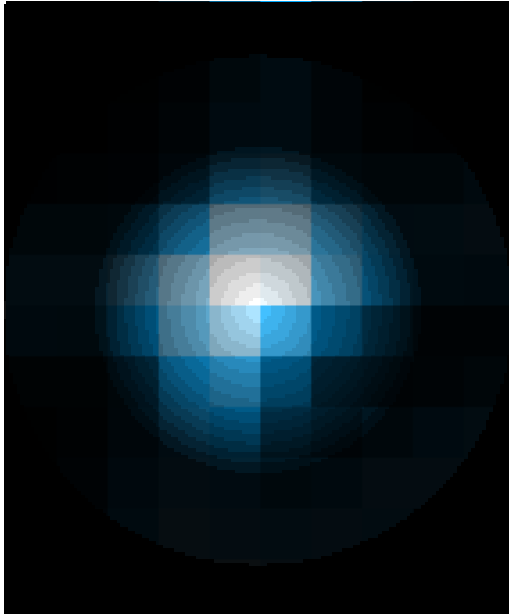
SIM (Gustafsson / Heintzmann)
SSIM (Gustafsson 2005)

Diffraction limited excitation and emission

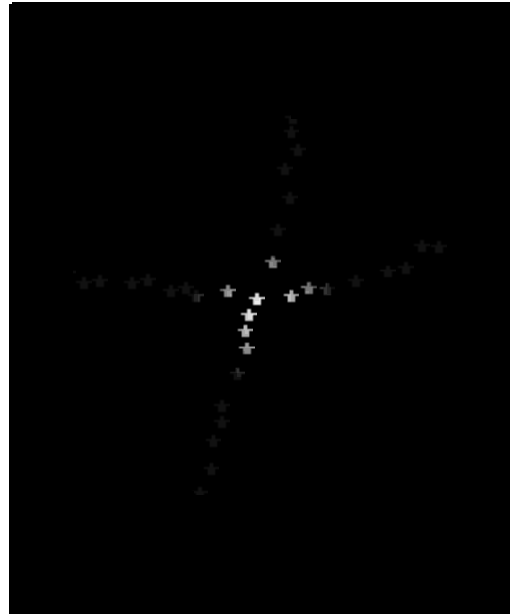
Doubled resolution

Super-resolution by differential depletion

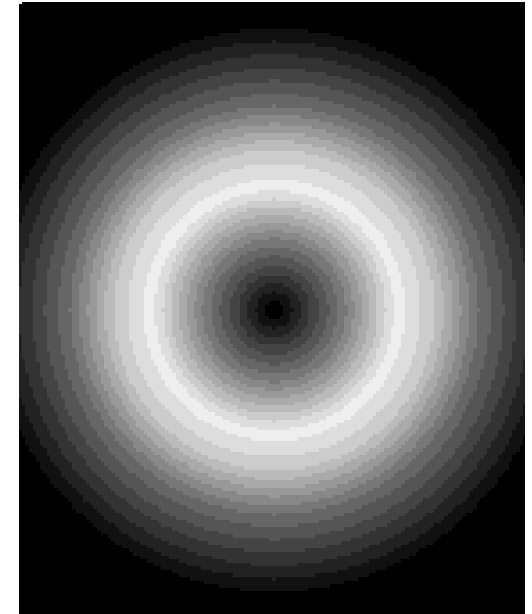
Fluorescence image



Underlying structure



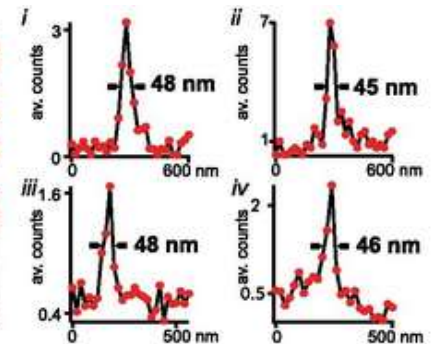
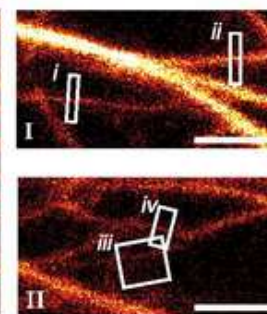
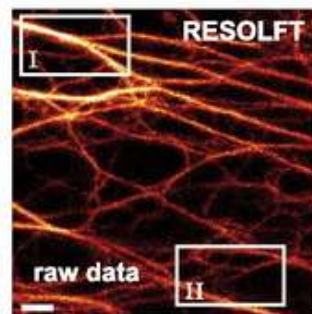
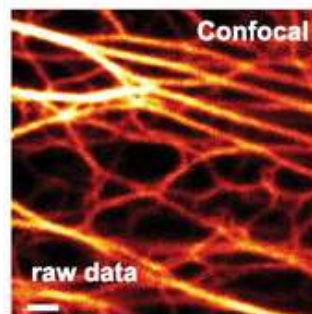
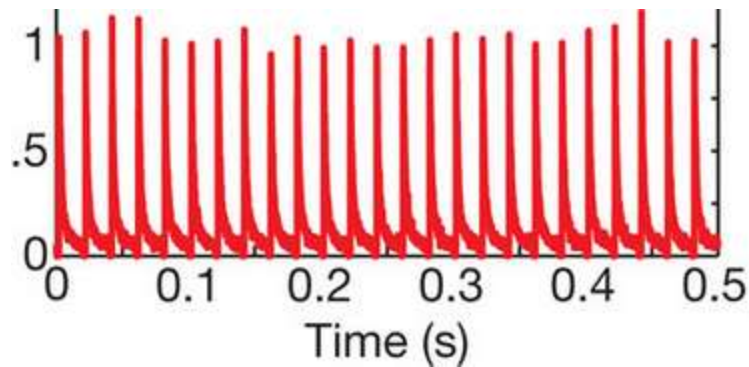
Depletion pattern



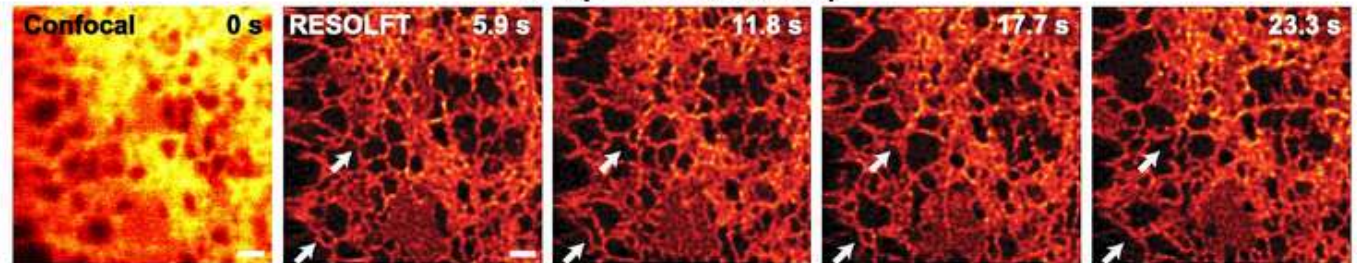
STED (Hell 1994, Hell 1999)
GSD (Hell 1995, Hell 2007)
RESOLFT (Hell 2003, Hell 2011)

Diffraction limited PSF Saturated depletion Smaller effective PSF

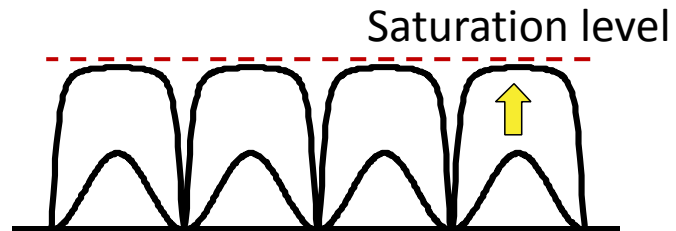
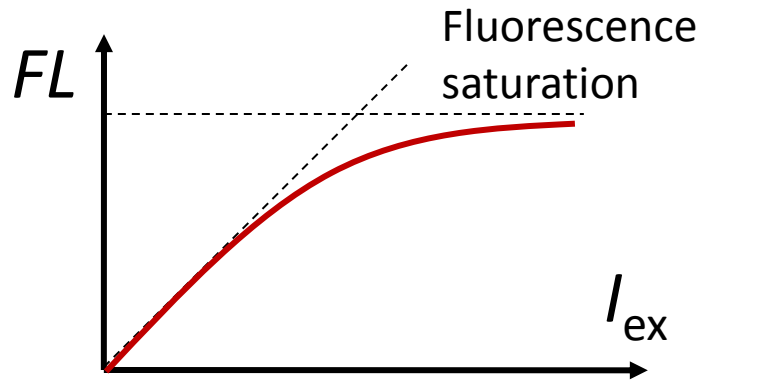
RESOLFT by rsEGFP and rsEGFP2



ER (rsEGFP2-KDEL)



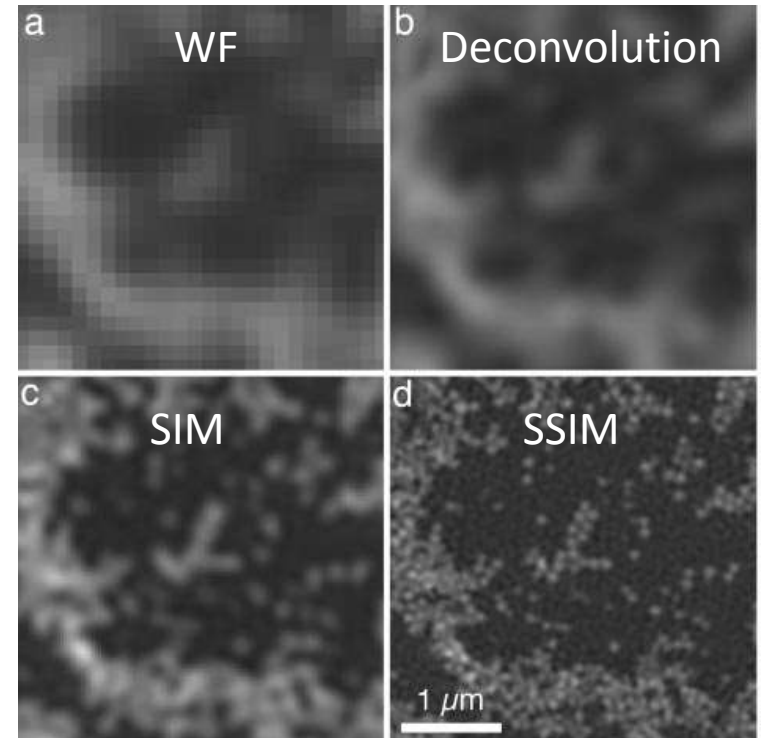
Saturated SIM



Saturated illumination pattern



Sharp zero lines



50 nm resolution

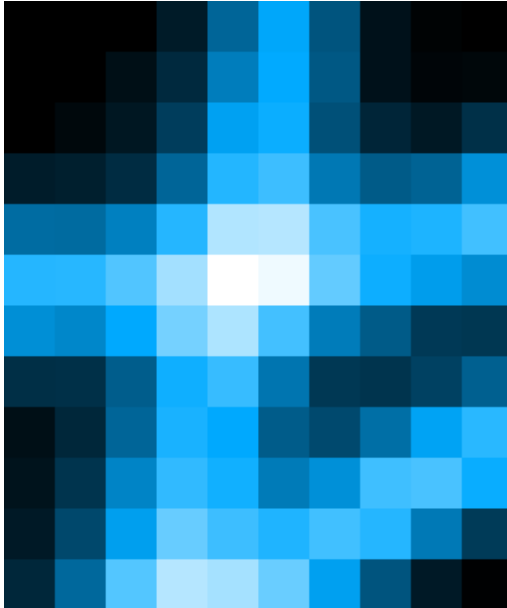
Suffers from fast photobleaching
under saturated excitation condition

Super-resolution by single-molecule switching

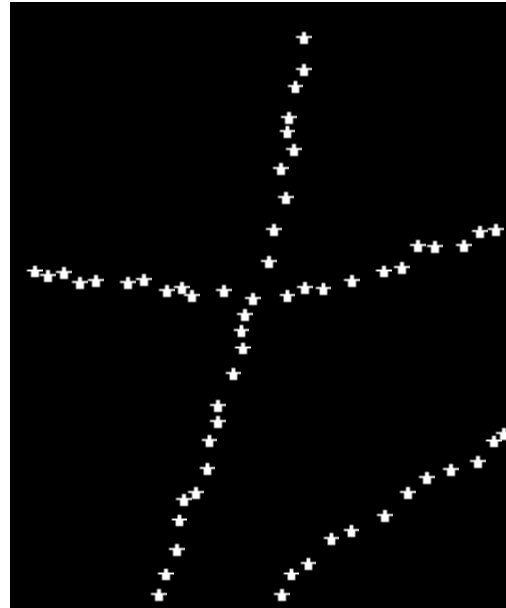


Super-resolution by single-molecule switching

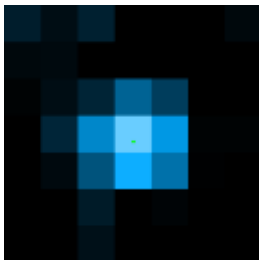
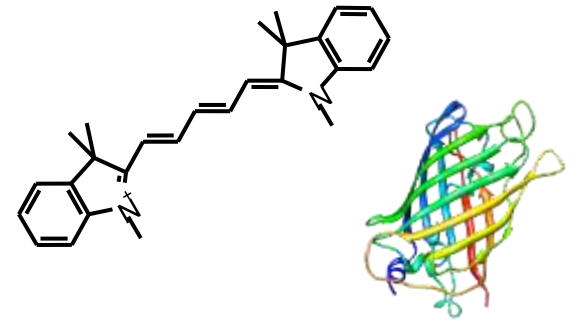
Fluorescence image



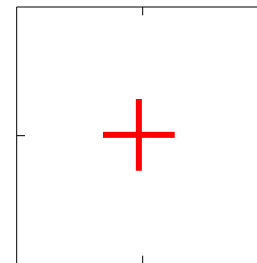
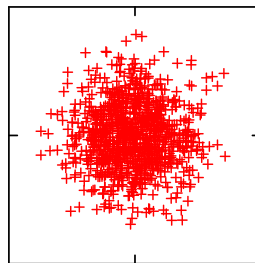
Underlying structure



Photoswitchable molecules



=



$$D \approx d / \sqrt{N}$$

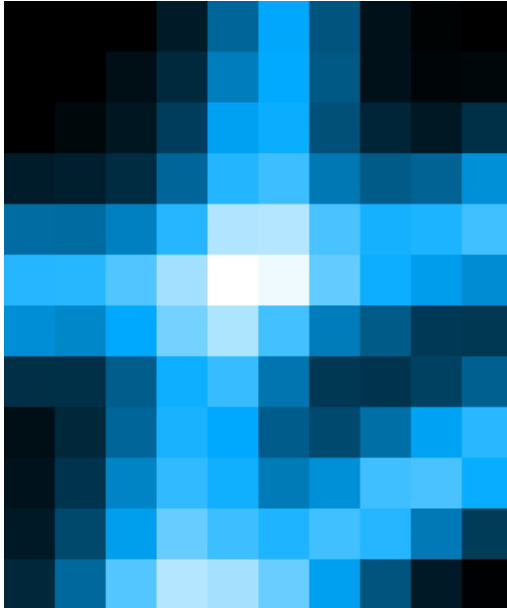
Single molecule image

N photons

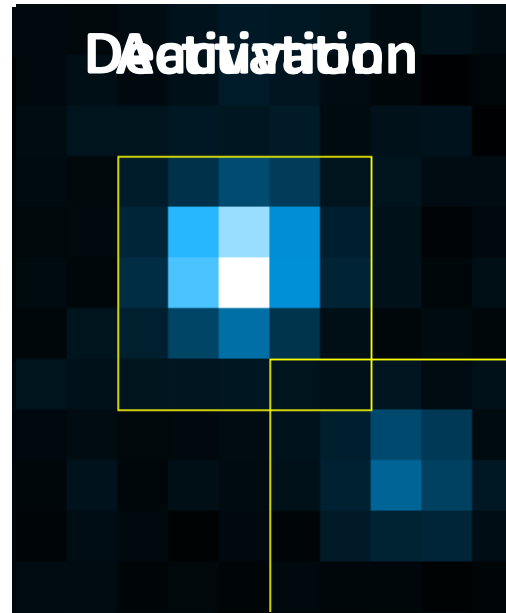
Single-molecule localization

Super-resolution by single-molecule switching

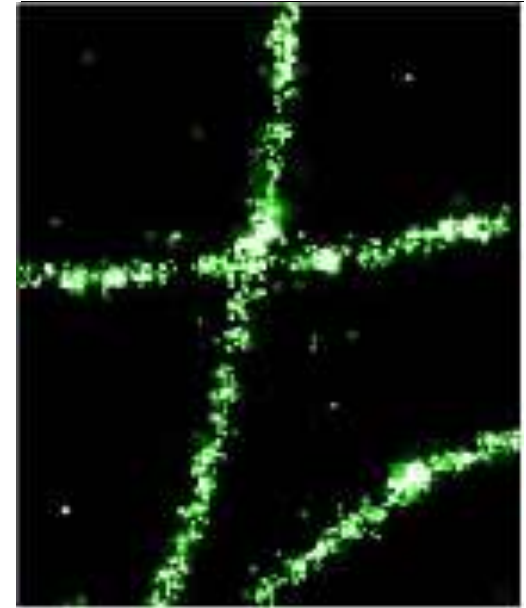
Fluorescence image



Raw images



STORM Image



2x real time

STORM = Stochastic Optical Reconstruction Microscopy (Zhuang 2006)

PALM = Photoactivated Localization Microscopy (Betzig & Hess 2006)

FPALM = Fluorescence Photoactivation Localization Microscopy (Hess 2006)

PALMIRA (Hell 2007), **GSDIM** (Hell 2008), **dSTORM** (Sauer 2008), **SMACM** (Moerner 2008)

PAINT (Hochstrasser 2006), **SPRAYPAINT** (Moerner 2011), **SOFI** (Weiss 2009)

Drosophila motoneuron dendrites

